

## Linear Regression - Revised

$$y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$$

- What do each of these symbols mean?

$x_i$  = predictor variable value at  $i$

$y_i$  = response variable value at  $i$

$\beta_0$  = y-intercept of best-fit line

$\beta_1$  = slope of best fit line

$\varepsilon_i$  = residual of observed  $x_i$  to  $\hat{y}_i$  based on line.

- What are we estimating?

$\beta_0, \beta_1$

- How do we do the estimation?

OLS or ML

Linear regression assumptions:

1. Normality
2. Homogeneity of variance
3. Independence

Others:

- linearity
- fixed X-values

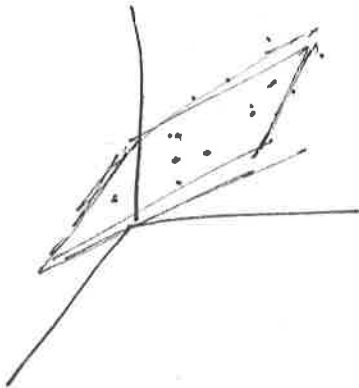
- Aside: standardized residuals =  $\frac{\text{residual}}{\text{standard deviation of residuals}}$
- Aside: F-statistic returned by 'lm' of regression  $\rightarrow$  comparison to model w/ only mean.
- Aside: adjusted  $R^2 = R^2$  that is adjusted for the number of predictors

How do we know if our model fits our assumptions?

- Regression diagnostics.

## Multiple Linear Regression

Rather than predicting the relationship between a response and the predictors with a single line, we are now looking at a plane.



The slope of a line in one-dimension of the plane is the partial regression coefficient.