# Appendix B: Modeling Flight Response

for 'paper\_title'; Bernat, AV, Cenzer, ML

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### 1 Details of the Analyses

This document was generated by R Markdown on 2021-12-09 using R version 4.0.5 (2021-03-31). The document provides the step-by-step analytical methods used in the manuscript by Anastasia Bernat (AVB) and Meredith Cenzer (MLC). Multiple draft scripts were written by AVB and MLC between 2020-03-01 and 2021-07-26 until being distilled and complied by AVB and code reviewed by MLC at the University of Chicago into this comprehensive script. All draft scripts can be viewed in the GitHub repository, SBB-dispersal (https://github.com/mlcenzer/SBB-dispersal), within the directory avbernat > Dispersal > Winter\_2020 > stats .

All code and output from the statistical analyses are shown. Code for data cleaning and the generation of plots is not displayed, but can be viewed in the **appendix\_B-flight\_summary.Rmd** file and its accompanying sourced scripts. To repeat analyses and the generation of plots, all data files and sourced scripts should follow the directory structure presented in the SBB-dispersal repository.

### 1.1 Description of the Data

Soapberry bugs, Jadera haematoloma, were flight tested in the Fall 2019 (2019-10-15 to 2019-11-08) and Winter 2020 (2020-02-17 to 2020-03-10) seasons using a flight mill machine. Soapberry bugs were flight tested twice for either set time increments or multiple hours in the flight mill and observed from 8 AM to (5-8 PM) each day. For each trial, the mass, flight response, egg-laying response, distance, duration, average speed, and max speed of each soapberry bug was recorded and then processed. All Python scripts used to process the flight records are located in the GitHub repository within the directory avbernat > Dispersal > Winter\_2020 > windaq\_processing . After trials, morphology measurements were taken for each bug. There are four morphology measurements: beak length, thorax width, wing length, and body length. The sex, wing morph (long-winged, shot-winged, or ambiguously-winged), host plant, and population of each bug were also recorded.

As a result of the experimental design, this document analyzes two main types of datasets: a full dataset and a unique dataset. A **full dataset** is a dataset where each row has a unique ID and trial type combination. A **unique dataset** is a dataset where each row has a unique ID because each trial has been grouped by ID. Examples are provided below. The advantage of generating a unique dataset is that changes between trials can be observed and analyzed.

### 1.2 Abbreviations Used in the Data and Code

- SBB soapberry bug, Jadera haematoloma
- S short-winged morph
- L long-winged morph
- LS or SL ambiguous wing morph
- **T1** trial 1 of flight testing
- **T2** trial 2 of flight testing
- EWM eggs when massed, binary response (yes or no)
- host\_\_ the host plant soapberry bugs were collected from, which was either *Koelreuteria elegans* or *Cardiospermum corindum*, occasionally called (and abbreviated) as goldenrain tree (GRT) or balloon vine (BV), respectively
- $\bullet$  sym\_dist distance from the local sympatric zone, which is demarked as Homestead
- wing2body a computed and unitless column that calculates the wing length divided by the body length of a soapberry bug
- $\bullet$  **sd** standard deviation
- se standard error
- w\_ a column name that starts with w\_ is abbreviated from "wing". Example column: w\_morph is "wing morph"

### 1.3 Data Transformations

- \_b a column name that ends in \_b is a column that has been recodified into binary data (0's and 1's). Example columns: flew\_b, eggs\_b
- \_c a column name that ends in \_c is a column that has been centered. Example columns: sex\_c, host\_c, avg\_days\_c
- \_s a column name that ends in \_s is a column that has been standardized. Example columns: wing2body\_s, sym\_dist\_s, thorax\_s
- avg\_ a column name that starts in avg\_ is a column that has been averaged across trial 1 (T1) and trial 2 (T2). Example columns: avg\_mass, avg\_days, avg\_time\_start, avg\_rec\_dur (exception: average\_speed)
- \_diff a column name that ends in \_diff is a column that is the difference between T1 and T2 data values. Formula: data values
- \_per a column name that ends in \_per is a column that is the percent change between T1 and T2 (T2-T1) data values. Formula: (T2-T1)/T1 \* 100.
- \_logsqrt a column name that ends in \_logsqrt is a column that has been normalized using a log-square-root transformation. Formula: log(sqrt(<data\_column>))-mean(log(sqrt(<data\_column>)). Example columns: avg\_mass\_logsqrt
- \_logsqrt\_i a column name that ends in \_logsqrt\_i is a column that has been normalized using a log-square-root transformation but its sign is the inverse of the column. Formula: log(sqrt(0.85-column))-mean(log(sqrt(0.85-column)). Example columns: wing2body\_logsqrt\_i

# 2 Winter 2020 Data Cleaning

### 2.1 Read Libraries

The flight response of *J. haematoloma* was analyzed using multivariate, generalized linear modeling (GLM) as implemented in the R packages lme4 and binom. All plots were generated using base R and supplemented with the popbio package to display logistic regressions and the rethinking package to display 95% confidence intervals of linear regressions. Additional R packages not show below but embedded in the sourced scripts are lubridate, chron, and dplyr. lubridate and chron both aid in datetime manipulation while dplry pipelines data grouping processes.

```
library(lme4) # fit regressions
library(rethinking) # Bayesian data analysis and plotting
library(popbio) # logistic regression plotting
library(binom) # binomial confidence intervals
```

### 2.2 Read Source Files

Each sourced script below aides in either data cleaning (read\_flight\_data(), center\_data()) or multivariate GLM (model\_comparisonsAIC(), get\_model\_probs(), catch\_warnings()). Additionally, the function model\_comparisonsAIC() takes in the path of a generic multi-factor script specific to the GLM family and link function needed to build the predictive models. All aforementioned, sourced scripts are located in the Rscr folder.

```
"compare_models.R", # 1 function: model_comparisonsAIC()
"get_Akaike_weights.R", # 1 function: get_model_probs()
"get_warnings.R") # 1 function: catch_warnings()

for (script in script_names) {
   path = paste0(source_path, script)
   source(path)
}
```

### 2.3 Read the Data

The flight performance data read directly below are only from Winter 2020 flight trials. The read\_flight\_data() function standardizes data types and names of the ID, trial type, host plant, flight response, egg-laying response, sex, population, and wing morph inputs. The date, start time, and end time of trails are also converted into datetimes. Variables of interest like wing-to-body ratio are also calculated and centered. Using the clean\_flight\_data() function, all morphology, mass, and flight performance measurements are centered and/or standardized within the read\_flight\_data() function. Then, what is returned is a full dataset (n=758) that includes all bugs collected during Winter 2020 and a subset of the full dataset (n=614) that includes only bugs tested from the Winter 2020 collection.

The create\_delta\_data() function generates the unique dataset by grouping by ID. The function also computes trial differences, percent differences, and averages for variables of interest such as mass, flight response, egg-laying response, distance, and speed. Then, the unique data variables are centered and/or standardized.

```
data_path = paste0(dir,"/Dispersal/Winter_2020/stats/data/all_flight_data-Winter2020.csv")

data = read_flight_data(data_path) # centers each subset of data
data_all = data[[1]] # full dataset
data_tested = data[[2]] # subset of data_all, contains only bugs flight tested

# create the unique dataset
d <- create_delta_data(data_tested, remove_bugs_tested_once = FALSE)

# keep all bugs (even bugs only tested once), then re-center
dc <- center_data(d, is_not_unique_data = FALSE)</pre>
```

Example of a **full dataset** (each row has unique ID and trial type):

```
data_tested[c(1:2,400:401), c("ID", "trial_type")]
```

```
## ID trial_type
## 1 114 T1
## 2 318 T1
## 400 316 T2
## 401 416 T2
```

Example of a **unique dataset** (each row has unique ID):

```
dc[c(1:2,295:296), c("ID", "trial_type")]
```

```
## # A tibble: 4 x 2
```

The datatype of the trial\_type column is a list because when expanded out, it would show list(T1, T2).

### 3 Across-Trial Flight Response (T1 & T2)

Flight response (yes flew or did not fly) was recorded and modeled. Multivariate, GLM was performed using the glm() function in the lme4 package. Models were compared using Akaike Information Criterion (AIC) and model selection was determined using Akaike weights. Model fit was further evaluated between two models using the anova() function.

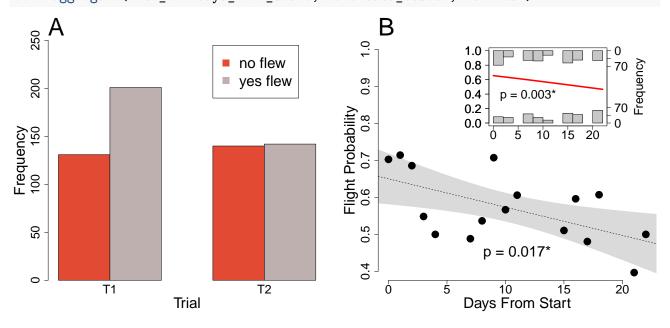
### 3.1 Experimental Effects

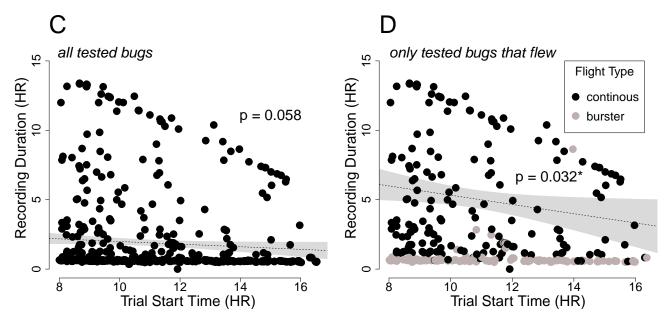
To determine how the design of the experiment affected flight response and/or performance, three design factors were modeled: trial type (T1 vs. T2), days from start, and trial start time.

### 3.1.1 Trial Type, Days from Start & Trial Start Time

```
# compute how many times flew yes or no per trial
binary_counts = table(data_tested$flew_b, data_tested$trial_type)[,2:3]

# aggregate by days since the trials began and flight response to determine flight prob
dd = aggregate(flew_b ~ days_from_start, data=data_tested, FUN=mean)
```





**A** & **B**. There was a negative effect of day a bug was tested (since the start of trials) on flight probability, but there was a significant effect only when the full dataset is considered. It is not significant for the unique dataset because days from start had to be averaged between trials. This is explored in the next section of the report. **C** & **D**. There was a negative effect of the trial start time on flight duration but only after removing bugs that did not fly (p = 0.031). Continuous flyers are driving this significant relationship (**D**).

### 3.2 Binomial Modeling

To understand SBB flight response, flight response across trials was modeled against sex, host plant, distance from the sympatric zone, wing-to-body ratio, and mass. This was done using the unique dataset.

Because the unique dataset was used, there exist multiple recorded counts of the number of times a SBB flew and did not fly between trials, T1 and T2. For that reason, we used cbind(num\_flew, num\_notflew) when modeling in order to account for all flight successes and failures for each individual.

Finally, we tested whether the data was over-dispersed, which could be resolved using a Quasibinomial:

```
# calculate the confidence interval for the mean of the data (Binomial vs. Quasibinomial)
fit <- glm(cbind(num_flew, num_notflew) ~ 1, family = binomial, data = dc)
plogis(confint(fit))

## 2.5 % 97.5 %
## 0.5191729 0.5976031

fit_q <- glm(cbind(num_flew, num_notflew) ~ 1, family = quasibinomial, data = dc)
plogis(confint(fit_q))

## 2.5 % 97.5 %
## 0.5108508 0.6056992

# estimate the dispersion parameter
summary(fit_q)$dispersion</pre>
```

## [1] 1.464596

If the dispersion parameter is close to 1, the data is not over-dispersed, so there is not much of a necessity to apply a Quasibinomial model. Therefore, we selected the family as "binomial".

### 3.2.1 Average Days Since Start

For the unique dataset, average days since start (log-square-root transformed) was computed in order to determine how an experimental factor affected flight response. It proved to not be significant:

```
avg_days_model<-glm(cbind(num_flew,num_notflew)~avg_days_c, data=dc, family=binomial)
summary(avg_days_model)</pre>
```

```
##
## Call:
   glm(formula = cbind(num_flew, num_notflew) ~ avg_days_c, family = binomial,
       data = dc)
##
##
  Deviance Residuals:
##
       Min
                  10
                       Median
                                     30
                                             Max
##
  -1.8429
            -1.7825
                      -0.1593
                                 1.5162
                                          1.5795
##
  Coefficients:
##
##
                Estimate Std. Error z value Pr(>|z|)
                0.22942
                            0.08236
                                       2.785
                                              0.00535 **
##
   (Intercept)
                                              0.64430
## avg_days_c
                0.01087
                            0.02354
                                       0.462
##
                    0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
##
   (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 668.05
##
                               on 332
                                        degrees of freedom
## Residual deviance: 667.84
                               on 331
                                        degrees of freedom
##
  AIC: 759.17
##
## Number of Fisher Scoring iterations: 3
Frequency
     9
     S
     0
```

Average Days Since Start

10

15

5

0

Average days since start accounts for bugs who died before they could be tested twice, which would most likely lead to an early average day value. The rest of the bugs that were tested twice would most likely have a later average day value. This testing regime shapes the bimodal distribution seen in the histogram. Additionally, the advantage of this computed variable is that it controls for the fact that some bugs were tested once late, and some by chance had been tested twice early. In turn, because we randomized test day, when repeated measures for each individual are combined across days, they

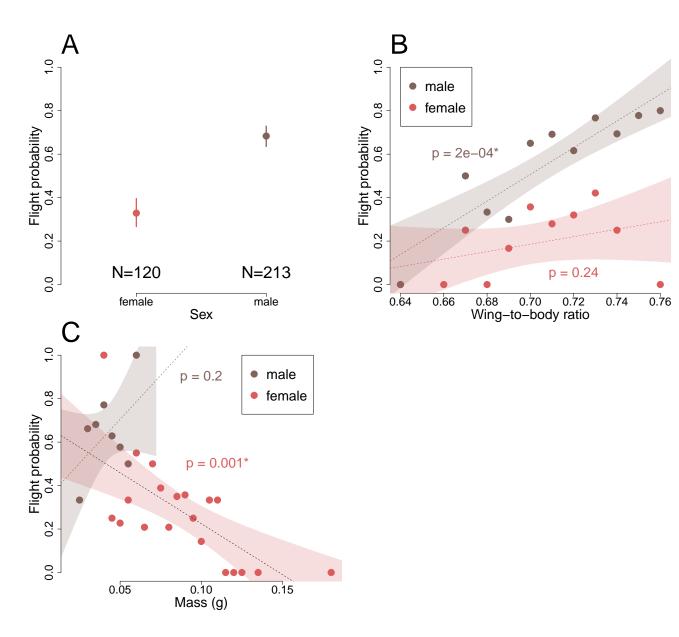
20

balance each other out. Thus, average days since start allows the multi-variate models, which control for repeated tests per ID number, to converge, and we can be confident that non-random mortality is not impacting flight response.[[AB FLAG: "can be confident..." not so founded...]]

### 3.2.2 Single-Variate Effects

We used aggregated datasets for single-variate modeling.

```
# tailoring variables for plotting
d$mass block=round(d$avg mass/0.005)*0.005
                                                # 0.005 q blocks
d$wing2body_block=round(d$wing2body, digits=2)
                                                # 0.01 blocks
d$days_block=round(d$avg_days, digits=0)
                                                # integer blocks
# aggregate data for plotting
dt=aggregate(flew_prob~sex, data=d, FUN=mean)
dt$trials=c(sum(d$num_flew[d$sex=="F"]+d$num_notflew[d$sex=="F"]),
            sum(d$num_flew[d$sex=="M"]+d$num_notflew[d$sex=="M"]))
ds=aggregate(flew_prob~sex*wing2body_block, data=d, FUN=mean)
ds$n=aggregate(flew_prob~sex*wing2body_block, data=d, FUN=length)$flew_prob
dm=aggregate(flew_prob~sex*mass_block, data=d, FUN=mean)
dm$n=aggregate(flew_prob~sex*mass_block, data=d, FUN=length)$flew_prob
# calculate binomial confidence interval
dt$successes = c(sum(d$num_flew[d$sex=="F"]), sum(d$num_flew[d$sex=="M"]))
dt$CI = binom.confint(dt$successes, dt$trials, methods="exact")
```



### 3.2.3 Multi-Variate Models

We used the unique dataset for multi-variate modeling.

```
data < - data.frame(R1 = dc$num_flew,
                 R2 = dc$num_notflew,
                 A = dc host_c
                 B = dc sex_c,
                 C = dc$sym_dist,
                 D = dc$avg_mass_logsqrt,
                 E = dc$avg_days_c)
model_script = pasteO(source_path, "generic models-binomial glm 2R ~ 4-FF + E.R")
errors = catch_warnings(model_comparisonsAIC(model_script))
cat("Number of models that failed to converge: ", length(errors$warnings))
##
          [,1]
                      [,2]
                                 [,3]
                                 684.4483
## AICs
          683.3791
                     683.95
## models 85
                     63
          0.08873418 0.06669969 0.05198815
  probs
##
       glm(formula = cbind(R1, R2) \sim A * D + B * D + C * D + E, family = binomial,
```

```
##
       data = data)
## m63 glm(formula = cbind(R1, R2) ~ A * D + C * D + B + E, family = binomial,
       data = data)
##
## m50 glm(formula = cbind(R1, R2) \sim A * D + B * D + E, family = binomial,
       data = data)
##
## Number of models that failed to converge: 0
anova(m63, m85, test="Chisq") # Adding B*D does not improve fit
anova(m63, m36, test="Chisq") # Adding C*D does improve fit
## Analysis of Deviance Table
## Model 1: cbind(R1, R2) ~ A * D + C * D + B + E
## Model 2: cbind(R1, R2) ~ A * D + B * D + C * D + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          325
                   580.61
           324
                   578.04 1
## 2
                               2.5709
                                        0.1088
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) \sim A * D + C * D + B + E
## Model 2: cbind(R1, R2) ~ A * D + B + C + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
           325
## 1
                   580.61
## 2
           326
                   585.11 -1 -4.4988 0.03392 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
M1 <- glm(cbind(num_flew, num_notflew) ~ host_c * avg_mass_logsqrt
          + sym_dist_s * avg_mass_logsqrt + sex_c + avg_days_c, data=d, family=binomial)
summary(M1)
3.2.3.1 Best Fit
##
## Call:
## glm(formula = cbind(num flew, num notflew) ~ host_c * avg_mass_logsqrt +
       sym_dist_s * avg_mass_logsqrt + sex_c + avg_days_c, family = binomial,
       data = d
##
##
## Deviance Residuals:
                   10
                         Median
                                       30
                                                Max
## -2.54691 -1.08562 -0.03924
                                  1.17713
                                            2.41023
##
## Coefficients:
##
                              Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                               0.03733
                                           0.11152 0.335 0.73785
                                           0.13044 -1.088 0.27643
## host_c
                               -0.14197
## avg_mass_logsqrt
                               -1.00302
                                           0.88134 -1.138 0.25510
                                           0.12352 -0.320 0.74890
## sym_dist_s
                               -0.03954
## sex_c
                                           0.16797 -2.743 0.00609 **
                               -0.46077
                                           0.02596 0.438 0.66111
## avg_days_c
                               0.01138
## host_c:avg_mass_logsqrt
                               1.85594
                                           0.59204
                                                     3.135 0.00172 **
```

```
## avg_mass_logsqrt:sym_dist_s -1.36386     0.66258 -2.058     0.03955 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 668.05 on 332 degrees of freedom
## Residual deviance: 580.61 on 325 degrees of freedom
## AIC: 683.95
##
## Number of Fisher Scoring iterations: 4
```

R2 = data\_fem\$num\_notflew,

### 3.2.4 Multi-Variate Models Split By Sex

```
data_fem <- dc[dc$sex=="F",]
data_fem <- center_data(data_fem, is_not_unique_data = FALSE)

data<-data.frame(R1 = data_fem$num_flew,</pre>
```

```
A = data_fem$host_c,
B = data_fem$sym_dist,
C = data_fem$avg_mass_logsqrt,
D = data_fem$wing2body_logsqrt_i,
E = data_fem$avg_days_c)

model_script = paste0(source_path, "generic models-binomial glm 2R ~ 4-FF + E.R")
errors = catch_warnings(model_comparisonsAIC(model_script))
cat("Number of models that failed to converge: ", length(errors$warnings))
```

### **3.2.4.1** Females

```
[,1]
                     [,2]
                                 [,3]
## AICs
          238.8713
                     239.0635
                                239.8444
## models 45
                     25
## probs 0.08178418 0.07429069 0.0502761
##
## m45 glm(formula = cbind(R1, R2) \sim A * C + A * D + E, family = binomial,
##
       data = data)
       glm(formula = cbind(R1, R2) ~ A * C + D + E, family = binomial,
## m25
       data = data)
## m10 glm(formula = cbind(R1, R2) ~ C + D + E, family = binomial, data = data)
## Number of models that failed to converge: 0
```

```
anova(m25, m45, test='Chisq') #adding A*D does not improve fit
anova(m25, m13, test='Chisq') #adding A*C improves fit
anova(m25, m17, test="Chisq") #adding D improves fit
anova(m25, m45, test="Chisq") #adding D improves fit
```

```
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) ~ A * C + D + E
```

```
## Model 2: cbind(R1, R2) \sim A * C + A * D + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           114
                   202.11
## 2
           113
                   199.92 1
                               2.1922
                                        0.1387
## Analysis of Deviance Table
## Model 1: cbind(R1, R2) \sim A * C + D + E
## Model 2: cbind(R1, R2) ~ A + C + D + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           114
                   202.11
## 2
           115
                   206.87 -1 -4.764 0.02906 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) \sim A * C + D + E
## Model 2: cbind(R1, R2) ~ A * C + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           114
                   202.11
## 2
           115
                   206.35 -1
                               -4.243 0.03941 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
## Model 1: cbind(R1, R2) ~ A * C + D + E
## Model 2: cbind(R1, R2) ~ A * C + A * D + E
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          114
                   202.11
## 2
                   199.92 1
                               2.1922
           113
                                        0.1387
M2 <- glm(cbind(num_flew, num_notflew) ~ host_c * avg_mass_logsqrt + wing2body_logsqrt_i +
            avg_days_c, data=data_fem, family=binomial)
summary(M2)
3.2.4.1.1 Best Fit
##
## Call:
## glm(formula = cbind(num_flew, num_notflew) ~ host_c * avg_mass_logsqrt +
       wing2body logsqrt_i + avg_days_c, family = binomial, data = data fem)
##
## Deviance Residuals:
##
      Min
                 10
                     Median
                                   3Q
                                           Max
## -2.1849 -1.1189 -0.7523
                               1.1182
                                        2.7357
##
## Coefficients:
##
                           Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                       0.34121 -0.466
                                                         0.6409
                           -0.15913
## host c
                           -0.61037
                                       0.33019 - 1.849
                                                          0.0645 .
## avg_mass_logsqrt
                                       1.45468 -1.435
                           -2.08700
                                                          0.1514
## wing2body_logsqrt_i
                           -5.37017
                                       2.66359 -2.016
                                                          0.0438 *
                                                 2.430
                                                          0.0151 *
## avg_days_c
                            0.11558
                                       0.04757
                                       1.39976
## host_c:avg_mass_logsqrt 3.02237
                                                2.159
                                                          0.0308 *
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 223.66 on 119
                                      degrees of freedom
## Residual deviance: 202.11 on 114 degrees of freedom
## AIC: 239.06
##
## Number of Fisher Scoring iterations: 4
data_male <- dc[dc$sex=="M",]</pre>
data_male <- center_data(data_male, is_not_unique_data = FALSE)</pre>
3.2.4.2 Males
## Warning in d$latitude - sym_zone: longer object length is not a multiple of
## shorter object length
data < - data_frame (R1 = data_male num_flew,
                 R2 = data_male$num_notflew,
                 A = data_male$host_c,
                 B = data_male$sym_dist,
                 C = data_male$avg_mass_logsqrt,
                 D = data_male$wing2body_logsqrt_i,
                 E = data_male$avg_days_c)
model_script = pasteO(source_path, "generic models-binomial glm 2R ~ 4-FF + E.R")
errors = catch_warnings(model_comparisonsAIC(model_script))
cat("Number of models that failed to converge: ", length(errors$warnings))
##
          [,1]
                     [,2]
                                 [,3]
                                428.1156
## AICs
          427.3929
                     427.649
## models 105
                     50
                                83
## probs 0.08393807 0.07384843 0.05848274
##
            glm(formula = cbind(R1, R2) \sim A * D + B * C + B * D + C * D +
## m105
       E, family = binomial, data = data)
## m50 glm(formula = cbind(R1, R2) ~ A * D + B * D + E, family = binomial,
##
       data = data)
## m83 glm(formula = cbind(R1, R2) \sim A * D + B * C + B * D + E, family = binomial,
##
       data = data)
## Number of models that failed to converge: 0
anova(m83, m105, test="Chisq") # adding C*D marginally improves fit
anova(m83, m62, test="Chisq") # adding B*C marginally improves fit
anova(m50, m62, test="Chisq") # adding C does not improve fit
## Analysis of Deviance Table
## Model 1: cbind(R1, R2) ~ A * D + B * C + B * D + E
## Model 2: cbind(R1, R2) ~ A * D + B * C + B * D + C * D + E
```

```
##
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          204
                  347.73
## 2
           203
                  345.01 1
                              2.7227 0.09893 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) ~ A * D + B * C + B * D + E
## Model 2: cbind(R1, R2) ~ A * D + B * D + C + E
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
          204
                  347.73
## 2
           205
                  351.01 -1 -3.2786 0.07019 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
## Model 1: cbind(R1, R2) \sim A * D + B * D + E
## Model 2: cbind(R1, R2) ~ A * D + B * D + C + E
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
          206
## 1
                  351.27
## 2
           205
                  351.01 1 0.25488
                                       0.6137
M3<-glm(cbind(num_flew, num_notflew)~host_c*wing2body_logsqrt_i + sym_dist*wing2body_logsqrt_i
        + avg_days_c, family=binomial, data=data_male)
summary(M3)
3.2.4.2.1 Best Fit
##
## Call:
## glm(formula = cbind(num_flew, num_notflew) ~ host_c * wing2body_logsqrt_i +
       sym_dist * wing2body_logsqrt_i + avg_days_c, family = binomial,
##
      data = data male)
## Deviance Residuals:
                    Median
                                          Max
##
      Min
                1Q
                                  3Q
                    0.8309
## -2.6331 -0.7526
                              1.1667
                                       2.0726
##
## Coefficients:
                                Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                                 0.46487
                                            0.22478
                                                    2.068 0.0386 *
## host_c
                                -0.38219
                                            0.18897 -2.023
                                                            0.0431 *
                               -15.20652
## wing2body_logsqrt_i
                                            5.22315 -2.911 0.0036 **
## sym_dist
                                            0.13852
                                                     0.811
                                 0.11229
                                                             0.4176
## avg_days_c
                                -0.03316
                                            0.03421 - 0.969
                                                             0.3323
## host_c:wing2body_logsqrt_i
                              -9.46041
                                            4.27524 -2.213
                                                              0.0269 *
## wing2body_logsqrt_i:sym_dist
                                            3.02643
                                                    2.085
                                                            0.0370 *
                                 6.31131
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 372.15 on 212 degrees of freedom
```

```
## Residual deviance: 351.27 on 206 degrees of freedom
## AIC: 427.65
##
## Number of Fisher Scoring iterations: 4
```

### 4 Between-Trial Flight Response (T1 vs. T2)

### 4.1 Read Libraries

```
library(dplyr) # data manipulation
library(zoo) # data manipulation
library(nnet) # multinomial modeling
library(kableExtra) # table formatting
library(plot.matrix) # enables matrix/heatmap plotting
```

### 4.2 Read Source Files

### 4.3 Read the Data

```
# only keep bugs tested twice
d = create_delta_data(data_tested, remove_bugs_tested_once=TRUE)
```

### 4.4 Encodings & Signs

We aimed to model the probability of different delta flight response cases with sex, host plant, percent changes in mass, and percent changes in egg-laying response as predictors. Since the outcomes (or response variables) were no longer binomial, we used multi-categorical logit models. Below are the categorical encodings and/or signs used. See the Appendix for additional explanations and examples of computing multi-categorical logit models.

| Delta Flight Response Key |          |  |  |
|---------------------------|----------|--|--|
| Event                     | Encoding |  |  |
| flew in both trials       | 2        |  |  |
| flew in T2 only           | 1        |  |  |
| flew in neither trials    | 0        |  |  |
| flew in T1 only           | -1       |  |  |

| Delta Percent Mass Key (%)      |      |  |
|---------------------------------|------|--|
| Event                           | Sign |  |
| gained % mass from T1 to T2     | +    |  |
| no % mass change between trails | 0    |  |
| lost % mass from T1 to T2       | -    |  |

| Host Plant Key         |          |  |
|------------------------|----------|--|
| Host                   | Encoding |  |
| Golden Rain Tree (GRT) | 1        |  |
| Balloon Vine (BV)      | -1       |  |

| Sex Key |          |  |
|---------|----------|--|
| Sex     | Encoding |  |
| Female  | 1        |  |
| Male    | -1       |  |

### 4.5 Multinomial Modeling

### 4.5.1 Baseline

```
# remove any missing values for flight case or mass percent change between trials
df = d[with(d,!is.na(flight_case) & !is.na(mass_per)),]

# order the dataset by ascending mass percent change values
df = df[with(df, order(mass_per)),]

# relevel the flight case factors so as to set 0 as the first level.
df$flight_case = relevel(as.factor(df$flight_case), ref = "0")
```

### 4.5.2 Null Model

```
null = multinom(flight_case ~ 1, data = df)

## # weights: 8 (3 variable)
## initial value 385.389832
## iter 10 value 319.269929
## final value 319.269680
## converged
```

### 4.5.3 Compare Models - predictors: % mass, sex, host

```
model_comparisonsAIC(model_script)
##
          [,1]
                                         [,4]
                    [,2]
                              [,3]
                                         592.4231
## AICs
          587.5607 591.9016 592.3168
## models 4
                    7
                              13
                                         12
## probs 0.7141852 0.0815063 0.06622882 0.06280119
##
## m4
        multinom(formula = R ~ A + B, data = data, trace = FALSE)
## m7
        multinom(formula = R ~ A + B + C, data = data, trace = FALSE)
## m13 multinom(formula = R ~ B * C + A, data = data, trace = FALSE)
## m12 multinom(formula = R ~ A * C + B, data = data, trace = FALSE)
anova(m4, m7, test="Chisq") # Adding C (host plant) does not improve fit
anova(m4, m8, test="Chisq") # Adding A*B does not improve fit
## Likelihood ratio tests of Multinomial Models
##
## Response: R
##
         Model Resid. df Resid. Dev
                                      Test
                                              Df LR stat.
                                                            Pr(Chi)
## 1
         A + B
                     825
                           569.5607
## 2 A + B + C
                     822
                           567.9016 1 vs 2
                                               3 1.659076 0.6460701
## Likelihood ratio tests of Multinomial Models
##
## Response: R
    Model Resid. df Resid. Dev
                                                         Pr(Chi)
                                  Test
                                          Df LR stat.
## 1 A + B
                 825
                       569.5607
## 2 A * B
                 822
                       569.4209 1 vs 2
                                        3 0.1398496 0.9866598
4.5.4 Best Fit
M4 = multinom(flight_case ~ mass_per + sex_c, data = df)
model_table4 = calculate_P2(M4, "mass_per", "sex_c")
## # weights: 16 (9 variable)
## initial value 385.389832
## iter 10 value 286.869825
## iter 20 value 284.809036
## iter 30 value 284.797822
## final value 284.780360
## converged
##
##
   AIC: 587.5607
##
      (Intercept) mass_per sex_c DF
                                       SEi
                                             SE1
                                                   SE2
                                                            zi
                                                                   z1
                                                                            7.2
           -1.015
                     0.043 -0.692 9 0.239 0.010 0.203 -4.248 4.390 -3.408
## -1
## 1
           -6.820
                    -0.009 -5.626 9 0.183 0.026 0.183 -37.245 -0.348 -30.721
                     0.019 -0.902 9 0.167 0.008 0.159
## 2
                                                         0.742 2.334 -5.684
##
         waldi wald1
                        wald2 Pi > |z| P1 > |z| P2 > |z|
        18.049 19.272 11.617
                                 0.000
                                          0.000
                                                   0.001
                                                   0.000
## 1 1387.197 0.121 943.764
                                 0.000
                                          0.728
## 2
         0.551 5.447 32.310
                                 0.458
                                          0.020
                                                   0.000
```

model\_script = pasteO(source\_path, "generic multinomial models- multinom 1RF + 3 FF.R")

Host plant was not a significant predictor, so we tested the wing-to-body ratio as a predictor next.

### 4.5.5 Compare Models - predictors: % mass, sex, wing2body (w2b)

```
df$wing2body_c = df$wing2body - mean(df$wing2body) # re-center the w2b predictor
data = data.frame(R = df$flight case,
                  A = df$mass_per,
                  B = df sex_c,
                  C = df$wing2body_c)
model_script = pasteO(source_path, "generic multinomial models- multinom 1RF + 3 FF.R")
model_comparisonsAIC(model_script)
##
          [,1]
                    [,2]
                              [,3]
## AICs
          582.2678
                    585.1197
                              587.133
## models 7
                    12
                              13
## probs 0.6671688 0.1603139 0.05858546
##
## m7
        multinom(formula = R ~ A + B + C, data = data, trace = FALSE)
## m12 multinom(formula = R ~ A * C + B, data = data, trace = FALSE)
## m13 multinom(formula = R ~ B * C + A, data = data, trace = FALSE)
anova(m7, m12, test="Chisq") # adding A*C does not improve fit
anova(m7, m13, test="Chisq") # Adding B*C does not improve fit
## Likelihood ratio tests of Multinomial Models
##
## Response: R
        Model Resid. df Resid. Dev
                                      Test
                                              Df LR stat.
                                                            Pr(Chi)
## 1 A + B + C
                     822
                           558.2678
## 2 A * C + B
                     819
                           555.1197 1 vs 2
                                               3 3.148182 0.3693379
## Likelihood ratio tests of Multinomial Models
##
## Response: R
         Model Resid. df Resid. Dev
                                      Test
                                              Df LR stat.
                                                            Pr(Chi)
## 1 A + B + C
                     822
                           558.2678
## 2 B * C + A
                     819
                           557.1330 1 vs 2 3 1.134887 0.7686596
4.5.6
     Best Fit
M5 = multinom(flight_case ~ mass_per + sex_c + wing2body_c, data = df)
model_table5 = calculate_P3(M5)
## # weights: 20 (12 variable)
## initial value 385.389832
## iter 10 value 286.740091
## iter 20 value 280.436850
## iter 30 value 279.437125
## iter 40 value 279.174660
## iter 50 value 279.134087
## final value 279.133921
## converged
```

```
##
##
   AIC: 582.2678
##
      (Intercept) mass %
                            sex wing2body DF
                                               SEi
                                                     SE1
                                                           SE2
                                                                  SE<sub>3</sub>
                                                                            zi
## -1
          -0.935 0.041 -0.571
                                   23.739 12 0.243 0.010 0.212 12.059
                                                                       -3.854
## 1
           -8.177 -0.005 -6.954
                                   -6.595 12 0.187 0.025 0.187 18.786 -43.767
            0.201 0.018 -0.760
                                   28.094 12 0.172 0.008 0.166 9.718
## 2
##
          z1
                  z2
                               waldi
                                     wald1
                                               wald2 wald3 Pi>|z| P1>|z| P2>|z|
## -1 4.254 -2.698 1.969
                              14.850 18.096
                                               7.278 3.875 0.000 0.000 0.007
## 1 -0.215 -37.102 -0.351 1915.510 0.046 1376.550 0.123 0.000
                                                                   0.830 0.000
       2.141 -4.590 2.891
                               1.375 4.585
## 2
                                              21.071 8.357 0.241 0.032 0.000
##
     P3>|z|
## -1 0.049
## 1
       0.726
       0.004
## 2
```

### 4.5.7 Prediction Equations

```
get_prediction_eq = function(tb, table_rowA, table_rowB, var_lab1, var_lab2, var_lab3,
                             log_lab, title_lab) {
  I = (tb[table_rowA,1] - tb[table_rowB,1])
 M = (tb[table_rowA,2] - tb[table_rowB,2])
  S = (tb[table_rowA,3] - tb[table_rowB,3])
  W = (tb[table_rowA,4] - tb[table_rowB,4])
  EQ = paste0(log_lab, round(I, 2), " + ", round(M,2), var_lab1, " + ", round(S, 2),
               var_lab2, " + ", round(W, 2), var_lab3, title_lab)
 print(EQ)
 return(EQ)
}
EQ1 = get_prediction_eq(model_table5, 1, 2, " Mass %", " Sex", " Wing-to-Body",
                        "log(pi_-1 / pi_1) = "," Flew in T1, not T2")
EQ2 = get_prediction_eq(model_table5, 3, 1, " Mass %", " Sex", " Wing-to-Body",
                        "log(pi_2 / pi_-1) = ", "
                                                  Flew in both, not T1" )
EQ3 = get_prediction_eq(model_table5, 3, 2, " Mass %", " Sex", " Wing-to-Body",
                        "log(pi_2 / pi_1) = ", " Flew in both, not T2")
```

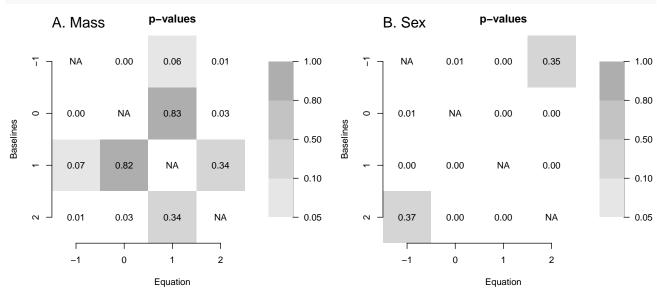
```
## [1] "log(pi_-1 / pi_1) = 7.24 + 0.05 Mass % + 6.38 Sex + 30.33 Wing-to-Body Flew in T1, n
## [1] "log(pi_2 / pi_-1) = 1.14 + -0.02 Mass % + -0.19 Sex + 4.36 Wing-to-Body Flew in both
## [1] "log(pi_2 / pi_1) = 8.38 + 0.02 Mass % + 6.19 Sex + 34.69 Wing-to-Body Flew in both,
```

### 4.5.8 Visualize Significant Multinomial Functions

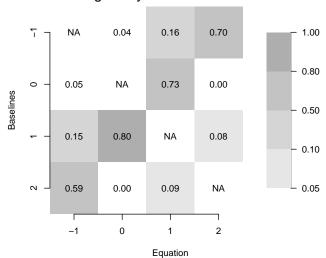
```
# define a run_multinom_model function based on the best fit model
run_multinom_model = function(d) {
    m = multinom(flight_case ~ mass_per + sex_c + wing2body_c, trace=FALSE, data = d)
    model_table = calculate_P3(m, print_table=FALSE)
    return(model_table)
}

# determine which multinomial model equations are significant with a plot
par(mfrow=c(2,2))
mass_per_ML = get_significant_models(19) # % mass
    mtext("A. Mass", side=3, adj=0, line=0.5, cex=1.3, font=1)
```

```
sex_ML = get_significant_models(20) # sex
mtext("B. Sex", side=3, adj=0, line=0.5, cex=1.3, font=1)
w2b_ML = get_significant_models(21) # wing2body
mtext("C. Wing2Body", side=3, adj=0, line=0.5, cex=1.3, font=1)
```



# C. Wing2Body p-values



```
[,2]
              [,1]
                                          [,3]
                                                      [,4]
##
## [1,]
                NA -0.041168533 -0.047132139 -0.02329390
## [2,] 0.04121460
                              NA -0.005450321
                                                0.01790830
## [3,] 0.04699220
                    0.005882702
                                                0.02378072
## [4,] 0.02331345 -0.017835748 -0.023938109
                                                        NA
##
                            [,2]
                                                      [,4]
              [,1]
                                          [,3]
## [1,]
                NA -0.041168533 -0.047132139 -0.02329390
## [2,] 0.04121460
                              NA -0.005450321
                                                0.01790830
## [3,] 0.04699220 0.005882702
                                                0.02378072
## [4,] 0.02331345 -0.017835748 -0.023938109
                                                        NA
                            [,2]
                                                      [,4]
              [,1]
                                          [,3]
## [1,]
                NA -0.041168533 -0.047132139 -0.02329390
## [2,] 0.04121460
                              NA -0.005450321
                                                0.01790830
## [3,] 0.04699220 0.005882702
                                            NA
                                                0.02378072
## [4,] 0.02331345 -0.017835748 -0.023938109
                                                        NA
```

### 4.5.9 Plot Predicted Probabilities

```
head(pp <- fitted(M4),3) # compute fitted values of the best fit model without wing-to-body ra
##
## 1 0.7917303 0.03003973 4.362037e-06 0.1782256
## 2 0.7894639 0.03073036 4.325625e-06 0.1798015
## 3 0.7844677 0.03228066 4.247094e-06 0.1832474
                                                                                            female
               Did Not Fly
                                                                                            male
Flight Case Probability
                                                                       Flew in T1 only
    9.0
    0.4
                                       Flew Twice
    0.2
    0.0
          -40
                      -20
                                              20
                                                          40
                                                                       60
                                                                                   80
                                                                                              100
                                   Percent Mass Change From T1 to T2 (%)
head(pp <- fitted(M5), 3) # compute fitted values of the best fit model with wing-to-body rati
## 1 0.7470322 0.03581826 2.459149e-07 0.2171493
## 2 0.8116776 0.02845344 2.925412e-07 0.1598686
## 3 0.6983200 0.04316854 2.166785e-07 0.2585113
        В
                                                                                          Wing-to-body
          Females
                                                          Males
                      Did Not Fly
                                        0.68
                                                                                0.70
                                  0.62
    0.8
Flight Case Probability
                                                     9.0
                                Flew in T1 only
                                                     0.4
                                                                            Flew in T1 only
                                       Flew Twice
                                                     0.2
                                                                                            Did Not Fly
                                                          lew in T2 only
```

-20

20

Percent Mass Change from T1 to T2 (%)

40

60

20

-20

40

Percent Change in Mass From T1 to T2 (%)

60

80

100

### 4.6 Multinomial Modeling (Females Only)

### **4.6.1** Egg Case

| Delta Egg Response Key      |          |  |
|-----------------------------|----------|--|
| Event                       | Encoding |  |
| laid eggs in both trials    | 2        |  |
| laid eggs in T2 only        | 1        |  |
| laid eggs in neither trials | 0        |  |
| laid eggs in T1 only        | -1       |  |

### 4.6.2 Baseline

##

```
# filter for females &
# remove any missing values for flight case, mass percent change, and egg case between trials
df = d[with(d,!is.na(flight_case) & !is.na(mass_per) & !is.na(egg_case) & sex=="F"),]
# order the dataset by ascending mass percent change values
df = df[with(df, order(mass_per)),]
# relevel the flight case factors so as to set 0 as the first level.
df$flight_case = relevel(as.factor(df$flight_case), ref = "0")
unique(df$flight_case) # no female bug only flew in T2, so can drop factor "1"
df$flight_case = droplevels(df$flight_case)
## [1] 2 0 -1
## Levels: 0 -1 1 2
4.6.3 Null model
null <- multinom(flight_case ~ 1, data = df)</pre>
## # weights: 6 (2 variable)
## initial value 102.170943
## final value 93.055466
## converged
```

### 4.6.4 Comparing Models - predictors: % mass, egg diff, host

```
data <- data.frame(R = df$flight_case,</pre>
         A = df$egg_case,
         B = df$mass_per,
         C = df$host c)
model_script = pasteO(source_path, "generic multinomial models- multinom 1RF + 3 FF.R")
model_comparisonsAIC(model_script)
##
                                [,3]
          [,1]
                     [,2]
                                          [,4]
                                                      [5]
                                                                  [,6]
## AICs
          164.3817
                     165.6054
                               166.336
                                          167.5638
                                                      167.9891
                                                                 168.3593
## models 7
                     4
                               13
                                          11
                                                      16
                                                                 12
## probs 0.3761191 0.2039899 0.1415644 0.07661927 0.06194208 0.0514745
```

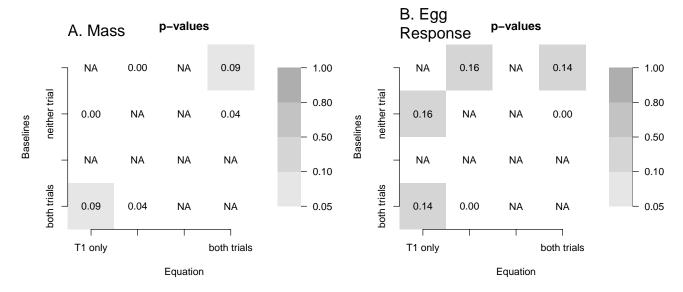
```
## m7
        multinom(formula = R ~ A + B + C, data = data, trace = FALSE)
## m4
        multinom(formula = R ~ A + B, data = data, trace = FALSE)
       multinom(formula = R ~ B * C + A, data = data, trace = FALSE)
## m13
## m11
       multinom(formula = R ~ A * B + C, data = data, trace = FALSE)
## m16
       multinom(formula = R ~ B * C + A * B, data = data, trace = FALSE)
## m12 multinom(formula = R ~ A * C + B, data = data, trace = FALSE)
anova(m4, m7, test="Chisq") # Adding C does not improve fit
anova(m7, m13, test="Chisq") # Adding mass_per*host does not improve fit
## Likelihood ratio tests of Multinomial Models
##
## Response: R
##
         Model Resid. df Resid. Dev
                                       Test
                                               Df LR stat.
                                                             Pr(Chi)
## 1
         A + B
                     180
                           153.6054
## 2 A + B + C
                     178
                           148.3817 1 vs 2
                                                2 5.223671 0.0733997
## Likelihood ratio tests of Multinomial Models
## Response: R
##
         Model Resid. df Resid. Dev
                                       Test
                                               Df LR stat.
                                                             Pr(Chi)
## 1 A + B + C
                     178
                           148.3817
## 2 B * C + A
                     176
                           146.3360 1 vs 2
                                               2 2.045698 0.3595691
Host plant was not a significant predictor for females as well, so we tested the wing-to-body ratio as a
predictor next.
      Comparing Models - predictors: % mass, egg diff, wing2body
4.6.5
##
          [,1]
                    [,2]
                               [,3]
                                         [,4]
## AICs
          164.5293
                    164.9831
                              165.6054
                                         167.7955
## models 7
                    13
## probs 0.3174096 0.2529723 0.1853291 0.06199495
##
## m7
        multinom(formula = R ~ A + B + C, data = data, trace = FALSE)
## m13 multinom(formula = R ~ B * C + A, data = data, trace = FALSE)
## m4
        multinom(formula = R ~ A + B, data = data, trace = FALSE)
## m12 multinom(formula = R ~ A * C + B, data = data, trace = FALSE)
anova(m4, m7, test="Chisq") # adding wing2body does not improve fit
anova(m7, m13, test="Chisq") # Adding A*C does not improve fit
anova(m7, m12, test="Chisq") # Adding B*C does not improve fit
## Likelihood ratio tests of Multinomial Models
##
## Response: R
         Model Resid. df Resid. Dev
##
                                       Test
                                               Df LR stat.
                                                              Pr(Chi)
## 1
         A + B
                     180
                           153.6054
## 2 A + B + C
                     178
                           148.5293 1 vs 2
                                                2 5.07612 0.07901956
## Likelihood ratio tests of Multinomial Models
```

##

```
## Response: R
        Model Resid. df Resid. Dev Test Df LR stat. Pr(Chi)
## 1 A + B + C
                    178
                          148.5293
## 2 B * C + A
                     176
                          144.9831 1 vs 2
                                             2 3.546174 0.169808
## Likelihood ratio tests of Multinomial Models
## Response: R
        Model Resid. df Resid. Dev
                                     Test
                                             Df LR stat.
                                                            Pr(Chi)
## 1 A + B + C
                    178
                          148.5293
## 2 A * C + B
                    176
                          147.7955 1 vs 2 2 0.7337197 0.6929067
4.6.6 Best Fit
M6 = multinom(flight_case ~ mass_per + egg_case, data = df) # same top model
model_table6 = calculate_P2(M6, "mass_per", "egg_case")
## # weights: 12 (6 variable)
## initial value 102.170943
## iter 10 value 76.802714
## final value 76.802689
## converged
##
## AIC: 165.6054
##
      (Intercept) mass_per egg_case DF
                                        SEi
                                              SE1
                                                    SE2
                                                            zi
                                                                  z1
## -1
                    0.041
                            -0.533 6 0.617 0.012 0.380 -1.539 3.389 -1.402 2.370
          -0.950
                            -1.098 6 0.424 0.011 0.297 0.957 2.038 -3.700 0.917
            0.406
                    0.022
      wald1 wald2 Pi > |z| P1 > |z| P2 > |z|
## -1 11.488 1.966
                      0.124
                               0.001
                                        0.161
## 2 4.154 13.693
                      0.338
                               0.042
                                        0.000
4.6.7 Prediction Equations
get_prediction_eq = function(tb, table_rowA, table_rowB, var_lab1, var_lab2,
                            log_lab, title_lab) {
 I = (tb[table_rowA,1] - tb[table_rowB,1])
 M = (tb[table_rowA,2] - tb[table_rowB,2])
  E = (tb[table_rowA,3] - tb[table_rowB,3])
 EQ = pasteO(log_lab, round(I, 2), " + ", round(M, 2), var_lab1, " + ", round(E, 2),
              var_lab2, title_lab)
 print(EQ)
 return(EQ)
}
EQ = get_prediction_eq(model_table6, 1, 2, " Mass %", " Egg Case",
                        "log(pi_-1 / pi_1) = "," Flew in T1, not T2")
## [1] "log(pi_-1 / pi_1) = -1.36 + 0.02 Mass % + 0.56 Egg Case Flew in T1, not T2"
4.6.8 Visualize Significant Multinomial Functions
# define a run_multinom_model function based on the best fit model
run_multinom_model = function(d) {
 m <- multinom(flight_case ~ mass_per + egg_case, trace=FALSE, data = d)
```

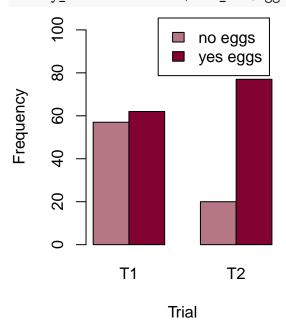
```
model_table = calculate_P2(m, "mass_per", "egg_case", print_table=FALSE)
return(model_table)
}

# determine which multinomial model equations are significant with a plot
par(mfrow=c(1,2))
mass_per_ML = get_significant_modelsf(15) # mass_per
mtext("A. Mass", side=3, adj=0, line=0.5, cex=1.6, font=1)
egg_case_ML = get_significant_modelsf(16) # egg_case
mtext("B. Egg \nResponse", side=3, adj=0, line=0.3, cex=1.6, font=1)
```



### 4.6.9 Barplot

```
data_fem = data_tested[data_tested$sex=="F",]
binary_counts <- table(data_fem$eggs_b, data_fem$trial_type)[,2:3]</pre>
```



Notice that female bugs were laying more during the second trial (T2) than the first trial (T1).

### 4.6.10 Plot Predicted Probabilities

```
head(pp <- fitted(M6),3)

## 0 -1 2

## 1 0.3182776 0.04652361 0.63519881

## 2 0.7833277 0.04039434 0.17627792

## 3 0.9015654 0.02877502 0.06965959

Females Only
```

# Pilot Not Fly Did Not Fly Flew in T1 only Flew Twice Flew Twice

40

Percent Change in Mass From T1 to T2 (%)

60

80

100

20

### 5 Fall 2019 Data Cleaning

-20

0

### 5.1 Read Libraries

-40

```
library(cvms) # cross-validating regressions
```

### 5.2 Read Source Files

### 5.3 Read the Data

```
data_path = pasteO(dir,"/Dispersal/Winter_2020/stats/data/full_data-Fall2019.csv")
dataFall = clean_flight_data.Fall(data_path)

# extract sets with an experimental design similar to the Winter tests
```

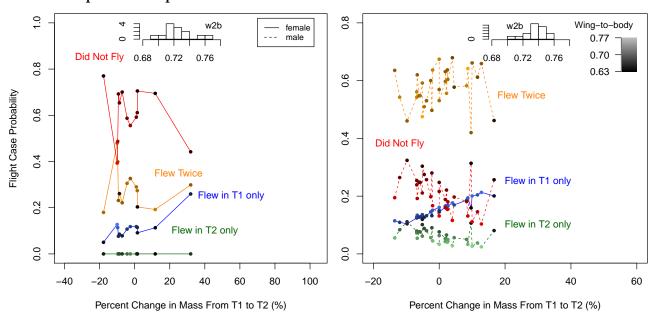
```
ongoing_data = dataFall[with(dataFall,!is.na(mass) & set_number > 71),]
# create delta data
d = create_delta_data.Fall(ongoing_data)
```

## 6 Flight Response Predictions

### 6.1 Compute predicted probabilities

```
d <- d[with(d, order(mass_per)),]</pre>
neither = c()
T1_rather_than_none = c()
T2_rather_than_none = c()
both_rather_than_none = c()
for (i in 1:nrow(d)) {
  m = d$mass_per[[i]]
  s = dsex_c[[i]]
  w = dswing2body_c[i]
  # extract effects from the best fit model
  top0 = exp(0) # equals 1
  top1 = exp(model_table5[1,1] + model_table5[1,2]*m + model_table5[1,3]*s + model_table5[1,4]
  top2 = exp(model_table5[2,1] + model_table5[2,2]*m + model_table5[2,3]*s + model_table5[2,4]
  top3 = exp(model_table5[3,1] + model_table5[3,2]*m + model_table5[3,3]*s + model_table5[3,4]
  bottom = top0 + top1 + top2 + top3
  # calculate predicted probabilities
  neither = c(neither, top0/bottom)
  T1_rather_than_none = c(T1_rather_than_none, top1/bottom)
  T2_rather_than_none = c(T2_rather_than_none, top2/bottom)
  both_rather_than_none = c(both_rather_than_none, top3/bottom)
}
```

### 6.2 Plot predicted probabilities

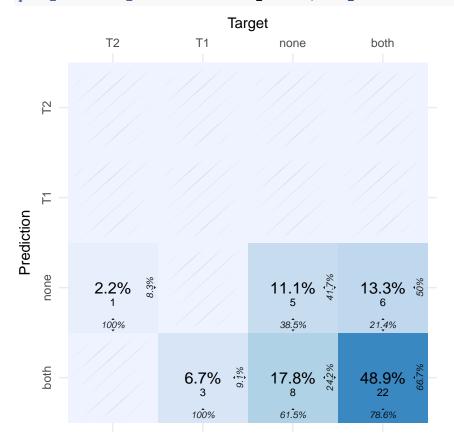


### 6.3 Overall and Grouped Accuracies

```
probs = round(cbind(neither, T1_rather_than_none, T2_rather_than_none, both_rather_than_none),
summary_probs = cbind(as.character(d$flight_case), as.character(d$sex), probs)
colnames(summary_probs) = c("event", "sex", "none", "T1", "T2", "both")
dataframe = as.data.frame(summary_probs)
nrow(dataframe)
## [1] 45
# overall
acc = calculate_accuracy(dataframe,3,6)
paste("Overall prediction accuracy, ", round(acc,2))
# by sex
femdata = dataframe[dataframe$sex=="F",]
maledata = dataframe[dataframe$sex=="M",]
accF = calculate_accuracy(femdata,3,6)
paste("Female prediction accuracy, ", round(accF,2))
accM = calculate_accuracy(maledata,3,6)
paste("Male prediction accuracy, ", round(accM,2))
## [1] "Overall prediction accuracy, 0.6"
## [1] "Female prediction accuracy, 0.38"
## [1] "Male prediction accuracy, 0.69"
6.4
    Confusion Matrix
acc_table = get_confusion_matrix(dataframe,3,6)
acc_table[,1:5]
## # A tibble: 1 x 5
     `Overall Accuracy` `Balanced Accuracy`
                                                F1 Sensitivity Specificity
                  <dbl>
##
                                      <dbl> <dbl>
                                                         <dbl>
                                                                      <dbl>
## 1
                    0.6
                                      0.538
                                               NaN
                                                         0.293
                                                                      0.784
confusion_matrix <- acc_table$'Confusion Matrix'[[1]]</pre>
confusion_matrix
## # A tibble: 16 x 3
##
      Prediction Target
                            N
      <chr>
                <chr> <int>
##
##
   1 both
                both
                           22
   2 none
                both
##
                            6
   3 T1
##
                 both
                            0
##
   4 T2
                both
                            0
                            8
## 5 both
                 none
   6 none
                            5
##
                 none
##
   7 T1
                            0
                 none
   8 T2
                            0
##
                 none
## 9 both
                 T1
                            3
## 10 none
                 T1
                            0
## 11 T1
                 T1
                            0
## 12 T2
                            0
                 Т1
## 13 both
                 T2
                            0
```

```
## 14 none T2 1
## 15 T1 T2 0
## 16 T2 T2 0
```

```
plot_confusion_matrix(confusion_matrix, add_sums=FALSE)
```



### 6.5 Females

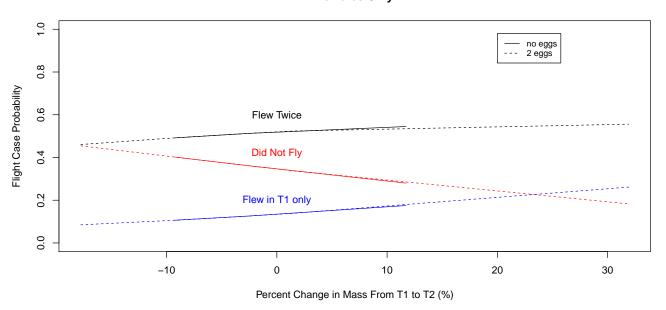
```
dfem = d[d$sex=="F",]
dfem <- dfem[with(dfem, order(mass_per)),]</pre>
neither = c()
T1_rather_than_none = c()
both_rather_than_none = c()
for (i in 1:nrow(dfem)) {
  M = dfem$mass_per[[i]]
  EC = dfem$egg_diff[[i]]
  top0 = exp(0) # equals 1
  top1 = exp(model_table6[1,1] + model_table6[1,2]*M + model_table6[1,3]*EC)
  top2 = exp(model_table6[2,1] + model_table6[2,2]*M + model_table6[2,3]*EC)
  bottom = top0 + top1 + top2
  neither = c(neither, top0/bottom)
  T1_rather_than_none = c(T1_rather_than_none, top1/bottom)
  both_rather_than_none = c(both_rather_than_none, top2/bottom)
}
```

### 6.5.1 Compute predicted probabilities

```
probs = round(cbind(neither, T1_rather_than_none, both_rather_than_none),2)
summary_probs = cbind(as.character(dfem\flight_case), as.character(dfem\flight), probs)
colnames(summary_probs) = c("event", "egg_diff", "none", "T1", "both")
egg2 = c(1,2,3,5,6,7,9,10,11,13)
noegg = c(4,8,12)
dataframe = as.data.frame(summary_probs)
dataframe = c(2,2,2,0,2,2,2,0,2,2,2,0,2)
```

### 6.5.2Plot predicted probabilities

### **Females Only**



### Overall and Grouped Accuracies

both

```
accF_eggs = calculate_accuracy(dataframe,3,5)
paste("Female prediction accuracy for mass diff and egg model, ", round(accF_eggs,2))
```

## 1 both

```
6.5.4 Confusion Matrix
acc_table = get_confusion_matrix(dataframe,3,5)
acc_table[,1:5]
## # A tibble: 1 x 5
     `Overall Accuracy` `Balanced Accuracy`
                                                 F1 Sensitivity Specificity
##
                   <dbl>
                                        <dbl> <dbl>
                                                           <dbl>
                                                                       <dbl>
## 1
                   0.462
                                          0.5
                                                NaN
                                                           0.333
                                                                       0.667
confusion_matrix <- acc_table$'Confusion Matrix'[[1]]</pre>
confusion_matrix
## # A tibble: 9 x 3
     Prediction Target
##
                            Ν
##
     <chr>
                <chr> <int>
```

| ## | 2 | none | both | 0 |
|----|---|------|------|---|
| ## | 3 | T2   | both | 0 |
| ## | 4 | both | none | 6 |
| ## | 5 | none | none | 0 |
| ## | 6 | T2   | none | 0 |
| ## | 7 | both | T2   | 1 |
| ## | 8 | none | T2   | 0 |
| ## | 9 | T2   | T2   | 0 |

plot\_confusion\_matrix(confusion\_matrix, add\_sums=FALSE)

