MSIS 510: Introduction to Data Mining and Analytics Group Project



The secret formula for the next hit artist on Spotify

By: MSIS Purple 2

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Project Goal

Oswald Records is an established record label with a strong history of artist management and content creation. In addition to the traditional processes, such as using Artists and Repertoires (A&Rs) that scout new musical talent and undertaking market research, we recently expanded our capabilities to include a business intelligence team focused on analyzing data to better understand demographic and social trends correlated with hit music at the top of the billboards. With increased competition today, the market is saturated, especially with the increased popularity of streaming services. Our analysis has determined the influx of tracks and artists into the market threatens our current business model. Moreover, any artists' ability to upload songs on a streaming service – regardless of popularity or name recognition – indicates a necessary change in Oswald Records' strategy.

This project aims to identify the characteristics that make a track popular on a streaming service such as Spotify, empowering our company to advise our artists and produce music that earns us the maximum return on investment through increased popularity and a larger number of streams.

More importantly, we are seeking to provide the answer to these questions:

- 1. What are the characteristics that an artist's tracks must have to be popular on Spotify?
- 2. What time of year is best suited to release particular types of music?
- 3. What is the optimal genre of music to be released in 2021?

Dataset description

For this exercise, our team selected the Spotify Dataset on Kaggle¹ which includes data from over 160 thousand songs / tracks released between 1921 to 2020. This can be referenced here. This data was extracted via the Spotify Web API and presented in multiple CSV files. Our team focused on the data.csv, data_by_artist.csv, and data_by_genres.csv files. There was a total of 202308 observations, and we summarize the variables we have focused on below. Our target variable for this exercise is **popularity**. As per Oswald Records' business requirements, and after analyzing the popularity of numerous top 1000 songs, we are designating a popularity of 70 or above as the score to identify a track as popular, 60 or above for an artist.

Field Name	Description	Туре	Range / Sample values
Id	Id of track – assigned by	Numerical	
	Spotify		
acousticness	Measure of how acoustic	Numerical	0 to 1
	a track is.		1 is the most acoustic
danceability	Suitability of a track for	Numerical	0 to 1
	dancing, based on		0 is least danceable.
	tempo, rhythm stability,		
	beat strength and		
	regularity.		
energy	Perceptual measure of	Numerical	0 to 1
	intensity and activity		1 is highest energy.
duration_ms / Avg	Duration of track in	Numerical	200K to 300K
Song Duration	milliseconds		
instrumentalness	Measure of whether a	Numerical	0 to 1
	track contains vocal		1 is the most
	content		instrumental, with no
			vocal content
valence	Measure of how positive	Numerical	0 to 1
	the music is (happy /		1 is the most positive
	cheerful)		

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¹ Spotify Dataset 1921 – 2020, 160K+ Tracks Version 9 by Yamac Eren Ay

Field Name	Description	Туре	Range / Sample values
tempo	Pace of the music	Numerical	50 to 150
	measured in beats per		
	minute		
liveness	Presence of an audience	Numerical	0 to 1
	during the recording		.8 or above indicates
			the track was recorded
			live
loudness	Loudness measured in	Numerical	-60 to 0
	decibels, averaged across		
	the entire track.		
speechiness	Presence of spoken	Numerical	0 to 1
	words in a track.		.66 or above are made
			entirely of spoken
			words
year	The release year of the	Categorical	1921 to 2020
	track		
mode	Modality of the track/	Dummy	0 = Minor, 1 = Major
	type of scale for melodic		
	content		
explicit	Indicator whether a track	Dummy	0 = No Explicit content,
	contains explicit content		1 = Explicit content
key	Overall key of a track	Categorical	0 to 11,
			0 = C, 1 = C#/Db
artists	The artist for the track	Categorical	list of artists
			E.g., Foo Fighters
release_date	The exact date the track	Categorical	YYYY-mm-dd
	was released		
release_month	The exact month that the	Categorical	1 – 12
	track was released in.		1 is January
	This was created during		
	our pre-processing steps		
name	The name of the track.	Categorical	
genres	The genre the track	Categorical	Genre name
	belongs to.		E.g., Alternative Rock
popularity	Indication of the	Numerical	0 – 100
	popularity of the Track.		

Data preparation details

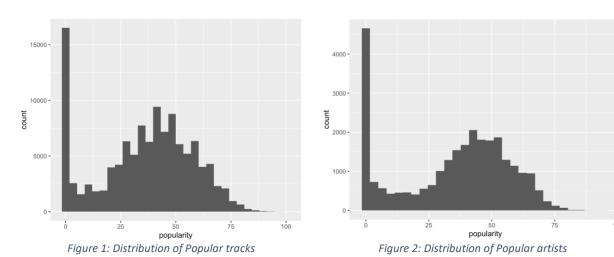
In order to prepare the data for our mining efforts, we undertook the following pre-processing steps:

1. All Datasets:

- a. Removed NULL values.
- b. Data transformation applied:
 - 1. Normalization, discretization, Concept Hierarchy Generation.
 - 2. Changed duration to seconds and changed column name to "Avg Song Duration".
- 2. data.csv: (Observations- Before processing: 170654, After processing: 118188)
 - a. Removed all rows with incomplete release dates.
 - b. Extracted month from release date field and added column release month.
 - c. Removed all non-alphanumeric characters from track name and artist name.
 - d. Removed rows with empty track names.
 - e. Removed the identifier column (id).
- 3. data_by_genre.csv: (Observations 2973)
 - a. Removed rows with empty genre values.
 - b. Removed all non-alphanumeric characters from genre.
 - c. Combined terms within a genre.
- 4. data_by_artist.csv: (Observations- Before processing: 28681, After processing: 27262)
 - a. Removed non-English terms from columns.
 - b. Removed rows with missing data

Data Visualization and Exploratory analysis

We structured our exploratory analysis efforts first by validating the playing field, i.e., the competition. The histograms below show that the distribution of popular tracks/artists gets much lower around the 70 + mark. This indicates the industry's competitive nature, as very few tracks/artists are rising to that level.



Next, we have dived into a better understanding of how the various features of tracks have evolved in music released from 1921 till the present day, and then comparing them with the popularity of tracks listed by Spotify. We have done this by selecting all the features associated with tracks, and then used line charts to identify trends in the change of these features over time and the impact on popularity.

To understand how the average valence, acousticness, danceability, energy, liveness, and loudness for all songs on Spotify changed over time relative to average song popularity, the team plotted those data elements in a single line chart, as seen in Figure 3, before diving into each feature individually.

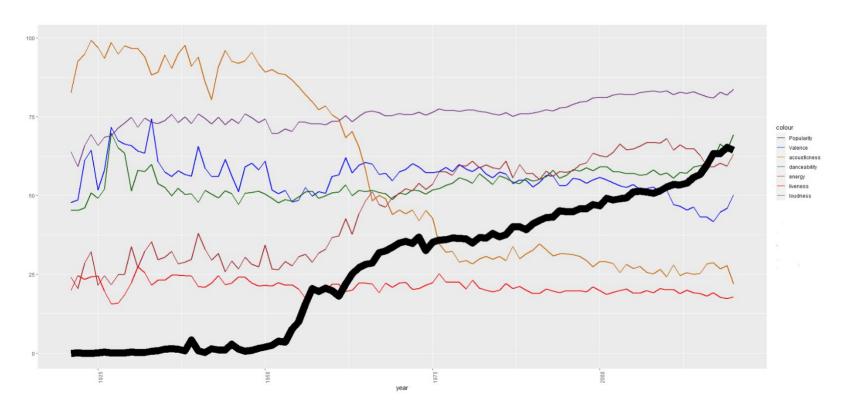


Figure 3: Average popularity and plotting valence, acousticness, danceability, energy, liveness and loudness for all songs on Spotify based on release date

Figure 3 shows that popularity of songs is much more for music released recently, compared to older release dates. Our team believes the increase is due to more music being created, especially due to the advent of technology that enabled and simplified music production and the easy availability of streaming services such as Spotify. This observation is reinforced by Figure 4, which illustrates the number of songs on Spotify by year created.

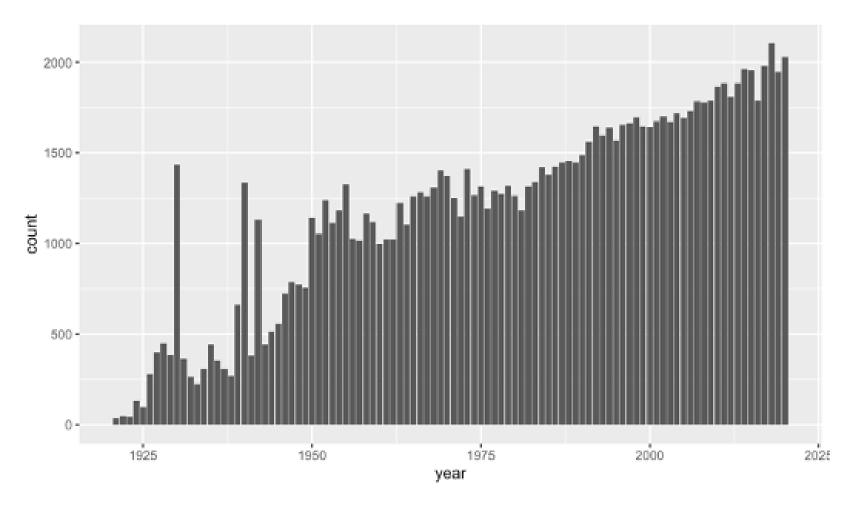


Figure 4: number of songs on Spotify by year created

As per figure 2, we can see that the average valence, acousticness, danceability, and energy of Spotify songs have changed significantly as average popularity has increased. Average loudness and liveness have not changed significantly. To explore these song features further, they are each broken out in separate line charts in Figure 5 below.

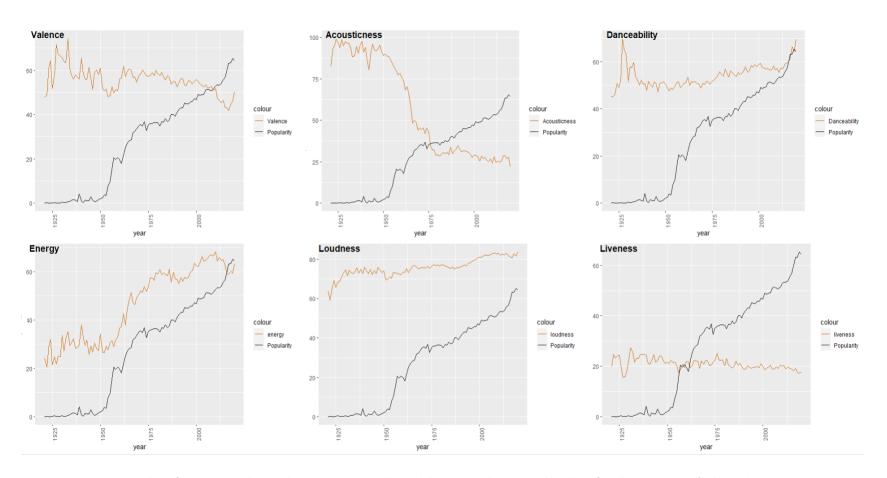


Figure 5: Deep dive of average popularity valence, acousticness, danceability, energy, liveness and loudness for all songs on Spotify changed over time

Figure 5 shows that average song valence and acousticness have dropped as song popularity has increased. There isn't a significant change for average song loudness and liveness.

Average song danceability and energy, on the other hand, have increased as popularity has increased. Notably, from this analysis, we can see spikes in danceability for songs released during challenging times, such as the Great Depression in the 1930s and the 2020 COVID pandemic.

Additional song features in the Spotify dataset were analyzed and found to not significantly correlated with popularity. Data visualizations for these features can be found in Appendix A. We also looked at the popularity of songs by month released. The findings from this analysis are captured in Figure 6. From our analysis, we were able to determine that tracks released in January and December are, on average, less popular than songs released in other months.

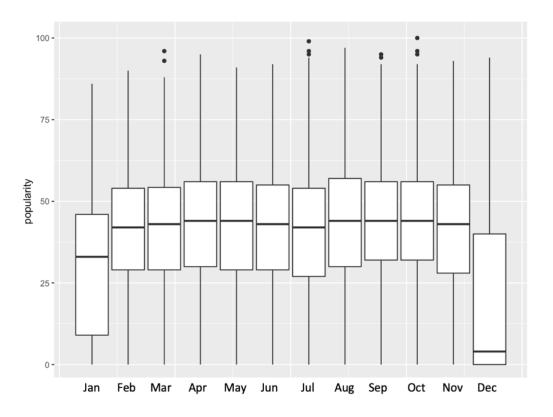


Figure 6: Song popularity by release month

The team was also curious what the most popular genres and song titles are on Spotify. As structured data was lacking, we used text analysis to identify trends, as seen in Figures 7 and 8. From our analysis in Figure 7, we learned that love is the most popular word for song titles.



Figure 7: Popular words in song titles

From the analysis in Figure 8, we learned the movie-tunes, pop and show-tunes are the most popular genres in Spotify.



Figure 8: Popular genres

Data Modeling and Methodology

At this point in our analysis, we will delve into setting up Data models needed to answer the key questions we outlined at the introduction of this report.

Q1: What are the characteristics that an artist's tracks must have to be popular on Spotify?

To answer this question, we set up a logistic regression model using the artists datasets. Also, we converted popularity into a categorical feature with a value of 1 if it is > 60 for artist data sets. The training dataset was set to 60 percent of the pre-processed data, which amounted to 16357 rows. We also ran a correlation matrix and a CORR plot (See Appendix C).

The correlation matrix indicated a strong relationship between energy and loudness and a negative correlation with acousticness. However, acousticness and loudness themselves are not correlated. This information guided our decision to remove energy from our analysis, as it is a redundant variable. The CORR plot below confirms our suspicions.

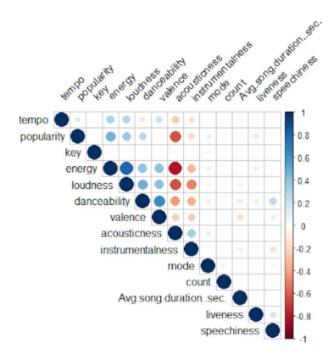


Figure 9: Corrplot to show correlation of variables

After this, we ran a logistic regression to come up with the following (Appendix C):

Feature	Coefficient	Interpretation
Valence	-4.034	This analysis further solidifies the negative correlation between positivity and
		popularity
Acousticness	-1.402	Confirms that more acoustic tracks are less popular
Danceability	4.009	Further confirms the importance of danceability
Liveness	-0.711	Liveness has an impact on popularity for artists, but we could not find
		correlation within the songs dataset. Hence, analysis for Liveness is inconclusive
Instrumentalness	0.507	This feature had a negative impact for songs, but a positive impact for artists.
		Hence analysis for Instrumentalness is also inconclusive
Loudness	0.045	Minimal impact, but confirms that loudness plays a role in popularity
Mode (Major)	-0.320	Further confirms that Mode 1 (Major modality) tends to be less popular
Speechiness	-0.133	Further confirmation that speechiness has a negative impact on popularity
Tempo	0.0003	Further confirms that tempo is not a relevant variable for our models
Keys (1 to 11)	Range -0.39	The wide range indicates that further analysis will be required
	to 0.106	
Average Track Duration	-0.009	Similar to before, longer tracks can have a minimal impact on popularity
Count	-0.003	Number of songs that an artist has created, but with such a minimal impact to
		popularity, we have concluded that this variable can be excluded

Running a prediction based on this model and evaluating the confusion matrix, we get an accuracy of 75.5%. Setting an optimal threshold of 0.12 gives us a sensitivity of .732 and a specific of 0.758 (See Appendix C). After this step, we created a decision tree for predicting whether a song/artist would be a hit or not. The results are shown below.

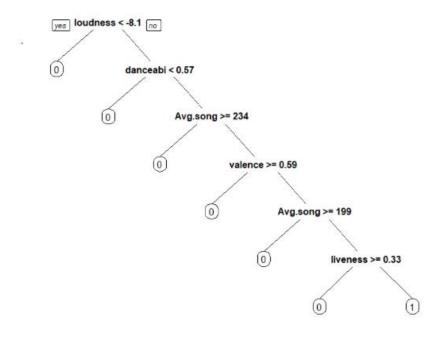


Figure 10: CART for hit song prediction

Based on our analysis, we came to the following conclusions for an optimal track an artist must produce to be popular on Spotify.

Feature	Impact on Track popularity	Conclusion for popularity
Valence	The models suggest a negative impact	There is no need for overt positivity in a
	on popularity, to a much more	track. The CART suggests less than .59.
	significant extent when artists are	
	generating	
Acousticness	Acousticness has a negative impact	Avoid acoustic tracks.
	overall	
Danceability	Has a significant positive impact on	Ensure tracks can have a high danceability
	popularity.	score. The CART suggests more than .57.
Explicit	Positive impact, but not to a significant extent	Having explicit lyrics does not detract from popularity.
Loudness	Has a positive impact on popularity,	Ensure that a song is not below a certain
	but not to a significant extent	level of loudness. The CART suggests not to
		go below -8.1.
Mode (Major)	Has a negative impact on popularity,	Avoiding Major modality and focusing on
	but not to a significant extent	Minor modality is an option.
Speechiness	Negative impact on popularity	Ensure there is less spoken words in a track.
Instrumentalness	Positive impact on popularity	Having songs with instrumentalness
		increased popularity here, but as per
		Appendix A, purely from the songs dataset,
		there was negative correlation. Hence the
		analysis for this attribute is inconclusive.
Average Track	Has a small negative impact on	Since the CART shows Average duration as a
duration	popularity.	node, there are sufficient records to
		consider this as having an impact. Hence the
		CART suggests below 234 seconds.
Keys	Negative or Positive impact on	To be further analyzed below.
	popularity – inconclusive from logit models.	

Now on to our second question.

Q2: What time of year is best suited to release particular types of music?

Since music is a creative field, sometimes it may not always be possible to stick to prescriptive features to generate tracks. This creates an opportunity for Oswald Records to maximize our investment return by ensuring we release music at an optimum time during the year.

Additionally, we wanted to see if the inconclusive attribute from our analysis above has further impact. Hence, we created a classification tree after running the following preprocessing steps:

- Excluded year, artist name, energy, and release_date as these do not have any analytical value or are redundant.
- 2. Converted month, explicit, key and mode as categorical values.
- 3. Set release month as the outcome variable.
- 4. Taking a subset of only those songs that have a popularity value > 70.

The resulting tree (shown in the next page), based on a track's attributes, provides guidance on when best to release a track during a year to ensure a popularity over 70. We also see that in this instance, the key of a track place a significant role.

For example, it suggests that if a song has a key value of 3 (D# or Eb), the best time to release it is in November. Similarly, if a song has a key value that is 8 (G# or Ab), additional decision points around acousticness, danceability, and song duration come into play. To further explain this, if the song with the key value of 8 has a song duration less than 252 seconds and a danceability less than .41, then the ideal time to release it is in February.

To further validate the CART, we ran a confusion matrix (See Appendix D) which reported an accuracy of 83.62%, with comparatively high Sensitivity scores throughout, except for April (0.491), and comparatively high Specificity scores except in September (0.268). Hence, we are confident that this CART can be used to make decisions on when to release a track on Spotify.

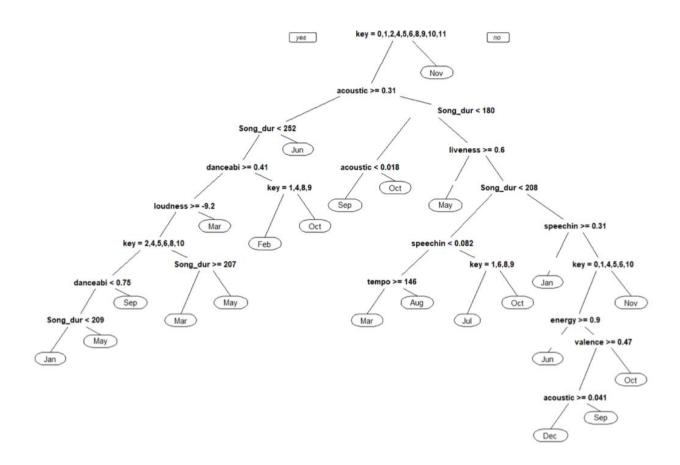


Figure 11: CART depicting model to determine ideal month to add to Spotify

Now on to our third question.

Q3: What is the optimal genre of music to release in 2021?

Genre plays an essential role in Spotify's classification of songs; hence selecting the right genre with the features mentioned above increases a song's chances of being added to the right playlist giving it more visibility. This allows for more streaming opportunities and hence more opportunities to ramp up a popularity score. To help identify the genres that have a high popularity and exhibit features similar to the ones discussed above, we ran a K-means cluster analysis. First, we ran the following pre-processing steps on the data_by_genre dataset.

- 1. Selected Genre as the target and all the other columns as predictors.
- 2. Normalizing the predictor values by subtracting mean and dividing by standard deviation.

Our next objective was to determine the best k, after running the following plots with multiple options.

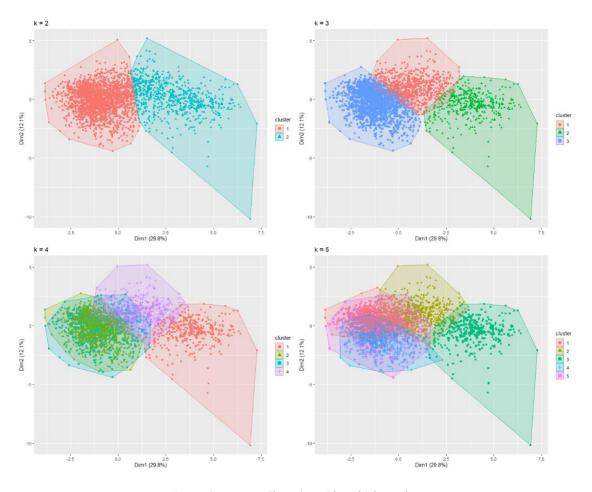


Figure 12: K-Means Clustering with multiple K values

Based on the findings above, we can see that as the value of K increases, the overlap between clusters also increased. Hence, we choose k = 2.

Running K-means clustering with k = 2 and plotting each cluster's characteristics by referring to their km centers as per below (Also see Appendix E), we can see that Cluster 2 has a higher popularity, and the features of this cluster corresponds to low acousticness, instrumentalness, and, high danceability, valence, loudness, and tempo. We were then able to review this with the word cloud for popular genres identified and found alignment.

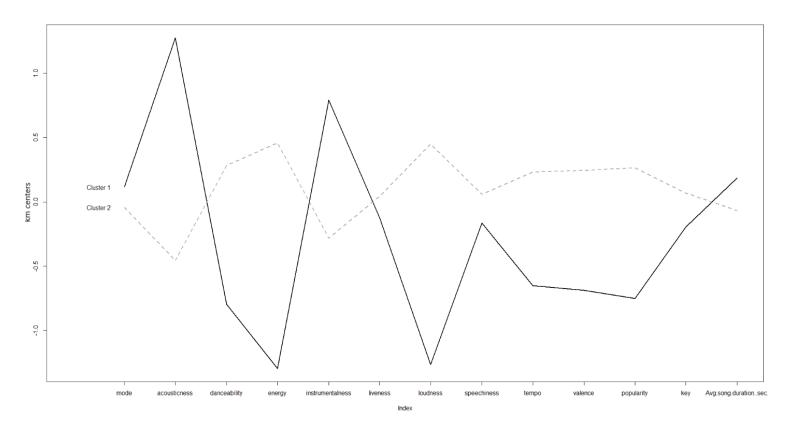


Figure 13: Plot to show features for each cluster

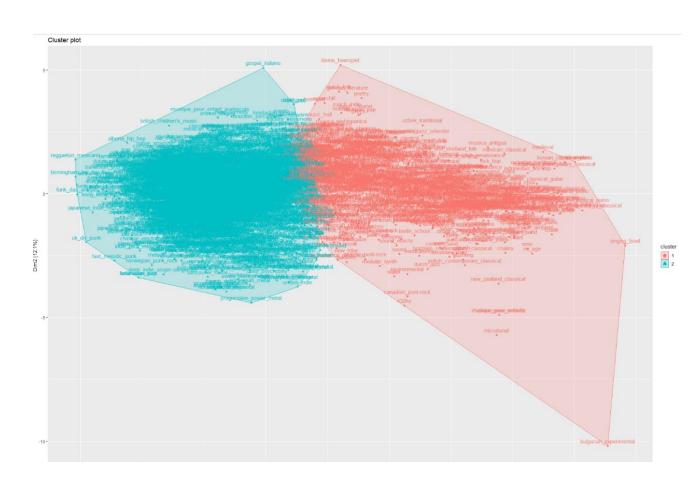




Figure 15: Word cloud to indicate popular Genres

Figure 14: Clusters showing actual Genre names

Based on our analysis, the most popular genres we would expect in 2021 would be the ones depicted in the word cloud, and some key ones to highlight are - Pop, Movie Tunes, Show Tunes, Rap, Trap, Latin, Dance-pop, Hip-hop, etc. A point of interest, the genre of "Sleep" has also appeared here, which provides unique insight as to how Spotify is used by people for assistance with sleep!

Conclusion

In summary, our team has found that there are a couple of factors that increase the probability of producing a hit song: the song has to have key characteristics such as high danceability and low valence, be released on an optimal date, contain "love" in the song name, and be in the pop, show tunes or movie tunes genre. The rules for determining the key characteristics for a hit song are shown in Figure 10, and the rules for determining the optimal release schedule are shown in Figure 11.

The biggest challenge we faced was handling this massive dataset with 5 different files. Understanding each dataset's significance was crucial to identifying the project's limitations and narrowing down the scope to suit our requirements. Exploring the raw format data, reading the descriptions, and understanding the meaning of each terminology used in the column names helped us clear the doubts around the initial hindrance.

We can also suggest the following scope for improvement when it comes to the datasets themselves:

- A column for genre in the song dataset would have provided more definitive conclusions about our analysis. It would have helped validate our assumptions about the relationship between a song and its release month.
- 2. A dataset containing lyrics of the top songs was not readily available and had to be collated from multiple sources. A solid dataset about the same could extend the scope of text mining and help us gain more insights about a song's contents and its popularity. However, we could not include lyrics in our analysis due to this issue.

3. Information about customer ratings would help us validate the significance of the popularity score, whether the score has been influenced by too few ratings or not.

Lastly, the team tested the framework above with a team favorite song: Dakiti by Bad Bunny.

Key characteristics of this song are:

Valence	Genre	Danceability	Energy	Explicit	Key	Liveness	Loudness	Release Date	Speechiness	Duration
0.145	Рор	0.731	0.573	Yes (1)	4	0.113	10.059	10/30/2020	0.0544	205.09

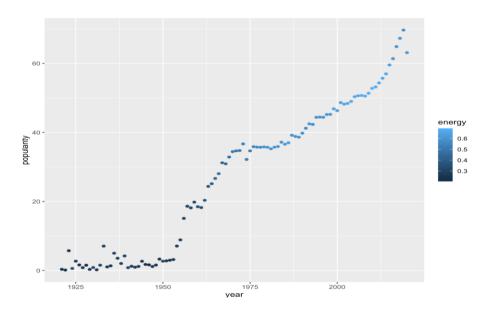
Based on the rules we've developed for identifying a hit song, this song does quality as a "hit" - which is accurate as it has a 100-popularity score according to Spotify. Based on our model, the optimal release schedule is in August, which is extremely close to the actual release date in October. This song also is in the pop genre. It doesn't contain "love" in the song title, but it meets many of the other criteria in our model or a "hit" song.

After this test, the team feels confident that our framework for identifying the next hit artist and song is accurate. We look forward to using this framework to inform investment decisions at Oswald Records – ROCK ON!

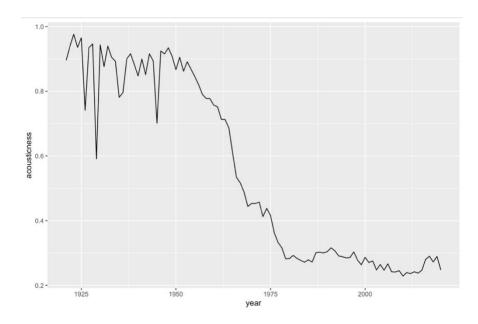
Appendix

Appendix A – Additional data visualizations

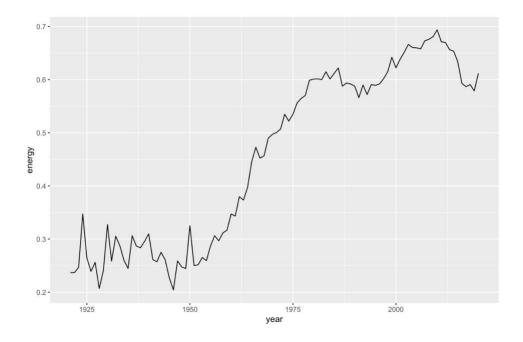
Average song popularity based on creation date and corresponding increase in energy.



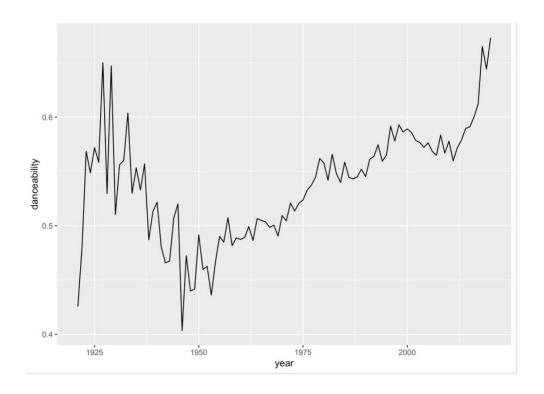
Average acousticness of songs over the years



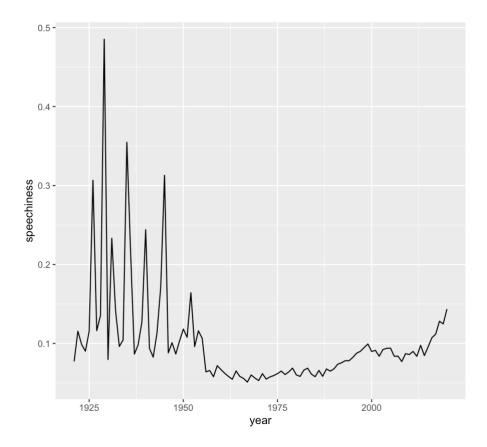
Energy of songs over the years



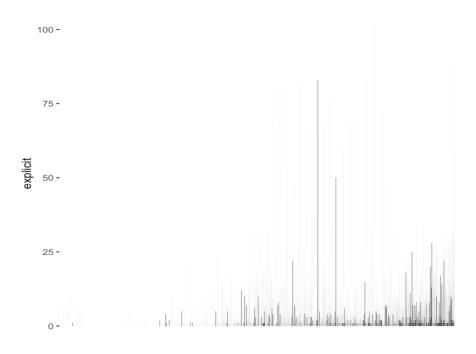
Average danceability of songs over the years



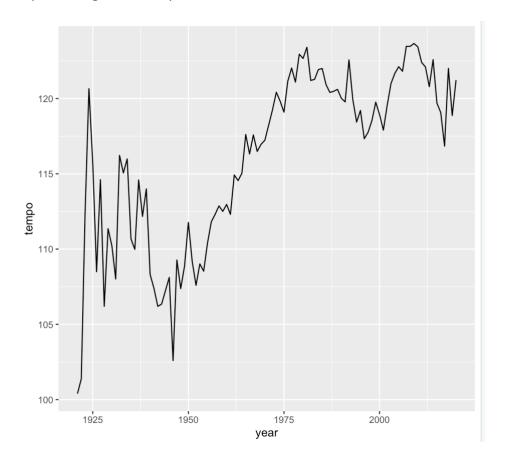
Average speechiness of songs over the years



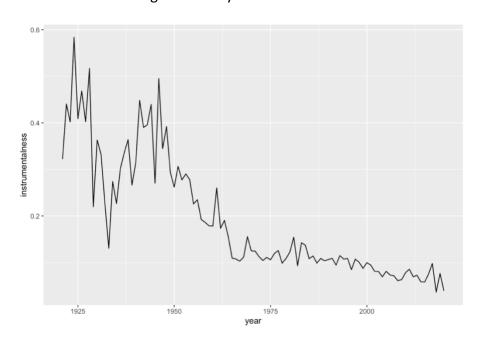
Count of explicit tracks over the years.



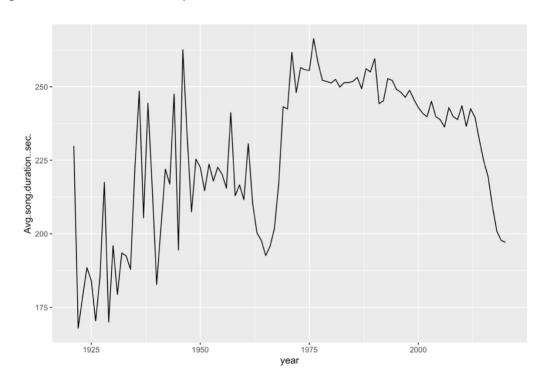
Average tempo of songs over the years



Average instrumentalness of songs over the years



Average track duration over the years



Appendix B

Logit

```
glm(formula = popularity ~ ., family = "binomial", data = train.df1)
Deviance Residuals:

Min 1Q Median 3Q Max

-1.6366 -0.2756 -0.1643 -0.0855 5.0061
Coefficients:
                                            (Intercept)
valence
acousticness
danceability
                                           3.1228028 0.1570777 19.881 < 2e-16 ***
-1.9580267 0.1725773 -11.346 < 2e-16 ***
-0.5267146 0.0545355 9.658 < 2e-16 ***
-1.9856695 0.1933446 -10.270 < 2e-16 ***
-0.2468038 0.0097256 25.377 < 2e-16 ***
-0.2556610 0.0414455 -6.169 6.89e-10 ***
-1.2135539 0.2293594 -5.291 1.22e-07 ***
-0.002419 0.0007245 3.32 0.00085 ***
energy
explicit1
instrumentalness
loudness
mode1
speechiness
                                              -1.2135539 0.2293594 0.0002145 0.0021419 0.0007245 1.1420501 0.1032867 1.1522648 0.935964 0.9150206 0.1011086 1.1592046 0.0934750 0.9356483 0.0934750 1.2219140 0.0951559 1.2455185 0.0901793
tempo
release_monthFeb
release_monthMar
release_monthApr
                                                                                       3.333 0.000858 ***
11.057 < 2e-16 ***
12.311 < 2e-16 ***
                                                                                       9.050
12.820
10.010
12.841
release_monthMay
release_monthJun
release_monthJul
                                                                                                       < 2e-16 ***
release_monthAug
                                                                                        13.812
< 2e-16 ***
< 2e-16 ***
< 2e-16 ***
                                                                                          8.079 6.52e-16 ***
signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for binomial family taken to be 1)
Null deviance: 25079 on 82730 degrees of freedom
Residual deviance: 20366 on 82708 degrees of freedom
AIC: 20412
Number of Fisher Scoring iterations: 8
```

Confusion Matrix and ROC Curve

Confusion Matrix and Statistics

```
Reference
Prediction 0 1
0 27591 308
1 6650 908
```

Accuracy : 0.8038 95% CI : (0.7996, 0.8079)

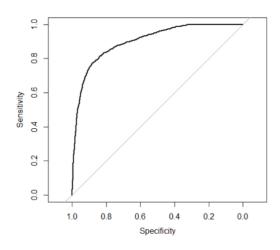
No Information Rate : 0.9657 P-Value [Acc > NIR] : 1

Карра : 0.1572

Mcnemar's Test P-Value : <2e-16

Sensitivity: 0.74671
Specificity: 0.80579
Pos Pred Value: 0.12014
Neg Pred Value: 0.98896
Prevalence: 0.03430
Detection Rate: 0.02561
Detection Prevalence: 0.21316
Balanced Accuracy: 0.77625

'Positive' Class : 1



Appendix C

Correlation Matrix:

	acousticness	danceability	Avg.song.durationsec.	energy	instrumentalness	liveness	1oudness	speechiness	tempo	valence	popularity	key	mode	count
acousticness	1.00	-0.42	-0.04	-0.80	0.33	0.04	-0.63	-0.02	-0.26	-0.23	-0.62	-0.04	0.11	0.02
danceability	-0.42	1.00	-0.12	0.40	-0.36	-0.10	0.48	0.27	0.12	0.62	0.28	0.04	-0.11	-0.03
Avg.song.durationsec.	-0.04	-0.12	1.00	-0.02	0.10	-0.02	-0.09	0.03	-0.05	-0.19	0.02	-0.01	-0.03	0.00
energy	-0.80	0.40	-0.02	1.00	-0.33	0.10	0.80	0.06	0.31	0.40	0.47	0.04	-0.10	-0.02
instrumentalness	0.33	-0.36	0.10	-0.33	1.00	-0.06	-0.48	-0.16	-0.15	-0.25	-0.20	-0.03	-0.02	0.01
liveness	0.04	-0.10	-0.02	0.10	-0.06	1.00	0.05	0.19	-0.03	0.01	-0.13	-0.01	0.02	0.01
loudness	-0.63	0.48	-0.09	0.80	-0.48	0.05	1.00	0.03	0.28	0.41	0.37	0.03	-0.07	-0.02
speechiness	-0.02	0.27	0.03	0.06	-0.16	0.19	0.03	1.00	-0.02	0.10	-0.04	0.01	-0.05	-0.02
tempo	-0.26	0.12	-0.05	0.31	-0.15	-0.03	0.28	-0.02	1.00	0.22	0.15	0.01	-0.01	0.01
valence	-0.23	0.62	-0.19	0.40	-0.25	0.01	0.41	9.10	0.22	1.00	-0.02	0.04	-0.02	0.00
popularity	-0.62	0.28	0.02	0.47	-0.20	-0.13	0.37	-0.04	0.15	-0.02	1.00	0.01	-0.11	-0.05
key	-0.04	0.04	-0.01	0.04	-0.03	-0.01	0.03	0.01	0.01	0.04	0.01	1.00	-0.08	-0.04
mode	0.11	-0.11	-0.03	-0.10	-0.02	0.02	-0.07	-0.05	-0.01	-0.02	-0.11	-0.08	1.00	0.08
count	0.02	-0.03	0.00	-0.02	0.01	0.01	-0.02	-0.02	0.01	0.00	-0.05	-0.04	0.08	1.00

Logit

```
glm(formula = popularity ~ ., family = "binomial", data = data)
Deviance Residuals:
Min 1Q Median 3Q
-2.1974 -0.4733 -0.3226 -0.2042
                                           5.3012
coefficients:
                            Estimate Std. Error z value Pr(>|z|)
1.2705411 0.2086502 6.089 1.13e-09 ***
-1.4024883 0.0847893 -16.541 < 2e-16 ***
(Intercept) acousticness
                            -1.4024883
danceability
                             4.0091667
                                          0.1684275
Avg. song. duration..sec. -0.0098199
instrumentalness 0.5077576
liveness -0.7111140
                                                                < 2e-16 ***
                                          0.0003792 -25.897
                                                       5.666 1.46e-08 ***
                                          0.0896148
                                          0.1727432
                                                       -4.117 3.85e-05
loudness
                             0.0455846
                                          0.0059704
speechiness
                            -0.1332391
                                          0.2028233
                                                       -0.657
                                          0.0009036 0.386
0.1170448 -34.470
tempo
                            0.0003489
                                                                0.69946
                            -4.0345916
valence
                                                                < 2e-16
                                          0.0909804
key1
                             0.0718793
                                                        0.790
                            -0.2827032
-0.2303447
                                                                0.00284 **
key2
                                          0.0947176
                                                       -2.985
                                          0.1337538
0.1089077
                                                       -1.722
                                                                0.08504
key3
                            -0.3456761
                                                       -3.174
kev4
                                                                0.00150
key5
                            -0.1515866
                                          0.0975749
                                                       -1.554
                                                                0.12029
                            0.1066496
                                          0.0983434
key6
                                                        1.084
                                                                0.27816
                                                       -3.014
                                                                0.00258
key7
key8
                            -0.0599071
                                          0.1080070
                                                       -0.555
                                                                0.57913
                                          0.0994671
                            -0.3927379
                                                       -3.948 7.87e-05
key9
                                                      -1.420 0.15562
-2.299 0.02149
-6.917 4.62e-12
                            -0.1455275
key10
                                          0.0969252
                            -0.2228574
kev11
                            -0.3288723
                                          0.0475465
mode1
                            -0.0038426 0.0009461 -4.062 4.87e-05 ***
signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for binomial family taken to be 1)
     Null deviance: 18814 on 27260 degrees of freedom
Residual deviance: 15467 on 27238 degrees of freedom
AIC: 15513
Number of Fisher Scoring iterations: 6
```

Confusion Matrix

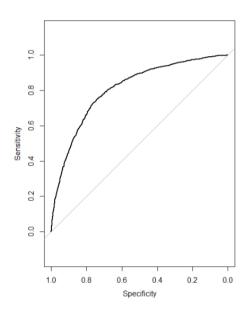
```
Reference
Prediction 0 1
0 7382 314
1 2349 860

Accuracy: 0.7558
95% CI: (0.7476, 0.7638)
No Information Rate: 0.8923
P-Value [Acc > NIR]: 1
Kappa: 0.2787

Mcnemar's Test P-Value: <2e-16

Sensitivity: 0.73254
Specificity: 0.75861
Pos Pred Value: 0.26800
Neg Pred Value: 0.95920
Prevalence: 0.10766
Detection Rate: 0.07886
Detection Prevalence: 0.29427
Balanced Accuracy: 0.74557

'Positive' Class: 1
```



Confusion Matrix for CART

```
Reference
Prediction 0 1
0 9635 1040
1 96 134

Accuracy : 0.8958
95% CI : (0.8899, 0.9015)
NO Information Rate : 0.8923
P-Value [Acc > NIR] : 0.123

Kappa : 0.1613

Mcnemar's Test P-Value : <2e-16

Sensitivity : 0.11414
Specificity : 0.90013
Pos Pred Value : 0.58261
Neg Pred Value : 0.90258
Prevalence : 0.10766
Detection Rate : 0.01229
Detection Prevalence : 0.01229
Balanced Accuracy : 0.55214
'Positive' Class : 1
```

Appendix D

Confusion Matrix for Month prediction CART

```
Confusion Matrix and Statistics
          Reference
                           May Jun Jul Aug Sep Oct Nov Dec 0 0 0 0 0 0 8
Prediction Jan Feb Mar Apr
       Jan 69
       Feb
             0
                37
                     0
                         0
                             0
                                  0
                                      0
                                          0
                                              0
                                                  0
                 0
                   29
                         0
                             0 11
       Mar
                                      0
                             0
                                      0
       Apr
                     0
                        20
                            72
2
1
             0
                 0
                     0
                         0
                                          0
                                              0
                         0
                                          0
                                                  0
                                                           0
       Jun
                 0
                     0
                                56
                                              0
                                                       0
       Jul
                         0
                                          Ö
                    10
                                     29
                     0
                         9
                              0
                                  0
                                      0
                                         56
                                              0
                                                  0
       Sep
                 0
                     1
                         0
                                  0
                                          5
9
                                             76
             ō
                 0
                          6
                             0
                                                 78
       oct
                                12
                          9
                                      0
                                                  0
                                                      90
       Dec
             0
                 0
                     0
                         0
                              0
                                      0
                                                  0
                                                       0
                                                          29
Overall Statistics
               Accuracy : 0.8362
95% CI : (0.8028, 0.8395)
    No Information Rate : 0.9304
P-Value [Acc > NIR] : 0.9961
                  карра : 0.1512
 Mcnemar's Test P-Value : <2e-14
Statistics by Class:
                     Sensitivity
                                                                                  0.6283
Specificity
                        0.84620
                                    0.89371
                                               0.96939
                                                           0.98904
                                                                       0.8384
                                                                                             0.78135
                                                                                                         1.9772
                                                                                                                    0.26830
Pos Pred Value
                         0.87672
                                    0.92672
                                                0.54854
                                                           0.25745
                                                                       0.9791
                                                                                   0.7901
                                                                                             0.01725
                                                                                                          0.0047
                                                                                                                    0.10345
Neg Pred Value
                        0.92495
                                    0.95413
                                               0.89623
                                                           0.95264
                                                                       0.1102
                                                                                  0.9191
                                                                                             0.89158
                                                                                                         0.8807
                                                                                                                    0.01250
Prevalence
                                               0.00092
                                                                       0.0367
                                                                                  0.1009
                        0.05505
                                    0.04587
                                                           0.04626
                                                                                             0.18257
                                                                                                         0.1193
                                                                                                                    0.09174
Detection Rate
                        0.71375
                                    0.56876
                                               0.67101
                                                           0.20726
                                                                       0.7830
                                                                                   0.4374
                                                                                             0.56428
                                                                                                         0.0263
                                                                                                                    0.79687
Detection Prevalence 0.28254
Balanced Accuracy 0.77386
                                    0.06627
                                               0.18752
                                                           0.00372
                                                                       0.2743
                                                                                  0.0917
                                                                                             0.02018
                                                                                                         0.0735
                                                                                                                    0.30606
Balanced Accuracy 0.77386 0.8/940 0.57575 Dec Class: Oct Class: Nov Class: Dec 0.81269
                                                                       0.8803
                                                           0.42834
                                                                                  0.6827
                                                                                             0.69264
                                                                                                         0.6602
                                                                                                                    0.89869
Sensitivity
                        0.88250
                                    0.93953
Specificity
Pos Pred Value
                        0.83871
                                    0.87234
                                               0.88273
                        0.85000
                                    0.74286
Neg Pred Value
                        0.17640
                                    0.26316
                                               0.17248
                  0.17640
0.14679
Prevalence
                                    0.13761
                                               0.12752
Detection Rate
                        0.64587
                                               0.77869
                                    0.81835
Detection Prevalence 0.12349
                                    0.39844
                                               0.25573
Balanced Accuracy
                        0.87560
                                    0.90284
                                               0.79572
```

Appendix E