

Recommender Systems

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Short biography

Short biography

- Mathematical highschool / ETF bachelor degree
- 12 years software/web development -> 8 years DS/AI/ML
- SAIS Advisory Board Member / Business Group Lead
- Leisure time: Freediving / Freeclimbing
- Values a good team more than anything else



Recommender systems

- Recommender systems are considered as an inevitable part of any larger system that is offering some kind of products/services to the final user
- Recommender systems are beneficial to both service providers and users
- They provide **personalized experience**



Industry

- 35% of what consumers purchase on Amazon
- 75% of what they watch on Netflix
- 60% of what they watch on YouTube comes from product recommendations

Industry





The New York Times







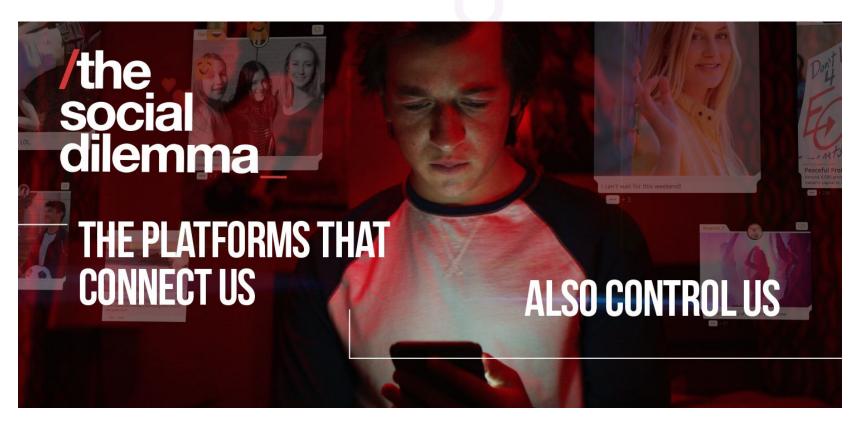








The Social Dilemma [2020]



Types of recommender systems

Types of recommender systems

- **Content-based**
- Collaborative
 - User/Item
 - Neighbourhood/Latent vector
- **Hybrid** models

Recommender Approaches

Attribute-based recommendations (You like action movies, starring Clint Eastwood, you might like "Good, Bad and the Ugly" Netflix)

Hierarchy (You bought Printer you will also need ink - BestBuy) Collaborative Filtering - User-**User Similarity** (People like you who bought beer

also bought diapers - Target)

Model Based Training SVM. LDA, SVD for implicit features

Item similarity (You like Godfather so vou will like Scarface - Netflix)

Collaborative

Filtering - Item-

Social+Interest Graph Based (Your

friends like Lady Gaga so you will like Lady Gaga, PYMK - Facebook LinkedIn)

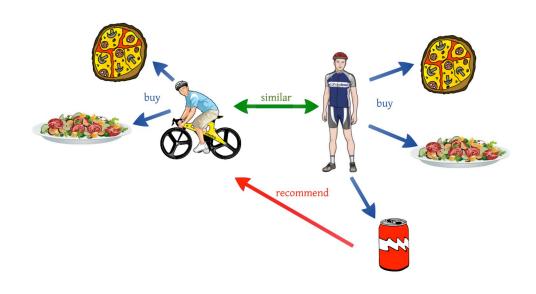
Content-based recommenders

- dependent on properties of an item (categorization, description etc.)
- independent of other users' behavior
- no cold-start problem
- cannot recommend anything genuinely "new"

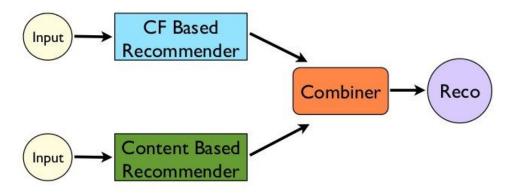


Collaborative recommenders

- better results than content-based
- domain free
- suffer fromcold-start problem
- sparsity of information



Hybrid recommenders



Few words about tools/libraries

SciPy stack

- NumPy // Provides an abundance of useful features for operations on N-dimensional arrays in Python. The library provides vectorization of mathematical operations on the NumPy array type, which boosts performance and speeds up the execution
- NumPy

 Pandas // Pandas is a Python package for data wrangling. It designed for quick and easy data manipulation, aggregation and visualization



Machine learning

Scikit-learn

Scikits are additional packages of SciPy Stack designed for specific functionalities like image processing and **machine learning** facilitation.

The library combines quality code and good documentation, ease of use and high performance and is de-facto industry standard for machine learning with Python.



Jupyter notebooks

- The Jupyter Notebook is an open-source web application that allows you to create and share documents that contain live code, equations, visualizations and narrative text
- Indispensable tool for exploratory data analysis in python



Dataset

Dataset

Movielens https://grouplens.org/datasets/movielens/

This dataset describes 5-star rating and free-text tagging activity from MovieLens, a movie recommender service.



University of Minnesota



Dataset // movies table

	movield	title	genres
0	1	Toy Story (1995)	AdventurelAnimationlChildrenlComedylFantasy
1	2	Jumanji (1995)	AdventurelChildrenlFantasy
2	3	Grumpier Old Men (1995)	ComedylRomance
3	4	Waiting to Exhale (1995)	ComedylDramalRomance
4	5	Father of the Bride Part II (1995)	Comedy
5	6	Heat (1995)	ActionlCrimelThriller
6	7	Sabrina (1995)	ComedylRomance
7	8	Tom and Huck (1995)	AdventurelChildren
8	9	Sudden Death (1995)	Action
9	10	GoldenEye (1995)	ActionIAdventurelThriller

Dataset // ratings table

- Another representation of the following table can be in a form of a sparse matrix
- Sparse matrix -> most elements are zero
- Movie recommendations -> ~99% missing entries

	userId	movield	rating	timestamp
17208	111	3608	3.5	1098374299
15886	102	3061	4.0	957980939
6527	36	32	5.0	847056901
15282	100	88	2.0	854194208
542	7	780	3.0	851866703
85159	572	52722	3.5	1436779789
11100	73	6953	3.5	1255588164
3241	19	441	3.0	855192455
23348	165	1923	3.5	1111482007
81851	558	4024	4.0	992788160

Dataset // ratings table

	31	1029	1061	1129	1172	1263	1287	1293	1339	1343	 134528	134783	137595	138204	60832	64997	72380	129	4736	6425
1	2.5	3.0	3.0	2.0	4.0	2.0	2.0	2.0	3.5	2.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
3	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
6	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
7	3.0	0.0	0.0	3.0	0.0	0.0	4.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
9	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
10	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

Simplified dataset

- rows -> users
- columns -> movies
- matrix R is sparse
 (~99% missing entries)

```
Alice
Bob
Charlie
Daniel
Eric
 Zoe
```

Content-based

Recommender Systems

Collaborative-based

Neighbourhood methods

 User/item-based similarity (similarity between vectors)

Latent factor models

Model users in reduced multi-dimensional space

Content-based

Content-based

- New user is registered into the system
- The user makes a selection of categories of interest

[Action, Comedy, Crime, Documentary, Drama, Romance, Thriller]

- Filter movies from the desired categories
- Calculate weighted ratings and vote counts
- Offer best rated items from the chosen categories

Weighted rating

An item with **rating 8** with **2 votes** cannot be considered better than an item with **rating 7.9** but with **200 votes**

$$WR = (v/(v+m)) * R + (m/(v+m)) * C$$

v - number of votes for the item

m - minimum votes required to be listed

R - average rating of an item

C - mean vote across the whole report

python code

```
In [56]: # choose only movies that are in at least one of the categories (but it can be in all)
    dmr = dmr[dmr[user_cats].sum(axis=1) == len(user_cats)]
    dmr = dmr[['movieId','title'] + user_cats]

In [57]: # calculate average rating and number of ratings for each of the movies
    dmr['rating'] = dmr['movieId'].apply(lambda x: weighted_rating(x))
    dmr['count'] = dmr['movieId'].apply(lambda x: dr[dr['movieId'] == x]['rating'].count())

In [60]: # filter and sort movie list
    dmr[dmr['count'] > MIN_REVIEW].sort_values('rating', ascending=False).head(5)
```

Out[60]:

	movield	title	Action	Drama	Thriller	rating	count
4432	6016	City of God (Cidade de Deus) (2002)	1	1	1	4.246190	69
2374	2959	Fight Club (1999)	1	1	1	4.162889	202
1018	1264	Diva (1981)	1	1	1	4.090423	14
263	293	Léon: The Professional (a.k.a. The Professiona	1	1	1	4.052686	132
7253	69481	Hurt Locker, The (2008)	1	1	1	4.039292	26

Content-based

- Later, categories can be derived from the user behavior
- We can use all sorts of item's additional metadata to make the recommendation list (e.g actors, directors)
- Using NLP (natural language processing) on the movie synopsis
- Using timestamp of the ratings, following monthly/yearly trends etc.

Collaborative filtering

Neighbourhood methods

(user/item similarity)

Recommender Systems

Collaborative-based

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 User/item-based similarity (similarity between vectors)

Latent factor models

Model users in reduced multi-dimensional space

Content-based

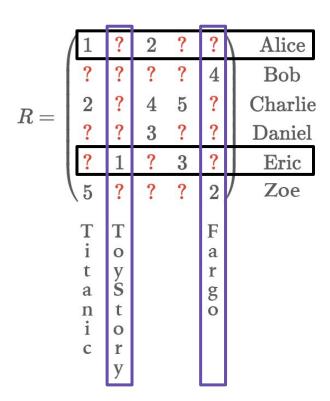
Neighbourhood methods

user similarity

items that are recommended to a user are based on an evaluation of items by users of the same neighborhood

item similarity

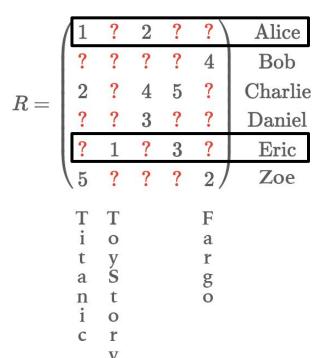
similar items build neighborhoods based on appreciations of users



Similarity measures

Plainly speaking, we're talking about similarity between two vectors

- Number of common rated items
- Manhattan distance
- Pearson correlation coefficient
- Cosine angle between vectors
- Adjusted cosine



Neighbourhood methods

- len(users) >> len(items)
- Amazon // users: ~310 MM, items: 12 MM

Users will have very few mutually rated items, while items will have a larger number of users who have co-rated them

user-based similarity

```
In [42]: # populate data from file
    rating_matrix = pd.read_csv('cf_matrix.csv',index_col=0)
In [63]: rating_matrix.head(10)
```

Out[63]:

	31	1029	1061	1129	1172	1263	1287	1293	1339	1343		134528	134783	137595	138204	60832	64997	72380	129	4736	6425
1	2.5	3.0	3.0	2.0	4.0	2.0	2.0	2.0	3.5	2.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
3	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
4	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
6	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
7	3.0	0.0	0.0	3.0	0.0	0.0	4.0	0.0	0.0	0.0	***	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
8	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
9	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
10	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

10 rows × 9066 columns

user-based similarity

```
In [44]: # calculate similarities between all users and selected user
         # here we've used cosine similarity, but that's open for debate of the particular problem
         sim = []
         for i in range(len(rating matrix)):
             sim.append(1 - spatial.distance.cosine(rating matrix.iloc[USER ID-1,:], rating matrix.iloc[i,:]))
In [45]: # put similarities into a dataframe for easier manipulation later on
         df sim = pd.Series(sim,index=rating matrix.index)
         df sim.sort values(ascending=False, inplace=True)
         df sim.head()
Out[45]: 19
                1.000000
                0.610957
         537
                0.522613
         21
                0.494830
         344
                0.468342
         dtype: float64
In [46]: # top rated user by defined similarity
         top sim user = df sim.index[1]
         top sim user
Out[46]: 514
```

user-based similarity

```
In [64]: # quick look at two vectors (ratings from both of the users)
    cf_sim = rating_matrix.loc[[top_sim_user,USER_ID]].T
    cf_sim.columns = ['top_sim_user', 'user']
    cf_sim.head(10)
```

Out[64]:

	top_sim_user	user
31	0.0	0.0
1029	3.0	5.0
1061	0.0	3.0
1129	3.0	3.0
1172	0.0	0.0
1263	0.0	4.0
1287	0.0	4.0
1293	5.0	0.0
1339	3.0	3.0
1343	4.0	4.0

user-based similarity

```
In [70]: # finding average rating of the top_similar_user (the threshold for the movies which we'll recommend)
# since we don't want to recommend all movies rated from a particular user

top_sim_user_avg = cf_sim[cf_sim['top_sim_user'] > 0]['top_sim_user'].mean()

# now the key is to find movies to recommend that are not rated by the user but are rated by the top_similar_user,
# since those are the films that are worth recommending

cf_sim['recommend'] = (cf_sim['top_sim_user'] > top_sim_user_avg) & (cf_sim['user'] == 0)
In [71]: cf sim[cf sim['recommend']].sort values('top sim_user', ascending=False).head()
```

In [71]: cf_sim[cf_sim['recommend']].sort_values('top_sim_user', ascending=False).head()

Out[71]:

	top_sim_user	user	recommend
175	5.0	0.0	True
1289	5.0	0.0	True
909	5.0	0.0	True
233	5.0	0.0	True
1120	5.0	0.0	True

user-based similarity

```
In [72]: # getting movie ids
    movie_ids = list(cf_sim['recommend']].sort_values('top_sim_user', ascending=False).index)

In [74]: res = dm[dm['movieId'].isin(movie_ids)].copy()

# append corresponding ratings
    res['rating'] = dr[(dr['movieId'].isin(movie_ids)) & (dr['userId'] == top_sim_user)]['rating'].values
    res.sort_values('rating', ascending=False).head(10)
```

Out[74]:

rating	genres	title	movield	
5.0	[Comedy, Drama, War]	M*A*S*H (a.k.a. MASH) (1970)	5060	3918
5.0	[Drama, Romance]	Farewell My Concubine (Ba wang bie ji) (1993)	446	395
5.0	[Comedy, Drama]	People vs. Larry Flynt, The (1996)	1120	899
5.0	[Comedy, Drama, Romance]	Apartment, The (1960)	909	730
5.0	[Documentary]	Microcosmos: Le peuple de l'herbe	1111	895
5.0	[Comedy, Drama]	Rosencrantz and Guildenstern Are Dead (1990)	1243	997
5.0	[Comedy, Drama, Thriller]	Shallow Grave (1994)	319	285
5.0	[Adventure, Animation, Comedy]	Wallace & Gromit: The Best of Aardman Animatio	720	607
5.0	[Comedy, Drama]	Madness of King George, The (1994)	272	244
5.0	[Drama]	Exotica (1994)	233	205

User-based vs item-based

- Two users will generally have very few mutually rated items, while two items will have a larger number of users who have co-rated them -> more stable
- User-based approach requires frequent updates of the similarity matrix -> very costly
- Item-based methods recommend obvious items and items that are not novel from previous experience

Collaborative filtering

Latent Factor Models

SVD // Singular Value Decomposition

Recommender Systems

Collaborative-based

Neighbourhood methods

 User/item-based similarity (similarity between vectors)

Latent factor models

Model users in reduced multi-dimensional space

Content-based

Dimensionality reduction

PCA // Principal Component Analysis

- Principal component analysis (PCA) is a mathematical procedure that transforms a number of (possibly) correlated variables into a (smaller) number of uncorrelated variables called principal components.
- The first principal component accounts for as much of the variability in the data as possible, and each succeeding component accounts for as much of the remaining variability as possible

1. Compute the mean feature vector

$$\mu = \frac{1}{p} \sum_{k=1}^{p} x_k$$
, where, x_k is a pattern $(k = 1 \text{ to } p)$, $p = \text{number of patterns}$, x is the feature matrix

2. Find the covariance matrix

$$C = \frac{1}{p} \sum_{k=1}^{p} \{x_k - \mu\} \{x_k - \mu\}^T \text{ where, } T \text{ represents matrix transposition}$$

3. Compute Eigen values λ_i and Eigen vectors v_i of covariance matrix

$$Cv_i = \lambda_i v_i$$
 (i = 1, 2, 3,....q), $q =$ number of features

- 4. Estimating high-valued Eigen vectors
 - (i) Arrange all the Eigen values (λ_i) in descending order
 - (ii) Choose a threshold value, θ
 - (iii) Number of high-valued λ_i can be chosen so as to satisfy the relationship

$$\left(\sum_{i=1}^{s} \lambda_i\right) \left(\sum_{i=1}^{q} \lambda_i\right)^{-1} \ge \theta$$
, where, $s = \text{number of high valued } \lambda_i \text{ chosen}$

- (iv) Select Eigen vectors corresponding to selected high valued λ_i
- 5. Extract low dimensional feature vectors (principal components) from raw feature matrix. $P = V^T x$, where, V is the matrix of principal components and x is the feature matrix

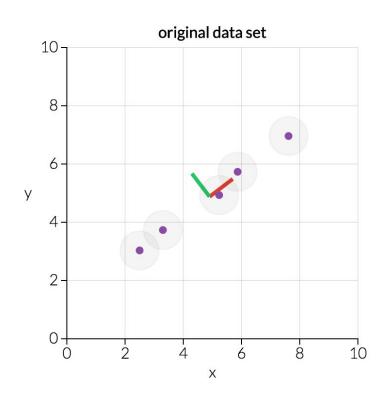
Original dataset

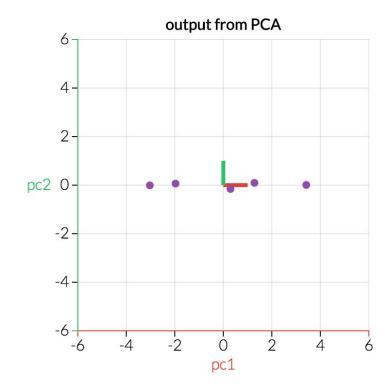
X	2.5	3.2	5.2	5.9	7.8	
у	3.1	3.8	5	5.8	6.9	



Output from PCA

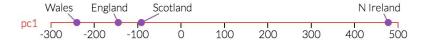
PCA // simple example (2-dim data)





PCA // 17-dim example

	England	N Ireland	Scotland	Wales
Alcoholic drinks	375	135	458	475
Beverages	57	47	53	73
Carcase meat	245	267	242	227
Cereals	1472	1494	1462	1582
Cheese	105	66	103	103
Confectionery	54	41	62	64
Fats and oils	193	209	184	235
Fish	147	93	122	160
Fresh fruit	1102	674	957	1137
Fresh potatoes	720	1033	566	874
Fresh Veg	253	143	171	265
Other meat	685	586	750	803
Other Veg	488	355	418	570
Processed potatoes	198	187	220	203
Processed Veg	360	334	337	365
Soft drinks	1374	1506	1572	12 56
Sugars	156	139	147	175



In a nutshell, this is what PCA is all about:

- Finding the directions of maximum variance in
 high-dimensional data and project it onto a smaller
 dimensional subspace while retaining most of the information
- Var(pc1) > Var(pc2) > Var(pc3) ...

Recommender Systems

Collaborative-based

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 User/item-based similarity (similarity between vectors)

Latent factor models

Model users in reduced multi-dimensional space

Content-based

Collaborative filtering // Netflix

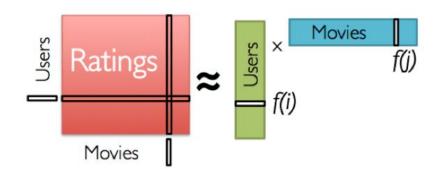
- Open competition to build a collaborative filtering algorithm
- 1,000,000 \$ prize
- Winner beat Netflix's accuracy by 10.06%
- Over 500 different approaches used



Latent Factor Models

- Latent => Hidden
- Better performance than neighbourhood (similarity-based) methods
- The factors (components) are called latent because they are there in our data but are not really discovered until you run the low-rank matrix factorization, then the factors emerge and hence the "latency"

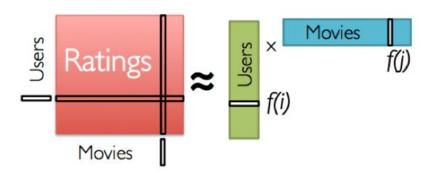
- Matrix factorization is breaking Low-Rank Matrix Factorization: down of one matrix into a **product** of multiple matrices
- $R = MU^T$
- c number of latents factors



shape(R) =
$$(u,m)$$
 shape(U) = (u,c) shape(M) = (c,m)

- PCA on R gives you the typical users U
- PCA on R^T gives you the
 typical movies M
- SVD gives youboth in one shot
- \bullet R = MU^T

Low-Rank Matrix Factorization:



shape(R) =
$$(u,m)$$
 shape(U) = (u,c) shape(M) = (c,m)

- Each principal component captures a specific latent factor
- Some of the factors can have semantics behind them

```
Alice
          =10\% Action fan
                          +10\% Comedy fan
                                            +50% Romance fan
Bob
          = 50% Action fan
                          +30% Comedy fan
                                            +10% Romance fan
Titanic
          =20\% Action
                           +00% Comedy
                                            +70% Romance
         =30\% Action
                           +60% Comedy
                                            +00% Romance
Toy Story
```

```
Alice
 Bob
Charlie
Daniel
 Eric
 Zoe
```

The value of $\mathbf{r}_{\mathbf{n}}$ is the result of a **dot product** between two vectors:

Vector $\mathbf{p}_{\mathbf{u}}$ which is a row of \mathbf{M} and which is specific to the user \mathbf{u} and **vector** $\mathbf{q}_{\mathbf{i}}$ which is a column of \mathbf{U}^{T} and which is specific to the item \mathbf{i}

$$R = MU^{T}$$

$$\begin{pmatrix} r_{ui} \end{pmatrix} = \begin{pmatrix} p_{u} & p_{u} \end{pmatrix} \begin{pmatrix} q_{i} & q_{i} \\ q_{i} & q_{i} \end{pmatrix}$$

$$r_{ui} = p_{u} \cdot q_{i}$$

$$r_{ui} = \sum_{c \in \text{concepts}} \text{affinity of } u \text{ for } c \times \text{affinity of } i \text{ for } c$$

SVD

- The SVD of sparse matrix R is not defined
- If R was dense, we could compute M and U easily
- A first option that was used for some time is to fill the missing entries of R with some simple heuristic
- Find an approximate solution to the SVD problem using Stochastic Gradient Descent

SVD - using surprise library

```
In [75]: from surprise import Reader, Dataset, SVD, evaluate
    reader = Reader()
    dr.head()
```

Out[75]:

	userld	movield	rating	timestamp
0	1	31	2.5	1260759144
1	1	1029	3.0	1260759179
2	1	1061	3.0	1260759182
3	1	1129	2.0	1260759185
4	1	1172	4.0	1260759205

```
In [76]: data = Dataset.load_from_df(dr[['userId', 'movieId', 'rating']], reader)
    data.split(n_folds=5)
```

```
In [ ]: svd = SVD()
    evaluate(svd, data, measures=['RMSE'])
```

```
In [213]: trainset = data.build_full_trainset()
    svd.fit(trainset)
```

Out[213]: <surprise.prediction_algorithms.matrix_factorization.SVD at 0x7f4c58c7ad68>

SVD - using surprise library

3112

3113

3114

19

19

19

10

11

14

3.0 855192496 3.0 855192773

5.0 855190167

```
In [82]: svd.predict(19, 2)
Out[82]: Prediction(uid=19, iid=2, r ui=None, est=3.120983027200581, details={'was impossible': False})
In [83]: dr[dr['userId'] == 19].head(10)
Out[83]:
                userld movield rating timestamp
          3105
                   19
                                3.0 855190091
          3106
                   19
                           2
                                3.0 855194773
                                3.0 855194718
          3107
                   19
                   19
          3108
                                3.0 855192868
          3109
                   19
                                3.0 855190128
                   19
                                3.0 855190128
           3110
                                3.0 855190232
           3111
                   19
```

Closing remarks

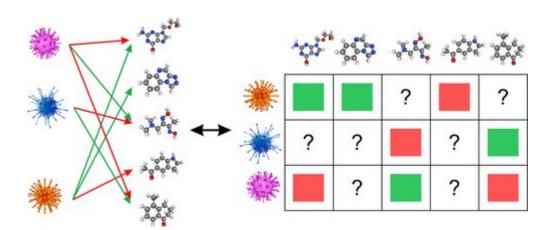
Modeling interaction

- Recommender systems are not reserved only for the product/item recommendation
- It's a great tool to model any kind of interaction between items/services



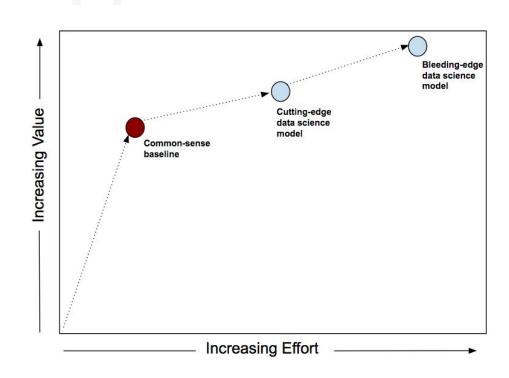
Drug discovery etc.

- Recommender systems have great potential for drug discovery.
- Modeling interaction between molecules and pathogens



Common-sense

Many real-world recommendation problems are best solved through thoughtful analysis, feature engineering, simple models and effective feedback systems.



Additional links

Additional links

- https://www.thesocialdilemma.com/
- http://setosa.io/ev/principal-component-analysis/
- https://www.youtube.com/watch?v=gilXNoiqO_U
- https://datajobs.com/data-science-repo/Recommender-Systems-%5BNetflix%5D.pdf
- https://www.coursera.org/specializations/recommender-systems
- https://www.quora.com/What-is-the-difference-between-content-based-filtering-an d-collaborative-filtering
- https://www.youtube.com/watch?v=z0dx-YckFko
- https://grouplens.org/blog/similarity-functions-for-user-user-collaborative-filtering/

Additional links

- https://www.youtube.com/watch?v=z0dx-YckFko
- http://thmsrey-ds.com/2017/06/27/recommender-systems-introduction-user-based
 -collaborative-filtering/
- https://stats.stackexchange.com/questions/2691/making-sense-of-principal-compo-nent-analysis-eigenvectors-eigenvalues
- https://arxiv.org/pdf/1404.1100.pdf?utm_content=bufferb37df&utm_medium=soci_ al&utm_source=facebook.com&utm_campaign=buffer
- https://buildingrecommenders.wordpress.com/2015/11/10/the-components-of-a-r
 ecommender-system/

Questions?

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