

A photograph of the Fallingwater house by Frank Lloyd Wright, built into a rocky cliff over a waterfall. The house features cantilevered stone and concrete overhangs. It is surrounded by dense green trees and foliage. The text is overlaid on the lower half of the image.

Machine Learning in Production Toward Architecture and Design

After requirements...

Fundamentals of Engineering AI-Enabled Systems

Holistic system view: AI and non-AI components, pipelines, stakeholders, environment interactions, feedback loops

Requirements:

- System and model goals
- User requirements
- Environment assumptions
- Quality beyond accuracy
- Measurement
- Risk analysis
- Planning for mistakes

Architecture + design:

- Modeling tradeoffs
- Deployment architecture
- Data science pipelines
- Telemetry, monitoring
- Anticipating evolution
- Big data processing
- Human-AI design

Quality assurance:

- Model testing
- Data quality
- QA automation
- Testing in production
- Infrastructure quality
- Debugging

Operations:

- Continuous deployment
- Contin. experimentation
- Configuration mgmt.
- Monitoring
- Versioning
- Big data
- DevOps, MLOps

Teams and process: Data science vs software eng. workflows, interdisciplinary teams, collaboration points, technical debt

Responsible AI Engineering

Provenance,
versioning,
reproducibility

Safety

Security and
privacy

Fairness

Interpretability
and explainability

Transparency
and trust

Ethics, governance, regulation, compliance, organizational culture

Learning Goals

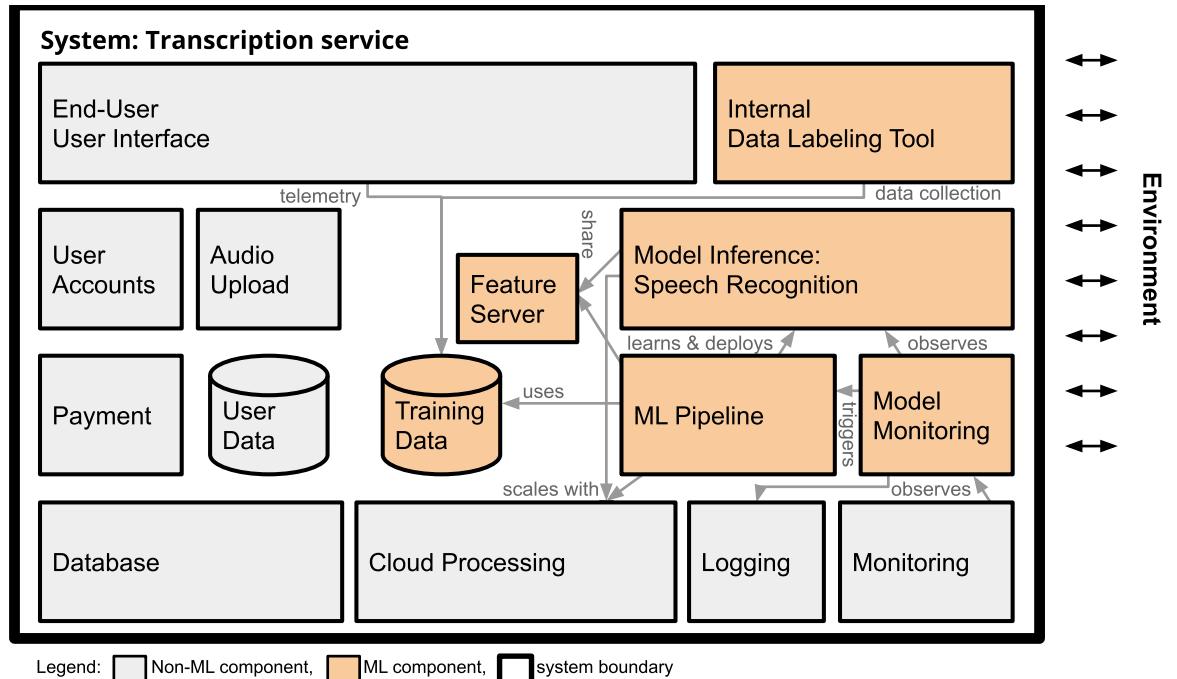
- Describe the role of architecture and design between requirements and implementation
- Identify the different ML components and organize and prioritize their quality concerns for a given project
- Explain the key ideas behind decision trees and random forests and analyze consequences for various qualities
- Demonstrate an understanding of the key ideas of deep learning and how it drives qualities
- Plan and execute an evaluation of the qualities of alternative AI components for a given purpose

Readings

Required reading: Hulten, Geoff. "Building Intelligent Systems: A Guide to Machine Learning Engineering." (2018), Chapters 17 and 18

Recommended reading: Siebert, Julien, Lisa Joeckel, Jens Heidrich, Koji Nakamichi, Kyoko Ohashi, Isao Namba, Rieko Yamamoto, and Mikio Aoyama. "Towards Guidelines for Assessing Qualities of Machine Learning Systems." In International Conference on the Quality of Information and Communications Technology, pp. 17–31. Springer, Cham, 2020.

Recall: ML is a Component
in a System in an
Environment



- **ML components** for transcription model, pipeline to train the model, monitoring infrastructure...
 - **Non-ML components** for data storage, user interface, payment processing, ...
 - User requirements and assumptions
 - System quality vs model quality
 - System requirements vs model requirements

Recall: Systems Thinking



A system is a set of inter-related components that work together in a particular environment to perform whatever functions are required to achieve the system's objective -- Donella Meadows

Thinking like a Software Architect



From Requirements to Implementations...

We know what to build, but how? How do we meet the quality goals?



Software architecture: Key design decisions, made early in the development, focusing on key product qualities

Architectural decisions are hard to change later

Software Architecture

The software architecture of a program or computing system is the structure or structures of the system, which comprise software elements, the externally visible properties of those elements, and the relationships among them. -- [Kazman et al. 2012](#)

Architecture Decisions: Examples

- What are the major components in the system? What does each component do?
- Where do the components live? Monolithic vs microservices?
- How do components communicate to each other? Synchronous vs asynchronous calls?
- What API does each component publish? Who can access this API?
- Where does the ML inference happen? Client-side or server-side?
- Where is the telemetry data collected from the users stored?
- How large should the user database be? Centralized vs decentralized?
- ...and many others

Software Architecture

*Architecture represents the set of **significant design** decisions that shape the form and the function of a system, where **significant** is measured by cost of change. -- [Grady Booch, 2006]*

How much Architecture/Design?



Software Engineering Theme: *Think before you code*

Like requirements: Slower initially, but upfront investment can prevent problems later and save overall costs

- > Focus on most important qualities early, but leave flexibility

Quality Requirements Drive Architecture Design

Driven by requirements, identify most important qualities

Examples:

- Development cost, operational cost, time to release
- Scalability, availability, response time, throughput
- Security, safety, usability, fairness
- Ease of modifications and updates
- ML: Accuracy, ability to collect data, training latency

Architecture Design Involves Quality Trade-offs



☰ Q. What are quality trade-offs between the two?

Why Architecture? (Kazman et al. 2012)

Represents earliest design decisions.

Aids in **communication** with stakeholders: Shows them “how” at a level they can understand, raising questions about whether it meets their needs

Defines **constraints** on implementation: Design decisions form “load-bearing walls” of application

Dictates **organizational structure**: Teams work on different components

Inhibits or enables **quality attributes**: Similar to design patterns

Supports **predicting** cost, quality, and schedule: Typically by predicting information for each component

Aids in software **evolution**: Reason about cost, design, and effect of changes

Case Study: Twitter



Speaker notes

Source and additional reading: Raffi. [New Tweets per second record, and how!](#) Twitter Blog, 2013



Twitter - Caching Architecture



Speaker notes

- Running one of the world's largest Ruby on Rails installations
- 200 engineers
- Monolithic: managing raw database, memcache, rendering the site, and * presenting the public APIs in one codebase
- Increasingly difficult to understand system; organizationally challenging to manage and parallelize engineering teams
- Reached the limit of throughput on our storage systems (MySQL); read and write hot spots throughout our databases
- Throwing machines at the problem; low throughput per machine (CPU + RAM limit, network not saturated)
- Optimization corner: trading off code readability vs performance



Twitter's Redesign Goals

- **Performance**
 - Improve median latency; lower outliers
 - Reduce number of machines 10x
- **Reliability**
 - Isolate failures
- **Maintainability**
 - "*We wanted cleaner boundaries with "related" logic being in one place*": encapsulation and modularity at the systems level (vs class/package level)
- **Modifiability**
 - Quicker release of new features: "*run small and empowered engineering teams that could make local decisions and ship user-facing changes, independent of other teams*"

Twitter: Redesign Decisions

- Ruby on Rails -> JVM/Scala
- Monolith -> Microservices
- RPC framework with monitoring, connection pooling, failover strategies, loadbalancing, ... built in
- New storage solution, temporal clustering, "roughly sortable ids"
- Data driven decision making



Twitter Case Study: Key Insights

Architectural decisions affect entire systems, not only individual modules

Abstract, different abstractions for different scenarios

Reason about quality attributes early

Make architectural decisions explicit

Question: Did the original architect make poor decisions?

Codifying Design Knowledge



System Decomposition



Identify components and their responsibilities

Establishes interfaces and team boundaries

Common Components in ML-based Systems

- **Model inference service:** Uses model to make predictions for input data
- **ML pipeline:** Infrastructure to train/update the model
- **Monitoring:** Observe model and system
- **Data sources:** Manual/crowdsourcing/logs/telemetry/...
- **Data management:** Storage and processing of data, often at scale
- **Feature store:** Reusable feature engineering code, cached feature computations

Common System-Wide Design Challenges

Separating concerns, understanding interdependencies

- e.g., anticipating/breaking feedback loops, conflicting needs of components

Facilitating experimentation, updates with confidence

Separating training and inference; closing the loop

- e.g., collecting telemetry to learn from user interactions

Learn, serve, and observe at scale or with resource limits

- e.g., cloud deployment, embedded devices

Each system is different...

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NOTES

Write your notes here

Speaker 5 ▶ 07:44

Yeah. So there's a slight story behind that. So back when I was in, uh, Undergrad, I wrote a program for myself to measure a, the amount of time I did data entry from my father's business and I was on windows at the time and there wasn't a function called time dot [inaudible] time, uh, which I needed to parse dates to get back to time, top of representation, uh, I figured out a way to do it and I gave it to what's called the python cookbook because it just seemed like something other people could use. So it was just trying to be helpful. Uh, subsequently I had to figure out how to make it work because I didn't really have to. Basically, it bothered me that you had to input all the locale information and I figured out how to do it over the subsequent months. And actually as a graduation gift from my Undergrad, the week following, I solved it and wrote it all out.

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How did we do on your transcript? ☆☆☆☆☆

Each system is different...



Each system is different...



Each system is different...



System Decomposition

Each system is different, identify important components

Examples:

- Personalized music recommendations: microservice deployment in cloud, logging of user activity, nightly batch processing for inference, regular model updates, regular experimentation, easy fallback
- Transcription service: irregular user interactions, large model, expensive inference, inference latency not critical, rare model updates
- Autonomous vehicle: on-board hardware sets limits, real-time needs, safety critical, updates necessary, limited experimentation in practice, not always online
- Smart keyboard: privacy focused, small model, federated learning on user device, limited telemetry

Common System Structures

Designers and architects accumulate tacit and codified knowledge based on their own experience and best practices.

In designing a new system, it is best to start with experience and a design vocabulary, focusing directly on the specific qualities relevant to the tradeoffs.

At the highest level of organizing components, there are common structures shared by many systems, also known as *architectural styles*.

Monolithic system



Client-Server Architecture



- A server provides functionality to multiple clients, typically over a network connection.
- Resources shared for many users, while clients are fairly simple.

Multi-tier architecture



Higher tiers send requests to lower tiers, but not vice versa.

Common for business and web applications.

Speaker notes

can be conceptually extended with components related to machine learning (as we will show in chapter Deploying a Model).



SOA and microservices



Multiple self-contained services/processes that communicate via
≡ RPC.

Speaker notes

allows independent deployment, versioning, and scaling of services and flexible routing of requests at the network level. Many modern, scalable web-based systems use this design, as we will discuss in chapter Scaling the System. Also independent development.



Event-based architecture



Individual system components listen to messages broadcasted by other components, typically through some message bus.

Speaker notes

Since the component publishing a message does not need to know who consumes it, this architecture strongly decouples components in a system and makes it easy to add new components. We will see this architecture style when discussing stream processing systems in chapter Scaling the System.



Data-flow architectures



Dataflow program composed of shell commands.

The system is organized around data, often in a sequential pipeline.

Speaker notes

This design allows flexible changes of components and flexible composition of pipelines from different subsets of components. Unix shell commands can be composed through pipes to perform more complex tasks and machine-learning pipelines often follow this design of multiple transformations to a dataset arranged in a sequence or directed acyclic graph. Machine-learning pipelines tend to follow this data-flow style, as do batch processing systems for very large datasets.



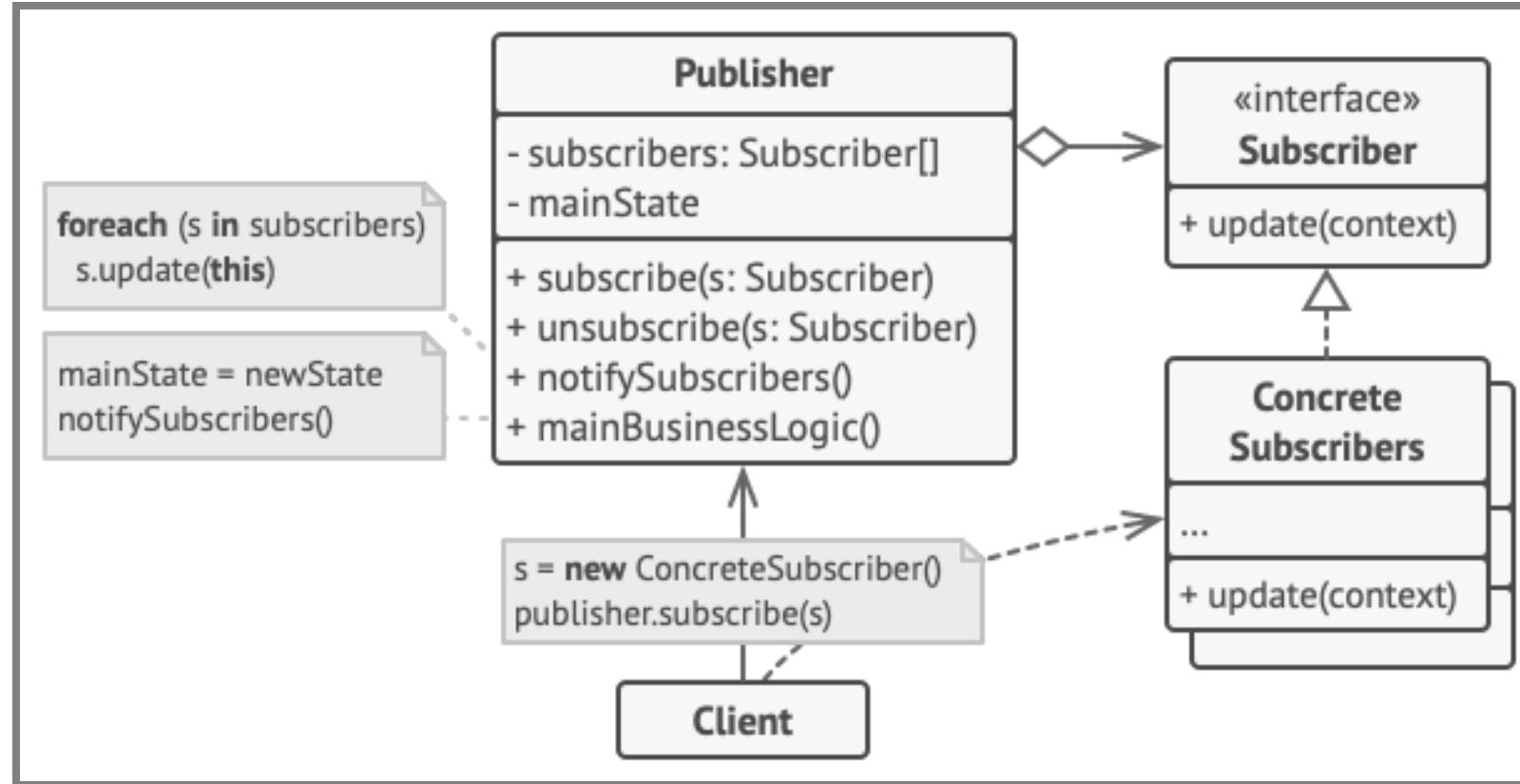
Design Patterns



Design patterns name and describe common solutions to known design problems, and known advantages and pitfalls.

Historically popular in OO; now applied broadly across system design, both architecturally and at a lower level (i.e., interactions among subsystems).

Observer or publish-subscribe



Intent: Define a one-to-many dependency between objects so that when one object changes state, all its dependents are notified and updated automatically.

Speaker notes

Motivation: [This would include an illustrative example of a user interface that needs to update multiple visual representations of data whenever input data changes, such as multiple diagrams in a spreadsheet.] Solution: [This would include a description of the technical structure with an observer interface implemented by observers and an observable object managing a list of observers and calling them on state changes.] Benefits, costs, tradeoffs: Decoupling of the observed object and observers; support of broadcast communication. Implementation overhead; observed objects unaware of consequences and costs of broadcast objects. [Typically this would be explained in more detail with examples.]



Architectural pattern: Heartbeat tactic



Intent: Detect when a component is unavailable to trigger mitigations or repair

Speaker notes

Motivation: Detect with low latency when a component or server becomes unavailable to automatically restart it or redirect traffic. Solution: The observed component sends heartbeat messages to another component monitoring the system in regular predictable intervals. When the monitoring component does not receive the message it assumes the observed component is unavailable and initiates corrective actions. Options: The heartbeat message can carry data to be processed. Standard data messages can stand in for heartbeat messages so that extra messages are only sent when no regular data messages are sent for a period. Benefits, costs, tradeoffs: Component operation can be observed. Only unidirectional messaging is needed. The observed component defines heartbeat frequency and thus detection latency and network overhead. Higher detection latency can be achieved at the cost of higher network traffic with more frequent messages; higher confidence in detection can be achieved at the cost of lower latency by waiting for multiple missing messages. Alternatives: Ping/echo tactic where the monitoring component requests responses. Source: <https://www.se.rit.edu/~swen-440/slides/instructor-specific/Kuehl/Lecture%2019%20Design%20Tactics.pdf>



Machine learning pattern for reproducibility: Feature Store



Intent: Reuse features across projects by decoupling feature creation from model development and serving

Source: <https://changyaochen.github.io/ML-design-pattern-1/> Motivation: The same feature engineering code is needed during model training and model serving; inconsistencies are dangerous. In addition, some features may be expensive to compute but useful in multiple projects. Also, data scientists often need the same or similar features across multiple projects, but often lack a systematic mechanism for reuse. Solution: Separate feature engineering code and reuse it both in the training pipeline and the model inference infrastructure. Catalog features with metadata to make them discoverable. Cache computed features used in multiple projects. Typically implemented in open-source infrastructure projects. Benefits: Reusable features across projects; avoiding redundant feature computations; preventing training-serving skew; central versioning of features; separation of concerns. Costs: Nontrivial infrastructure; extra engineering overhead in data science projects. This concept is discussed in more depth in chapter Deploying a Model.



Scoping Relevant Qualities of ML Components

From System Quality Requirements to Component Quality Specifications

AI = DL?



Design Decision: ML Model Selection

How do I decide which ML algorithm to use for my project?

Criteria: Quality Attributes & Constraints

Accuracy is not Everything

Beyond prediction accuracy, what qualities may be relevant for an ML component?



Speaker notes

Collect qualities on whiteboard



Qualities of Interest?

Scenario: ML component for transcribing audio files

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How did we do on your transcript? ⭐⭐⭐⭐⭐

Speaker notes

Which of the previously discussed qualities are relevant? Which additional qualities may be relevant here?

Cost per transaction; how much does it cost to transcribe? How much do we make?



Qualities of Interest?

Scenario: Component for detecting lane markings in a vehicle



Speaker notes

Which of the previously discussed qualities are relevant? Which additional qualities may be relevant here?

Realtime use



Qualities of Interest?

Scenario: Component for detecting credit card frauds, as a service for banks

Speaker notes

Very high volume of transactions, low cost per transaction, frequent updates

Incrementality



Common ML Qualities to Consider

- Accuracy
- Correctness guarantees? Probabilistic guarantees (--> symbolic AI)
- How many features?
- How much data needed? Data quality important?
- Incremental training possible?
- Training time, memory need, model size -- depending on training data volume and feature size
- Inference time, energy efficiency, resources needed, scalability
- Interpretability, explainability
- Robustness, reproducibility, stability
- Security, privacy, fairness

Constraints and Tradeoffs



Speaker notes

How do I decide which ML algorithm to use for my project?

Criteria: Quality Attributes & Constraints



Constraints

Constraints define the space of attributes for valid design solutions



Speaker notes

Design space exploration: The space of all possible designs (dotted rectangle) is reduced by several constraints on qualities of the system, leaving only a subset of designs for further consideration (highlighted center area).



Types of Constraints

Problem constraints: Minimum required QAs for an acceptable product

Project constraints: Deadline, project budget, available personnel/skills

Design constraints

- Type of ML task required (regression/classification)
- Available data
- Limits on computing resources, max. inference cost/time

Constraints: Cancer Prognosis?



Constraints: Music Recommendations?



Trade-offs between ML algorithms

If there are multiple ML algorithms that satisfy the given constraints, which one do we select?

Different ML qualities may conflict with each other; this requires making a **trade-off** between these qualities

Among the qualities of interest, which one(s) do we care the most about?

- And which ML algorithm is most suitable for achieving those qualities?
- (Similar to requirements conflicts)

Common ML Algorithms and their Qualities

Linear Regression



- Tasks: Regression
- Qualities: Advantages: ?? Drawbacks: ??

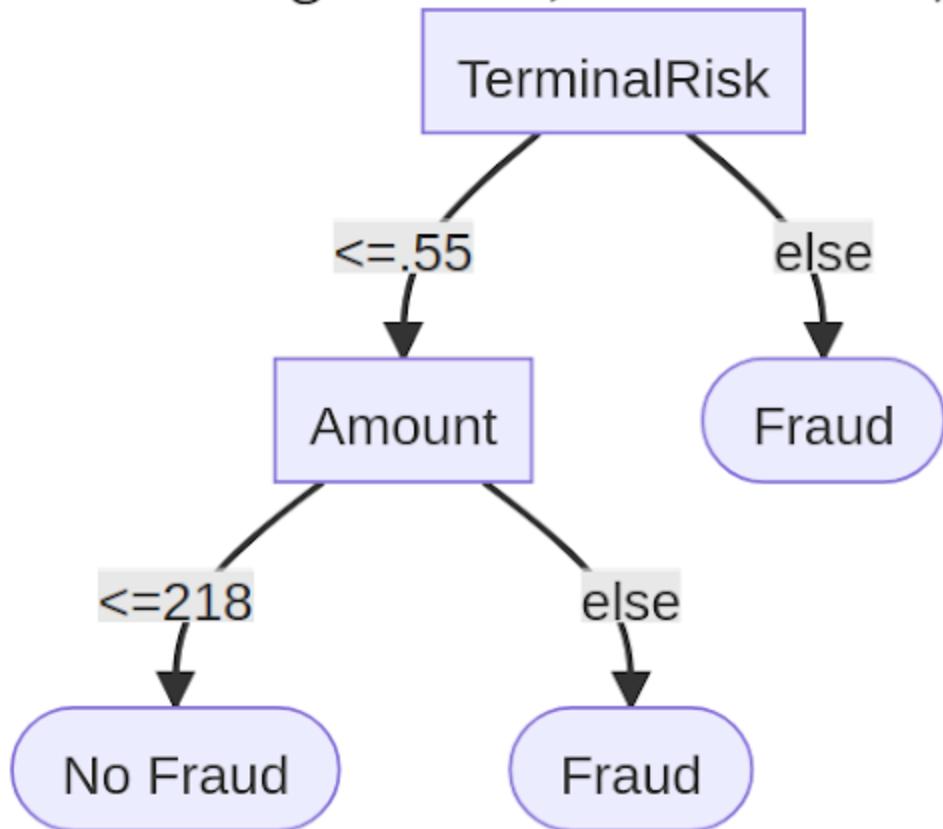
Speaker notes

- Easy to interpret, low training cost, small model size
- Can't capture non-linear relationships well



Decision Trees

$f(\text{amount}, \text{weekend}, \text{atNight}, \text{customerAvgAmount}, \text{terminalRisk}) =$



- Tasks: Classification & regression
- Qualities: Advantages: ?? Drawbacks: ??

Building:

- Identify all possible decisions
- Select the decision that best splits the dataset into distinct outcomes (typically via entropy or similar measure)
- Repeatedly further split subsets, until stopping criteria reached
- random forests do the same but with multiple trees, prediction of multiple trees

Neural Networks + Deep Learning

Simulating biological neural networks of neurons (nodes) and synapses (connections). Basic building blocks: Artificial neurons, in layers.

Deep learning: more layers, different numbers of neurons. Different kinds of connections.

Advantages ?? Drawbacks??

Speaker notes

Artificial neural networks are inspired by how biological neural networks work ("groups of chemically connected or functionally associated neurons" with synapses forming connections)

- High accuracy; can capture a wide range of problems (linear & non-linear)
- Difficult to interpret; high training costs (time & amount of data required, hyperparameter tuning)

From "Texture of the Nervous System of Man and the Vertebrates" by Santiago Ramón y Cajal, via

https://en.wikipedia.org/wiki/Neural_circuit#/media/File:Cajal_actx_inter.jpg



Example Scenario

MNIST Fashion dataset of 70k 28x28 grayscale pixel images, 10 output classes

Example Scenario

- MNIST Fashion dataset of 70k 28x28 grayscale pixel images, 10 output classes
- $28 \times 28 = 784$ inputs in input layers (each 0..255)
- Example model with 3 layers, 300, 100, and 10 neurons

```
model = keras.models.Sequential([
    keras.layers.Flatten(input_shape=[28, 28]),
    keras.layers.Dense(300, activation="relu"),
    keras.layers.Dense(100, activation="relu"),
    keras.layers.Dense(10, activation="softmax")
])
```

≡ How many parameters does this model have?

Example Scenario

```
model = keras.models.Sequential([
    keras.layers.Flatten(input_shape=[28, 28]),
    # 784*300+300 = 235500 parameter
    keras.layers.Dense(300, activation="relu"),
    # 300*100+100 = 30100 parameters
    keras.layers.Dense(100, activation="relu"),
    # 100*10+10 = 1010 parameters
    keras.layers.Dense(10, activation="softmax")
])
```

Total of 266,610 parameters in this small example! (Assuming float types, that's 1 MB)

Network Size

- 50 Layer ResNet network -- classifying 224x224 images into 1000 categories
 - 26 million weights, computes 16 million activations during inference, 168 MB to store weights as floats
- Google in 2012(!): 1TB-1PB of training data, 1 billion to 1 trillion parameters
- OpenAI's GPT-2 (2019) -- text generation
 - 48 layers, 1.5 billion weights (~12 GB to store weights)
 - released model reduced to 117 million weights
 - trained on 7-8 GPUs for 1 month with 40GB of internet text from 8 million web pages
- OpenAI's GPT-3 (2020): 96 layers, 175 billion weights, 700 GB in memory, \$4.6M in approximate compute cost for training

Speaker notes

<https://lambdalabs.com/blog/demystifying-gpt-3/>



Cost & Energy Consumption

Consumption	CO2 (lbs)	Training one model (GPU)	CO2 (lbs)
Air travel, 1 passenger, NY↔SF	1984	NLP pipeline (parsing, SRL)	39
Human life, avg, 1 year	11,023	w/ tuning & experimentation	78,468
American life, avg, 1 year	36,156	Transformer (big)	192
Car, avg incl. fuel, 1 lifetime	126,000	w/ neural architecture search	626,155

Cost & Energy Consumption

Model	Hardware	Hours	CO2	Cloud cost in USD
Transformer	P100x8	84	192	289-981
ELMo	P100x3	336	262	433-1472
BERT	V100x64	79	1438	3751-13K
NAS	P100x8	274,120	626,155	943K-3.2M
GPT-2	TPUv3x32	168	—	13K-43K
GPT-3			—	4.6M

Strubell, Emma, Ananya Ganesh, and Andrew McCallum. "[Energy and Policy Considerations for Deep Learning in NLP](#)." In Proc. ACL, pp. 3645-3650. 2019.

Trade-offs: Cost vs Accuracy

The screenshot shows the Netflix Prize Leaderboard page. At the top, it says "Netflix Prize" and has a large red "COMPLETED" stamp. Below that is a navigation bar with links for Home, Rules, Leaderboard, Update, and Download. The main section is titled "Leaderboard" and says "Showing Test Score. [Click here to show quiz score](#)". It includes a dropdown menu to "Display top 20 leaders". The table below lists the top 8 teams:

Rank	Team Name	Best Test Score	% Improvement	Best Submit Time
1	BellKor's Pragmatic Chaos	0.8567	10.06	2009-07-26 18:18:28
2	The Ensemble	0.8567	10.06	2009-07-26 18:38:22
3	Grand Prize Team	0.8582	9.90	2009-07-10 21:24:40
4	Opera Solutions and Vandelay United	0.8588	9.84	2009-07-10 01:12:31
5	Vandelay Industries!	0.8591	9.81	2009-07-10 00:32:20
6	PragmaticTheory	0.8594	9.77	2009-06-24 12:06:56
7	BellKor in BigChaos	0.8601	9.70	2009-05-13 08:14:09
8	Dace	0.8612	9.59	2009-07-24 17:18:43

"We evaluated some of the new methods offline but the additional accuracy gains that we measured did not seem to justify the engineering effort needed to bring them into a production environment."

Amatriain & Basilico. Netflix Recommendations: Beyond the 5 stars, Netflix Technology Blog (2012)

Trade-offs: Accuracy vs Interpretability



Q. Examples where one is more important than the other?

Bloom & Brink. [Overcoming the Barriers to Production-Ready Machine Learning Workflows](#),
Presentation at O'Reilly Strata Conference (2014).

Breakout: Qualities & ML Algorithms

Consider two scenarios:

1. Credit card fraud detection
2. Pedestrian detection in sidewalk robot

As a group, post to #lecture tagging all group members:

- *Qualities of interests: ??*
- *Constraints: ??*
- *ML algorithm(s) to use: ??*

Summary

Software architecture focuses on early key design decisions, focused on key qualities

Between requirements and implementation

Decomposing the system into components, many ML components

Many qualities of interest, define metrics and operationalize

Constraints and tradeoff analysis for selecting ML techniques in production ML settings

Further Readings

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- Habibullah, Khan Mohammad, Gregory Gay, and Jennifer Horkoff. "[Non-Functional Requirements for Machine Learning: An Exploration of System Scope and Interest](#)." arXiv preprint arXiv:2203.11063 (2022).

