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Introduction

Coastal areas are attractive for human settlement, and up to 39% of human population lives within 100km of the coast (Magdalena et al. 2021), including many of the world's largest cities. 10% of the world's population live in the an area that is less than 10m above sea level (B. Neumann et al. 2015; Lichter et al. 2010), an area known as the Low Elevation Coastal Zone. All coastal populations face increasing vulnerability to coastal flooding hazards, due to increases in the sea level and changes in extreme weather patterns. To protect populations from these increasing risks, further investment in coastal protection is required; without more investment in coastal defense infrastructure, the population exposed to flooding risk is projected to increase by 50% (Kirezci et al. 2020). One approach to mitigating these hazards is to employ the techniques of Building with Nature, using natural processes and ecosystem functions to create resilient coastal defenses. Of particular interest in the tropical regions of the world are Mangroves, a coastal tree whose dense roots and sturdy branches can provide resilient protection from flooding hazards.

Mangroves provide coastal protection by reducing wave energy, while also adapting naturally to sea level rise, and providing other ecosystem services like increasing water quality and increasing fish spawning areas. Mangroves already provide flood protection to over 15 million people (Menéndez et al. 2020), but in the last 50 years between 30-50 percent of the world's mangrove area has been lost (Goldberg et al. 2020). To rebuild and enhance the world's mangrove belts, significant research on these ecosystems is required.

Towards this goal, this project aims to capitalize on recent advances in remotely sensing techniques, specifically high resolution optical imagery from Sentinel-2 and Spaceborne lidar from NASA's ICESat-2 to create a global database of bathymetry in mangrove forest ecosystems.

1.1 Motivation and Relevance

One current weakness of mangroves as a flood defense strategy is that the response of these natural ecosystems is not well known. The persistance of mangroves over the long term is not as well understood as for traditional hard infrastructure (Gijsman et al. 2021). Traditional hard coastal infrastructure like dams, dikes and seawalls have many years of research on their mechanical responses. To increase the use of BwN solutions, we need increased understanding of the risks and benefits of relying on mangroves for flood defense.

1.1.1 Limitations of conventional nearshore survey

The nearshore zone is a very difficult environment to perform bathymetric surveying. (C. E. Parrish et al. 2019). All current bathymetric survey techniques face limitations that restrict their use in the shallowest 5-10m of the nearshore zone. Most deep water survey is done using multi-beam echo sounders (MBES) attached to ships. This limits their operation in water shallower than 4-5 meters or in areas with navigational hazards (Cesbron et al. 2021; Monteys et al. 2015). To survey the nearshore zone, airborne lidar survey is a common choice, and allows simultaneous surveying of the topography and high resolution. However, airborne surveys are extremely expensive to perform and require extensive post-processing effort to create a usable surface model.

1.1.2 Importance of Nearshore Bathymetric Data

Nearshore bathymetry is crucial data for many aspects of coastal management and research. Bathymetric data is essential for many aspects of the blue economy, including aquaculture, marine energy, submarine cables, dredging operations, design of sea defenses, navigation, scientific research, and ecosystem preservation (Cesbron et al. 2021; Ashphaq et al. 2021). However, the nearshore zone is notoriously difficult to survey. There is currently a global lack of data in the 5-10m zone (Albright and Glennie 2021) and up to 50% of the world's shallow coastal zones remain unsurveyed (IHO/OHI 2022). Where surveys do exist, they can be decades out of date, especially in the 40% of the world's coasts that are sandy and highly dynamic (Almar et al. 2021).

There have been attempts at global bathymetric datasets, most notably the General Bathymetric Chart of the Ocean (GEBCO), which is an annually updated global bathymetric and topographic dataset. The bathymetry in GEBCO grids is derived by assimilation of acoustic soundings provided by ships and gravimetric bathymetry measurements (Cesbron et al. 2021). While it provides useful information about deep oceans, GEBCO accuracy in the nearshore zone is limited because sonar data is limited in many shallow nearshore zones. (Monteys et al. 2015). The resolution, both horizontally and vertically, is not sufficient for wave transformation studies.

1.2 Identified Knowledge gaps

A major restriction in modeling how mangroves and waves interact is the lack of global nearshore bathymetry data. In the context of researching the impact of mangroves on flood risk, one of the most important aspects of a wave model is the nearshore bathymetry, since the exact shape and depth of the profile has a large impact on the hydrodynamic response of mangrove ecosystems (Horstman et al. 2014; Maza et al. 2019). The current state of wave modeling of mangrove ecosystems either relies on insitu survey data, or uses an idealized profile shape. The further development of mangrove wave modeling will benefit from better quantification of bathymetry (Menéndez et al. 2020; Gijón Mancheño et al. 2021). This detailed data could be particularly useful given the heterogeneity between different mangrove forests (Mazda 2013).

The objective of this project is to determine where remote sensing might be able to fill this gap in nearshore data availability.

1.3 Research Question

The primary question that this project intends to answer is:

How can spaceborne remote sensing data be used to improve estimates of nearshore bathymetry along mangrove-lined coasts?

To answer this question, the following subquestions will be investigated:

- In which mangrove forests might spaceborne lidar and optical SDB be an effective survey method?
- How can spaceborne lidar transects that contain bathymetry be identified algorithmically?
- Once transects with bathymetry are found, how can the seafloor elevation data be extracted?
- How can lidar photon return locations reflecting the seafloor be separated from background noise?
- How can gaps be filled in areas with missing lidar photons?
- Which of the established optical SDB methods are most reliable in mangrove ecosystems?

Background

2.1 Lidar Bathymetric surveying

The earliest attempts to use Light Detecting and Ranging (lidar) to survey the coastal zone date back to the late 1960s. (Bailly et al. 2016). The technology has matured significantly since then and currently airborne lidar using a strong 532nm laser beam is a common technique for high accuracy bathymetric and topographic surveying. The downside of this technique is that it does not scale well to large areas, because of the expensive equipment, and extensive post-processing work to correct for refraction of the laser beam in the water column, calibration to in situ data, and outlier detection.

Recent advances in lidar technology have allowed the development of the photon-counting lidar, which requires significantly less energy to detect a return signal. These have allowed the practical application of constant lidar data collection in satellites. The use of spaceborne lidar is a more recent area of research, but some early results have shown that spaceborne lidar can find depths as deep as 40m (C. E. Parrish et al. 2019).

The potential for bathymetric mapping using spaceborne laser observations has been noted since before the advent of the ICESat-2 mission. The predecessor mission carried a lidar instrument called the Geoscience Laser Altimeter System (GLAS). GLAS was a green-light laser intended for measuring atmospheric aerosols (Abshire et al. 2005). However, because of the laser architecture, GLAS was not able to penetrate the water column (Forfinski-Sarkozi and C. Parrish 2016). However, a prototype of ATLAS, called the Multiple Altimeter Beam Experimental lidar (MABEL) instrument was tested with high-altitude aircraft missions, allowing a simulation of the data that would be provided by ATLAS (Mcgill et al. 2013). Early experiments with MABEL showed good agreement between bathymetric measurements from MABEL and high-quality airborne reference data (Jasinski et al. 2016; Forfinski-Sarkozi and C. Parrish 2016).

2.2 Mangroves as Coastal Defense

Sea level rise, and the resultant increase in flood risk poses a threat to all coastal communities, including many of the world's largest population centers. The risk is even more existential for low-lying tropical that are disproportionately affected by the sea level rise. Low-lying nations often do not have any available high ground to move cities to, and sometimes do not have access to the resources to fully mitigate these risks through hard infrastructure. For these reasons, mangroves forests are an important resource for these communities, providing coastal protection that can adapt to sea level rise by trapping sediment and expanding outward if conditions permit.

One way to adapt to the changing sea levels, and possible increases in extreme weather events is to promote the restoration and expansion of mangrove forests. It is well-established that mangrove forests can reduce wave energy (Maza et al. 2019; Menéndez et al. 2020; Hadi et al. 2003; Sánchez-Núñez et al. 2020), and to a more limited extent, storm surges (Montgomery et al. 2019; Chen et al. 2021; Mcivor et al. 2012). Mangroves also offer many other ecosystem benefits including enhancing fish stocks, improving water quality, storing significant amounts of carbon, and attracting tourism (Atkinson et al. 2016). Mangroves also have the unique property of creating their own ecosystem, by trapping sediment and expanding seaward under certain conditions Gijsman et al. 2021.

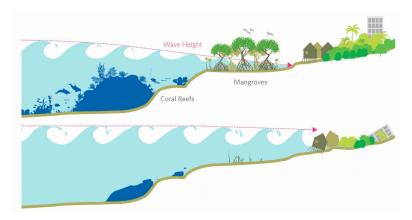


Figure 2.1: The protective effects of Mangroves. From (Losada et al. 2018)

Shallow water bathymetry and mangrove height are difficult to survey manually, due to the difficulty of field work in dense mangrove environments (Gijsman et al. 2021). Current study of the effects of mangroves on wave attenuation are limited by this lack of hydrodynamic data about these ecosystems (Horstman et al. 2014). Therefore, finding an automated way of calculating bathymetry anywhere in the world from publicly available data is a improvement when modeling sites that do not have existing survey data, and can be used to as the basis for wave modeling and process-based models. Improved models can allow better characterization of the morphologic response to mechanical factors like sea level rise and sediment supply that need further study to understand the

system response to climate change.

One weakness of mangroves as a flood protection mechanism is that their response to long term changes in the biogeomorphic environment is not well understood (Gijsman et al. 2021). This uncertainty about the long term persistance of mangrove structures is an impediment to widespread adoption of mangrove greenbelt restoration as a coastal protection strategy.

2.3 ICESat-2

The ICESat-2 mission is intended to gather high resolution topographic data on a global scale. The satellite carries the Advanced Topographic Laser Altimeter System (ATLAS). ATLAS is a highly sensitive photon-counting, green-light lidar. The satellite instrument points at reference ground tracks (RGT) along the earth's surface, and returns with a repeat time of 91 days. Along the reference track, there are 3 beams, one pointing directly at the reference track, and two that are offset by approximately 3km on either side. The layout of the beams relative to the RGT are shown in figure 2.2.

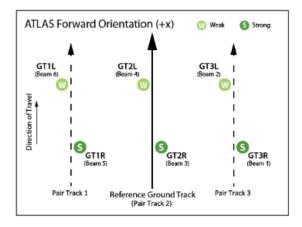


Figure 2.2: Layout of the ICESat-2 beams

Each of the 3 beams emits both a strong and weak beam, with the strong beam being approximately 4x more powerful (T. A. Neumann et al. 2019). Of the approximately 10^{14} of photons emitted per pulse, up to 10 make it back to the sensor and are detected (T. A. Neumann et al. 2019). The exact number of emitted photons that are subsequently detected at the sensor depends on the local atmospheric conditions and the reflectivity of the surface (T. Neumann et al. 2019). The highly sensitive instrument also receives significant noise, due to scattering and signal from the sun.

The main mission of the satellite is to gather data about mass and elevation changes in ice sheets and glaciers, and to study global global canopy height (Markus et al. 2017). To increase the spatial coverage of the vegetation height, the observatory is sometimes pointed away from the reference ground track when flying over land to increase the spatial

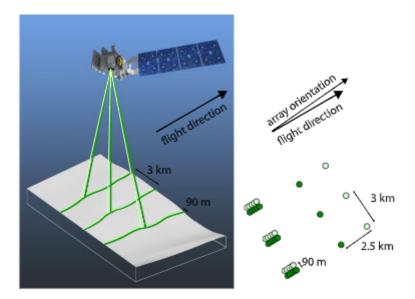


Figure 2.3: The layout of the ICESat-2 beams in 3D space. from T. A. Neumann et al. 2019

density of the observations of vegetation height (Markus et al. 2017). This offpointing begins before the satellite begins to record data over land, so the nearshore coastal area is also included, and therefore bathymetric and hydrological applications also benefit from increased spatial coverage (Magruder et al. 2021).

To locate the position of each photon in 3D space, the time of flight of the photon is calculated with a precision of 800 ps (T. A. Neumann et al. 2019). The location of the center of mass of the instrument is found using Global Positioning System (GPS) systems onboard the satellite. By combining the measured time of flight and satellite position, the geolocation of each returning photon is calculated. (T. A. Neumann et al. 2019).

2.3.1 Weak vs. Strong Beams

The beams are divided into weak and strong signals to enhance the radiometric dynamic range. The strong beams are expected to provide better signal-noise ratios over low-reflectivity surfaces, like the ocean and seafloor (T. A. Neumann et al. 2019). Therefore, these beams are expected to provide the best data for lidar bathymetry measurements. The weak beams are better for capturing very high reflectivity surfaces like ice, which might otherwise saturate the sensor and not provide useful data.

2.3.2 Refraction Correction

The locations calculated by the data products from the satellite do not correct of the refraction induced by the different speeds and which light travels in water and in the atmosphere. This effect introduces both a horizontal and vertical error in the photon location, as shown in figure 2.4.

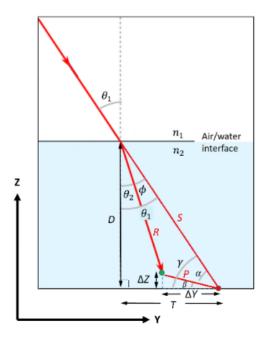


Figure 2.4: The errors caused by the refraction at the air-water interface

When the instrument is pointed directly at the RGT, the laser beams point nearly directly at the satellite's nadir. When directly on-nadir, the additional horizontal error induced by refraction is approximately 9cm (C. E. Parrish et al. 2019), which for bathymetric purposes is negligible. However, by design ATLAS can point up to 5° off-nadir (equal to 43km away from the RGT (Magruder et al. 2021)). When pointing off-nadir, the horizontal error is much more significant and must be corrected for accurate measurements (C. E. Parrish et al. 2019).C. E. Parrish et al. propose an method to correct for both horizontal and vertical error that is widely cited in other studies. The Parrish method assumes a flat water surface, but other studies have extended their method to include the effect of water slope or wave action on the refraction error (Ma et al. 2020; Zhang et al. 2022). Some studies only use data that is collected when the instrument is pointing on-nadir, and therefore only correct for the vertical error using Snell's law. This is referred to as first order refraction correction in the summary table.

2.3.3 Vertical Height Reference

The ATL03 data product reports the photon heights relative to the WGS84 reference ellipsoid. These ellipsoidal heights already include corrections for the solid earth tides, ocean loading, ocean pole tides, and atmospheric delays.

The height provided in ATL03 is calculated by the following equation:

$$H_{GC} = H_P - H_{OPT} - H_{OL} - H_{SEPT} - H_{SET} - H_{TCA}$$

Where:

- H_{GC} is the geophysically corrected photon height above the WGS84 ellipsoid
- \bullet H_P is the raw photon height above the WGS84 ellipsoid
- H_{OPT} is the height of the Ocean Pole tide
- H_{OL} is the height of the ocean load tide
- H_{SEPT} is the height of the solid earth pole tide
- H_{SET} is the solid earth tide
- H_{TCA} is the height of the total column atmospheric delay

The elevation value reported in ATL03 does not include the geoid or any tides. To find these values from the reported ellipsoidal height, the dataset includes correction factors for the tide-free geoid, the height difference between the tide-free and mean-tide geoid, and the height of the tide relative to the mean tide geoid as calculated by the GOT4.8 model. The mean sea level can be estimated by adding these correction factors to the ellipsoidal height. However, the GOT4.8 model tidal height is a based on a relatively low resolution grid, and therefore is less accurate in nearshore coastal areas and within embayments (T. Neumann et al. 2019). Therefore, it is proposed to use the data from the operational runs of the Global Tide and Surge Model (GTSM), developed by Deltares, to convert the mean tide geoid elevation to the water depth at the date and time of the satellite pass.

2.3.4 Signal Photon Identification

The ATL03 data product includes a calculated confidence that a given photon return is signal or noise. The probability is assigned for each of the 5 surface types. Because bathymetric survey was not part of the original mission scope, there is no official classification for subsurface returns. Therefore within the default classification bathymetric photons are often classified as noise. However, the classification of ocean surface classification is reliable and can be used to filter out points at or above the sea surface.

To find bathymetric signal, a separate algorithm specifically calibrated to distinguish bathymetric signal from noise photons is applied to this data. There are several different techniques proposed in the literature. Some early research on small sites used manual classification (Forfinski-Sarkozi and C. Parrish 2016). Other researchers have used implementations of DBSCAN (Ester et al. 1996), with parameters that are set adaptively based on the local density of returns. Others

2.4 Satellite Derived bathymetry

There are several established methods for calculating bathymetric data from passive optical and SAR satellite data, and recent advances in cloud computing capabilities like Google Earth Engine (GEE) (Gorelick et al. 2017) make large catalogs of remote sensing data more accessible (Pike et al. 2019; Turner et al. 2021). The major approaches can be classified into wave-kinematic and optical inversion techniques.

2.4.1 Wave-Kinematic Bathymetry

This approach uses the hydrodynamic properties of a wave field to estimate the bathymetry. The hydrodynamic variables like wave celerity and wave length are estimated from either optical or SAR satellite data. The bathymetry can then be calculated using the wave dispersion relation Almar et al. 2021. The major advantage of this method is that the results do not depend on the turbidity, which can be a significant limitation to optical SDB along many coastlines. The downsides to this approach are that the horizontal resolution is limited compared to optical methods, and the depth that it can reach is limited by the wavelength: longer waves feel the bottom earlier, so only in areas with significant swells can deeper bathymetry measurements be found (Almar et al. 2021).

2.4.2 Bathymetry from Optical Remote Sensing

Optical remote sensing is a passive technique, as it detects light from the sun reflected by the earth. Since the 1970s many methods of estimating bathymetry based on the optical quality of the water have been found, all based on the physical principle that water attenuates light. Optical methods require to the water to be *optically shallow*, or clear enough that light can reach the sea floor. This is a significant restriction, but in places where it is applicable it gives very high resolution data of the seafloor. There are two broad types of algorithms for extracting bathymetric data from optical satellite imagery, analytical and empirical. Empirical models link the amount of attenuation of each pixel to in-situ depth measurements, and derive a relationship between color and depth. One advantage is that they are generally computationally inexpensive. Analytical or physics-based approaches require corrections for atmospheric and subsurface factors (Turner et al. 2021), but require more sophisticated computational capabilities to run.

Because of the ability to incorporate in-situ data and the computational ease, empirical methods are considered for this project.

2.4.3 Active-passive Sensor Fusion: The best of both worlds

C. E. Parrish et al. conclude that the best way to use ICESat-2 data for bathymetric survey is to combine it with optical/multispectral techniques. Because the lidar-derived data provides highly accurate point estimates along a linear track, and optical methods allow the estimation for a 2D area but require a priori depth data, combining the two techniques provides a synergistic fusion of the strengths of both. The lidar-derived

depths are used as training data for the optical SDB models, creating a 2D picture of the bathymetry.

There have since been several studies that employ this approach, and evaluate different techniques for correcting refraction, finding bathymetric signal points, and combining the lidar data with optical techniques.

2.4.4 Summary of Prior Research Combining Optical and Lidar SDB

The studies that have used some version of the proposed technique are summarized in table 2.1.

Table 2.1: Summary of SDB research that combines spaceborne lidar and optical data

Paper	Year	Dataset	Refraction Correc-	S/N Classification	Tide Correction	Notes
			tion Method	method		
Forfinski-Sarkozi and	2016	MABEL	First-order depth	Manual	N/A	non-tidal
C. Parrish			correction			
C. E. Parrish et al.	2019	ATL03	Parrish method	Manual	N/A	Compared ellipsoidal heights
Ma et al.	2020	ATL03	Parrish + sloping	Adaptive DBSCAN	OTPS2	-
			sea surface			
Thomas et al.	2020	ATL03	Parrish Method	Manual	Not Specified	-
Albright and Glennie	2021	ATL03	First-order	Manual	N/A	Converted to NAD83
Xie et al.	2021	ATL03	Parrish Method	Adaptive DBSCAN	Not specified	DBSCAN is used iteratively
Cao et al.	2021	ATL03	First-order depth	A-DRAGANN	OTPS2	-
			correction			
Lee et al.	2021	ATL03	Not specified	Not specified	$T_{-}TIDE$	-
Liu et al.	2021	ATL03	Liu method	DBSCAN after Ma	TMD tidal model	-
				et al.		
Le Quilleuc et al.	2022	ATL03	Parrish	DBSCAN with man-	N/A	Compared ellipsoidal heights
				ual correction		

Proposed Methodology

The following method is proposed to evaluate the effectiveness of combining optical SDB methods with lidar data along mangrove coasts.

3.1 Find Areas for Global Analysis

There are several datasets of the global distribution of mangrove forests (Worthington, Andradi-Brown, et al. 2020). This study will use the recent Giri et al. 2011 dataset. To find the areas of interest, the mangrove extent data will be buffered by a distance large enough so that it includes the offshore area, and these polygons will be generalized to snap to a rectangular grid. Polygons with an area under a certain threshold will be dropped from the dataset. The remaining polygons will be used as sites for the global analysis.

To compare the the effect that the mangrove typology has on the quality of the bathymetric output, data on the local biogeographic environment for each site can be added using the data from Worthington, Ermgassen, et al. 2020 which classifies every mangrove forest as either carbonate or terrigenous, and is assigned a coast type (Delta, Estuary, Lagoon, Open Coast). This data can provide valuable information on which types of mangrove environments might be more favorable for automated bathymetry extraction. Certain mangrove types might have higher average turbidity which will impede remotely sensed bathymetry. To check the effect of turbidity on the results, the local turbidity at the time of the satellite pass can be found using the GlobColour dataset of ocean color (Garnesson et al. 2019), which reports the Secchi Disk Depth (SDD) at a given time.

As part of this step, a series of test sites with surveyed in-situ bathymetry will be found for testing the error present in the satellite derived data. To ensure good coverage, these sites will have varied mangrove typology and and geographic location.

3.2 Download Lidar Data Within Areas of Interest

Using a Python script that interacts with the NASA National Snow and Ice Data Center (NSIDC) data download API, the ATL03 variables of interest can be downloaded for each polygon.

3.3 Develop Bathymetric Photon Identification algorithm

The data from the satellite consists of raw photon locations along a given track. To answer the subquestion *How can spaceborne lidar transects that contain bathymetry be identified algorithmically*, the noise extraction algorithm needs reliably find bathymetric photon returns, if they are present, and indicate if no signal can be found.

Many most previous papers use a variation of the *Density-based spatial clustering of applications with noise (DBSCAN)* algorithm, from Ester et al. for this purpose. For this project it is proposed to use the DBSCAN method iteratively with adaptive parameters to identify bathymetric points. The first pass of the DBSCAN algorithm will find clusters of signal using a modified version of the approach from Ma et al., which runs the algorithm on clusters of 10,000 points in the along track direction. The results of Ma's technique are shown in figure 3.1. In the figure, the red points are the locations of photon returns, and the green points are classified as signal by Ma's approach.

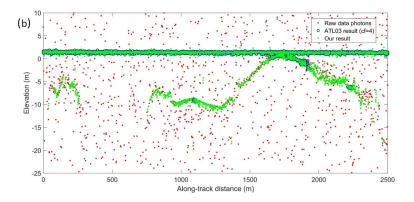


Figure 3.1: Results of DBSCAN as used by Ma et al.

This algorithm reliably detects signal, but also produces several clusters of false positives, below the seafloor. Ma et al. manually removes these points, but for a global approach this is not a feasibly solution. Therefore, it is proposed to run the algorithm a second time, on the entire result of the first iteration, to detect any clusters which maybe have been false positives in the first iteration.

The exact details of the implementation will be tested against the test sites to see which produce the best results. This allows an answer to the subquestion *How can lidar photon return locations reflecting the seafloor be separated from background noise?*

Some sites, either due to turbidity, depth, or instrument data quality issues, will not provide reliable bathymetry lidar photons. Any sites without lidar reference data will be removed from the analysis. This will lead to an answer to the subquestion *In which mangrove forests might spaceborne lidar and optical SDB be an effective survey method?*

3.4 Correction for Refraction and Tides

To correct for the effects of refraction and the tidal elevation, first the tide level at the time and location of the ICESat-2 pass will be found from the archives of the GTSM. Using this tidal data the local depth relative to MSL is calculated from the ellipsoidal height. Then using the Parrish method the vertical and horizontal error induced by refraction will be calculated and corrected.

This will adjust individual photon heights, but it does not provide a profile along of the seafloor. To find a seafloor profile, different methods of finding a profile can be tested, like using a windowed median function of the photon heights, or bayesian updating of other data like GEBCO. This will serve to answer the subquestion *once transects with bathymetry are found, how can the seafloor elevation data be extracted?*.

The validity of different approaches to seafloor profile extraction and tidal/refraction correction can be found by calculating the root mean square (RMS) and mean absolute error (MAE) values at test sites with surveyed data available.

3.5 Apply Optical SDB Where Spaceborne Lidar is Available

In the last step, a list of mangrove coasts that have spaceborne lidar data available is established. To extend this to a 2D map of the bathymetry, first we need satellite scenes that are approximately contemporaneous with the lidar data. These can be found using Google Earth Engine, a cloud platform that provides access to computational resources and a large catalog of remote sensing data (Gorelick et al. 2017). Because of the computational simplicity, the bathymetric will be calculated using an empirical algorithm.

The results of this step will be a series of 2D bathymetric rasters. To evaluate the accuracy of the SDB bathymetry output, the error can be calculated against the surveyed data at test sites.

3.6 Summarize and Analyze Results

In the end, the global distribution of mangrove coasts where spaceborne bathymetry is effective can be created. In the sites where the approach is successful, profile data can be extracted from the 2D bathymetry output to provide information about the profile shapes.

3.7 Strengths and Limitations

The proposed method could allow a significant increase in the global data available about mangrove ecosystems, and the analysis could potentially be repeated in the future and more data is available to give a temporal dimension, allowing for assessment of offshore erosion or deposition processes around mangroves. The largest limitation forseen is the turbidity limiting the optical clarity of the water. This might make it difficult to find meaningful data along muddy coasts, and limit the bathymetric analysis to carbonate mangroves, which tend to occur in clearer waters.

Practicalities

4.1 Planned Schedule

Figure 4.1 shows the tentative schedule for the project. The early stages of some steps have already been started to assess their feasibility.

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Figure 4.1: Proposed Schedule

4.2 Planned Final Document Outline

- 1. Introduction
- 2. Background
 - (a) mangroves
 - i. Morphodynamics
 - ii. Wave-vegetation interation
 - iii. Importance of bathymetry
 - (b) Lidar Bathymetry
 - i. History
 - ii. Strengths
 - iii. Weaknesses
 - iv. Snell's law and lidar refraction in the water column
 - v. Photon counting lidar technology
 - vi. Geodetic reference systems in oceanography
 - vii. ICESat-2
 - A. Photo geolocation algorithm
 - B. Geophysical corrections
 - C. Known issues
 - (c) Satellite-derived Optical bathymetry
 - i. Wave-kinematic vs Optical
 - ii. Analytical vs Empirical
 - iii. Sentinel-2
 - iv. Processing in GEE
- 3. Methodology
 - (a) Selection of test sites
 - (b) selection of global analysis sites
 - (c) Processing of Lidar data
 - i. Extracting sea surface returns
 - ii. Extracting subsurface returns

iii. DBSCAN

4. Results

- (a) Geographic distribution of sites with useable data
- (b) error
 - i. RMSE and MAE between Lidar and sea-truth data
 - ii. RMSE and MAE between SDB raster and sea-truth data

5. Discussion

- (a) Effect of turbidity on data usability
- (b) Terrigenous vs carbonate mangrove environment
- (c) Geographic patterns in ability to extract bathymetry
- 6. Conclusion
- 7. Recommendations
- 8. Appendix A: Python module documentation
- 9. Appendix B: Google Earth Engine Javascript code
- 10. Appendix C: Full output data from all test sites

Bibliography

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