



# Interpretability

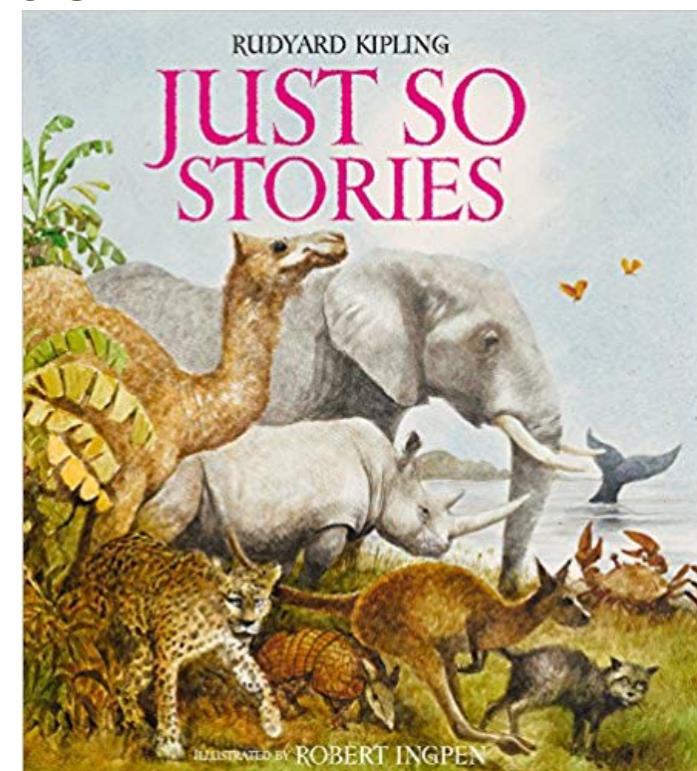


Massachusetts  
Institute of  
Technology

# Interpretability Issues

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- People understand simple models
  - George Miller, 7±2: “There seems to be some limitation built into us either by learning or by the design of our nervous systems, a limit that keeps our channel capacities in this general range.”
    - “... the number of chunks of information is constant for immediate memory. The span of immediate memory seems to be almost independent of the number of bits per chunk ...”
  - Not surprising that one cannot “keep in mind” complex models
- What leads to complex models? And what to do about it?
  - Overfitting
    - Restrict model complexity; e.g., regularization
  - True complexity
    - Make up “just-so” stories that give a simplified explanation of how the complex model applies to specific cases
    - Trade off lower performance for simplicity of model



# Trust

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- Critical for adoption of ML models
  - Case-specific prediction
    - Clinical decision support
  - Confidence in model
    - Population health
- Recall my critique of randomized controlled trials
  - Simplest cases (no comorbidities), smallest sample needed for significance test, shortest follow-up time
  - Results applied to very different populations
- Same concerns for ML models
  - Train and test samples often drawn from same population
  - Are results applicable elsewhere?

# Explanation – Not a New Idea!

## Mycin, 1975

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- In light of the site from which the culture was obtained, and the method of collection, do you feel that a significant number of ORGANISM-1 were obtained?  
**\*\*WHY**
- [1.0] It is important to find out whether there is therapeutically significant disease associated with this occurrence of ORGANISM-1  
It has already been established that:
  - [1.1] the site of the culture is not one of those which are normally sterile, and
  - [1.2] the method of collection is sterile
- Therefore, if:
  - [1.3] the organism has been observed in significant numbers
- Then: there is strongly suggestive evidence (.9) that there is therapeutically significant disease associated with this occurrence of the organism
- [Also : there is strongly suggestive evidence (.8) that the organism is not a contaminant]

- **\*\*WHY**
- [2.0] . . . in order to find out a locus of infection in PATIENT-1  
It has already been established that:
  - [2.1] the site of the culture is known, and
  - [2.2] the number of days since the specimen for the culture was obtained is less than 7
- Therefore, if:
  - [2.3] there is therapeutically significant disease associated with this occurrence of the organism
- Then: it is definite (1.0) that the site of the culture is a locus of infection in the patient
-

- \*\*WHY [i.e., WHY is it important to find out a locus of infection in PATIENT-1?]
- [3.0] . . . in order to find out about an organism or class of organisms for which therapy should cover

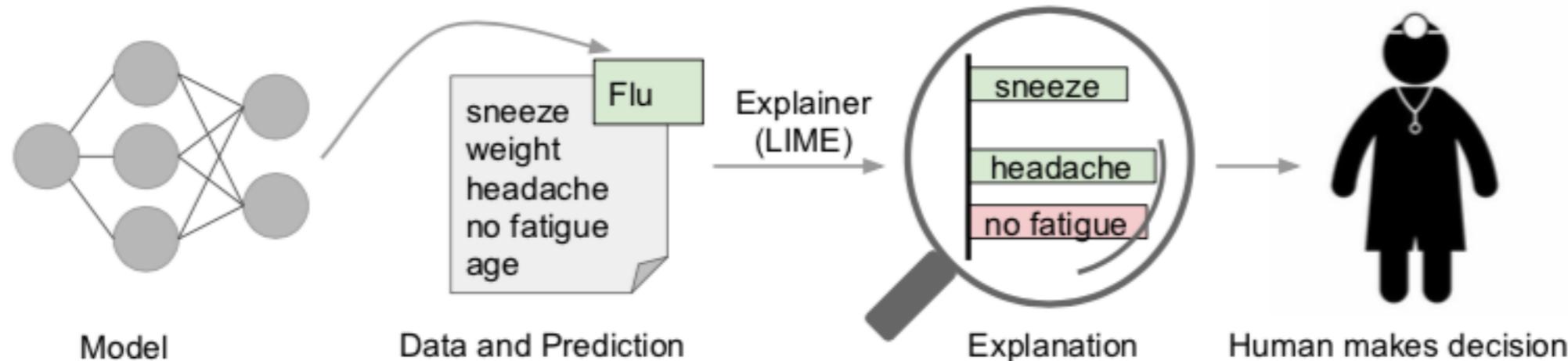
It has already been established that:

- [3.1] the site of the culture is blood, and
- [3.2] the stain of the organism is grampos, and
- [3.3] the portal of entry of the organism is GI
- Therefore, if:
  - [3.4] [A- abdomen is a locus of infection in the patient, or B- pelvis is a locus of infection in the patient]
- Then : there is strongly suggestive evidence (.9) that enterobacteriaceae is a class of organisms for which therapy should cover

- \*\* **HOW 3.0** [i.e., HOW were you finding out about an organism or class of organisms for which therapy should cover?]
- [4.0] At that point RULE095 was being used.  
In addition :
  - [4.1] RULE162 was used to conclude that bacteroides is an organism for which therapy should cover, and
  - [4.2] RULE115 will be tried later, as well.
- \*\* **HOW 4.1** [i.e., HOW was RULE162 used?]
- [5.0] We have already established that:
  - [5.1] the site of the culture is blood, and
  - [5.2] the portal of entry of the organism is GI, and
  - [5.3] the patient is a compromised host
- Therefore : it is definite (1.0) that bacteroides is an organism for which therapy should cover (RULE162)

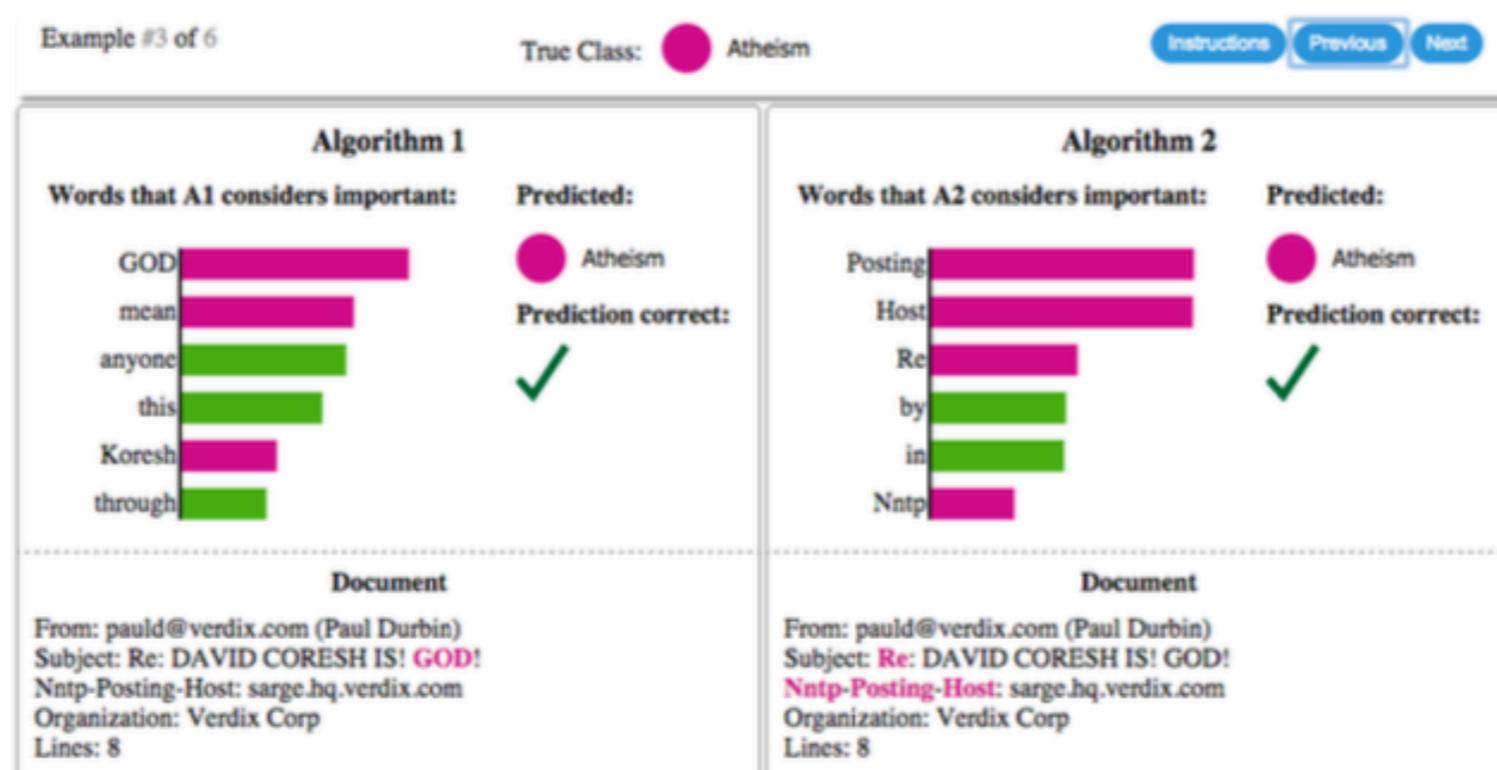
- **\*\* DO YOU EVER PRESCRIBE CARBENICILLIN FOR PSEUDOMONAS INFECTIONS?**
- RELEVANT RULES: RULE064 RULE119 RULE120  
WHICH ONES DO YOU WISH TO SEE?  
\*\* RULE064  
IF: 1) IT IS KNOWN WITH CERTAINTY THAT THE IDENTITY OF THE ORGANISM IS PSEUDOMONAS, AND  
2) THE DRUG UNDER CONSIDERATION IS GENTAMICIN
- THEN: RECORD THE FOLLOWING AS A MORE APPROPRIATE THERAPY:  
GENTAMICIN-AND-CARBENICILLIN

# Local Interpretable Model-agnostic Explanations (LIME)



- A model predicts that a patient has the flu, and LIME highlights:
  - Sneeze and headache are portrayed as contributing to the “flu” prediction
  - “no fatigue” is evidence against it.
- With these, a doctor can make an informed decision about whether to trust the model’s prediction.
- *Approach helps detect data leakage, data set shift, using human expertise*

# Explanation of Cases May be Useful to Compare Models



- Predict whether a post is about “Christianity” or “Atheism”
- Algorithm 2 may be overall more accurate, but Algorithm 1 makes more sense, at least on this example.
- *Again, relies on human expertise, which is much broader than any of our models*

# Desiderata for Explanations

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- Interpretable — “provide qualitative understanding between the input variables and the response”
  - depends on audience
  - requires sparsity
  - features must make sense
    - e.g., eigenvectors in principal component analysis are not explainable features
- Local fidelity — “it must correspond to how the model behaves in the vicinity of the instance being predicted”
- Model-agnostic — “treat the original model as a black box”
  - *Is this really a good idea for all models?*

# How to Make Interpretable Models

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- If the original data are  $x \in \mathbb{R}^d$ , define a new set of variables,  $x' \in \{0, 1\}^{d'}$  that can serve as the interpretable representation of the data
- An *explanation* is a model  $g \in G$  where  $G$  is the class of interpretable models
  - E.g., linear models, additive scores, decision trees, falling rule lists, ...
  - The domain of  $g$  is  $\{0, 1\}^{d'}$ , i.e., the interpretable representation of the data
- The *complexity* of a model is  $\Omega(g)$ 
  - E.g., depth of a decision tree, number of non-zero weights in a linear model
- The full model is  $f : \mathbb{R}^d \rightarrow \mathbb{R}$ 
  - E.g., for classification,  $f$  is probability that  $x$  belongs to a certain class
- $\pi_x(z)$  is a proximity measure of how close  $z$  is to  $x$ , thus defining a locality around  $x$
- Let  $\mathcal{L}(f, g, \pi_x)$  be a measure of how *unfaithful*  $g$  is to  $f$  in the locality defined by  $\pi_x$
- Then

$$\xi(x) = \arg \min_{g \in G} \mathcal{L}(f, g, \pi_x) + \Omega(g)$$

is the best explanatory model for  $x$  given our choices for  $\{\mathcal{L}, \pi_x, \Omega\}$

# Use Sampling to Generate Data in a Local Neighborhood

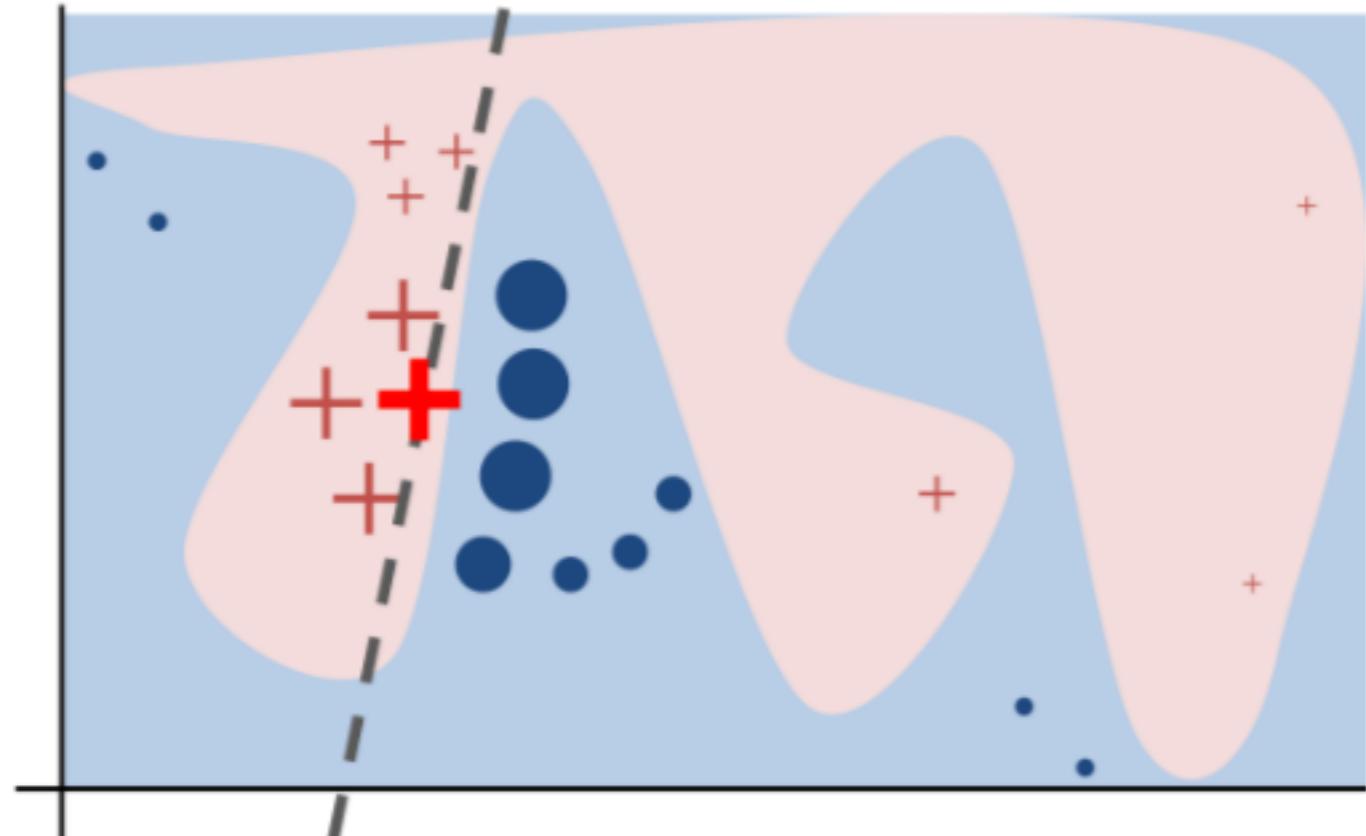
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- Goal is model-agnostic explanation capability
  - Thus, cannot rely on knowing anything about the model  $f$
- To explain the model's result around the interpretable point  $x'$ ,
  - sample in the interpretable representation space to get a set of points  $z' \in \{0, 1\}^{d'}$  to create a dataset  $\mathcal{Z}$  of perturbed samples
  - recover sample  $z \in \mathbb{R}^d$  and compute  $f(z)$  as the label for  $z \in \mathcal{Z}$
  - optimize  $\xi(x) = \arg \min_{g \in G} \mathcal{L}(f, g, \pi_x) + \Omega(g)$ , weighting contributions of  $z$  by  $\pi_x(z)$

# Sparse Linear Explanation

- Choose  $G$  to be the class of linear models such that  $g(z') = w_g \cdot z'$
- Let  $\pi_x(z) = \exp(-D(x, z)^2/\sigma^2)$  be an exponential kernel on some distance function  $D$  with width  $\sigma$ 
  - E.g., cosine distance for bag-of-words, L2 distance or DICE for images

$$\mathcal{L}(f, g, \pi_x) = \sum_{z, z' \in \mathcal{Z}} \pi_x(z)(f(z) - g(z'))^2$$



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**Algorithm 1** Sparse Linear Explanations using LIME

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**Require:** Classifier  $f$ , Number of samples  $N$   
**Require:** Instance  $x$ , and its interpretable version  $x'$   
**Require:** Similarity kernel  $\pi_x$ , Length of explanation  $K$

```
 $\mathcal{Z} \leftarrow \{\}$ 
for  $i \in \{1, 2, 3, \dots, N\}$  do
     $z'_i \leftarrow \text{sample\_around}(x')$ 
     $\mathcal{Z} \leftarrow \mathcal{Z} \cup \langle z'_i, f(z_i), \pi_x(z_i) \rangle$ 
end for
 $w \leftarrow \text{K-Lasso}(\mathcal{Z}, K)$   $\triangleright$  with  $z'_i$  as features,  $f(z_i)$  as target
return  $w$ 
```

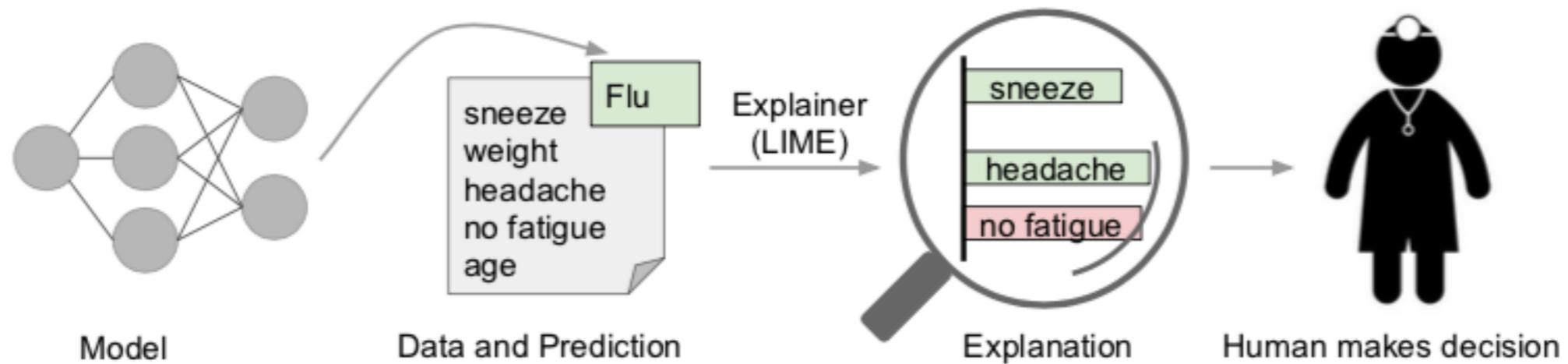
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Toy example to present intuition for LIME. The black-box model's complex decision function  $f$  (unknown to LIME) is represented by the blue/pink background, which cannot be approximated well by a linear model. The bold red cross is the instance being explained. LIME samples instances, gets predictions using  $f$ , and weighs them by the proximity to the instance being explained (represented here by size). The dashed line is the learned explanation that is locally (but not globally) faithful.

# Apply to Text Classification

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- Bag of words, cosine distance for  $\pi_x$
- Choose K as a limit on the number of words in an explanation



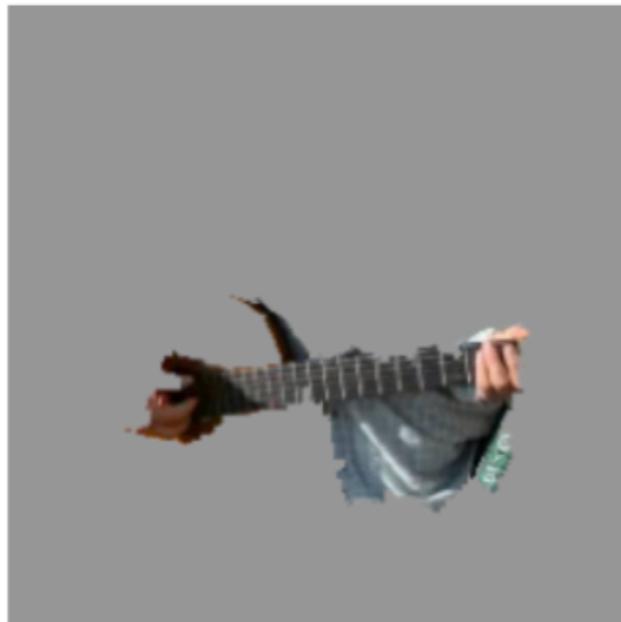
# Apply to Image Interpretation

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- Superpixel is a group of connected pixels with similar colors or gray levels
  - Image is segmented into super pixels
  - $K$  is chosen as the number of superpixels to represent
- K-LASSO predicts label from superpixels, to select which  $K$  of them to use for explanation
- with  $N=5000$ , scikit-learn random forests with 1000 trees  $\Rightarrow 3$  sec
- explaining Inception network results  $\Rightarrow \sim 10$  min



(a) Original Image



(b) Explaining *Electric guitar*



(c) Explaining *Acoustic guitar*



(d) Explaining *Labrador*

Figure 4: Explaining an image classification prediction made by Google’s Inception neural network. The top 3 classes predicted are “Electric Guitar” ( $p = 0.32$ ), “Acoustic guitar” ( $p = 0.24$ ) and “Labrador” ( $p = 0.21$ )

# Choosing a Suite of Examples to Explain

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- Choose a diverse, comprehensive set of  $B$  examples to explain
- Given explanations for a set of instances  $X$  ( $|X| = n$ ), consider the  $n \times d'$  explanation matrix  $\mathcal{W}$  whose rows are examples and columns are features
  - Each entry gives the local importance of that feature for that example
  - For linear models, for instance  $x_i$ ,  $g_i = \xi(x_i)$ , set  $\mathcal{W}_{ij} = |w_{g_{ij}}|$ 
    - recall that  $g(z') = w_g \cdot z'$
  - $I_j$  is a measure of *global* importance of that feature
    - $I_j = \sqrt{\sum_{i=1}^n \mathcal{W}_{ij}}$  for text
    - more difficult to superpixels because they don't recur over different instances



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**Algorithm 2** Submodular pick (SP) algorithm

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**Require:** Instances  $X$ , Budget  $B$

```
for all  $x_i \in X$  do
     $\mathcal{W}_i \leftarrow \text{explain}(x_i, x'_i)$            ▷ Using Algorithm 1
end for
for  $j \in \{1 \dots d'\}$  do
     $I_j \leftarrow \sqrt{\sum_{i=1}^n |\mathcal{W}_{ij}|}$     ▷ Compute feature importances
end for
 $V \leftarrow \{\}$ 
while  $|V| < B$  do      ▷ Greedy optimization of Eq (4)
     $V \leftarrow V \cup \operatorname{argmax}_i c(V \cup \{i\}, \mathcal{W}, I)$ 
end while
return  $V$ 
```

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$$c(V, \mathcal{W}, I) = \sum_{j=1}^{d'} \mathbb{1}_{[\exists i \in V : \mathcal{W}_{ij} > 0]} I_j$$

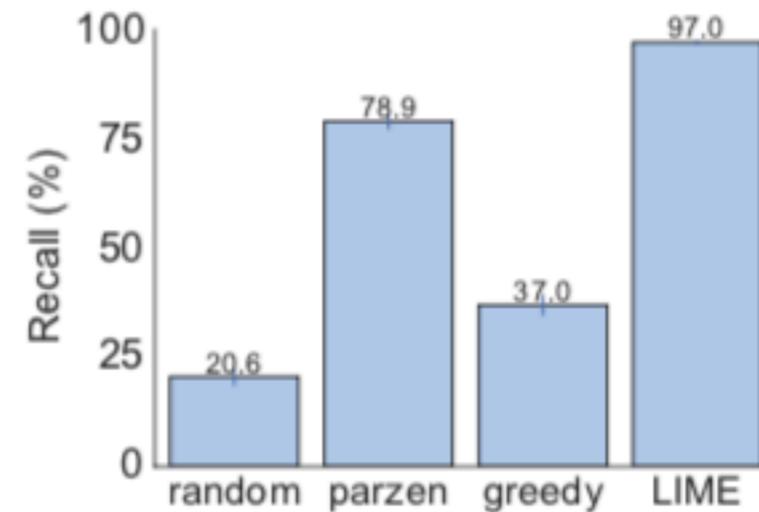
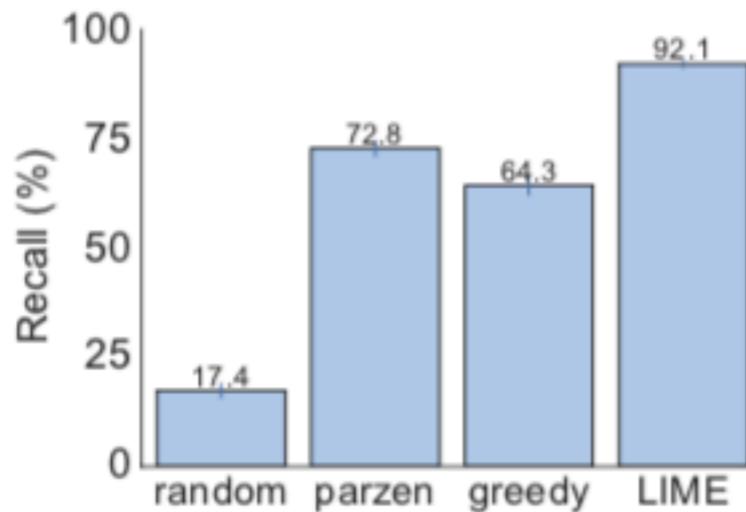
$$\text{Pick}(\mathcal{W}, I) = \arg \max_{V, |V| \leq B} c(V, \mathcal{W}, I)$$

Choosing  $i$  that maximizes marginal coverage  $c(V \cup \{i\}, \mathcal{W}, I) - c(V, \mathcal{W}, I)$  approximates optimum

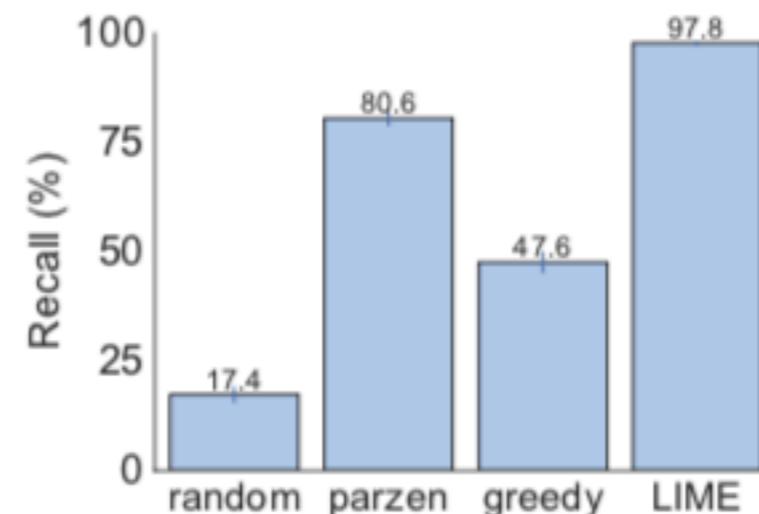
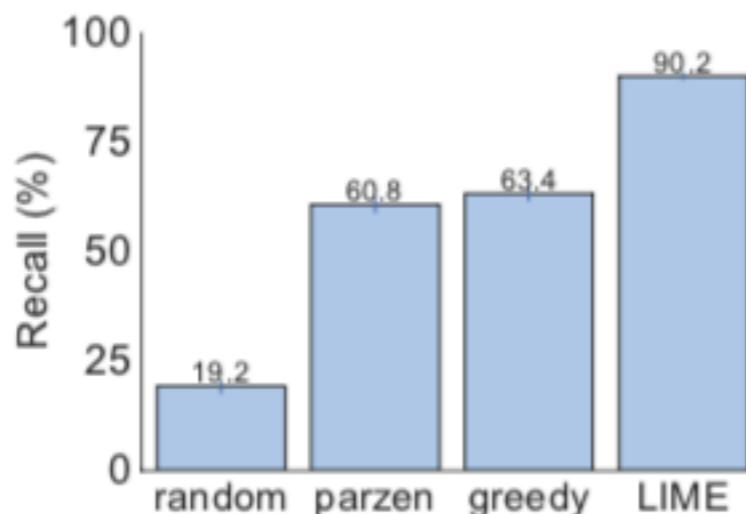
# LIME Experiments

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- Two sentiment analysis datasets (2000 instances, each; used 1600/400 test/train)
- Bag-of-words as features
- Models:
  - Decision Trees
  - Logistic Regression with L2 regularization
  - Nearest Neighbors
  - Support Vector Machines with RBF kernels
  - Random Forest (1000 trees) with word2vec embeddings
- $K = 10$



**Figure 6: Recall on truly important features for two interpretable classifiers on the books dataset.**

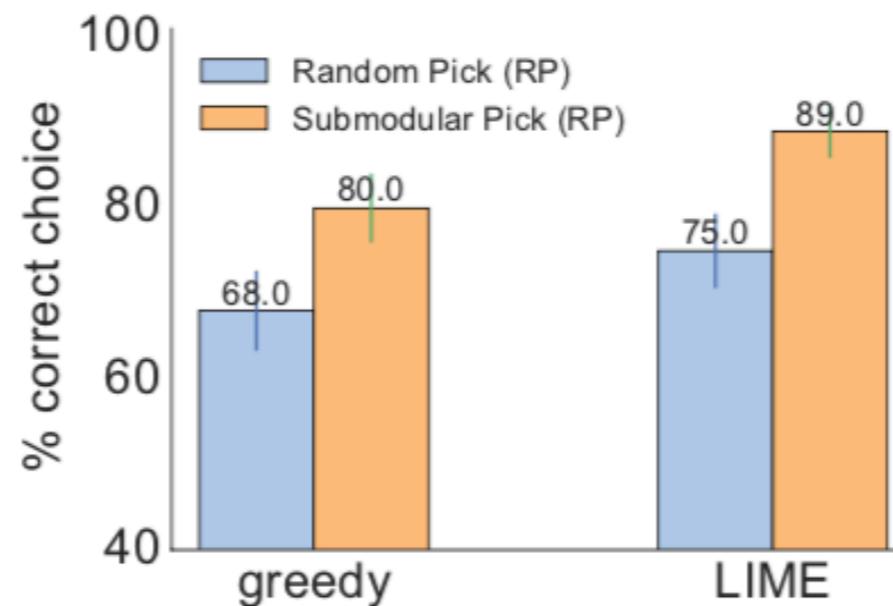


**Figure 7: Recall on truly important features for two interpretable classifiers on the DVDs dataset.**

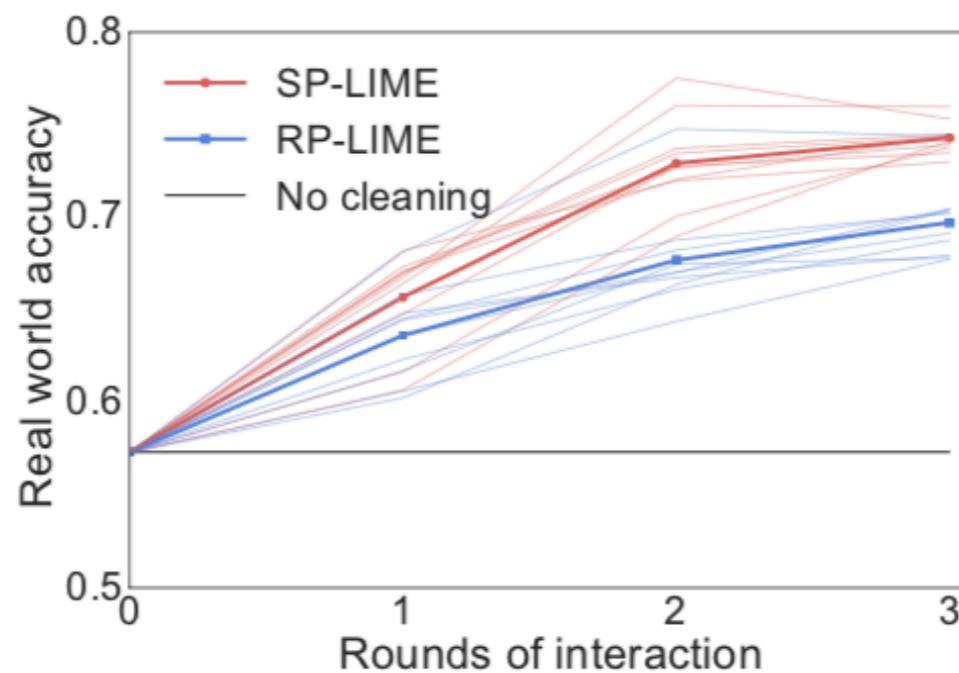
# Human Experiments

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- Questions:
  - Can users choose which of two classifiers generalizes better
  - Based on the explanations, can users perform feature engineering to improve the model
  - Are users able to identify and describe classifier irregularities by looking at explanations
- “Christianity” vs. “Atheism” from 20-newsgroups dataset
  - known problems of data leakage from headers, ...
  - trained original and “cleaned” classifiers for comparison
  - test set accuracy favors the “wrong” classifier!!!
- Separate test set of 819 web pages about these topics from <http://dmoz-odp.org>
- SVM with RBF kernels, trained on the 20-newsgroup data
- Mechanical Turk, 100 users,  $K=6$  words,  $B=6$  documents/Turk
  - in 2nd experiment, they are asked to remove word features they believe inappropriate



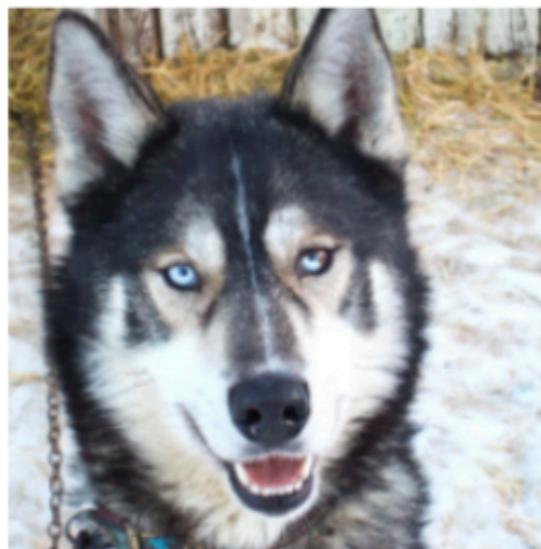
**Figure 9:** Average accuracy of human subject (with standard errors) in choosing between two classifiers.



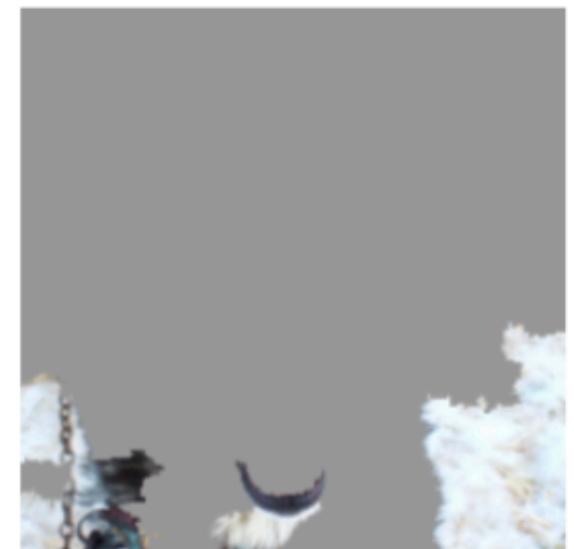
**Figure 10:** Feature engineering experiment. Each shaded line represents the average accuracy of subjects in a path starting from one of the initial 10 subjects. Each solid line represents the average across all paths per round of interaction.

# Can People Gain Insight from these Explanations?

- Trained a deliberately bad classifier between Wolf and Husky
  - All wolves in training set had snow in the picture, no huskies did
- Presented cases to graduate students with ML background
  - 10 balanced test predictions, with one husky in snow, one wolf not in snow
- Comparison between pre- and post-experiment trust and understanding



(a) Husky classified as wolf



(b) Explanation

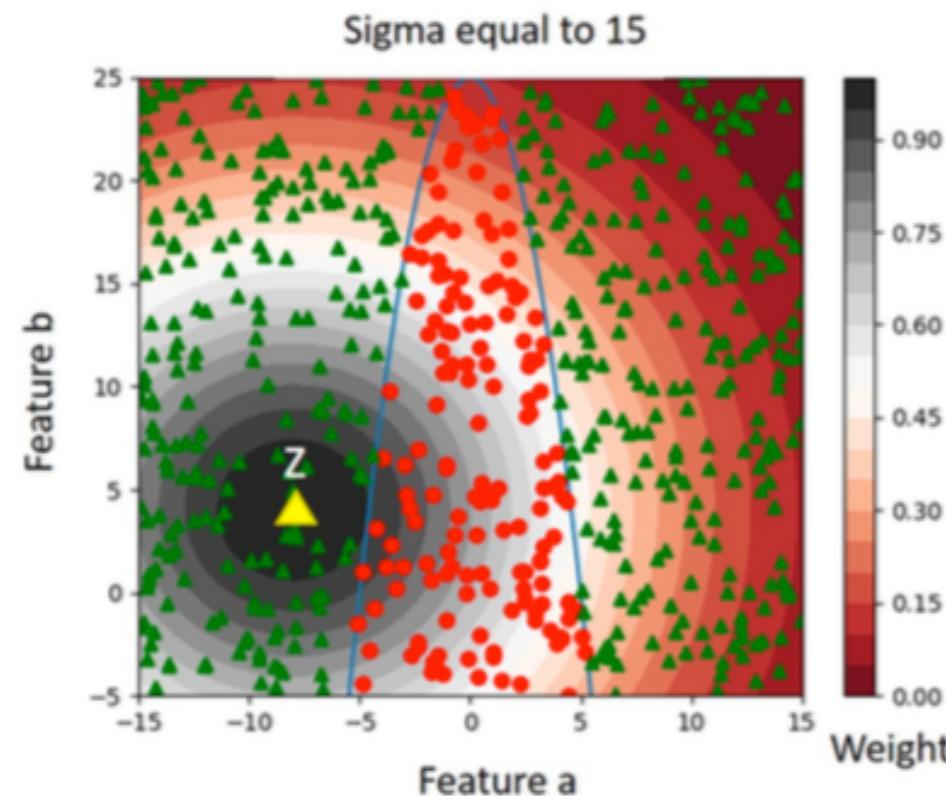
**Figure 11:** Raw data and explanation of a bad model’s prediction in the “Husky vs Wolf” task.

	Before	After
Trusted the bad model	10 out of 27	3 out of 27
Snow as a potential feature	12 out of 27	25 out of 27

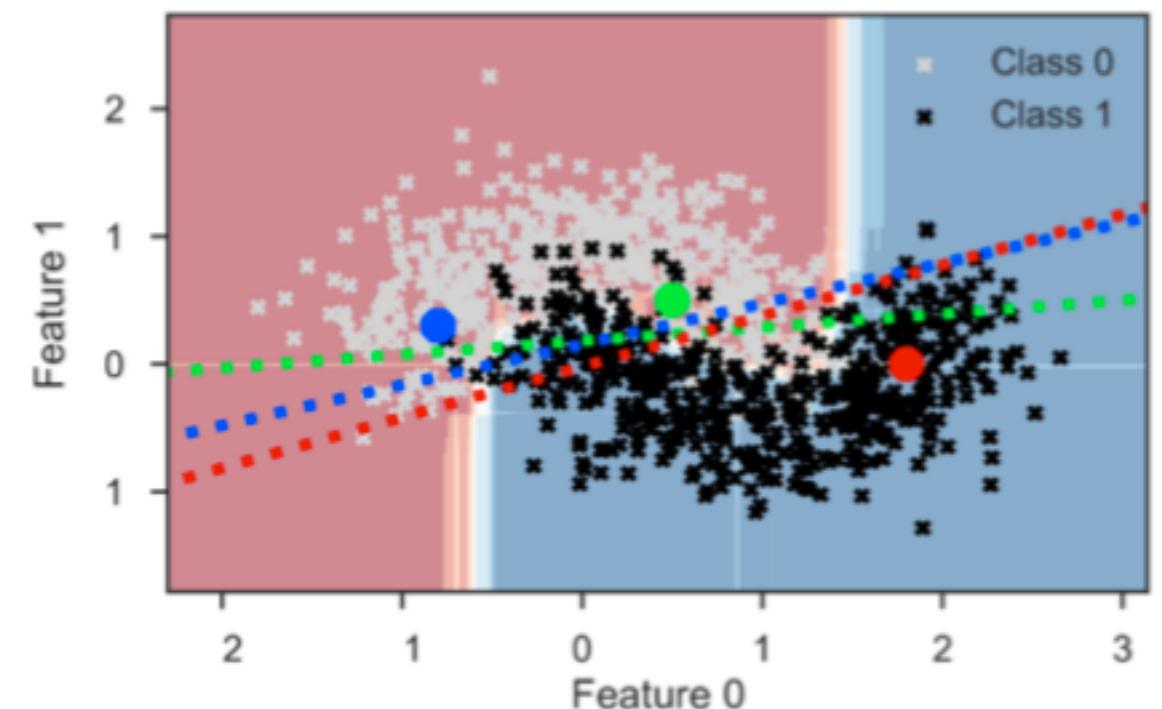
**Table 2:** “Husky vs Wolf” experiment results.

# Critique of LIME

- Choice of  $\sigma$  is arbitrary and can lead to bad sampling
  - in implementation, often set to  $0.75\sqrt{d}$
- it is important to tune the size of the neighbourhood according to how far  $z$  is to the closest decision boundary



(a) A bad sampling scenario of LIME.



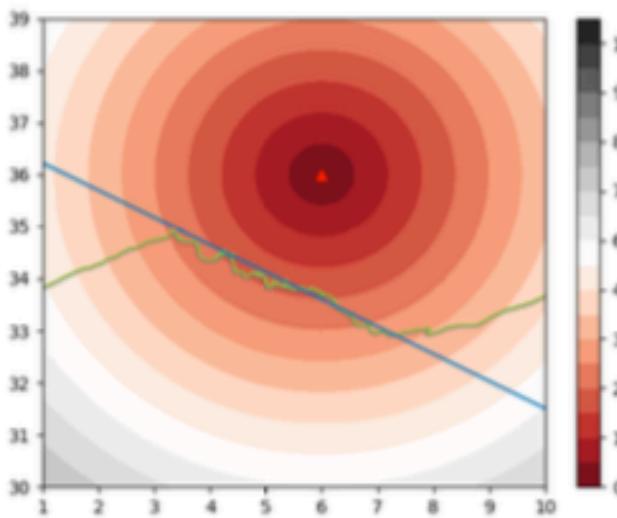
(b) Limitation of LIME spotted by Laugel et al. [14]

# LEAFAGE - Local Example and Feature importance-based model AGnostic Explanations

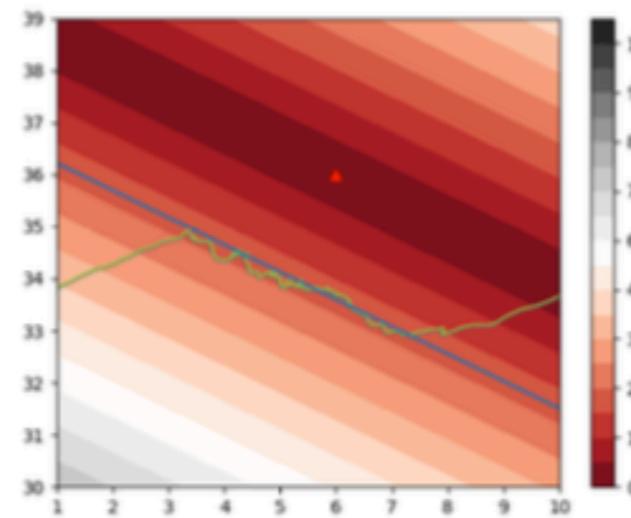
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- Experts often reason by analogy from previous cases
  - In law, this is formally enshrined as *precedent*
  - In medicine, we see it in the behavior of experts
- Case-based reasoning: retrieve, adapt, learn
- Contrastive justification
  - Not “why did you choose  $x$ ”,
  - but “why did you choose  $x$  rather than  $y$ ?”
- Assume that a black-box model  $f : \mathcal{X} \rightarrow \mathcal{Y}$  solves a classification problem where
  - $\mathcal{X} = \mathbb{R}^d$  and  $\mathcal{Y} = \{c_1, c_2\}$
  - training set  $X = [x_1, \dots, x_n]$  and  $y_{\text{true}} = [y_1, \dots, y_n]$ ,  $y_{\text{predicted}} = \{f(x) \mid x_i \in X\}$
- To explain  $f(z) = c_z$ , use
  - allies =  $\{x \in X \mid f(x) = c_z\}$ , enemies =  $\{x \in X \mid f(x) \neq c_z\}$

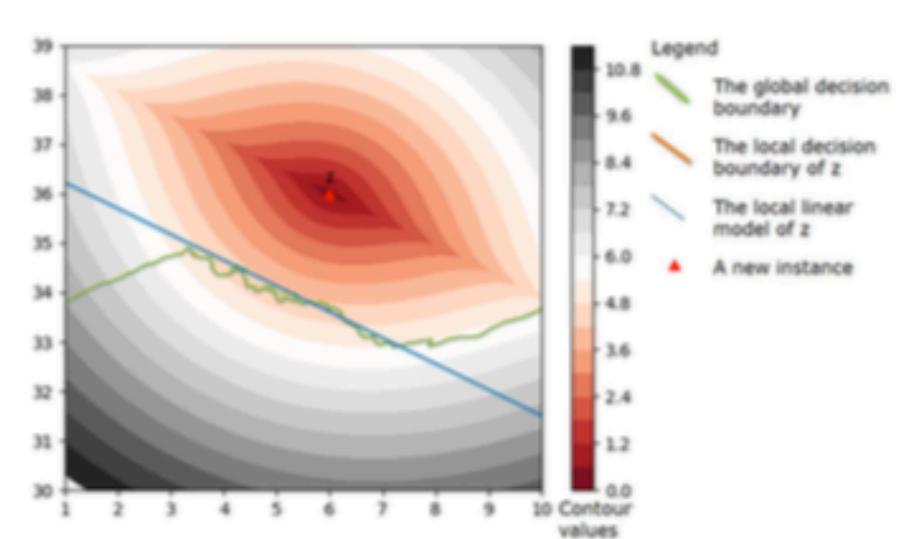
- Choose a subset of training examples in the neighborhood of  $z$
- Build a linear model from that subset
- Compute importance of each feature in that model
- Define a similarity measure based on features weighted by their importance
  - $g(\mathbf{x}) = \mathbf{w}_z \mathbf{x} + c$  defines the decision boundary
  - $b(t) = \sqrt{d} \cdot \|\mathbf{w}_z^T \mathbf{t} - \mathbf{w}_z^T \mathbf{z}\| + \|\mathbf{t} - \mathbf{z}\|$  is the distance function,  $\mathbf{w}_z = (w_{z1}, \dots, w_{zd})^T$
- Explanation gives
  - Most important features
  - Most similar examples that give the same answer
- (*details in paper*)



(a) Contour-lines of the first term of the similarity measure.



(b) Contour-lines of the second term of the similarity measure.



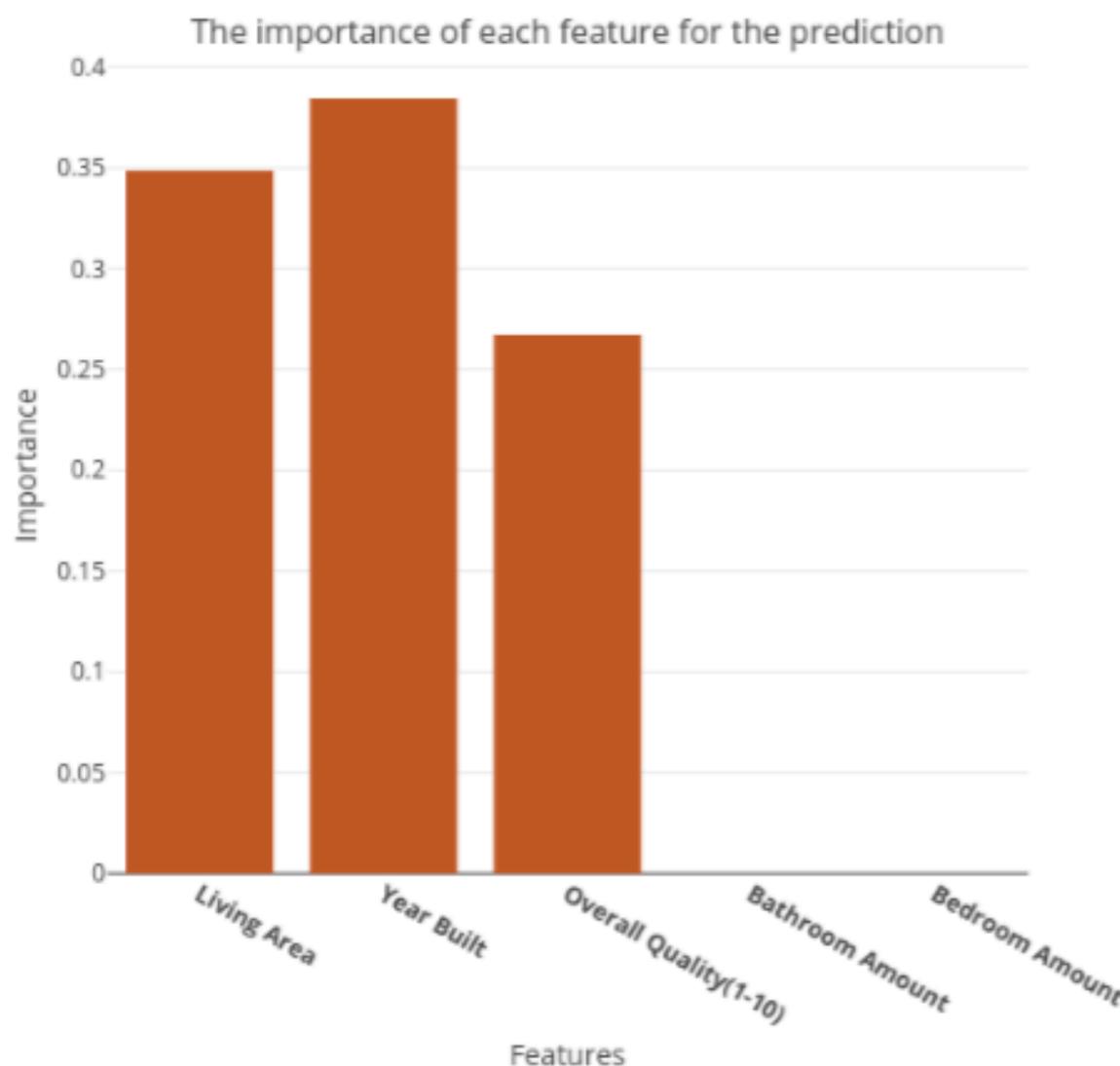
(c) Contour-lines of the black-box similarity measure.

Figure 5: An example to illustrate the black-box similarity measure.

Living Area	Year Built	Overall Quality(1-10)	Bathroom Amount	Bedroom Amount
184 m <sup>2</sup> (1982 ft <sup>2</sup> )	1989	7	2	3

Figure 7: Example of a house that is predicted as value low by the machine learning model.

## Prediction: High



Most similar houses with value Low

Living Area	Year Built	Overall Quality(1-10)	Bathroom Amount	Bedroom Amount
135 m <sup>2</sup> (1456 ft <sup>2</sup> )	1978	6	2	3
137 m <sup>2</sup> (1479 ft <sup>2</sup> )	1976	6	2	3
133 m <sup>2</sup> (1441 ft <sup>2</sup> )	1978	6	2	3
135 m <sup>2</sup> (1456 ft <sup>2</sup> )	1976	6	2	3
113 m <sup>2</sup> (1218 ft <sup>2</sup> )	2009	6	2	2

Most similar houses with value High

Living Area	Year Built	Overall Quality(1-10)	Bathroom Amount	Bedroom Amount
171 m <sup>2</sup> (1850 ft <sup>2</sup> )	1994	7	2	3
194 m <sup>2</sup> (2093 ft <sup>2</sup> )	1986	7	2	3
181 m <sup>2</sup> (1950 ft <sup>2</sup> )	1997	7	2	3
194 m <sup>2</sup> (2097 ft <sup>2</sup> )	1993	7	2	3
149 m <sup>2</sup> (1614 ft <sup>2</sup> )	2005	7	2	3

See user study in paper

Figure 8: Example of a LEAFAGE explanation.

# Can Attention Models in Deep Learning Serve as Explanations?

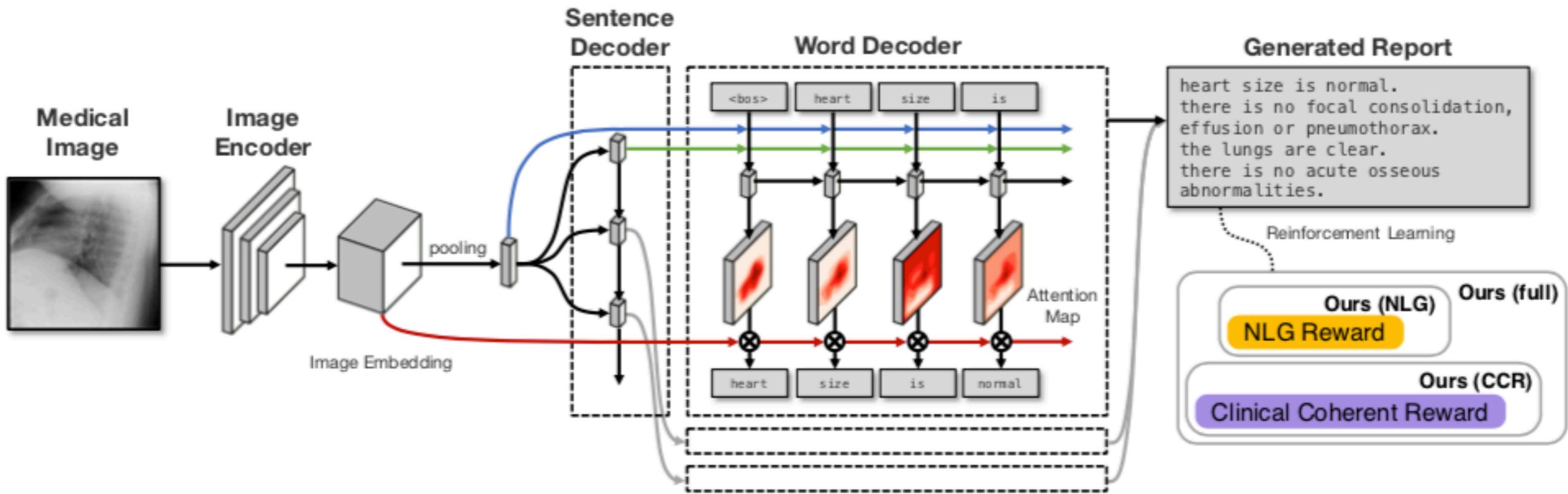


Figure 2: **The model for our proposed *Clinically Coherent Reward*.** Images are first encoded into image embedding maps, and a sentence decoder takes the pooled embedding to recurrently generate topics for sentences. The word decoder then generates the sequence from the topic with attention on the original images. NLG reward, clinically coherent reward, or combined, can then be applied as the reward for reinforcement policy learning.

- **Image encoder (CNN)**

- Spacial image features  $V = \{v\}_{k=1}^K$ 
  - computed by fully connected layer on pre-global-pooling layer of CNN

- **Sentence decoder (RNN/LSTM) uses image features**

- $h_i, m_i = \text{LSTM}(\bar{v}; h_{i-1}, m_{i-1})$ 
  - topic vector and stop signal  $\tau_i = \text{ReLU}(W_\tau^T h_i + b_\tau)$ ,  $u_i = \sigma(w_u^T h_i + b_u)$

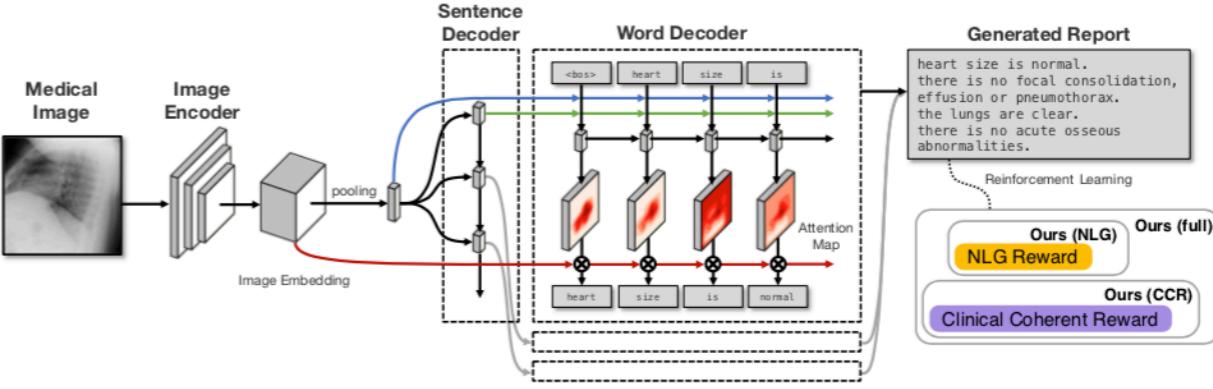
- **Word decoder (RNN/LSTM)**

- Uses  $\bar{v}$ ,  $\tau$ , and embedding of previous word generated
- Word is sampled from either conditional probability or overall corpus probability

- Reinforcement learning to favor most readable and clinically correct output

- Use CheXpert annotations for 12 diagnoses: pos, neg, uncertain, absent

- Hack: remove duplicate generated sentences





### Ground Truth

cardiomegaly is moderate. bibasilar atelectasis is mild. there is no pneumothorax. a lower cervical spinal fusion is partially visualized. healed right rib fractures are incidentally noted.

### TieNet

ap portable upright view of the chest. there is no focal consolidation, effusion, or pneumothorax. the cardiomediastinal silhouette is normal. imaged osseous structures are intact.

### Ours (full)

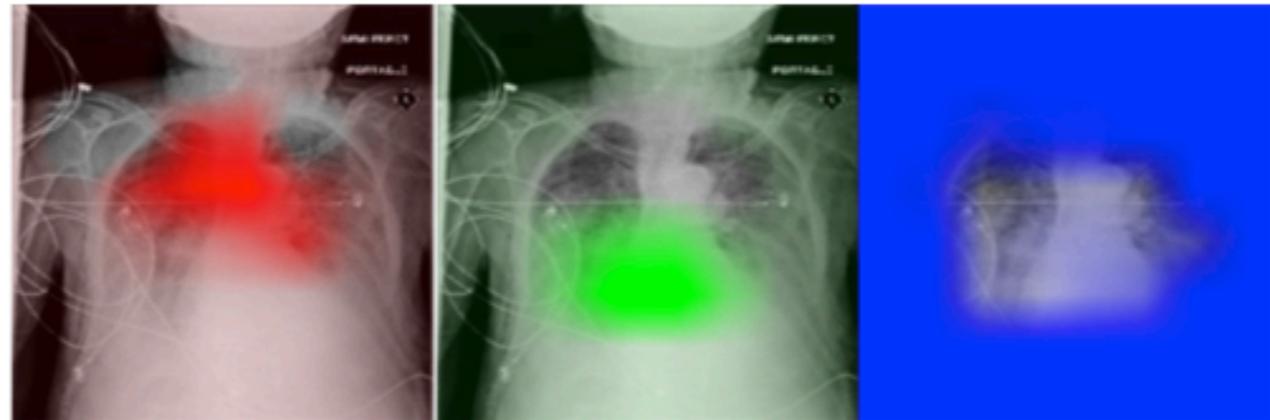
pa and lateral views of the chest. there is mild enlargement of the cardiac silhouette. there is no pleural effusion or pneumothorax. there is no acute osseous abnormalities.

# Attention Map Identified Relevant Parts of the Image

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(a)



(b)

ap upright and lateral views of the chest. there is moderate cardiomegaly. there is no pleural effusion or pneumothorax. there is no acute osseous abnormalities.

as compared to the previous radiograph, there is no relevant change. tracheostomy tube is in place. there is a layering pleural effusions. NAME bilateral pleural effusion and compressive atelectasis at the right base. there is no pneumothorax.

Figure 3: **Visualization of the generated report and image attention maps.** Different words are underlined with its corresponding attention map shown in the same color.

# Attention is not Explanation

# But

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- “assumption that the input units (e.g., words) accorded high attention weights are responsible for model outputs”
- Desiderata if *attention* actually is to give insight into how a DNN operates
  - Attention weights should correlate with feature importance measures (e.g., gradient-based measures)
  - Alternative (or counterfactual) attention weight configurations ought to yield corresponding changes in prediction
- Mixed results, though the study has been criticized for methodology
  - “evidence that correlation between intuitive feature importance measures (including gradient and feature erasure approaches) and learned attention weights is weak”
  - counterfactual attention distributions — which would tell a different story about why a model made the prediction that it did — often have no effect on model output

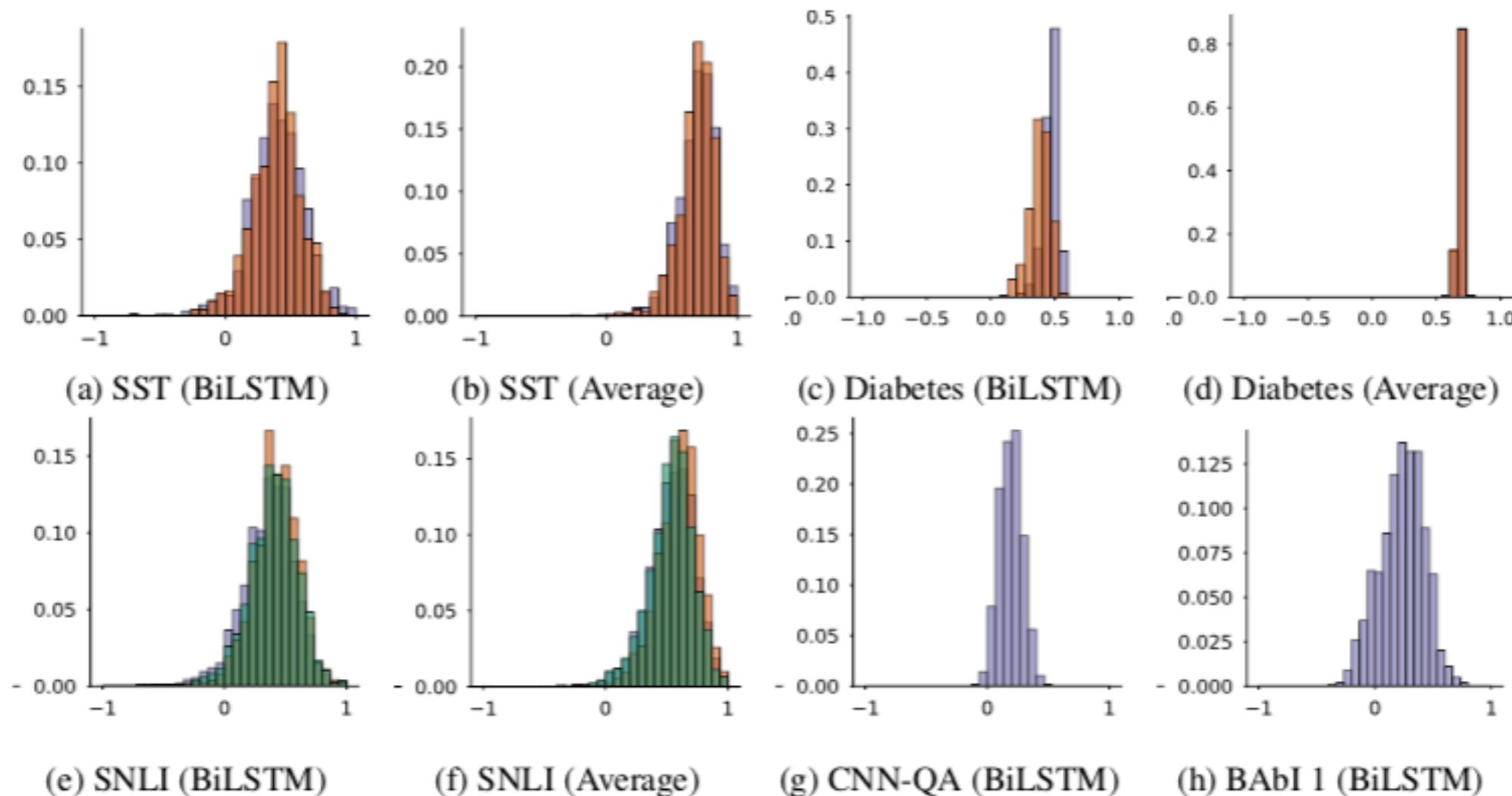


Figure 2: Histogram of **Kendall**  $\tau$  between attention and gradients. Encoder variants are denoted parenthetically; colors indicate predicted classes. Exhaustive results are available for perusal online.

# Building Simple Models

## Falling Rule Lists

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- Willing to sacrifice (some) performance for simplicity of model
- Falling Rule List is a form of Decision List, a one-sided Decision Tree
  - the order of rules determines which example should be classified by each rule
  - the estimated probability of success decreases monotonically down the list
- Rank rules to form a predictive model
- Stratify patients into decreasing risk sets

	Conditions		Probability	Support
IF	IrregularShape AND Age $\geq 60$	THEN malignancy risk is	85.22%	230
ELSE IF	SpiculatedMargin AND Age $\geq 45$	THEN malignancy risk is	78.13%	64
ELSE IF	IllDefinedMargin AND Age $\geq 60$	THEN malignancy risk is	69.23%	39
ELSE IF	IrregularShape	THEN malignancy risk is	63.40%	153
ELSE IF	LobularShape AND Density $\geq 2$	THEN malignancy risk is	39.68%	63
ELSE IF	RoundShape AND Age $\geq 60$	THEN malignancy risk is	26.09%	46
ELSE		THEN malignancy risk is	10.38%	366

Table 1: Falling rule list for mammographic mass dataset.

# Learning Falling Rule Lists

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- Data:  $D = \{(x_n, y_n)\}_{n=1,\dots,N}$ ,  $x_n \in X$ ,  $y_n \in \{0, 1\}$
- Bayesian approach:
  - Hyperparameters  $H$
  - Falling Rule List parameters  $\theta$  with prior  $p_\theta(\cdot; H)$
  - Likelihood  $p_Y(\{y_n\} \mid \theta; \{x_n\})$
  - Size of rule list  $L \in \mathbb{Z}^+$
  - Space of possible IF clauses (Boolean functions on  $X$ )  $B_X(\cdot)$
  - Clauses  $c_l(\cdot) \in B_X(\cdot) \ni c_l = 1$  iff  $x$  satisfies a set of conditions, for  $l = 1, \dots, L - 1$
  - Risk scores  $r_l \in \mathbb{R}$ , for  $l = 0, \dots, L \ni r_{l+1} \leq r_l$ 
    - These will be scaled by logistic function to yield a probability

Given  $L$ , let  $Z(x; \{c_l(\cdot)\}_{l=0}^{L-1}) : X \rightarrow \{0, \dots, L\}$  be the mapping from feature  $x$  to the index of the length  $L$  rule list it “belongs” to (equals  $L$  for default patients):

$$Z(x; \{c_l(\cdot)\}_{l=0}^{L-1}) = \quad (5)$$

$$\begin{cases} L & \text{if } c_l(x) = 0 \text{ for } l = 0, \dots, L-1 \\ \min(l : c_l(x) = 1, l = 0, \dots, L-1) & \text{otherwise.} \end{cases}$$

Then, the likelihood is:

$$y_n | L, \{c_l(\cdot)\}_{l=0}^{L-1}, \{r_l\}_{l=0}^L; x_n \sim \text{Bernoulli}(\text{logistic}(r_{z_n})), \text{ where} \quad (6)$$

$$z_n = Z(x_n; \{c_l(\cdot)\}_{l=0}^{L-1}). \quad (7)$$

- Lots of details (see the paper)
  - use a “frequent itemset mining” algorithm to find clauses with enough support
  - choose  $r_l$  to be log of products of real numbers
  - $L$  is drawn from a Poisson distribution
  - use can express preference over lengths of clauses
  - MAP decision list is computed by simulated annealing: {swap, replace, add, delete} a clause
  - Gibbs sampling to estimate posteriors

# Empirical Test: 30-Day Hospital Readmission

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- 8,000 patients
- Features: “impaired mental status,” “difficult behavior,” “chronic pain,” “feels unsafe” and over 30 other features
- Mined rules with support  $\geq 5\%$ , no more than two conditions
- Expected length of decision list = 8
- Compared to SVM, Random Forest, Logistic Regression, CART, Inductive Logic Programming

Method	Mean AUROC (STD)
FRL	.80 (.02)
NF_FRL	.75 (.02)
NF_GRD	.75 (.02)
RF	.79 (.03)
SVM	.62 (.06)
Logreg	.82 (.02)
Cart	.52 (.01)

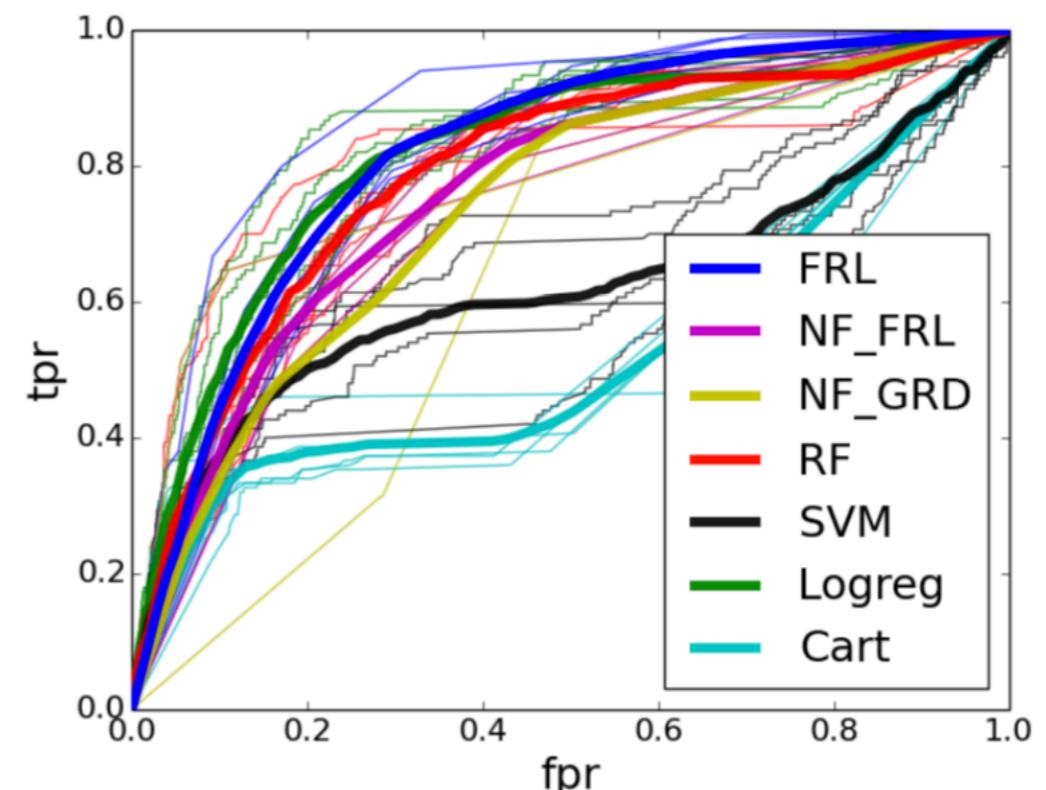


Figure 2: ROC curves for readmissions prediction.

# Readmission Rule List

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	Conditions		Probability	Support
IF	BedSores AND Noshow	THEN readmissions risk is:	33.25%	770
ELSE IF	PoorPrognosis AND MaxCare	THEN readmissions risk is:	28.42%	278
ELSE IF	PoorCondition AND Noshow	THEN readmissions risk is:	24.63%	337
ELSE IF	BedSores	THEN readmissions risk is:	19.81%	308
ELSE IF	NegativeIdeation AND Noshow	THEN readmissions risk is:	18.21%	291
ELSE IF	MaxCare	THEN readmissions risk is:	13.84%	477
ELSE IF	Noshow	THEN readmissions risk is:	6.00%	1127
ELSE IF	MoodProblems	THEN readmissions risk is:	4.45%	1325
ELSE		Readmissions risk is:	0.88%	3031

Table 2: Falling rule list for patients with no multiple readmissions history.

# Test on Various UCI Data Sets

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Method	Spam	Mamm	Breast	Cars
FRL	.91(.01)	.82(.02)	.95(.04)	.89(.08)
NF_FRL	.90(.03)	.67(.03)	.70(.11)	.60(.21)
NF_GRD	.91(.03)	.72(.04)	.82(.12)	.62(.20)
SVM	.97(.03)	.83(.01)	.99(.01)	.94(.08)
Logreg	.97(.03)	.85(.02)	.99(.01)	.92(.09)
CART	.88(.05)	.82(.02)	.93(.04)	.72(.17)
RF	.97(.03)	.83(.01)	.98(.01)	.92(.05)

Table 4: AUROC value comparisons over datasets