# Appendix B: Modeling Flight Response

for 'paper\_title'; Bernat, AV, Cenzer, ML

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# Details of the Analyses

This document was generated by R Markdown on 2021-12-07 using R version 4.0.5 (2021-03-31). The document provides the step-by-step analytical methods used in the manuscript by Anastasia Bernat (AVB) and Meredith Cenzer (MLC). Multiple draft scripts were written by AVB and MLC between 2020-03-01 and 2021-07-26 until being distilled and complied by AVB and code reviewed by MLC at the University of Chicago into this comprehensive script. All draft scripts can be viewed in the GitHub repository, SBB-dispersal (https://github.com/mlcenzer/SBB-dispersal), within the directory avbernat > Dispersal > Winter\_2020 > stats .

All code and output from the statistical analyses are shown. Code for data cleaning and the generation of plots is not displayed, but can be viewed in the **appendix\_B-flight\_summary.Rmd** file and its accompanying sourced scripts. To repeat analyses and the generation of plots, all data files and sourced scripts should follow the directory structure presented in the SBB-dispersal repository.

# Description of the Data

Soapberry bugs, Jadera haematoloma, were flight tested in the Fall 2019 (2019-10-15 to 2019-11-08) and Winter 2020 (2020-02-17 to 2020-03-10) seasons using a flight mill machine. Soapberry bugs were flight tested twice for either set time increments or multiple hours in the flight mill and observed from 8 AM to (5-8 PM) each day. For each trial, the mass, flight response, egg-laying response, distance, duration, average speed, and max speed of each soapberry bug was recorded and then processed. All Python scripts used to process the flight records are located in the GitHub repository within the directory avbernat\_working\_on > Dispersal > Winter\_2020 > windaq\_processing . After trials, morphology measurements were taken for each bug. There are four morphology measurements: beak length, thorax width, wing length, and body length. The sex, wing morph (long-winged, shot-winged, or ambiguously-winged), host plant, and population of each bug were also recorded.

As a result of the experimental design, this document analyzes two main types of datasets: a full dataset and a unique dataset. A **full dataset** is a dataset where each row has a unique ID and trial type. A **unique dataset** is a dataset where each row has a unique ID because each trial has been grouped by ID. Examples are provided below. The advantage of generating a unique dataset is that changes between trials can be observed and analyzed.

# Abbreviations Used in the Data and Code

- SBB soapberry bug, Jadera haematoloma
- S short-winged morph
- L long-winged morph
- LS or SL ambiguous wing morph
- **T1** trial 1 of flight testing
- **T2** trial 2 of flight testing
- EWM eggs when massed, binary response (yes or no)
- host\_\_ the host plant soapberry bugs were collected from, which was either *Koelreuteria elegans* or *Cardiospermum corindum*, occasionally called (and abbreviated) as goldenrain tree (GRT) or balloon vine (BV), respectively
- $\bullet$  sym\_dist distance from the local sympatric zone, which is demarked as Homestead
- wing2body a computed and unitless column that calculates the wing length divided by the body length of a soapberry bug
- sd standard deviation
- se standard error
- w\_ a column name that starts with w\_ is abbreviated from "wing". Example column: w\_morph is "wing morph"

#### **Data Transformations**

- \_b a column name that ends in \_b is a column that has been recodified into binary data (0's and 1's). Example columns: flew\_b, eggs\_b
- \_c a column name that ends in \_c is a column that has been centered. Example columns: sex\_c, host\_c, avg\_days\_c
- \_s a column name that ends in \_s is a column that has been standardized. Example columns: wing2body\_s, sym\_dist\_s, thorax\_s
- avg\_ a column name that starts in avg\_ is a column that has been averaged across trial 1 (T1) and trial 2 (T2). Example columns: avg\_mass, avg\_days, avg\_time\_start, avg\_rec\_dur (exception: average\_speed)
- \_diff a column name that ends in \_diff is a column that is the difference between T1 and T2 data values. Formula: data values
- \_per a column name that ends in \_per is a column that is the percent change between T1 and T2 (T2-T1) data values. Formula: (T2-T1)/T1 \* 100.
- \_logsqrt a column name that ends in \_logsqrt is a column that has been normalized using a log-square-root transformation. Formula: log(sqrt(<data\_column>))-mean(log(sqrt(<data\_column>)). Example columns: avg\_mass\_logsqrt
- \_logsqrt\_i a column name that ends in \_logsqrt\_i is a column that has been normalized using a log-square-root transformation but its sign is the inverse of the column. Formula: log(sqrt(0.85-column))-mean(log(sqrt(0.85-column)). Example columns: wing2body\_logsqrt\_i (AB FLAG: max value is this 0.7633366)

# Winter 2020 Data Cleaning

#### Read Libraries

The flight response of *J. haematoloma* was analyzed using multivariate, generalized linear modeling (GLM) as implemented in the R packages lme4 and binom. All plots, except the histogram, were generated using base R and supplemented with the popbio package to display logistic regressions and the rethinking package to display 95% confidence intervals of linear regressions. The histogram below was generated using ggplot libraries and helper functions found in ggformula package.

Additional R packages not show below, but embedded in the sourced scripts are lubridate, chron, and dplyr. lubridate and chron both aid in datetime manipulation while dplry pipelines data grouping processes.

```
library(lme4) # fit regressions
library(rethinking) # Bayesian data analysis and plotting
library(popbio) # logistic regression plotting
library(binom) # binomial confidence intervals
library(ggformula) # ggplot plotting
```

#### Read Source Files

Each sourced script below aides in either data cleaning (read\_flight\_data(), center\_data()) or multivariate GLM (model\_comparisonsAIC(), get\_model\_probs(), catch\_warnings()). Additionally, the function model\_comparisonsAIC() takes in the path of a generic multi-factor script specific to the GLM family and link function needed to build the predictive models. All aforementioned, sourced scripts are located in the Rscr folder.

#### Read the Data

The flight performance data read directly below is only from Winter 2020 flight trials. The read\_flight\_data() function standardizes data types and names of the ID, trial type, host plant, flight response, egg-laying response, sex, population, and wing morph inputs. The date, start time, and end time of trails are also converted into datetimes. Variables of interest like wing-to-body ratio are also calculated and centered. Using the clean\_flight\_data function, all morphology, mass, and flight performance measurements are centered and/or standardized within the read\_flight\_data() function. Then, full dataset (n=758) that includes all bugs collected during Winter 2020 and a subset of the full dataset (n=614) that includes only bugs tested from that collection are returned.

The create\_delta\_data() function generates the unique dataset by grouping by ID. The function also computes trial differences, percent differences, and averages for variables of interest such as mass, flight response, egg-laying response, distance, and speed. Then, the unique data variables are centered and/or standardized.

```
data_path = paste0(dir, "/Dispersal/Winter_2020/stats/data/all_flight_data-Winter2020.csv")
data = read_flight_data(data_path) # centers each subset of data
data all = data[[1]]
                                     # full dataset
data_tested = data[[2]]
                                    # subset of data_all, contains only bugs flight tested
# create the unique dataset
d <- create_delta_data(data_tested, remove_bugs_tested_once = FALSE)</pre>
# keep all bugs (even bugs only tested once), then re-center
dc <- center_data(d, is_not_unique_data = FALSE)</pre>
Example of a full dataset (each row has unique ID and trial type):
data_tested[c(1:2,400:401), c("ID", "trial_type")]
##
        ID trial_type
## 1
                    T1
       114
## 2
                    T1
       318
## 400 316
                    T2
## 401 416
                    T2
Example of a unique dataset (each row has unique ID):
dc[c(1:2,295:296), c("ID", "trial_type")]
## # A tibble: 4 x 2
```

The datatype of the trial\_type column is a list because when expanded out, it would show list(T1, T2).

# Across-Trial Flight Response (T1 & T2)

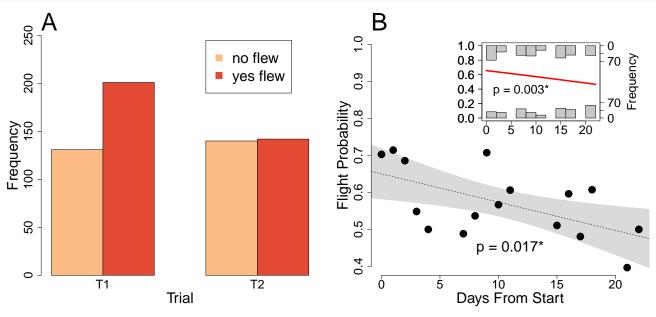
Flight response (yes flew or did not fly) was recorded and modeled. Multivariate, GLM was performed using the glm() function in the lme4 package. Models were compared using Akaike Information Criterion (AIC) and model selection was determined using Akaike weights. Model fit was further evaluated between two models using the anova() function.

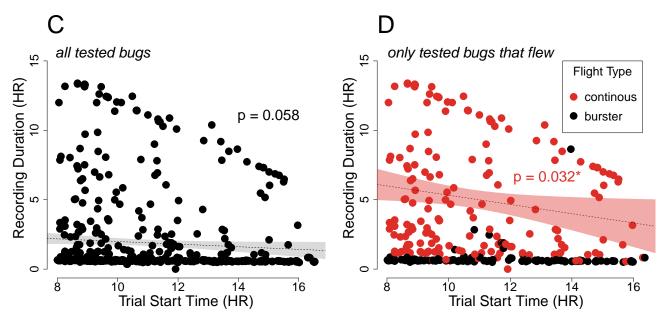
## **Experimental Effects**

To determine how the design of the experiment affected flight response and/or performance, three design factors were modeled: trial type (T1 vs. T2), days from start, and trial start time.

### Trial Type, Days from Start & Trial Start Time

```
# compute how many times flew yes or no per trial
binary_counts = table(data_tested$flew_b, data_tested$trial_type)[,2:3]
# aggregate by days since the trials began and flight response to determine flight prob
dd = aggregate(flew_b ~ days_from_start, data=data_tested, FUN=mean)
```





**A** & **B.** There was a negative effect of day a bug was tested (since the start of trials) on flight probability, but there was a significant effect only when the full dataset is considered. It is not significant for the unique dataset because days from start had to be averaged between trials. This is explored in the next section of the report. **C** & **D**. There was a negative effect of the trial start time on flight duration but only after removing bugs that did not fly (p = 0.031). Continuous flyers are driving this significant relationship (**D**).

# **Binomial Modeling**

## [1] 1.464596

To understand SBB flight response, flight response across trials was modeled against sex, host plant, distance from the sympatric zone, wing-to-body ratio, and mass. This was done using the unique dataset.

Because the unique dataset was used, there exist multiple recorded counts of the number of times a SBB flew and did not fly between trials, T1 and T2. For that reason, we used cbind(num\_flew, num\_notflew) when modeling in order to account for all flight successes and failures for each individual.

Finally, we tested whether the data was over-dispersed, which could be resolved using a Quasibinomial:

```
# calculate the confidence interval for the mean of the data (Binomial vs. Quasibinomial)
fit <- glm(cbind(num_flew, num_notflew) ~ 1, family = binomial, data = dc)
plogis(confint(fit))

## 2.5 % 97.5 %
## 0.5191729 0.5976031
fit_q <- glm(cbind(num_flew, num_notflew) ~ 1, family = quasibinomial, data = dc)
plogis(confint(fit_q))

## 2.5 % 97.5 %
## 0.5108508 0.6056992
# estimate the dispersion parameter
summary(fit_q)$dispersion</pre>
```

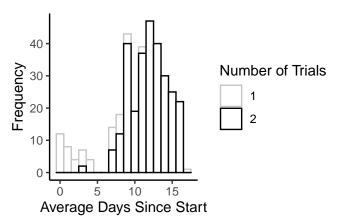
If the dispersion parameter is close to 1, the data is not over-dispersed, so there is not much of a necessity to apply a Quasibinomial model. Therefore, we selected the family as "binomial".

#### Average Days Since Start

For the unique dataset, average days since start (log-square-root transformed) was computed in order to determine how an experimental factor affected flight response. It proved to not be significant:

```
avg_days_model<-glm(cbind(num_flew,num_notflew)~avg_days_c, data=dc, family=binomial)
summary(avg_days_model)</pre>
```

```
##
## Call:
   glm(formula = cbind(num_flew, num_notflew) ~ avg_days_c, family = binomial,
       data = dc)
##
##
  Deviance Residuals:
##
                       Median
       Min
                  1Q
                                     3Q
##
                                             Max
##
   -1.8429
            -1.7825
                      -0.1593
                                1.5162
                                          1.5795
##
   Coefficients:
##
##
               Estimate Std. Error z value Pr(>|z|)
                0.22942
                            0.08236
                                       2.785
                                              0.00535 **
##
   (Intercept)
  avg_days_c
                0.01087
                            0.02354
                                       0.462
                                              0.64430
##
##
                    0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 668.05
                               on 332
                                        degrees of freedom
## Residual deviance: 667.84
                               on 331
                                        degrees of freedom
## AIC: 759.17
##
## Number of Fisher Scoring iterations: 3
```



Average days since start accounts for bugs who died before they could be tested twice, which would most likely lead to an early average day value. The rest of the bugs that were tested twice would most likely have a later average day value. This testing regime shapes the bimodal distribution seen in the histogram. Additionally, the advantage of this computed variable is that it controls for the fact that some bugs were tested once late, and some by chance had been tested twice early. In turn, because we randomized test day, when repeated measures for each individual are combined across days, they balance each other out. Thus, average days since start allows the multi-variate models, which control for repeated tests per ID number, to converge, and we can be confident that non-random mortality is not impacting flight response. [[AB FLAG: "can be confident..." not so founded...]]

#### Single-Variate Effects

We used aggregated datasets for single-variate modeling.

```
# tailoring variables for plotting
d$mass_block=round(d$avg_mass/0.005)*0.005
                                                        # 0.005 q blocks
d$wing2body_block=round(d$wing2body, digits=2)
                                                        # 0.01 blocks
d$days_block=round(d$avg_days, digits=0)
                                                        # integer blocks
# aggregate data for plotting
dt=aggregate(flew_prob~sex, data=d, FUN=mean)
dt$trials=c(sum(d$num flew[d$sex=="F"]+d$num notflew[d$sex=="F"]),
              sum(d$num_flew[d$sex=="M"]+d$num_notflew[d$sex=="M"]))
ds=aggregate(flew_prob~sex*wing2body_block, data=d, FUN=mean)
ds$n=aggregate(flew_prob~sex*wing2body_block, data=d, FUN=length)$flew_prob
dm=aggregate(flew_prob~sex*mass_block, data=d, FUN=mean)
dm$n=aggregate(flew_prob~sex*mass_block, data=d, FUN=length)$flew_prob
# calculate binomial confidence interval
dt$successes = c(sum(d$num_flew[d$sex=="F"]), sum(d$num_flew[d$sex=="M"]))
dt$CI = binom.confint(dt$successes, dt$trials, methods="exact")
  1.0
                                   1.0
                                                                    1.0
                                         male
                                                                                         male
                                                                                 p = 0.2
                                         female
                                                                                         female
  0.8
Flight probability 0.4 0.6
                                                                  Flight probability 0.4
                                 Flight probability 0.6
                                        p = 2e - 04
                                                                                  p = 0.001*
  0.2
                                   0.2
                                                                    0.2
                                                    p = 0.24
       N = 120
                    N = 213
  0.0
                                                                    0.0
                                                                           0.05
                                            0.68 0.70 0.72 0.74
                                                              0.76
                                                                                   0.10
                                                                                          0.15
         female
                      male
                                    0.64
                                         0.66
                                                                                 Mass (g)
                Sex
                                            Wing-to-body ratio
```

# Multi-Variate Models

We used the unique dataset for multi-variate modeling.

```
[,2]
                                 [,3]
##
          [,1]
## AICs
          683.3791
                     683.95
                                 684.4483
## models 85
                     63
                                50
## probs 0.08873418 0.06669969 0.05198815
##
## m85 glm(formula = cbind(R1, R2) \sim A * D + B * D + C * D + E, family = binomial,
##
       data = data)
## m63 glm(formula = cbind(R1, R2) \sim A * D + C * D + B + E, family = binomial,
       data = data)
## m50 glm(formula = cbind(R1, R2) \sim A * D + B * D + E, family = binomial,
##
       data = data)
## Number of models that failed to converge: 0
anova(m63, m85, test="Chisq") # Adding B*D does not improve fit
anova(m63, m36, test="Chisq") # Adding C*D does improve fit
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) ~ A * D + C * D + B + E
## Model 2: cbind(R1, R2) \sim A * D + B * D + C * D + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
           325
                   580.61
## 2
           324
                   578.04
                          1
                               2.5709
                                         0.1088
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) ~ A * D + C * D + B + E
## Model 2: cbind(R1, R2) ~ A * D + B + C + E
##
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           325
                   580.61
## 2
           326
                   585.11 -1 -4.4988 0.03392 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
M1 <- glm(cbind(num_flew, num_notflew) ~ host_c * avg_mass_logsqrt
          + sym_dist_s * avg_mass_logsqrt + sex_c + avg_days_c, data=d, family=binomial)
summary(M1)
Best Fit
##
## Call:
## glm(formula = cbind(num_flew, num_notflew) ~ host_c * avg_mass_logsqrt +
##
       sym_dist_s * avg_mass_logsqrt + sex_c + avg_days_c, family = binomial,
##
       data = d
## Deviance Residuals:
                         Median
                                        3Q
##
        Min
                   1Q
                                                 Max
## -2.54691 -1.08562 -0.03924
                                  1.17713
                                             2.41023
##
## Coefficients:
##
                               Estimate Std. Error z value Pr(>|z|)
```

```
## (Intercept)
                              0.03733
                                         0.11152 0.335 0.73785
                                         0.13044 -1.088 0.27643
## host_c
                             -0.14197
## avg_mass_logsqrt
                             -1.00302
                                         0.88134 -1.138 0.25510
## sym_dist_s
                             -0.03954
                                         0.12352 -0.320 0.74890
## sex_c
                             -0.46077
                                         0.16797 -2.743 0.00609 **
## avg_days_c
                                         0.02596 0.438 0.66111
                              0.01138
## host_c:avg_mass_logsqrt
                              1.85594
                                         0.59204 3.135 0.00172 **
## avg mass logsqrt:sym dist s -1.36386
                                         0.66258 -2.058 0.03955 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 668.05 on 332 degrees of freedom
## Residual deviance: 580.61 on 325 degrees of freedom
## AIC: 683.95
##
## Number of Fisher Scoring iterations: 4
```

## Multi-Variate Models Split By Sex

#### **Females**

```
[,2]
##
          [,1]
                                 [,3]
## AICs
          238.8713
                     239.0635
                                239.8444
                     25
## models 45
                                 10
## probs 0.08178418 0.07429069 0.0502761
##
## m45 glm(formula = cbind(R1, R2) ~ A * C + A * D + E, family = binomial,
##
       data = data)
## m25 glm(formula = cbind(R1, R2) \sim A * C + D + E, family = binomial,
       data = data)
## m10 glm(formula = cbind(R1, R2) ~ C + D + E, family = binomial, data = data)
## Number of models that failed to converge: 0
```

```
anova(m25, m45, test='Chisq') #adding A*D does not improve fit
anova(m25, m13, test='Chisq') #adding A*C improves fit
anova(m25, m17, test="Chisq") #adding D improves fit
anova(m25, m45, test="Chisq") #adding D improves fit
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) \sim A * C + D + E
## Model 2: cbind(R1, R2) \sim A * C + A * D + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
           114
                   202.11
## 1
## 2
           113
                   199.92 1
                               2.1922
                                        0.1387
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) \sim A * C + D + E
## Model 2: cbind(R1, R2) \sim A + C + D + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           114
                   202.11
## 2
           115
                   206.87 -1
                              -4.764 0.02906 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) \sim A * C + D + E
## Model 2: cbind(R1, R2) ~ A * C + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           114
                   202.11
## 2
           115
                   206.35 -1
                               -4.243 0.03941 *
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
## Model 1: cbind(R1, R2) \sim A * C + D + E
## Model 2: cbind(R1, R2) ~ A * C + A * D + E
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           114
                   202.11
## 2
                   199.92 1
           113
                               2.1922
                                        0.1387
M2 <- glm(cbind(num_flew, num_notflew) ~ host_c * avg_mass_logsqrt + wing2body_logsqrt_i +
            avg_days_c, data=data_fem, family=binomial)
summary(M2)
Best Fit
##
## Call:
## glm(formula = cbind(num_flew, num_notflew) ~ host_c * avg_mass_logsqrt +
       wing2body_logsqrt_i + avg_days_c, family = binomial, data = data_fem)
##
##
## Deviance Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -2.1849 -1.1189 -0.7523
                                        2.7357
                               1.1182
##
```

```
## Coefficients:
##
                           Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                           -0.15913
                                       0.34121 -0.466
                                                          0.6409
## host_c
                           -0.61037
                                       0.33019 -1.849
                                                          0.0645 .
## avg_mass_logsqrt
                           -2.08700
                                       1.45468 -1.435
                                                          0.1514
## wing2body_logsqrt_i
                                       2.66359 -2.016
                                                          0.0438 *
                           -5.37017
## avg_days_c
                            0.11558
                                       0.04757
                                                 2.430
                                                          0.0151 *
## host_c:avg_mass_logsqrt 3.02237
                                      1.39976
                                                2.159
                                                          0.0308 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 223.66 on 119 degrees of freedom
## Residual deviance: 202.11 on 114 degrees of freedom
## AIC: 239.06
##
## Number of Fisher Scoring iterations: 4
data_male <- dc[dc$sex=="M",]</pre>
data_male <- center_data(data_male, is_not_unique_data = FALSE)</pre>
Males
## Warning in d$latitude - sym_zone: longer object length is not a multiple of
## shorter object length
data < - data .frame (R1 = data male $ num flew,
                 R2 = data_male$num_notflew,
                 A = data_male$host_c,
                 B = data_male$sym_dist,
                 C = data_male$avg_mass_logsqrt,
                 D = data_male$wing2body_logsqrt_i,
                 E = data_male$avg_days_c)
model_script = paste0(source_path, "generic models-binomial glm 2R ~ 4-FF + E.R")
errors = catch_warnings(model_comparisonsAIC(model_script))
cat("Number of models that failed to converge: ", length(errors$warnings))
##
          [,1]
                     [,2]
                                [,3]
## AICs
          427.3929
                     427.649
                                428.1156
## models 105
                     50
                                83
## probs 0.08393807 0.07384843 0.05848274
##
## m105
            glm(formula = cbind(R1, R2) \sim A * D + B * C + B * D + C * D +
       E, family = binomial, data = data)
##
## m50 glm(formula = cbind(R1, R2) \sim A * D + B * D + E, family = binomial,
       data = data)
## m83 glm(formula = cbind(R1, R2) \sim A * D + B * C + B * D + E, family = binomial,
       data = data)
##
## Number of models that failed to converge: 0
```

```
anova(m83, m105, test="Chisq") # adding C*D marginally improves fit
anova(m83, m62, test="Chisq") # adding B*C marginally improves fit
anova(m50, m62, test="Chisq") # adding C does not improve fit
## Analysis of Deviance Table
## Model 1: cbind(R1, R2) ~ A * D + B * C + B * D + E
## Model 2: cbind(R1, R2) ~ A * D + B * C + B * D + C * D + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           204
                   347.73
## 2
           203
                   345.01 1
                               2.7227 0.09893 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
##
## Model 1: cbind(R1, R2) \sim A * D + B * C + B * D + E
## Model 2: cbind(R1, R2) \sim A * D + B * D + C + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           204
                   347.73
## 2
           205
                   351.01 -1 -3.2786 0.07019 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Analysis of Deviance Table
## Model 1: cbind(R1, R2) ~ A * D + B * D + E
## Model 2: cbind(R1, R2) ~ A * D + B * D + C + E
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           206
                   351.27
           205
## 2
                   351.01 1 0.25488
                                        0.6137
M3<-glm(cbind(num_flew, num_notflew)~host_c*wing2body_logsqrt_i + sym_dist*wing2body_logsqrt_i
        + avg_days_c, family=binomial, data=data_male)
summary(M3)
Best Fit
##
## Call:
## glm(formula = cbind(num_flew, num_notflew) ~ host_c * wing2body_logsqrt_i +
       sym_dist * wing2body_logsqrt_i + avg_days_c, family = binomial,
##
       data = data_male)
##
##
## Deviance Residuals:
                     Median
      Min
                 10
                                   30
                                           Max
## -2.6331 -0.7526
                     0.8309
                               1.1667
                                        2.0726
##
## Coefficients:
                                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                                  0.46487
                                             0.22478
                                                       2.068
                                                               0.0386 *
                                             0.18897 -2.023
## host_c
                                 -0.38219
                                                                0.0431 *
## wing2body_logsqrt_i
                                -15.20652
                                             5.22315
                                                      -2.911
                                                                0.0036 **
## sym_dist
                                  0.11229
                                             0.13852
                                                       0.811
                                                                0.4176
## avg_days_c
                                 -0.03316
                                             0.03421 - 0.969
                                                                0.3323
```

```
## host_c:wing2body_logsqrt_i
                                -9.46041
                                            4.27524
                                                    -2.213
                                                              0.0269 *
## wing2body_logsqrt_i:sym_dist
                                 6.31131
                                            3.02643
                                                      2.085
                                                              0.0370 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 372.15 on 212
                                     degrees of freedom
## Residual deviance: 351.27 on 206 degrees of freedom
## AIC: 427.65
## Number of Fisher Scoring iterations: 4
```

# Between-Trial Flight Response (T1 vs. T2)

#### Read Libraries

```
library(dplyr) # data manipulation
library(zoo) # data manipulation
library(nnet) # multinomial modeling
library(kableExtra) # table formatting
library(plot.matrix) # enables matrix/heatmap plotting
```

#### Read Source Files

#### Read the Data

```
# only keep bugs tested twice
d = create_delta_data(data_tested, remove_bugs_tested_once=TRUE)
```

# Encodings & Signs

We aimed to model the probability of different delta flight response cases with sex, host plant, percent changes in mass, and percent changes in egg-laying response as predictors. Since the outcomes (or response variables) were no longer binomial, we used multi-categorical logit models. Below are the categorical encodings and/or signs used. See the Appendix for additional explanations and examples of computing multi-categorical logit models.

Delta Flight Response Key		
Event	Encoding	
flew in both trials	2	
flew in T2 only	1	
flew in neither trials	0	
flew in T1 only	-1	

Delta Percent Mass Key (%)		
Event	Sign	
gained % mass from T1 to T2	+	
no % mass change between trails	0	
lost % mass from T1 to T2	-	

Host Plant Key		
Host	Encoding	
Golden Rain Tree (GRT)	1	
Balloon Vine (BV)	-1	

Sex Key			
Sex	Encoding		
Female	1		
Male	-1		

# Multinomial Modeling

#### Baseline

```
# remove any missing values for flight case or mass percent change between trials
df = d[with(d,!is.na(flight_case) & !is.na(mass_per)),]

# order the dataset by ascending mass percent change values
df = df[with(df, order(mass_per)),]

# relevel the flight case factors so as to set 0 as the first level.
df$flight_case = relevel(as.factor(df$flight_case), ref = "0")
```

## Null Model

```
null = multinom(flight_case ~ 1, data = df)

## # weights: 8 (3 variable)

## initial value 385.389832

## iter 10 value 319.269929

## final value 319.269680
```

Compare Models - predictors: % mass, sex, host

```
data = data.frame(R = df$flight_case,
         A = df$mass_per,
         B = df sex_c
         C = df$host_c)
model_script = pasteO(source_path, "generic multinomial models- multinom 1RF + 3 FF.R")
model_comparisonsAIC(model_script)
##
          [,1]
                    [,2]
                              [,3]
                                         [,4]
## AICs
         587.5607 591.9016 592.3168
                                         592.4231
## models 4
                    7
                              13
## probs 0.7141852 0.0815063 0.06622882 0.06280119
##
       multinom(formula = R ~ A + B, data = data, trace = FALSE)
## m4
       multinom(formula = R ~ A + B + C, data = data, trace = FALSE)
## m7
## m13 multinom(formula = R ~ B * C + A, data = data, trace = FALSE)
## m12 multinom(formula = R \sim A * C + B, data = data, trace = FALSE)
anova(m4, m7, test="Chisq") # Adding C (host plant) does not improve fit
anova(m4, m8, test="Chisq") # Adding A*B does not improve fit
## Likelihood ratio tests of Multinomial Models
##
## Response: R
        Model Resid. df Resid. Dev Test
                                             Df LR stat.
                                                            Pr(Chi)
## 1
        A + B
                     825
                           569.5607
## 2 A + B + C
                     822
                           567.9016 1 vs 2
                                               3 1.659076 0.6460701
## Likelihood ratio tests of Multinomial Models
##
## Response: R
   Model Resid. df Resid. Dev
                                  Test Df LR stat.
                                                         Pr(Chi)
## 1 A + B
                825
                       569.5607
## 2 A * B
                822
                       569.4209 1 vs 2
                                         3 0.1398496 0.9866598
Best Fit
M4 = multinom(flight_case ~ mass_per + sex_c, data = df)
model_table4 = calculate_P2(M4, "mass_per", "sex_c")
## # weights: 16 (9 variable)
## initial value 385.389832
## iter 10 value 286.869825
## iter 20 value 284.809036
## iter 30 value 284.797822
## final value 284.780360
## converged
##
##
  AIC: 587.5607
      (Intercept) mass_per sex_c DF
                                       SEi
                                             SE1
                                                   SE2
                                                                           z2
                                                            zi
                                                                   z1
## -1
          -1.015 0.043 -0.692 9 0.239 0.010 0.203 -4.248 4.390 -3.408
```

```
-0.009 -5.626 9 0.183 0.026 0.183 -37.245 -0.348 -30.721
## 1
          -6.820
                                                       0.742 2.334 -5.684
## 2
           0.124
                    0.019 -0.902 9 0.167 0.008 0.159
##
                       wald2 Pi > |z| P1 > |z| P2 > |z|
        waldi wald1
## -1
       18.049 19.272 11.617
                                0.000
                                         0.000
                                                  0.001
## 1 1387.197 0.121 943.764
                                0.000
                                         0.728
                                                  0.000
        0.551 5.447 32.310
                                0.458
                                         0.020
                                                  0.000
## 2
```

Host plant was not a significant predictor, so we tested the wing-to-body ratio as a predictor next.

```
Compare Models - predictors: % mass, sex, wing2body (w2b)

df$wing2body_c = df$wing2body - mean(df$wing2body) # re-center the w2b predictor
```

```
## AICs 582.2678 585.1197 587.133
## models 7 12 13
## probs 0.6671688 0.1603139 0.05858546
##
## m7 multinom(formula = R ~ A + B + C, data = data, trace = FALSE)
## m12 multinom(formula = R ~ A * C + B, data = data, trace = FALSE)
## m13 multinom(formula = R ~ B * C + A, data = data, trace = FALSE)
```

[,3]

```
anova(m7, m12, test="Chisq") # adding A*C does not improve fit
anova(m7, m13, test="Chisq") # Adding B*C does not improve fit
```

```
## Likelihood ratio tests of Multinomial Models
##
## Response: R
         Model Resid. df Resid. Dev
##
                                      Test
                                              Df LR stat.
                                                             Pr(Chi)
## 1 A + B + C
                     822
                           558.2678
## 2 A * C + B
                     819
                           555.1197 1 vs 2
                                               3 3.148182 0.3693379
## Likelihood ratio tests of Multinomial Models
##
## Response: R
         Model Resid. df Resid. Dev
                                      Test
                                              Df LR stat.
                                                             Pr(Chi)
## 1 A + B + C
                     822
                           558.2678
## 2 B * C + A
                     819
                           557.1330 1 vs 2
                                              3 1.134887 0.7686596
```

#### Best Fit

##

[,1]

[,2]

```
M5 = multinom(flight_case ~ mass_per + sex_c + wing2body_c, data = df)
model_table5 = calculate_P3(M5)
```

```
## # weights: 20 (12 variable)
```

```
## initial value 385.389832
## iter 10 value 286.740091
## iter 20 value 280.436850
## iter 30 value 279.437125
## iter 40 value 279.174660
## iter 50 value 279.134087
## final value 279.133921
## converged
##
   AIC: 582.2678
##
                           sex wing2body DF
##
      (Intercept) mass %
                                             SEi
                                                   SE1
                                                         SE2
                                                                SF.3
## -1
          -0.935 0.041 -0.571 23.739 12 0.243 0.010 0.212 12.059
                                                                    -3.854
## 1
          -8.177 -0.005 -6.954
                                 -6.595 12 0.187 0.025 0.187 18.786 -43.767
                                  28.094 12 0.172 0.008 0.166 9.718
## 2
           0.201 0.018 -0.760
##
                 z2
                        z3
                              waldi wald1
                                             wald2 wald3 Pi>|z| P1>|z| P2>|z|
         z1
                                             7.278 3.875 0.000 0.000 0.007
## -1 4.254 -2.698 1.969
                             14.850 18.096
## 1 -0.215 -37.102 -0.351 1915.510 0.046 1376.550 0.123 0.000 0.830
                                                                       0.000
## 2
      2.141 -4.590 2.891
                           1.375 4.585
                                            21.071 8.357 0.241 0.032 0.000
##
     P3>|z|
## -1 0.049
      0.726
## 1
## 2
      0.004
```

#### **Prediction Equations**

```
get_prediction_eq = function(tb, table_rowA, table_rowB, var_lab1, var_lab2, var_lab3,
                             log_lab, title_lab) {
 I = (tb[table_rowA,1] - tb[table_rowB,1])
 M = (tb[table_rowA,2] - tb[table_rowB,2])
 S = (tb[table rowA,3] - tb[table rowB,3])
  W = (tb[table_rowA,4] - tb[table_rowB,4])
 EQ = pasteO(log_lab, round(I, 2), " + ", round(M, 2), var_lab1, " + ", round(S, 2),
               var_lab2, " + ", round(W, 2), var_lab3, title_lab)
 print(EQ)
 return(EQ)
}
EQ1 = get_prediction_eq(model_table5, 1, 2, " Mass %", " Sex", " Wing-to-Body",
                        "log(pi_-1 / pi_1) = "," Flew in T1, not T2")
EQ2 = get_prediction_eq(model_table5, 3, 1, " Mass %", " Sex", " Wing-to-Body",
                        \log(pi_2 / pi_-1) = ", " Flew in both, not T1")
EQ3 = get_prediction_eq(model_table5, 3, 2, " Mass %", " Sex", " Wing-to-Body",
                        "log(pi_2 / pi_1) = ", " Flew in both, not T2")
```

# Visualize Significant Multinomial Functions

```
# define a run_multinom_model function based on the best fit model
run_multinom_model = function(d) {
   m = multinom(flight_case ~ mass_per + sex_c + wing2body_c, trace=FALSE, data = d)
```

## [1] "log( $pi_2$  /  $pi_1$ ) = 8.38 + 0.02 Mass % + 6.19 Sex + 34.69 Wing-to-Body Flew in both,

## [1]  $\log(pi_1) = 7.24 + 0.05 \text{ Mass } \% + 6.38 \text{ Sex} + 30.33 \text{ Wing-to-Body}$ 

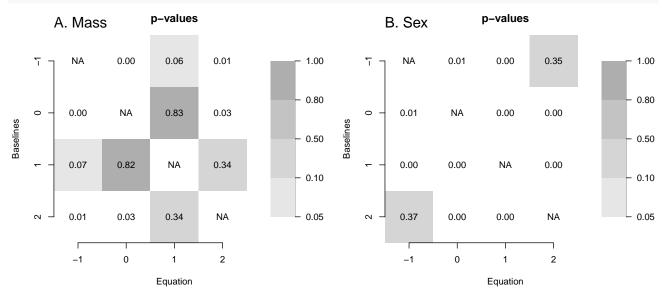
## [1] "log(pi\_2 / pi\_-1) = 1.14 + -0.02 Mass % + -0.19 Sex + 4.36 Wing-to-Body

Flew in T1, n

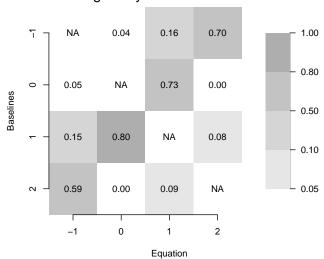
Flew in both

```
model_table = calculate_P3(m, print_table=FALSE)
  return(model_table)
}

# determine which multinomial model equations are significant with a plot
par(mfrow=c(2,2))
mass_per_ML = get_significant_models(19) # % mass
  mtext("A. Mass", side=3, adj=0, line=0.5, cex=1.3, font=1)
sex_ML = get_significant_models(20) # sex
  mtext("B. Sex", side=3, adj=0, line=0.5, cex=1.3, font=1)
w2b_ML = get_significant_models(21) # wing2body
  mtext("C. Wing2Body", side=3, adj=0, line=0.5, cex=1.3, font=1)
```



# C. Wing2Body p-values



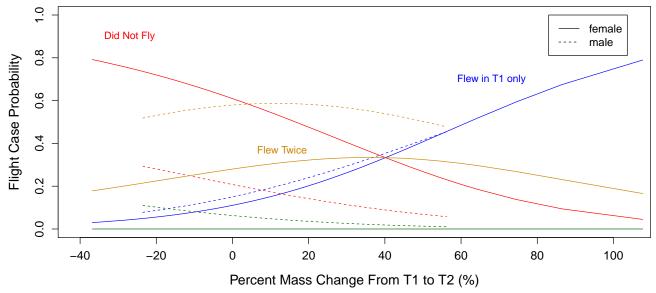
```
##
              [,1]
                                          [,3]
                                                       [,4]
                            [,2]
## [1,]
                NA -0.041168533 -0.047132139 -0.02329390
## [2,] 0.04121460
                              NA -0.005450321
                                                0.01790830
## [3,] 0.04699220
                                                0.02378072
                    0.005882702
                                            NA
## [4,] 0.02331345 -0.017835748 -0.023938109
                                                        NA
##
              [,1]
                            [,2]
                                          [,3]
                                                       [,4]
## [1,]
                NA -0.041168533 -0.047132139 -0.02329390
## [2,] 0.04121460
                              NA -0.005450321
                                                0.01790830
```

```
## [3,] 0.04699220 0.005882702
                                               0.02378072
## [4,] 0.02331345 -0.017835748 -0.023938109
                                                       NA
                                                     [,4]
##
              [,1]
                            [,2]
                                         [,3]
## [1,]
                NA -0.041168533 -0.047132139 -0.02329390
## [2,] 0.04121460
                             NA -0.005450321
                                               0.01790830
## [3,] 0.04699220 0.005882702
                                               0.02378072
                                           NA
## [4,] 0.02331345 -0.017835748 -0.023938109
                                                       NA
```

#### Plot Predicted Probabilities

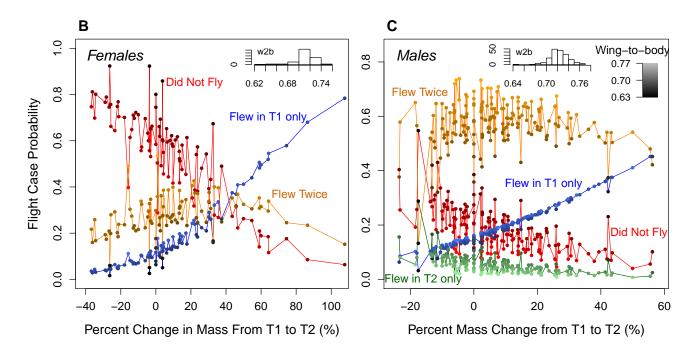
head(pp <- fitted(M4),3) # compute fitted values of the best fit model without wing-to-body ra

```
## 0 -1 1 2
## 1 0.7917303 0.03003973 4.362037e-06 0.1782256
## 2 0.7894639 0.03073036 4.325625e-06 0.1798015
## 3 0.7844677 0.03228066 4.247094e-06 0.1832474
```



head(pp <- fitted(M5), 3) # compute fitted values of the best fit model with wing-to-body rati

```
## 0 -1 1 2
## 1 0.7470322 0.03581826 2.459149e-07 0.2171493
## 2 0.8116776 0.02845344 2.925412e-07 0.1598686
## 3 0.6983200 0.04316854 2.166785e-07 0.2585113
```



## Multinomial Modeling (Females Only)

null <- multinom(flight\_case ~ 1, data = df)</pre>

Egg Case

Delta Egg Response Key		
Event	Encoding	
laid eggs in both trials	2	
laid eggs in T2 only	1	
laid eggs in neither trials	0	
laid eggs in T1 only	-1	

#### Baseline

```
# filter for females &
# remove any missing values for flight case, mass percent change, and egg case between trials
df = d[with(d,!is.na(flight_case) & !is.na(mass_per) & !is.na(egg_case) & sex=="F"),]
# order the dataset by ascending mass percent change values
df = df[with(df, order(mass_per)),]
# relevel the flight case factors so as to set 0 as the first level.
df$flight_case = relevel(as.factor(df$flight_case), ref = "0")
unique(df$flight_case) # no female bug only flew in T2, so can drop factor "1"
df$flight_case = droplevels(df$flight_case)
## [1] 2 0 -1
## Levels: 0 -1 1 2
Null model
```

```
## final value 93.055466
## converged
Comparing Models - predictors: % mass, egg diff, host
data <- data.frame(R = df$flight_case,</pre>
         A = df$egg_case,
         B = df$mass_per,
         C = df$host_c)
model_script = pasteO(source_path, "generic multinomial models- multinom 1RF + 3 FF.R")
model_comparisonsAIC(model_script)
##
          [,1]
                     [,2]
                               [,3]
                                         [,4]
                                                     [,5]
                                                                [,6]
          164.3817
## AICs
                    165.6054 166.336
                                         167.5638
                                                     167.9891
                                                                168.3593
## models 7
                    4
                               13
                                         11
                                                     16
                                                                12
## probs 0.3761191 0.2039899 0.1415644 0.07661927 0.06194208 0.0514745
##
        multinom(formula = R ~ A + B + C, data = data, trace = FALSE)
## m7
## m4
        multinom(formula = R ~ A + B, data = data, trace = FALSE)
## m13 multinom(formula = R ~ B * C + A, data = data, trace = FALSE)
## m11 multinom(formula = R ~ A * B + C, data = data, trace = FALSE)
## m16 multinom(formula = R ~ B * C + A * B, data = data, trace = FALSE)
## m12 multinom(formula = R ~ A * C + B, data = data, trace = FALSE)
anova(m4, m7, test="Chisq") # Adding C does not improve fit
anova(m7, m13, test="Chisq") # Adding mass_per*host does not improve fit
## Likelihood ratio tests of Multinomial Models
##
## Response: R
##
         Model Resid. df Resid. Dev
                                       Test
                                               Df LR stat.
                                                              Pr(Chi)
## 1
         A + B
                     180
                            153.6054
## 2 A + B + C
                     178
                            148.3817 1 vs 2
                                                2 5.223671 0.0733997
## Likelihood ratio tests of Multinomial Models
##
## Response: R
         Model Resid. df Resid. Dev
##
                                       Test
                                               Df LR stat.
                                                              Pr(Chi)
## 1 A + B + C
                     178
                            148.3817
## 2 B * C + A
                     176
                            146.3360 1 vs 2
                                                2 2.045698 0.3595691
Host plant was not a significant predictor for females as well, so we tested the wing-to-body ratio as a
predictor next.
```

```
Comparing Models - predictors: % mass, egg diff, wing2body
```

```
## AICs 164.5293 164.9831 165.6054 167.7955
## models 7 13 4 12
## probs 0.3174096 0.2529723 0.1853291 0.06199495
```

## # weights: 6 (2 variable)
## initial value 102.170943

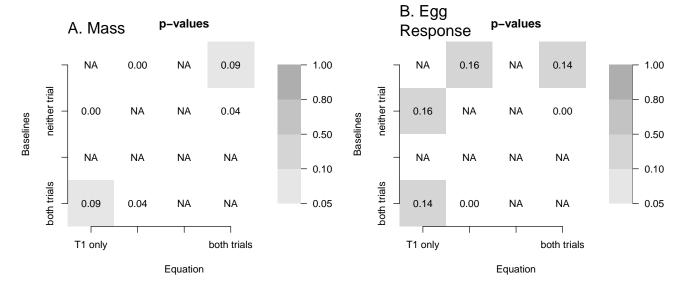
```
##
        multinom(formula = R ~ A + B + C, data = data, trace = FALSE)
## m7
## m13 multinom(formula = R \sim B * C + A, data = data, trace = FALSE)
## m4
       multinom(formula = R ~ A + B, data = data, trace = FALSE)
## m12 multinom(formula = R ~ A * C + B, data = data, trace = FALSE)
anova(m4, m7, test="Chisq") # adding wing2body does not improve fit
anova(m7, m13, test="Chisq") # Adding A*C does not improve fit
anova(m7, m12, test="Chisq") # Adding B*C does not improve fit
## Likelihood ratio tests of Multinomial Models
##
## Response: R
##
         Model Resid. df Resid. Dev
                                      Test
                                              Df LR stat.
                                                             Pr(Chi)
                     180
## 1
         A + B
                           153.6054
## 2 A + B + C
                     178
                           148.5293 1 vs 2
                                               2 5.07612 0.07901956
## Likelihood ratio tests of Multinomial Models
## Response: R
##
         Model Resid. df Resid. Dev
                                      Test
                                              Df LR stat. Pr(Chi)
## 1 A + B + C
                 178
                           148.5293
## 2 B * C + A
                     176
                           144.9831 1 vs 2
                                               2 3.546174 0.169808
## Likelihood ratio tests of Multinomial Models
##
## Response: R
         Model Resid. df Resid. Dev
                                      Test
                                              Df LR stat.
                                                             Pr(Chi)
## 1 A + B + C
                     178
                           148.5293
## 2 A * C + B
                     176
                           147.7955 1 vs 2
                                             2 0.7337197 0.6929067
Best Fit
M6 = multinom(flight_case ~ mass_per + egg_case, data = df) # same top model
model_table6 = calculate_P2(M6, "mass_per", "egg_case")
## # weights: 12 (6 variable)
## initial value 102.170943
## iter 10 value 76.802714
## final value 76.802689
## converged
##
   AIC: 165.6054
##
      (Intercept) mass_per egg_case DF
                                         SEi
                                               SE1
                                                     SE2
##
                                                             zi
                                                                   z1
          -0.950
                             -0.533 6 0.617 0.012 0.380 -1.539 3.389 -1.402 2.370
## -1
                     0.041
## 2
                             -1.098 6 0.424 0.011 0.297 0.957 2.038 -3.700 0.917
            0.406
                     0.022
       wald1 wald2 Pi > |z| P1 > |z| P2 > |z|
## -1 11.488 1.966
                       0.124
                                0.001
                                         0.161
     4.154 13.693
                       0.338
                                0.042
                                         0.000
Prediction Equations
get_prediction_eq = function(tb, table_rowA, table_rowB, var_lab1, var_lab2,
                             log_lab, title_lab) {
 I = (tb[table_rowA,1] - tb[table_rowB,1])
```

## [1] "log(pi\_-1 / pi\_1) = -1.36 + 0.02 Mass % + 0.56 Egg Case Flew in T1, not T2"

#### Visualize Significant Multinomial Functions

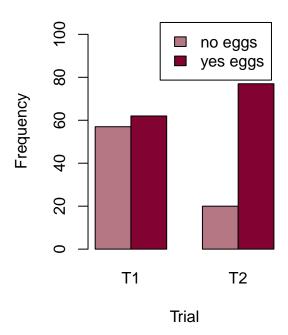
```
# define a run_multinom_model function based on the best fit model
run_multinom_model = function(d) {
    m <- multinom(flight_case ~ mass_per + egg_case, trace=FALSE, data = d)
    model_table = calculate_P2(m, "mass_per", "egg_case", print_table=FALSE)
    return(model_table)
}

# determine which multinomial model equations are significant with a plot
par(mfrow=c(1,2))
mass_per_ML = get_significant_modelsf(15) # mass_per
    mtext("A. Mass", side=3, adj=0, line=0.5, cex=1.6, font=1)
egg_case_ML = get_significant_modelsf(16) # egg_case
    mtext("B. Egg \nResponse", side=3, adj=0, line=0.3, cex=1.6, font=1)</pre>
```



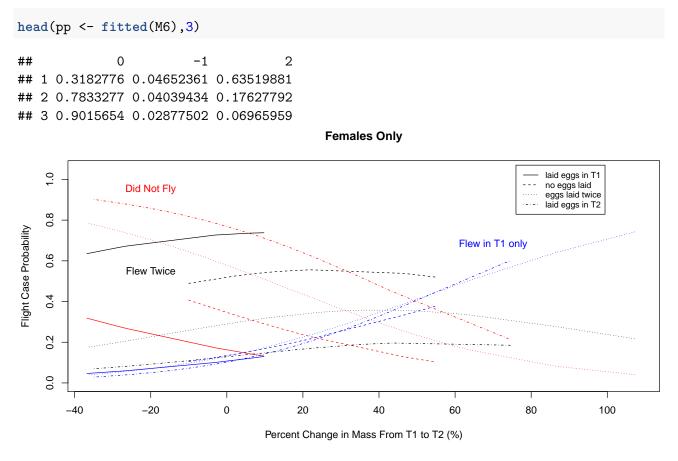
#### **Barplot**

```
data_fem = data_tested[data_tested$sex=="F",]
binary_counts <- table(data_fem$eggs_b, data_fem$trial_type)[,2:3]</pre>
```



Notice that female bugs were laying more during the second trial (T2) than the first trial (T1).

# Plot Predicted Probabilities



# Fall 2019 Data Cleaning

## Read Libraries

```
library(cvms) # cross-validating regressions
```

#### Read Source Files

#### Read the Data

```
data_path = paste0(dir,"/Dispersal/Winter_2020/stats/data/full_data-Fall2019.csv")
dataFall = clean_flight_data.Fall(data_path)

# extract sets with an experimental design similar to the Winter tests
ongoing_data = dataFall[with(dataFall,!is.na(mass) & set_number > 71),]

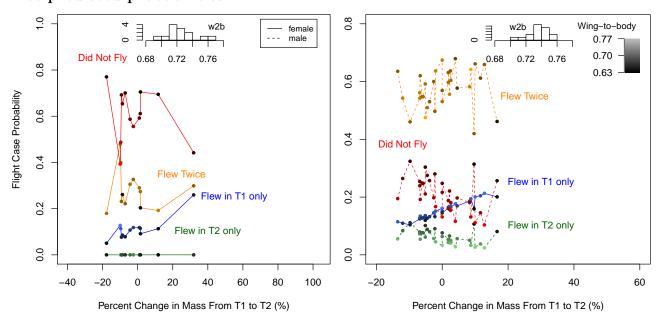
# create delta data
d = create_delta_data.Fall(ongoing_data)
```

# Flight Response Predictions

## Compute predicted probabilities

```
d <- d[with(d, order(mass_per)),]</pre>
neither = c()
T1_rather_than_none = c()
T2_rather_than_none = c()
both_rather_than_none = c()
for (i in 1:nrow(d)) {
 m = d$mass_per[[i]]
  s = d$sex_c[[i]]
  w = d$wing2body_c[i]
  # extract effects from the best fit model
  top0 = exp(0) # equals 1
  top1 = exp(model_table5[1,1] + model_table5[1,2]*m + model_table5[1,3]*s + model_table5[1,4]
  top2 = exp(model_table5[2,1] + model_table5[2,2]*m + model_table5[2,3]*s + model_table5[2,4]
  top3 = exp(model_table5[3,1] + model_table5[3,2]*m + model_table5[3,3]*s + model_table5[3,4]
  bottom = top0 + top1 + top2 + top3
  # calculate predicted probabilities
  neither = c(neither, top0/bottom)
  T1_rather_than_none = c(T1_rather_than_none, top1/bottom)
  T2_rather_than_none = c(T2_rather_than_none, top2/bottom)
  both_rather_than_none = c(both_rather_than_none, top3/bottom)
}
```

# Plot predicted probabilities



# Overall and Grouped Accuracies

```
probs = round(cbind(neither, T1_rather_than_none, T2_rather_than_none, both_rather_than_none),
summary_probs = cbind(as.character(d$flight_case), as.character(d$sex), probs)
colnames(summary_probs) = c("event", "sex", "none", "T1", "T2", "both")
dataframe = as.data.frame(summary_probs)
nrow(dataframe)
## [1] 45
# overall
acc = calculate_accuracy(dataframe,3,6)
paste("Overall prediction accuracy, ", round(acc,2))
# by sex
femdata = dataframe[dataframe$sex=="F",]
maledata = dataframe[dataframe$sex=="M",]
accF = calculate_accuracy(femdata,3,6)
paste("Female prediction accuracy, ", round(accF,2))
accM = calculate_accuracy(maledata,3,6)
paste("Male prediction accuracy, ", round(accM,2))
## [1] "Overall prediction accuracy, 0.6"
## [1] "Female prediction accuracy,
## [1] "Male prediction accuracy, 0.69"
```

#### Confusion Matrix

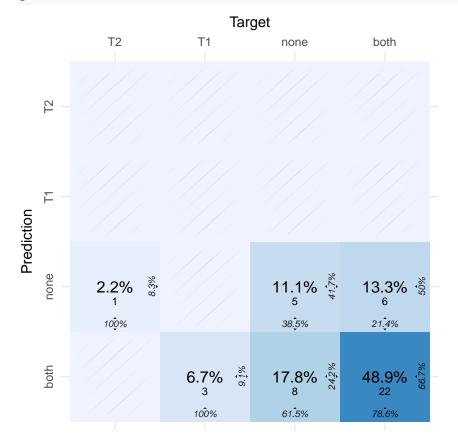
```
acc_table = get_confusion_matrix(dataframe,3,6)
acc_table[,1:5]
## # A tibble: 1 x 5
     `Overall Accuracy` `Balanced Accuracy`
##
                                                 F1 Sensitivity Specificity
                                                          <dbl>
##
                   <dbl>
                                       <dbl> <dbl>
                                                                       <dbl>
```

```
## 1 0.6 0.538 NaN 0.293 0.784
```

confusion\_matrix <- acc\_table\$'Confusion Matrix'[[1]]
confusion\_matrix</pre>

```
## # A tibble: 16 x 3
##
      Prediction Target
                   <chr>
##
      <chr>
                           <int>
    1 both
                   both
                              22
##
                   both
                               6
##
    2 none
                               0
##
    3 T1
                   both
##
    4 T2
                   both
                               0
    5 both
                               8
##
                   none
                               5
##
    6 none
                   none
    7 T1
                               0
##
                   none
    8 T2
                               0
##
                   none
##
    9 both
                   T1
                               3
## 10 none
                   T1
                               0
## 11 T1
                   T1
                               0
  12 T2
                   T1
                               0
## 13 both
                   T2
                               0
## 14 none
                   T2
                               1
## 15 T1
                   T2
                               0
## 16 T2
                               0
```

plot\_confusion\_matrix(confusion\_matrix, add\_sums=FALSE)



# **Females**

dfem = d[d\$sex=="F",]

```
dfem <- dfem[with(dfem, order(mass_per)),]

neither = c()

T1_rather_than_none = c()

both_rather_than_none = c()

for (i in 1:nrow(dfem)) {
    M = dfem$mass_per[[i]]
    EC = dfem$egg_diff[[i]]
    top0 = exp(0) # equals 1
    top1 = exp(model_table6[1,1] + model_table6[1,2]*M + model_table6[1,3]*EC)
    top2 = exp(model_table6[2,1] + model_table6[2,2]*M + model_table6[2,3]*EC)
    bottom = top0 + top1 + top2
    neither = c(neither, top0/bottom)
    T1_rather_than_none = c(T1_rather_than_none, top1/bottom)
    both_rather_than_none = c(both_rather_than_none, top2/bottom)
}</pre>
```

## Compute predicted probabilities

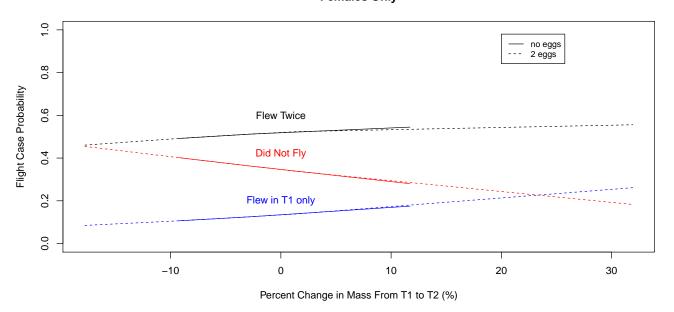
```
probs = round(cbind(neither, T1_rather_than_none, both_rather_than_none),2)
summary_probs = cbind(as.character(dfem$flight_case), as.character(dfem$egg_diff), probs)
colnames(summary_probs) = c("event", "egg_diff", "none", "T1", "both")

egg2 = c(1,2,3,5,6,7,9,10,11,13)
noegg = c(4,8,12)

dataframe = as.data.frame(summary_probs)
dataframe$egg_cat = c(2,2,2,0,2,2,2,0,2,2,2,0,2)
```

#### Plot predicted probabilities

#### **Females Only**



## Overall and Grouped Accuracies

```
accF_eggs = calculate_accuracy(dataframe,3,5)
paste("Female prediction accuracy for mass diff and egg model, ", round(accF_eggs,2))
```

#### **Confusion Matrix**

```
acc_table = get_confusion_matrix(dataframe,3,5)
acc_table[,1:5]
## # A tibble: 1 x 5
     `Overall Accuracy` `Balanced Accuracy`
                                                F1 Sensitivity Specificity
##
                  <dbl>
                                       <dbl> <dbl>
                                                          <dbl>
                                                                       <dbl>
## 1
                  0.462
                                         0.5
                                                NaN
                                                          0.333
                                                                       0.667
confusion_matrix <- acc_table$'Confusion Matrix'[[1]]</pre>
confusion_matrix
## # A tibble: 9 x 3
```

```
Prediction Target
     <chr>
                 <chr>
##
                        <int>
## 1 both
                 both
                             6
## 2 none
                 both
                             0
## 3 T2
                 both
## 4 both
                 none
## 5 none
                             0
                 none
## 6 T2
                             0
                 none
## 7 both
                 T2
                             1
## 8 none
                 T2
                             0
## 9 T2
                 T2
                             0
```

plot\_confusion\_matrix(confusion\_matrix, add\_sums=FALSE)

