Pruning neural networks

Optimizing AI - Session 3



Course organisation

Sessions

- Introduction/Refresher on Deep Learning
- Quantization,
- Pruning,
- Data Augmentation,
- 5 Factorization,
- 6 Distillation,
- Embedded Software and Hardware for DL,
- 8 Final session.

Course organisation

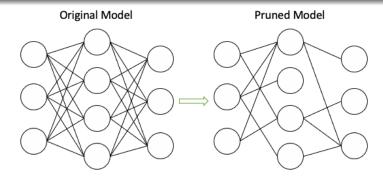
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What is pruning?

Intuitive principle

Removing parts of the network to reduce its cost (in memory, computation power, etc.).



What does it involve?

The three big questions of pruning

- What kind of part should I prune?
- How to tell which parts can be pruned?
- How to prune parts without harming the network?
- Pruning structure: the kind of part you will remove, how it will affect the network's cost.
- ⇒ **Pruning criterion**: the metric to use to identify parts to prune.
- ⇒ Pruning method: the removal strategy and schedule, how to reduce the loss in performance, how to avoid some known pitfalls...

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Mainly two kinds of pruning:

- "Unstructured" (weight) pruning: removing individual weights
 - More straightforward to implement
 - More fine-grained
 - Allows better accuracy/parameters ratio
 - But, very hard to optimize: you not always get any speedup out of it! (cf. Non-Structured DNN Weight Pruning Is It Beneficial in Any Platform?, by Ma et. al. 2019)
 - However good as a proof of concept
- "Structured" (filter) pruning: removing convolution filters (or neurons)
 - Watch out for dimensional consistency between layers!
 - More coarse-grained (watch out not to prune entire layers by accident!)
 - Produces a smaller network that allows real speedup on any framework
 - Lighter to run because of fewer feature maps

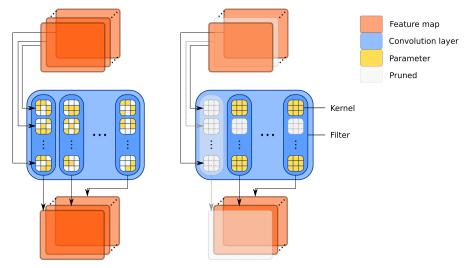


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"Unstructured" : weight pruning

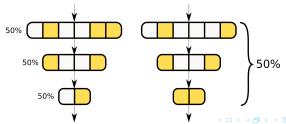
"Structured" : filter pruning

- Local pruning: remove the same proportion to each layer
 - A lot simpler to implement
 - Sub-optimal
- Global pruning: remove different proportions to each layer to reach a global target
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Two widespread examples for individual weights:

- **Weight magnitude**: prune weights of least \mathcal{L}_1 norm
- Weight gradient: do a back-propagation over a minibatch and prune weights whose gradients are of least \mathcal{L}_1 norm

- **2.** \mathcal{L}_1 , \mathcal{L}_2 of the filter or its gradient... (cf. Pruning Filters for Efficient ConvNets, by Li et. al. 2016)
- Magnitude of the batch-normalization layer's multiplicative parameter (cf. Learning Efficient Convolutional Networks through Network Slimming, by Liu et. al. 2017)
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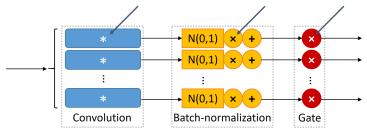
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Remarks:

- Criteria reported previously are among the simplest: the literature has been very prolific on the topic of pruning criteria and include many complex ones. For example:
 - Filter identification through reinforcement learning (cf. AMC: AutoML for Model Compression and Acceleration on Mobile Devices, by He et. al. 2018)
 - Optimization through variational inference (cf. Variational Dropout Sparsifies Deep Neural Networks, by Molchanov et. al. 2017)
 - Computation of the network's second derivative (Hessian)... (cf. Optimal Brain Damage, by Le Cun et. al. 1989)
- Warning, in the case of global pruning:
 - Some criteria may be unbalanced: for example, magnitude-based criteria tend to prune mostly the last layers.
 - There are risks to prune entire layers by accident, a.k.a. "layer collapse". (cf. Pruning neural networks without any data by iteratively conserving synaptic flow, by Tanaka et. al. 2020)

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 - Removal strategy
 - Training schedule

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 - Removal strategy
 - Set weights to prune to 0 definitely
 - Same but iterative with a growing pruning rate (cf. Learning both Weights and Connections for Efficient Neural Networks, by Han et. al. 2015)
 - Progressively all throughout pruning, until the target is reached (cf.
 To prune, or not to prune: exploring the efficacy of pruning for model
 compression, by Zhu et. al. 2017)
 - At each epoch, set targeted weights to 0 but let them train again until the end, a.k.a. "Soft pruning" (cf. Soft Filter Pruning for Accelerating Deep Convolutional Neural Networks, by He et. al. 2018)
 - Training schedule

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- Two aspects that encompasses most simple ones:
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 - Train, prune and fine-tune once (or prune while training) (cf. Learning Efficient Convolutional Networks through Network Slimming, by Liu et. al. 2017)
 - Fine-tune after each pruning step (cf. Learning both Weights and Connections for Efficient Neural Networks, by Han et. al. 2015)
 - Train, prune, and wholly retrain, a.k.a. LR-Rewinding (cf. Comparing Rewinding and Fine-tuning in Neural Network Pruning, by Renda et. al. 2020)

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Remark 1

For the sake of convenience, many methods/paper count as pruned weights that are simply set to 0. Even though it does not produce any speedup, it allows measuring a parameters/performance ratio without worrying about dimensional discrepancies or efficiency issues.

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Remark 2

Iterative or progressive methods are more robust to layer-collapse, because values of remaining weights values may be updated so that they are less likely to be targeted afterward.

- Learning both Weights and Connections for Efficient Neural Networks, by Han et. al. 2015
 - Structure: global individual weights
 - Criterion: weights magnitude
 - Method: train, then iterate between pruning and fine-tuning
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- Learning both Weights and Connections for Efficient Neural Networks, by Han et. al. 2015
- To prune, or not to prune: exploring the efficacy of pruning for model compression, by Zhu et. al. 2017
 - Structure: local individual weights
 - Criterion: weights magnitude
 - Method: train while pruning progressively the smallest weights, no fine-tuning
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- To prune, or not to prune: exploring the efficacy of pruning for model compression, by Zhu et. al. 2017
- Comparing Rewinding and Fine-tuning in Neural Network Pruning, by Renda et. al. 2020
 - Structure: global individual weights
 - Criterion: weights magnitude
 - Method: train, prune the lowest 20%, re-train and repeat until pruned enough
 - Remark: the principle of retraining, with its learning-rate schedule, instead of fine-tuning with the lowest learning-rate is the heart of Learning Rate Rewinding.

- Pruning Filters for Efficient ConvNets, by Li et. al. 2016
 - Structure: local convolution filters and corresponding kernels in the following layer (with varying rates)
 - \blacksquare Criterion: \mathcal{L}_1 norm of filters
 - Method: train, then iterate between pruning and fine-tuning
- Learning Efficient Convolutional Networks through Network Slimming, by Liu et. al. 2017
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- Pruning Filters for Efficient ConvNets, by Li et. al. 2016
- Learning Efficient Convolutional Networks through Network Slimming, by Liu et. al. 2017
 - Structure: global convolution filters
 - Criterion: magnitude of multiplicative parameter in batch-normalization layers
 - Method: train, prune and fine-tune once
 - Remark: applies a smooth- \mathcal{L}_1 penalty on multiplicative parameters in batch-normalization layers during training
- Importance Estimation for Neural Network Pruning, by Molchanov et. al. 2019

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 - Structure: global gates (or global individual weights)
 - Criterion: gradient magnitude
 - Method: train, then iterate between pruning and fine-tuning

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Advice

Refer to the original papers (available online) for more details on methods, implementation or eventual variants.

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To go further:

Neural Network Pruning 101 on towardsdatascience.com.

Some results

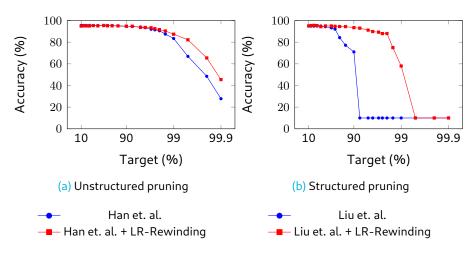


Figure: Pruning rate/Accuracy tradeoff, ResNet-20 on CIFAR-10

Lab Session and Project

Lab Session

- Implement one of the pruning methods from this course
- Apply it on MiniCIFAR

Presentation at next session

Present your current explorations on MiniCIFAR, CIFAR10 and / or CIFAR100 using the methods seen so far!