

ML@B SAP Algorithm Outline

Notation:

• D: Data matrix

- D_i : Datapoint of format {close price - open price, low, high, volume, F_{i-1} }

 \bullet F: Trade value

$$- F_i = D_i \cdot \Theta = D_{i0}\Theta_0 + D_{i1}\Theta_1 + D_{i2}\Theta_2 + D_{i3}\Theta_3 + D_{i4}\Theta_4$$

 The 0th - 3rd components are calculated at initialization, the fourth component is calculated later

$$-F_i' = D_{i0}\Theta_0 + D_{i1}\Theta_1 + D_{i2}\Theta_2 + D_{i3}\Theta_3$$

$$- F_i = F'_i + \Theta_4 F_{i-1} = \sum_{j=0}^i \Theta_4^{i-j} F'_j$$

• R_i : The reward function at time step i

$$-R_i = F_i D_0 - \delta |F_i - F_{i-1}|$$

• Gradient Equations

$$\frac{\partial R_t}{\partial F_t} = \begin{cases} -1 & \text{if } F_{t-1} < F_t \\ +1 & \text{else} \end{cases}$$

$$\frac{\partial R_t}{\partial F_{t-1}} = D_{t0} - \begin{cases} -1 & \text{if } F_{t-1} < F_t \\ +1 & \text{else} \end{cases} = D_{t0} - \frac{\partial R_t}{\partial F_t}$$

$$\frac{\partial F_t}{\partial \Theta} = D_t$$

$$\frac{\partial U_t}{\partial \Theta} = \sum_{t=1}^t \frac{\partial U_t}{\partial R_t} \left(\frac{\partial R_t}{\partial F_t} \frac{\partial F_t}{\partial \Theta} + \frac{\partial R_t}{\partial F_{t-1}} \frac{\partial F_{t-1}}{\partial \Theta} \right)$$

• *U*: The stock sharpe ratio