Appendix A: Modeling Wing Morphology

for 'paper_title'; Bernat, AV, Cenzer, ML

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Details of the Analyses

This document was generated by R Markdown on 2021-11-23 using R version 4.0.5 (2021-03-31). The document provides the step-by-step analytical methods used in the manuscript by Anastasia Bernat (AVB) and Meredith Cenzer (MLC). Multiple draft scripts were written by AVB between 2021-03-01 and 2021-07-26 until being distilled and complied by AVB and code reviewed by MLC at the University of Chicago into this comprehensive script. All draft scripts can be viewed in the GitHub repository, SBB-dispersal (https://github.com/mlcenzer/SBB-dispersal), within the directory avbernat_working_on > All_Morphology > stats.

All code and output from the statistical analyses is shown. Code for data cleaning and the generation of plots is not displayed, but can be viewed in the wing_summary.Rmd file and its accompanying sourced scripts. To repeat analyses and the generation of plots, all data files and sourced scripts should follow the directory structure presented in the SBB-dispersal repository.

Description of the Data

This document analyzes two main datasets, raw_data and data_long. The raw_data set provides morphology measurements for each soapberry bug, Jadera haematoloma, collected and measured between the April 2013 and February 2020. There are four morphology measurements: beak length, thorax width, wing length, and body length. The sex, wing morph (long-winged, shot-winged, or ambiguously-winged), and host plant the bug was collected from as well as the month and year each bug was collected in was recorded. The data_long set provides the same recordings as the raw_data set, but it has been filtered for only long-winged soapberry bugs.

Abbreviations Used in the Data and Code

- SBB soapberry bug, Jadera haematoloma
- L long-winged morph
- LS or SL ambiguous wing morph
- **pophost** the host plant soapberry bugs were collected from, which was either *Koelreuteria* elegans or *Cardiospermum corindum*, occasionally called (and abbreviated) as goldenrain tree (GRT) or balloon vine (BV), respectively
- months since start proxy for year where the first collection occurred on April 2013
- month_of_year proxy for season where collections occurred only in months February, April, May, August, September, October, and September
- wing2body a computed and unitless column that calculates the wing length divided by the body length of a soapberry bug
- wing2thorax a computed and unitless column that calculates the wing length divided by the thorax width of a soapberry bug
- sd standard deviation
- se standard error
- w_ a column name that starts with w_ is shortened from "wing" (e.g. w_morph is "wing morph")
- _c a column name that ends in _c is a column that has been centered. Example columns: wing2body_c, month_of_year_c, and months_since_start_c
- _binom a column name that ends in _binom is a column that has been recodified into binary data (0's and 1's). Example columns: sex_binom, pophost_binom, and wing_morph_binom

Data Cleaning And Exploration

Read Libraries

The occurrence of long-wing morphology and the wing-to-body ratio of *J. haematoloma* were analyzed using multivariate, generalized linear modeling (GLM) as implemented in the R packages lme4 and

binom. The dplyr package helped pipeline data manipulation processes by grouping data quickly. All plots, except the histograms, were generated using ggplot libraries and helper functions found in R packages ggformula and cowplot.

Additional R packages not shown below, but embedded in the sourced scripts are zoo and lubridate, which aid in data manipulation and datetime manipulation, respectively.

```
library(lme4)  # fit regressions
library(dplyr)  # data manipulation
library(ggformula)  # ggplot plotting
library(cowplot)  # ggplot helper functions to arrange multi-panel figures
library(binom)  # binomial confidence intervals
```

Read Source Files

Each sourced script below aides in either data cleaning (read_morph_data(), remove_torn_wings()) or multivariate GLM (model_comparisonsAIC(), get_model_probs()). Additionally, the function model_comparisonsAIC() takes in the path of a generic multi-factor script specific to the GLM family and link function needed to build the predictive models. All aforementioned, sourced scripts are located in the Rscr folder.

Read the Data

The morphology data were started in 2013-04-28 and last updated on 2021-05-18. The read_morph_data() function standardizes population names, host plant names, and month and year inputs. Month and year inputs are also converted into datetimes. Variables of interest like wing-to-body ratio and wing-to-thorax ratio are also calculated and centered. Then, the full dataset, raw_data (n=3532), and a long-winged bug only dataset, data_long (n=2096) are returned.

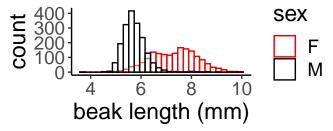
```
datapath = paste0(dir, "All_Morphology/stats/data/allmorphology05.18.21.csv")
data_list = read_morph_data(datapath)
```

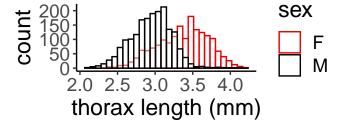
```
## number of missing dates: 0
##
## morph types: L S NA LS SL
## recoding missing morph types...
## S if wing2thorax <=2.2, L if wing2thorax >=2.5
##
## ambiguous wing morph bug count: 48
##
## filtered out NA wing2body for data_long...
raw_data = data_list[[1]]
data_long = data_list[[2]] # long-wing bugs only
```

```
data_long = remove_torn_wings(data_long)
```

##
number of bugs with torn wings: 193

Bugs marked as having torn wings during measurements were only filtered out of the data_long dataset (n=1903). That was because data_long is used only to analyze the wing-to-body ratio, which was computed for long-winged bugs since no short-winged bugs can fly. raw_data is only used to analyze long-wing morph frequency.

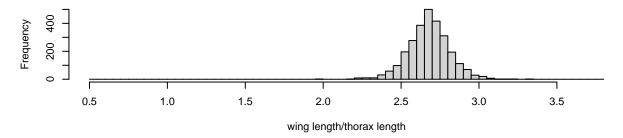




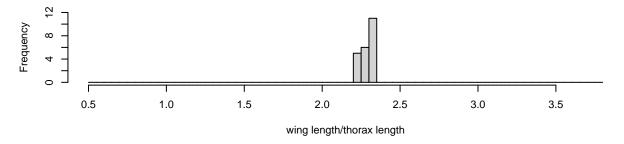
Histograms of Wing Morph Data

To better visualize how wing morph relates to another allometric measurement, wing-to-thorax ratio, the following histograms were plotted:

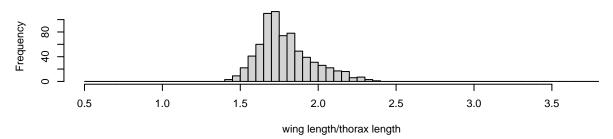
wing-to-thorax for long-winged SBB



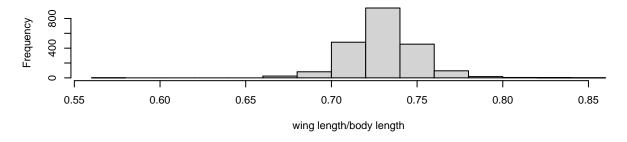
wing-to-thorax for SBB w/o recorded wing morph



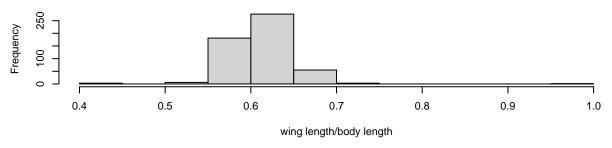
wing-to-thorax for short-winged SBB



wing-to-body for long-winged SBB

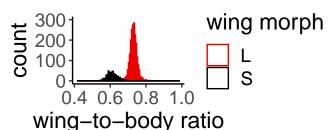


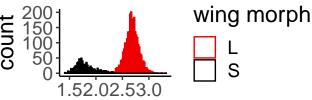
wing-to-body for short-winged SBB



raw_data\$wing2body = raw_data\$wing/raw_data\$body

```
d = raw_data %>%
  filter(!is.na(w_morph)) %>%
  filter(w_morph != "LS" & w_morph != "SL" & w_morph !="") %>%
  filter(!is.na(wing2body))
d$`wing morph` = d$w_morph
unique(d$`wing morph`)
## [1] "L" "S"
max(d$wing2body)
## [1] 0.9861432
ggplot(d, aes(x = wing2body, color = `wing morph`)) +
  geom_histogram(position = "identity", alpha = 0.4, fill="white", bins=100) +
  ylim(0,300) +
  labs(title=" ",
       x="wing-to-body ratio", y = "count") +
  theme classic() +
  scale_color_manual(values=c("red2", "black")) +
  theme(text = element_text(size = 17))
```





wing-to-thorax ratio

```
# ggplot(raw\_data, aes(x = thorax, color = sex)) +
# geom\_histogram(position = "identity", alpha = 0.4, fill="white") +
```

```
# labs(title=" ",
#
         x="thorax length (mm)", y = "count") +
#
  theme classic() +
# scale_color_manual(values=c("red2", "black")) +
    theme(text = element_text(size = 17))
Round <- function(number){</pre>
  # for plotting
  x <- round(number, 1)</pre>
  if(x\frac{%1}{1} == 0){
   return(paste(as.character(x), ".0", sep = ""))
  else{
    return(x)
  }
}
PCA_graphs <- function(dataset, PCA_title){</pre>
    # cos2 and the alpha.var: alpha.var colours variables by cos2
    # (importance of most important PC to variable),
    # see https://personal.utdallas.edu/~herve/abdi-awPCA2010.pdf
    GFpca <- PCA(dataset, scale.unit = TRUE, graph = TRUE, ncp = 10)
    eig.val <- get_eigenvalue(GFpca)</pre>
    var.val <- GFpca$var</pre>
    print(eig.val) #will only show in in console
    print(var.val)
    scree <- fviz_eig(GFpca, addlabels = TRUE, ylim = c(0, 100))</pre>
    print(scree)
    labX <- paste("PC1 (", Round(eig.val[1, 2]), "%)", sep = "")
    labY <- paste("PC1 (", Round(eig.val[2, 2]), "%)", sep = "")
    leplot <- fviz_pca_biplot(GFpca, geom.id = c("point"),</pre>
                               geom.var = c("arrow", "text"),
                               alpha.var = "cos2",
                               label = "var", repel = T,
                               col.ind = "gray", col.var = "black")
    print(leplot)
    ggpubr::ggpar(leplot, title = PCA_title, xlab = labX, ylab = labY,
                   ggtheme = theme_classic(), font.main = c(20, "bold"),
                   font.x = 14, font.y = 14, font.tickslab = 12
                   )
    D = cor(dataset)
    test <- cor.mtest(dataset)$p</pre>
    par(mfrow=c(1,2))
    corrplot.mixed(D,lower.col = "black", number.cex = .7, p.mat=test, sig.level=0.05)
    corrplot.mixed(D,lower.col = "black", number.cex = .7)
   return(GFpca)
}
```

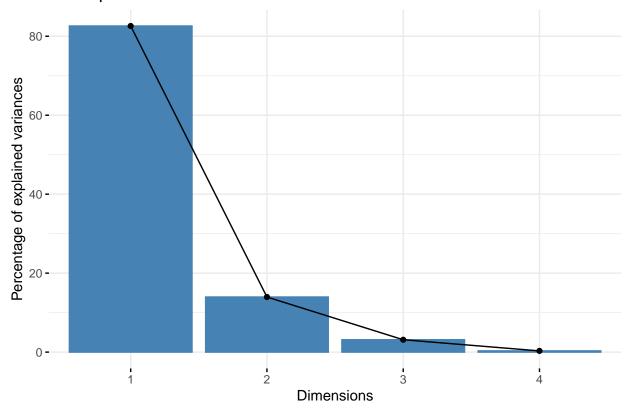
```
# delete
# temp <- data_long %>%
# select(thorax, wing2body, beak) %>%
# filter(!is.na(wing2body))
# colnames(temp) <- c("thorax", "wing2body", "beak")
# MorphPCA = PCA_graphs(temp, "(a) ")</pre>
```

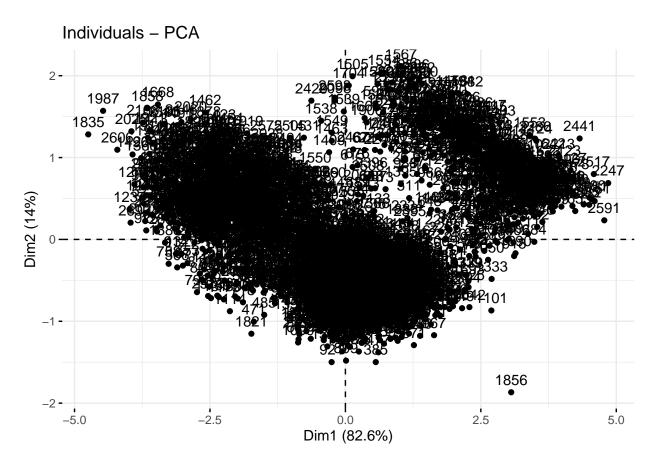
library(factoextra)

```
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
temp = cbind(d$wing, d$body, d$thorax, d$beak)
temp2 = temp[complete.cases(temp),]
res.pca <- prcomp(temp2, scale = TRUE)
fviz_eig(res.pca)</pre>
```

```
## Registered S3 methods overwritten by 'car':
## method from
## influence.merMod lme4
## cooks.distance.influence.merMod lme4
## dfbeta.influence.merMod lme4
## dfbetas.influence.merMod lme4
```

Scree plot



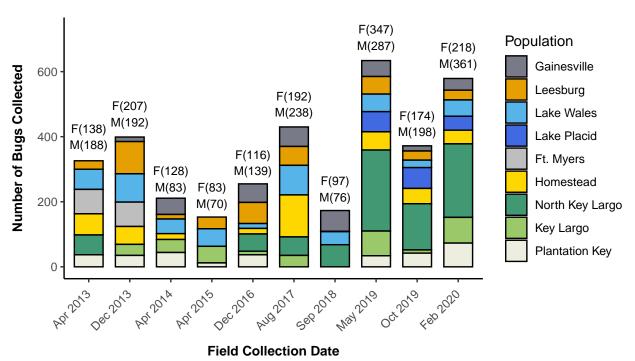


From the histograms, the relationship between wing morph and wing-to-thorax ratio is bimodal. Long-winged bugs have larger wing-to-thorax ratios with a frequency peak around 2.75, whereas short-winged bugs have much smaller wing-to-thorax ratios with a frequency peak around 1.75. It is then noticeable that there are 22 bugs who had not been identified as either S or L during measurements, but cannot be categorized into S or L based on wing-to-thorax bimodality because these data reside in-between the two modes.

Barplots

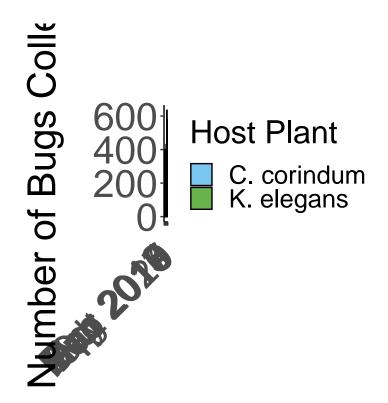
Bugs were collected during different years and months. The barplots below display the bugs collected per **population**, **host plant**, and **sex** across the years and months:

Plot 1: Collection numbers grouped by Population and Datetime

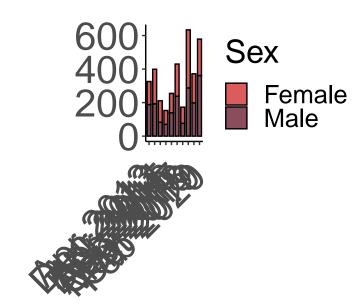


It is noticeable here that there was a heterogeneous population collection pattern across collection datetimes. However, collection numbers by host plant and sex were relatively homogeneous:

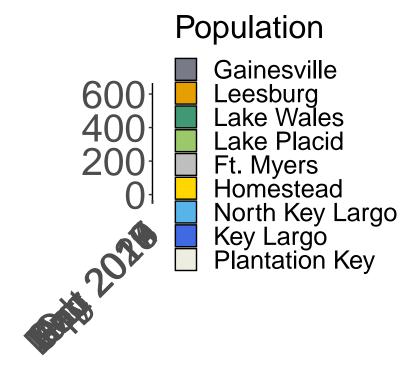
Plot 2: Collection numbers grouped by Host Plant and Datetime

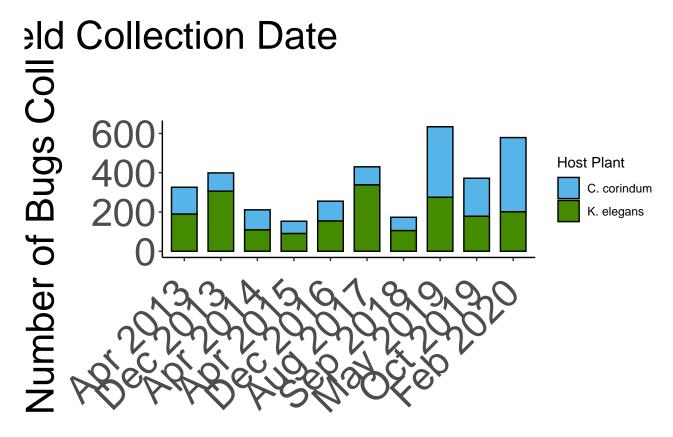


ield Collection Date



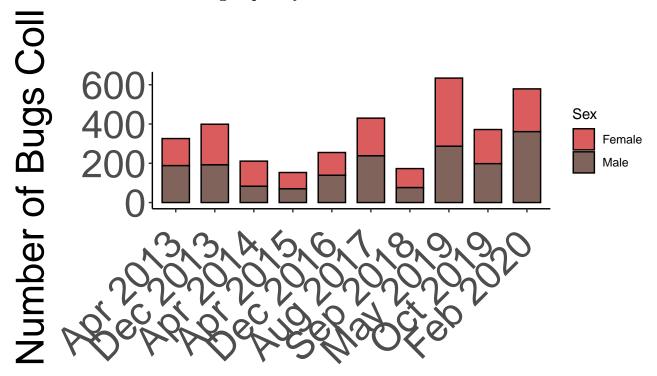
Field Collection Date





Field Collection Date

Plot 3: Collection numbers grouped by Sex and Datetime



Field Collection Date

Regression Modeling

Multivariate, GLM was performed using the glm() function in the lme4 package. Models were compared using Akaike Information Criterion (AIC) and model selection was determined using Akaike weights. Model fit was further evaluated between two models using the anova() function.

Long-Wing Morph Frequency

We tested how sex, host plant, month, and/or year effected whether a soapberry bug is long-winged (wing_morph_binom=1) or short-winged (wing_morph_binom=0).

```
data = data.frame(R=raw_data$wing_morph_binom,
                  A=raw_data$sex_binom,
                  B=raw_data$pophost_binom,
                  C=(raw_data$month_of_year),
                  D=raw_data$months_since_start)
model_script = paste0(source_path, "generic models-binomial glm 4-FF.R")
model_comparisonsAIC(model_script)
##
                     [,2]
                                          [,4]
                                                     [,5]
          [,1]
                               [,3]
## AICs
          3145.306
                    3146.842 3147.157
                                         3147.201
                                                     3148.521
## models 98
                    110
                               84
                                          107
                                                     105
          0.2529382 0.1173602 0.1002697 0.09808583 0.05068685
## probs
##
        glm(formula = R \sim A * B + A * D + B * C + C * D, family = binomial,
## m98
       data = data)
##
```

```
## m110
            glm(formula = R \sim A * B + A * D + B * C + B * D + C * D, family = binomial,
##
       data = data)
## m84 glm(formula = R ~ A * D + B * C + C * D, family = binomial, data = data)
## m107
            glm(formula = R \sim A * B + A * C + A * D + B * C + C * D, family = binomial,
       data = data)
##
            glm(formula = R \sim A * D + B * C + B * D + C * D, family = binomial,
## m105
       data = data)
anova(m98, m110, test="Chisq") # adding B*D does not improve fit
anova(m84, m98, test="Chisq") # adding A*B improves fit
anova(m63, m84, test="Chisq") # Adding C*D improves fit
anova(m51, m63, test="Chisq") # Adding B improves fit
## Analysis of Deviance Table
##
## Model 1: R ~ A * B + A * D + B * C + C * D
## Model 2: R ~ A * B + A * D + B * C + B * D + C * D
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          3461
                   3127.3
## 2
          3460
                   3126.8 1 0.46421
                                        0.4957
## Analysis of Deviance Table
## Model 1: R ~ A * D + B * C + C * D
## Model 2: R ~ A * B + A * D + B * C + C * D
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          3462
                   3131.2
## 2
          3461
                   3127.3 1
                               3.8506 0.04973 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
##
## Model 1: R ~ A * D + C * D + B
## Model 2: R ~ A * D + B * C + C * D
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
## 1
          3463
                   3137.3
## 2
                   3131.2 1
          3462
                               6.1886 0.01286 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
##
## Model 1: R ~ A * D + C * D
## Model 2: R ~ A * D + C * D + B
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
## 1
          3464
                   3497.3
## 2
          3463
                   3137.3 1
                               359.93 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The best fit model is m98. That is confirmed by its minimum AIC value, maximum Akaike weight, and the addition of A*B (sex_binom*pophost_binom) leading to a significant improvement in model fit as detected by the ANOVA test.

Best Fit

```
M1 = glm(wing_morph_binom ~ sex_binom * pophost_binom + sex_binom * months_since_start +
           pophost_binom * month_of_year + month_of_year * months_since_start,
         data=raw_data, family="binomial")
summary(M1)
##
## Call:
## glm(formula = wing_morph_binom ~ sex_binom * pophost_binom +
       sex_binom * months_since_start + pophost_binom * month_of_year +
##
##
       month_of_year * months_since_start, family = "binomial",
       data = raw_data)
##
##
## Deviance Residuals:
##
       Min
                 10
                      Median
                                           Max
                                   30
## -2.3803
                      0.4321
                                        1.2552
             0.3597
                               0.8450
##
## Coefficients:
##
                                      Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                     0.7516501 0.1841942
                                                            4.081 4.49e-05 ***
## sex_binom
                                    -0.2597900 0.0902673 -2.878 0.004002 **
## pophost_binom
                                     1.1256358 0.1142931
                                                            9.849
                                                                  < 2e-16 ***
## months_since_start
                                     0.0107239 0.0029582
                                                            3.625 0.000289 ***
## month_of_year
                                     0.0995560
                                                0.0255307
                                                            3.899 9.64e-05 ***
## sex_binom:pophost_binom
                                     0.0973323
                                                0.0495811
                                                            1.963 0.049635 *
                                                0.0015337
## sex_binom:months_since_start
                                                            2.426 0.015254 *
                                     0.0037212
## pophost_binom:month_of_year
                                    -0.0379395
                                                0.0150617
                                                          -2.519 0.011771 *
## months_since_start:month_of_year -0.0014557
                                                0.0004553 -3.198 0.001386 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 3562.3
                             on 3469 degrees of freedom
## Residual deviance: 3127.3
                             on 3461
                                       degrees of freedom
     (62 observations deleted due to missingness)
## AIC: 3145.3
##
## Number of Fisher Scoring iterations: 5
```

All single effects and their interactions are significant in the best fit model for predicting wing morph. It may be because of the size of the dataset that the model is more sensitive at detecting weak interactions as significant.

Long-Wing Morph Variance

We then tested how sex, host plant, month, and/or year effected long-wing morph frequency variance.

First, the long-wing morph mean frequency was computed using aggregate() to group the long-wing morph recordings in raw_data according to sex, host plant, month, and year. The subsequent subset data created was wmorph_table (n=40) Then, summary statistics were applied to the data subset and variance (sd) was modeled.

```
wmorph_table = aggregate(wing_morph_binom ~
                           sex_binom*pophost_binom*month_of_year*months_since_start,
                           data=raw_data, FUN=mean)
SE = function(x){sd(x)/sqrt(length(x))}
wmorph_table$sd = aggregate(wing_morph_binom ~
                              sex_binom*pophost_binom*month_of_year*months_since_start,
                              data=raw_data, FUN=sd) $wing_morph_binom
wmorph_table$se = aggregate(wing_morph_binom ~
                              sex binom*pophost binom*month of year*months since start,
                              data=raw_data, FUN=SE) $wing_morph_binom
wmorph_table$n = aggregate(wing_morph_binom ~
                             sex_binom*pophost_binom*month_of_year*months_since_start,
                              data=raw_data, FUN=length) $wing_morph_binom
data = wmorph_table
data = data.frame(R=data$sd,
                  A=data$sex_binom,
                  B=data$pophost_binom,
                  C=(data$month_of_year),
                  D=data$months_since_start)
model_script = pasteO(source_path, "generic models-gaussian glm 4-FF.R")
model_comparisonsAIC(model_script)
##
          [,1]
                    [,2]
                              [,3]
                                          [,4]
          -92.39855 -90.95292 -90.75898
## AICs
                                         -90.41465
## models 2
                    5
                              8
## probs 0.183788 0.0892081 0.08096352 0.06815837
##
## m2
        glm(formula = R ~ B, family = gaussian, data = data)
## m5
        glm(formula = R ~ A + B, family = gaussian, data = data)
        glm(formula = R ~ B + C, family = gaussian, data = data)
## m8
        glm(formula = R ~ B + D, family = gaussian, data = data)
## m9
anova(m2, m5, test="Chisq") # Adding A does not improve fit
anova(m2, m8, test="Chisq") # Adding C does not improve fit
anova(m2, m9, test="Chisq") # Adding D does not improve fit
anova(m0, m2, test="Chisq") # Adding B improves fit
## Analysis of Deviance Table
##
## Model 1: R ~ B
## Model 2: R ~ A + B
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
            38
                  0.20009
## 2
            37
                  0.19734 1 0.0027541
                                         0.4724
## Analysis of Deviance Table
##
## Model 1: R ~ B
## Model 2: R ~ B + C
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
```

```
## 1
            38
                  0.20009
## 2
            37
                  0.19830
                          1 0.0017949
                                         0.5628
## Analysis of Deviance Table
##
## Model 1: R ~ B
## Model 2: R ~ B + D
     Resid. Df Resid. Dev Df
                               Deviance Pr(>Chi)
            38
## 1
                  0.20009
            37
## 2
                  0.20001 1 8.0534e-05
                                          0.9029
## Analysis of Deviance Table
##
## Model 1: R ~ 1
## Model 2: R ~ B
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
            39
                  0.62439
## 2
            38
                  0.20010
                          1 0.42429 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The best fit model is m2. That is confirmed by its minimum AIC value, maximum Akaike weight, and the addition of B (pophost_binom) to the null model leading to a significant improvement in model fit as detected by the ANOVA test.

Best Fit

```
M2 = glm(sd ~ pophost_binom, data=wmorph_table, family="gaussian")
summary(M2)
##
## glm(formula = sd ~ pophost_binom, family = "gaussian", data = wmorph_table)
##
## Deviance Residuals:
##
                                            30
         Min
                     1Q
                            Median
                                                      Max
##
  -0.249168 -0.041487
                          0.005877
                                      0.041147
                                                 0.171269
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                  0.35216
                             0.01147
                                      30.693 < 2e-16 ***
##
  (Intercept)
## pophost_binom -0.10299
                             0.01147
                                      -8.976 6.28e-11 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for gaussian family taken to be 0.005265667)
##
##
##
       Null deviance: 0.62439
                               on 39
                                       degrees of freedom
## Residual deviance: 0.20010
                               on 38
                                      degrees of freedom
## AIC: -92.399
##
## Number of Fisher Scoring iterations: 2
```

Host plant (K. elegans = 1, C. corindum = -1) is significant in predicting long-wing morph frequency variance. Soapherry bugs collected from C. corindum, balloon vine, experience more variance in long-wing morph frequency than those collected from K. elegans, goldenrain tree.

Wing-to-Body Ratio

We tested how sex, host plant, month, and/or year effected whether the wing-to-body ratio of long-winged soapberry bugs.

```
data = data.frame(R=data_long$wing2body_c,
                  A=data_long$sex_binom,
                  B=data_long$pophost_binom,
                  C=data_long$month_of_year_c,
                  D=data_long$months_since_start_c)
model_script = paste0(source_path, "generic models-gaussian glm 4-FF.R")
model_comparisonsAIC(model_script)
##
          [,1]
                    [,2]
                               [,3]
                                          [,4]
                                                     [,5]
                                                                 [,6]
                                                     -9720.331
                                                                -9719.674
## AICs
          -9722.301 -9721.371 -9720.852
                                         -9720.339
## models 88
                    99
                              58
                                          92
                                                     97
                                                                76
## probs 0.1948772 0.1224324 0.09441271 0.07306166 0.07277994 0.05239229
## m88 glm(formula = R \sim A * B + A * D + B * D + C, family = gaussian,
##
       data = data)
       glm(formula = R \sim A * B + A * D + B * D + C * D, family = gaussian,
## m99
##
       data = data)
## m58 glm(formula = R \sim A * B + B * D + C, family = gaussian, data = data)
## m92 glm(formula = R \sim A * B + A * C + A * D + B * D, family = gaussian,
##
       data = data)
       glm(formula = R \sim A * B + A * D + B * C + B * D, family = gaussian,
## m97
       data = data)
##
## m76 glm(formula = R \sim A * B + B * D + C * D, family = gaussian, data = data)
anova(m88, m99, test="Chisq") # adding C*D does not improve fit
anova(m58, m88, test="Chisq") # Adding A*D marginally improves fit
anova(m58, m76, test="Chisq") # Adding C*D does not improve fit
anova(m34, m58, test="Chisq") # Adding B*D improves fit
## Analysis of Deviance Table
##
## Model 1: R ~ A * B + A * D + B * D + C
## Model 2: R ~ A * B + A * D + B * D + C * D
##
     Resid. Df Resid. Dev Df
                               Deviance Pr(>Chi)
## 1
          1895
                  0.66692
## 2
          1894
                  0.66655 1 0.00037502
                                          0.3019
## Analysis of Deviance Table
## Model 1: R ~ A * B + B * D + C
## Model 2: R ~ A * B + A * D + B * D + C
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
                  0.66813
## 1
          1896
## 2
          1895
                  0.66692 1 0.00121 0.06371 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
##
## Model 1: R ~ A * B + B * D + C
```

```
## Model 2: R ~ A * B + B * D + C * D
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          1896
                  0.66813
## 2
          1895
                  0.66784 1 0.0002886
                                         0.3655
## Analysis of Deviance Table
## Model 1: R ~ A * B + C + D
## Model 2: R ~ A * B + B * D + C
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
          1897
                  0.67063
## 1
## 2
          1896
                  0.66813 1 0.0024994 0.00774 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The best fit model is m58. It did not have the minimum AIC value or maximum Akaike weight, but the addition of A*D (sex_binom*months_since_start_c) was not detected as a significant improvement in model fit, according to the ANOVA test.

Best Fit

```
M3 = glm(wing2body_c ~ sex_binom*pophost_binom + pophost_binom*months_since_start_c
         + month_of_year_c, data=data_long, family=gaussian)
summary(M3)
##
## Call:
## glm(formula = wing2body_c ~ sex_binom * pophost_binom + pophost_binom *
##
       months_since_start_c + month_of_year_c, family = gaussian,
##
       data = data long)
## Deviance Residuals:
                                           3Q
         Min
                     1Q
                            Median
                                                     Max
                                                0.113993
## -0.070837 -0.010794 -0.000093
                                     0.010596
##
## Coefficients:
##
                                        Estimate Std. Error t value Pr(>|t|)
                                      -4.542e-04 4.601e-04 -0.987 0.32368
## (Intercept)
## sex_binom
                                      -1.787e-03 4.467e-04 -4.001 6.55e-05 ***
## pophost_binom
                                       4.289e-03 4.613e-04
                                                              9.297 < 2e-16 ***
## months_since_start_c
                                      -1.727e-05 2.225e-05 -0.776 0.43763
## month of year c
                                       7.155e-04 1.379e-04
                                                              5.188 2.35e-07 ***
## sex binom:pophost binom
                                       1.804e-03 4.466e-04
                                                              4.038 5.60e-05 ***
## pophost_binom:months_since_start_c 5.904e-05 2.217e-05
                                                              2.663 0.00781 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for gaussian family taken to be 0.0003523901)
##
       Null deviance: 0.72538
##
                              on 1902
                                       degrees of freedom
## Residual deviance: 0.66813 on 1896
                                       degrees of freedom
## AIC: -9720.9
##
## Number of Fisher Scoring iterations: 2
```

All single effects except months_since_start and all interactions are significant in the best fit model

for predicting wing-to-body ratio. It is noticeable that month and year effect sizes are relatively small.

Wing-to-Body Ratio Variance

We then tested how sex, host plant, month, or year effects the wing-to-body ratio variance of long-winged soapberry bugs.

First, the mean wing-to-body ratio was computed using aggregate() to group the wing-to-body ratio recordings in data_long according to sex, host plant, month, and year. The subsequent subset data created was w2b_table (n=36). Then, summary statistics were applied to the data subset and variance (sd) was modeled.

```
w2b_table = aggregate(wing2body ~
                        sex_binom*pophost_binom*month_of_year*months_since_start,
                        data=data_long, FUN=mean)
w2b_table$sd = aggregate(wing2body ~
                           sex_binom*pophost_binom*month_of_year*months_since_start,
                           data=data_long, FUN=sd) $wing2body
w2b_table$se = aggregate(wing2body ^
                           sex_binom*pophost_binom*month_of_year*months_since_start,
                           data=data_long, FUN=SE)$wing2body
data = w2b_table
data = data.frame(R=data$sd,
                 A=data$sex_binom,
                 B=data$pophost_binom,
                 C=(data$month of year),
                 D=data$months_since_start)
model_script = paste0(source_path, "generic models-gaussian glm 4-FF.R")
model_comparisonsAIC(model_script)
##
                    [,2]
                               [,3]
          [,1]
## AICs
          -280.1872 -279.8713 -279.4758
## models 8
                    19
## probs 0.1198675 0.1023577 0.08398967
##
        glm(formula = R ~ B + C, family = gaussian, data = data)
## m8
## m19
        glm(formula = R ~ B * C, family = gaussian, data = data)
## m2
        glm(formula = R ~ B, family = gaussian, data = data)
anova(m8, m19, test="Chisq") # Adding B*C does not improve fit
anova(m2, m8, test="Chisq") # Adding C does not improve fit
anova(m0, m2, test="Chisq") # Adding B improves fit
## Analysis of Deviance Table
##
## Model 1: R ~ B + C
## Model 2: R ~ B * C
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
## 1
            33 0.00070342
## 2
            32 0.00067127 1 3.215e-05
                                          0.2157
## Analysis of Deviance Table
```

```
##
## Model 1: R ~ B
## Model 2: R ~ B + C
##
    Resid. Df Resid. Dev Df
                              Deviance Pr(>Chi)
## 1
           34 0.00075844
           33 0.00070342 1 5.5025e-05
## Analysis of Deviance Table
##
## Model 1: R ~ 1
## Model 2: R ~ B
    Resid. Df Resid. Dev Df
                              Deviance Pr(>Chi)
## 1
           35 0.00087733
           34 0.00075844 1 0.00011888 0.02097 *
## 2
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The best fit model is m2. It did not have the minimum AIC value or maximum Akaike weight, but the addition of B (pophost_binom) to the null model lead to a significant improvement in model fit detected by the ANOVA test.

Best Fit

```
M4 = glm(sd ~ pophost_binom, data=w2b_table, family=gaussian)
summary(M4)
##
## Call:
## glm(formula = sd ~ pophost_binom, family = gaussian, data = w2b_table)
## Deviance Residuals:
         Min
                       1Q
                               Median
                                               3Q
                                                          Max
## -0.0059374 -0.0033018 -0.0006274
                                        0.0022332
                                                    0.0147212
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 0.0165999 0.0007872 21.088
                                                <2e-16 ***
## pophost_binom 0.0018172 0.0007872
                                        2.309
                                                0.0272 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for gaussian family taken to be 2.230719e-05)
##
       Null deviance: 0.00087733 on 35
                                         degrees of freedom
## Residual deviance: 0.00075844
                                        degrees of freedom
                                 on 34
## AIC: -279.48
##
## Number of Fisher Scoring iterations: 2
```

Host plant (K. elegans = 1,C. corindum = -1) is significant in predicting wing-to-body ratio variance. Soapherry bugs collected from K. elegans, goldenrain tree, experience more variance in wing-to-body ratio than those collected from C. corindum, balloon vine.

LOESS & Linear Regression Plots

Locally-weighted scatterplot smoothing (LOESS) helped display and explore the non-linear fluctuations in long-wing morph frequency and wing-to-body ratio across time. Each data set was fit with a local polynomial regression using lowess() to determine LOESS parameters (α and λ) and geom_smooth() for plotting more aesthetic visuals.

Wing Morph Frequency

Group significant elements

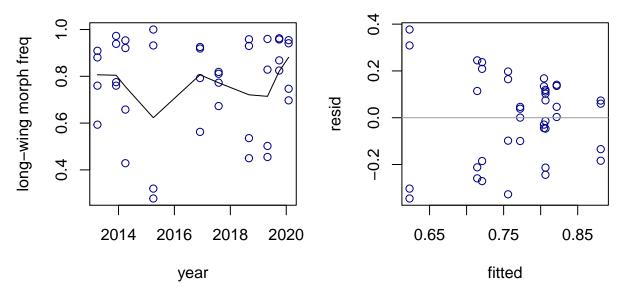
Data are aggregated according to predictors present in their respective aforementioned best fit GLM model. For predicting long-wing morph frequency (raw_data), the best fit model had the following predictors: sex, host plant, month, and year. We used dates, a datetime object, instead of months_since_start for cleaner plotting, but the two are interchangeable.

```
# function to calculate 95% confidence interval (CI).
CI_95 = function(x) \{qnorm(0.975)*sd(x)/sqrt(length(x))\}
CI_95_binom_upper = function(y) {
                        binom.confint(x=sum(y, na.rm=TRUE),
                                      n=length(y[!is.na(y)]),
                                       conf.level=0.95,
                                      methods='exact')$upper}
CI_95_binom_lower = function(y) {
                        binom.confint(x=sum(y, na.rm=TRUE),
                                      n=length(y[!is.na(y)]),
                                       conf.level=0.95,
                                      methods='exact')$lower}
# aggregate the full data
w_morph_summary = aggregate(wing_morph_binom ~
                            sex*pophost*month_of_year*dates,
                            data=raw_data, FUN=mean)
# compute standard error (SE), upper and lower CI, & sample size (n)
w_morph_summary$se = aggregate(wing_morph_binom ~
                               sex*pophost*month_of_year*dates,
                               data=raw_data,
                               FUN=SE)$wing_morph_binom
w_morph_summary$upper = aggregate(wing_morph_binom ~
                                   sex*pophost*month_of_year*dates,
                                   data=raw_data,
                                  FUN=CI_95_binom_upper)$wing_morph_binom
w_morph_summary$lower = aggregate(wing_morph_binom ~
                                  sex*pophost*month_of_year*dates,
                                   data=raw_data,
                                  FUN=CI_95_binom_lower)$wing_morph_binom
w_morph_summary$n = aggregate(wing_morph_binom ~
                              sex*pophost*month_of_year*dates,
                              data=raw_data,
                              FUN=length) $wing_morph_binom
dd = w_morph_summary
```

Check for LOESS Residuals

To determine the span (α) , the smoothing parameter) and the degree of zero (λ) of the LOESS, smoothers were applied with increasing weights until the residuals appeared to have constant variance. Only the best LOESS parameters are shown below:

```
plot_lowess_residuals = function(lfit, x, y, color) {
  lfun = approxfun(lfit)
  fitted = lfun(x)
  resid = y-fitted
  plot(fitted,resid,col=color)
  abline(h=0,col=8)
}
# loess models (month and year)
IM = lowess(dd$month_of_year, dd$wing_morph_binom, f=0.4) # f = alpha, the smoother span
1Y = lowess(dd$dates, dd$wing_morph_binom, f=0.4)
# plot loess fit and residuals
par(mfrow=c(1,2), mai=c(0.80,0.80,0.3,0.3))
plot(dd$month_of_year, dd$wing_morph_binom,
     xlab="month of year", ylab="long-wing morph freq", col="darkgreen")
lines(1M, type = "1")
plot_lowess_residuals(lM, dd$month_of_year, dd$wing_morph_binom, "darkgreen")
plot(dd$dates, dd$wing_morph_binom,
     xlab="year", ylab="long-wing morph freq", col="darkblue")
lines(lY, type = "l")
plot_lowess_residuals(lY, dd$dates, dd$wing_morph_binom, "darkblue")
                0
                             8 0
                                     8
                  0
                                                 0.2
ong-wing morph freq
           0
                                                                  8
     0.8
                  0
                                                                                 0
                                     8
                                                 0.0
           000
                           0
                                                               0
                0
     9.0
                                                                  0
                0
                                                      00
                                                                  0
                                     0
                             0
                                                                      0
                                                                         0
                             0
     0.4
                0
                                                                  0
                                                                      0
                                                 ġ.
                00
                                                                  8
           2
                4
                     6
                           8
                               10
                                     12
                                                       0.70
                                                                   0.80
                                                                               0.90
                  month of year
                                                                  fitted
```



From these residual plots (right-side), we selected a $\lambda=0$ and $\alpha=0.4$. With a zero degree polynomial, LOESS acts as a weighted moving average and a span of 0.4 demonstrates independence between the residuals.

Figure: Panels A, B, C, D (long-wing morph freq with month) & E (long-wing morph freq with year)

In addition to plotting local polynomial regression lines, the effects (slopes) of the best fit GLM models were also plotted. However, due to multiple interaction terms, we substituted the complex GLM models with single-variate or simpler models. This led to cleaner GLM line plotting, and the plots still reasonably reflected the aforementioned GLM models. Finally, all p-values displayed were extracted from the aforementioned best fit GLM model.

Panels A and B Regression Computations:

```
# single-variate model of month predicting wing morph
fit1 = glm(wing_morph_binom ~ month_of_year, family="binomial", data=raw_data)
xmonth = seq(2,12, 0.01)
wing_probs = predict(fit1, list(month_of_year=xmonth), type="response")

# extract p-value from best fit regression model
fit_pvalue = round(summary(M1)$coeff[,"Pr(>|z|)"][5],5)
pvalue = paste0("italic(p)[glm]==", fit_pvalue)
```

Panels C and D Regression Computations:

```
pred = as.data.frame(pred)

predFK = pred[pred$bhost==1 & pred$bsex==1,]

predFC = pred[pred$bhost==-1 & pred$bsex==1,]

predMK = pred[pred$bhost==1 & pred$bsex==-1,]

predMC = pred[pred$bhost==-1 & pred$bsex==-1,]

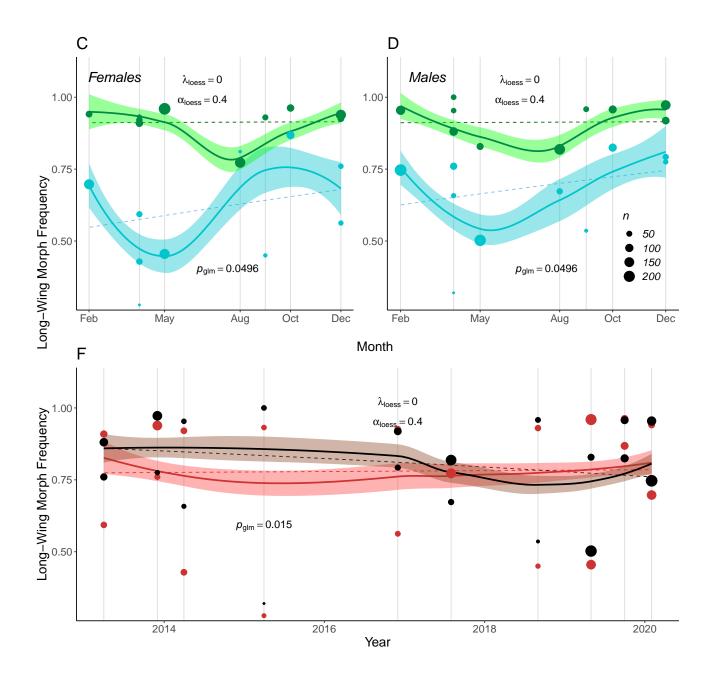
# extract p-value from best fit regression model

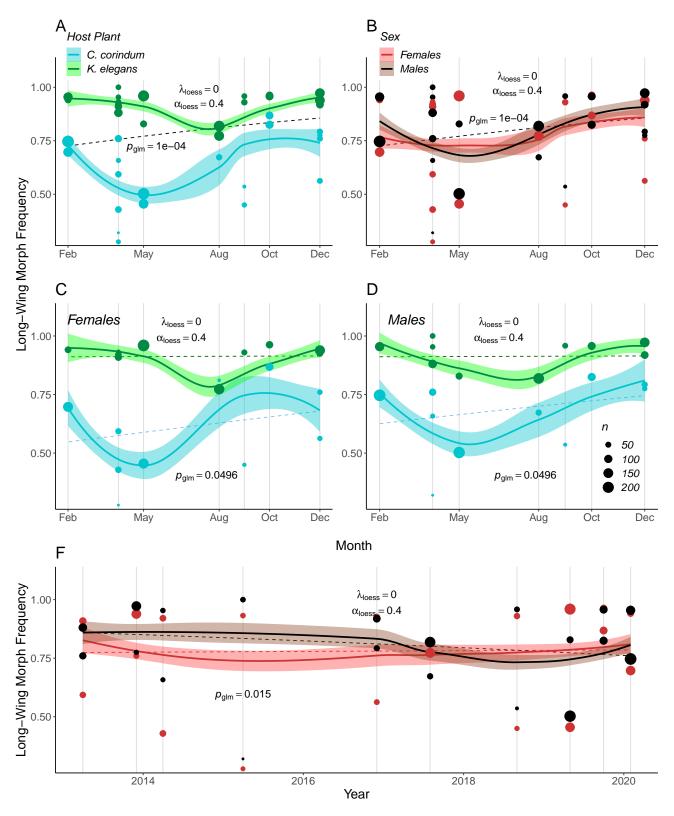
fit_pvalue = round(summary(M1)$coeff[,"Pr(>|z|)"][6],4)

pvalue = pasteO("italic(p)[glm]==", fit_pvalue)
```

Panel F Regression Computations:

```
# multi-variate model with year, sex, and host plant predicting wing morph
fit3 = glm(wing_morph_binom ~ sex_binom * dates, family = "binomial", data = raw_data)
set.seed(194842)
xyr = seq(sort(unique(dd$dates))[1],sort(unique(dd$dates))[10], 1)
bsex = sample(c(-1,1), replace=TRUE, size=length(xyr))
bhost = sample(c(-1,1), replace=TRUE, size=length(xyr))
wprobs = predict(fit3, list(sex_binom = bsex,
                                pophost_binom = bhost,
                                dates = xyr), type="response")
pred = cbind(xyr, bsex, bhost, wprobs)
pred = as.data.frame(pred)
pred$xyr = as.Date.numeric(pred$xyr)
predF = pred[pred$bsex==1,]
predM = pred[pred$bsex==-1,]
# extract p-value from best fit regression model
fit_pvalue = round(summary(M1)$coeff[,"Pr(>|z|)"][7],3)
pvalue = paste0("italic(p)[glm]==", fit_pvalue)
```





Extension of Figure 4. Evaluation of the frequency of long-winged morph soapberry bugs averaged across month and year from April 2013 to February 2020 using exploratory plots. For each point, the mean frequency of long-winged morphs of each month and year is plotted with LOESS smooth lines (solid lines) and 95% confidence intervals (shading) and linear regression line(s) (dashed line(s)).

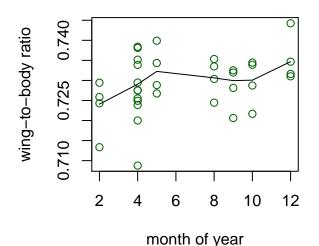
Wing-to-Body Ratio

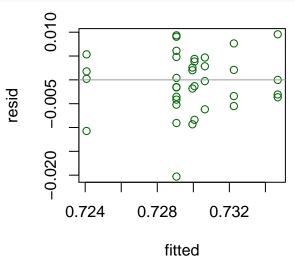
Group significant elements

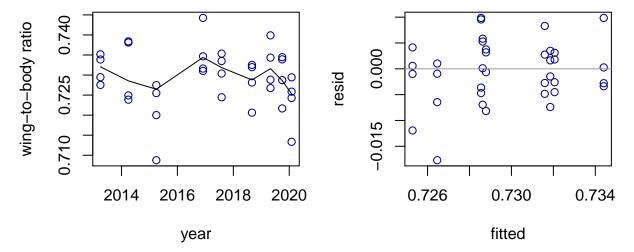
Data are aggregated according to predictors present in their respective aforementioned best fit GLM model. For predicting wing-to-body ratio (data_long), the best fit model had the following predictors: sex, host plant, month, and year. We used dates, a datetime object, instead of months_since_start for cleaner plotting, but the two are interchangeable.

Check for LOESS Residuals

To determine the span (α, β) the smoothing parameter) and the degree of zero (λ) of the LOESS, smoothers were applied with increasing weights until the residuals appeared to have constant variance. Only the best LOESS parameters are shown below:







Similarly, from these residual plots (right-side), we selected a $\lambda=0$ and $\alpha=0.4$.

Figure: Panels A, B, (wing-to-body ratio with month) & C (wing-to-body ratio with year)

In similar fashion, the local polynomial regression lines and the effects (slopes) of the best fit GLM models were plotted together. Due to multiple interaction terms, we substituted the complex GLM models with single-variate or simpler models. This led to cleaner GLM line plotting, and the plots still reasonably reflected the aforementioned GLM models. Finally, all p-values displayed were extracted from the aforementioned best fit GLM model.

Panels A and B Regression Computations:

Wing-to-body ratio is continuous data, unlike the wing morph data which is binary data. As a result, rather than using the predict() function to calculate the best fit line between wing-to-body and month, we used a single line of ggplot code, geom_smooth(data=data_long, method="glm", mapping = aes(x = month_of_year, y = wing2body)...). This line of code can be see in the wing_summary.Rmd script.

Panel C Regression Computations:

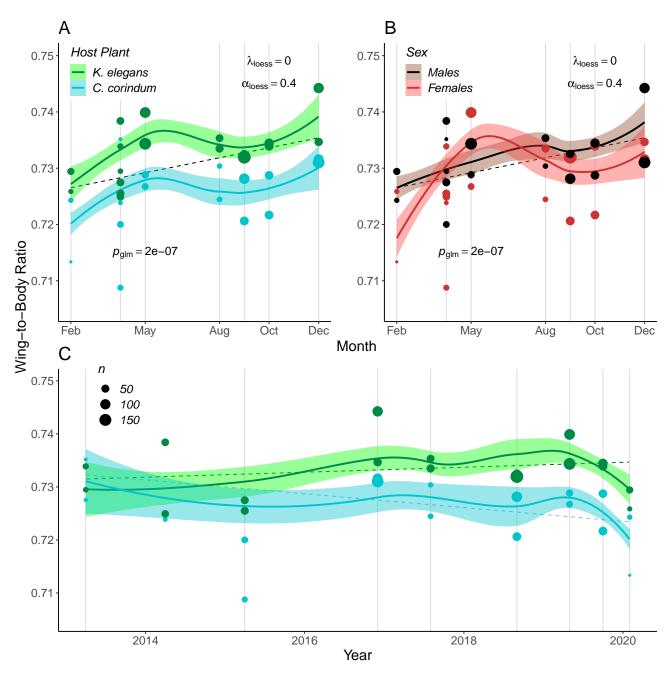


Figure 5. Evaluation of the wing-to-body ratio of soapberry bugs averaged across month and year from April 2013 to February 2020 using exploratory plots. For each point, the mean wing-to-body ratio of soapberry bugs collected in each month and year is plotted with LOESS smooth lines (solid lines) and 95% confidence intervals (shading) and linear regression line(s) (dashed line(s)).