**M6.5.** 1 punkt Wyznaczyć wielomian  $H_5 \in \Pi_5$ , spełniający warunki  $H_5(x_i) = y_i$ ,  $H'_5(x_i) = y'_i$  (i = 0, 1, 2), gdzie  $x_i$ ,  $y_i$ ,  $y'_i$  mają następujące wartości:

i	$x_i$	$y_i$	$y_i'$
0	-1	7	-1
1	0	6	0
2	2	22	56

$$f[x_{i},x_{i}] = f'(x_{i}), bo$$

$$f[x_{i},x_{i}] = \frac{f'(x_{i}) - f(x)}{x_{i}h - x} = \frac{f(x_{i}h) - f(x)}{h} \xrightarrow{h \to 0} f'(x)$$

$$H_{5}(x) = \sum_{k=0}^{5} f[x_{0}, -, x_{k}] p_{k}(x) =$$

$$= 7 - \lambda(x+\lambda) + (x+\lambda)^{2}x + (x+\lambda)^{2}x^{2}(x-2)$$

$$= 7 - x - 1 + x^{3} + 2x^{2} + x + (x-2)[x^{4} + 2x^{3} + x^{2}] =$$

$$= x^{3} + 2x^{2} + 6 + x^{5} + 2x^{4} + x^{3} - 2x^{4} - hx^{3} - 2x^{2} =$$

$$= x^{5} - 2x^{3} + 6$$

$$H_5' \omega = 5x^4 - 6x^2$$

$$H_5(-1) = -1+2+6 = 7$$
 $H_5(0) = 6$ 
 $H_6(2) = 32-16+6=22$ 

$$H_5(0) = 0$$
 $H_5(2) = 32 - 16 + 6 = 22$ 
 $H_5'(-1) = 5 - 6 = -1$ 
 $H_5'(0) = 0$ 
 $H_5'(0) = 5.16 - 6.4 = 80 - 24 = 56$ 
 $git$