CS 310

Homework Assignment No. 5

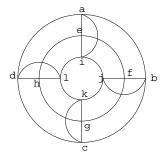
Due on Tue 2/24/2004

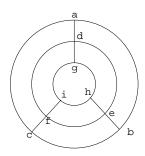
1. Assume that the 26 (capital) letters of the English alphabet

$\{A,B,C,D,E,F,G,H,I,J,K,L,M,N,O,P,Q,R,S,T,U,V,W,X,Y,Z\}$

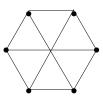
are represented as graphs with a vertex at each endpoint, corner or intersection point. Classify them by homeomorphism. How many classes of graph-homeomorphic letters are there?

2. For each of the following graphs find an Euler cycle and a Hamiltonian cycle, or prove that there is none.

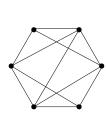




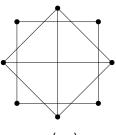
3. For each of the following graphs draw a planar representation or show that it has a subgraph homeomorphic to K_5 or $K_{3,3}$:



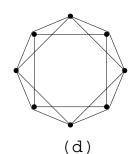




(b)



(C)



- **4.** In each of the following cases draw a connected simple planar graph with the given characteristics, or prove that none exists:
 - (a) 4 vertices all of degree 3, 4 faces.
 - (b) 4 vertices, 6 edges, 5 faces.
 - (c) 4 vertices all of degree 4.
 - (d) 6 vertices all of degree 3, 5 faces.

5. Write the adjacency matrix and the incidence matrix of the following graph:

