

# MATH 1700

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**Instructor: Mehdi Maadooliat**

## **Chapter 2A**

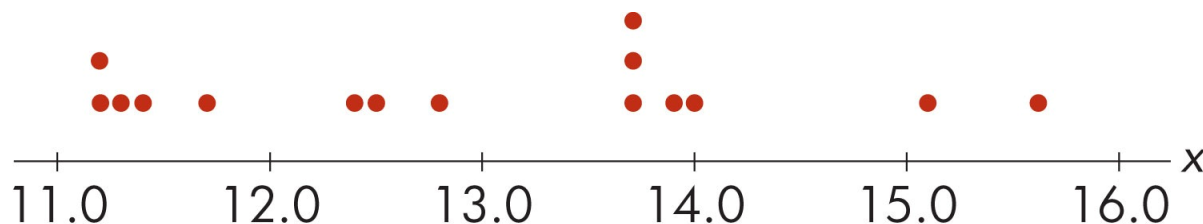


**Department of Mathematical and Statistical Sciences**

# CHAPTER 2A

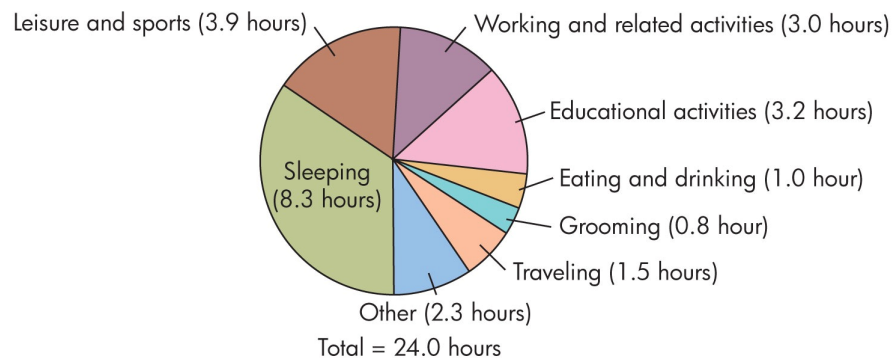


- **Descriptive Analysis**
- **Presentation of Single-Variable Data**
- **Graphs for Qualitative Data**
  - **Pie Chart**
  - **Bar Graph**
- **Graphs for Quantitative Data**
  - **Dot plot**
  - **Stem and Leaf Plot**
  - **Histogram**
- **Measures of Central Tendency**
  - **Mean, Median, and Mode, Midrange**
- **Measures of Dispersion**
  - **Range**
  - **Sample Variance, and Sample Standard deviation**

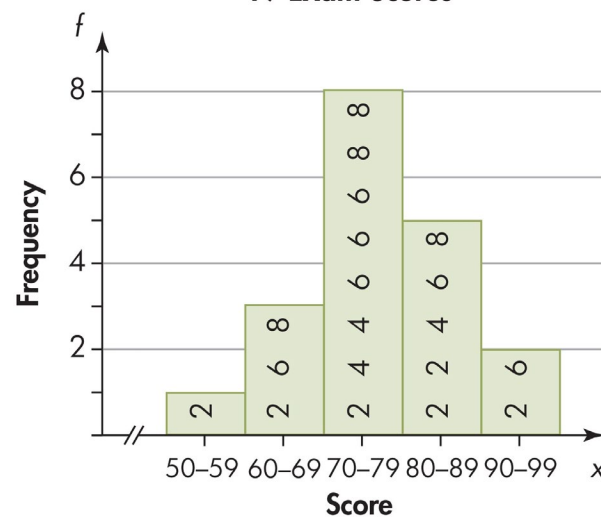


# Graphical Summaries

## Time Use on an Average Weekday for Full-time University and College Students



## 19 Exam Scores



## EXAMPLE 1 – GRAPHING QUALITATIVE DATA

- **Table 2.1 lists the number of cases of each type of operation performed at General Hospital last year.**

| Type of Operation          | Number of Cases |
|----------------------------|-----------------|
| Thoracic                   | 20              |
| Bones and joints           | 45              |
| Eye, ear, nose, and throat | 58              |
| General                    | 98              |
| Abdominal                  | 115             |
| Urologic                   | 74              |
| Proctologic                | 65              |
| Neurosurgery               | 23              |
| <i>Total</i>               | 498             |

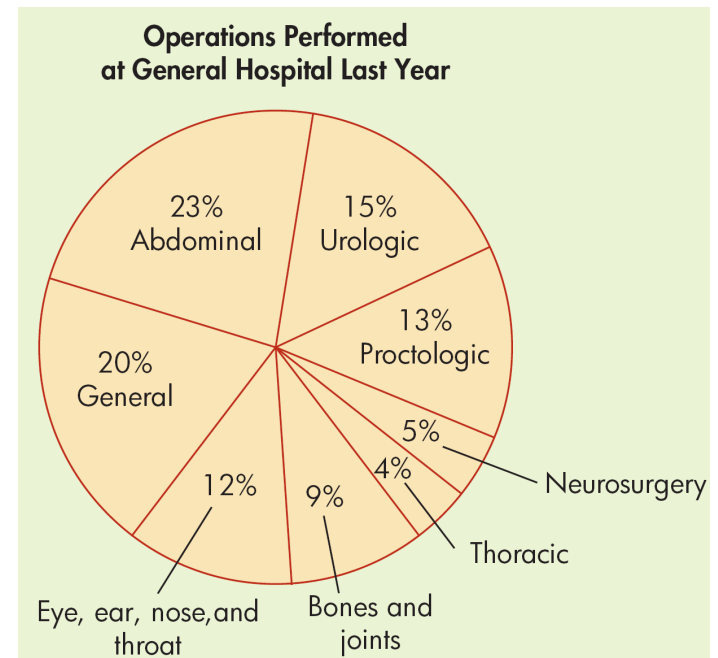
Operations Performed at General Hospital Last Year [TA02-01]

Table 2.1

# QUALITATIVE DATA (PIE CHART)

- **Pie charts (circle graphs) and bar graphs** Graphs that are used to summarize **qualitative, or attribute, or categorical data.**
- **Pie charts (circle graphs)** show the amount of data that belong to each category as a proportional part of a circle.

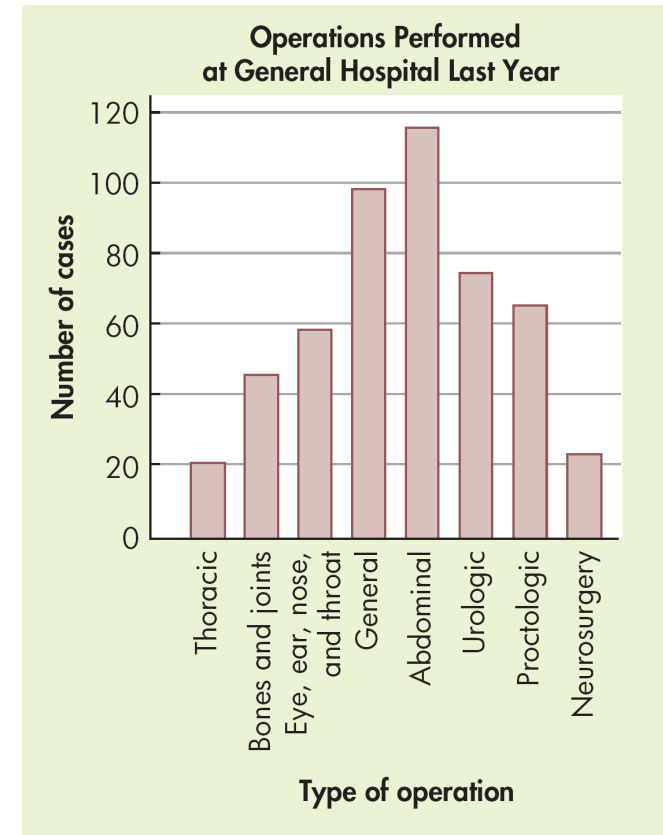
| Type of Operation          | Number of Cases |
|----------------------------|-----------------|
| Thoracic                   | 20              |
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| Eye, ear, nose, and throat | 58              |
| General                    | 98              |
| Abdominal                  | 115             |
| Urologic                   | 74              |
| Proctologic                | 65              |
| Neurosurgery               | 23              |
| <i>Total</i>               | 498             |



# QUALITATIVE DATA (BAR GRAPH)

- **Bar graphs show the amount of data that belong to each category as a proportionally sized rectangular area.**

| Type of Operation          | Number of Cases |
|----------------------------|-----------------|
| Thoracic                   | 20              |
| Bones and joints           | 45              |
| Eye, ear, nose, and throat | 58              |
| General                    | 98              |
| Abdominal                  | 115             |
| Urologic                   | 74              |
| Proctologic                | 65              |
| Neurosurgery               | 23              |
| <i>Total</i>               | 498             |



- **Bar graphs of attribute data should be drawn with a space between bars of equal width.**



# EXAMPLE 2- AUSTRALIAN INSTITUTE OF SPORT DATA

- **Description**

- Data on 102 male and 100 female athletes collected at the Australian Institute of Sport, courtesy of Richard Telford and Ross Cunningham.

- **Source**

- Cook and Weisberg (1994), *An Introduction to Regression Graphics*. John Wiley & Sons, New York.

## AIS Data

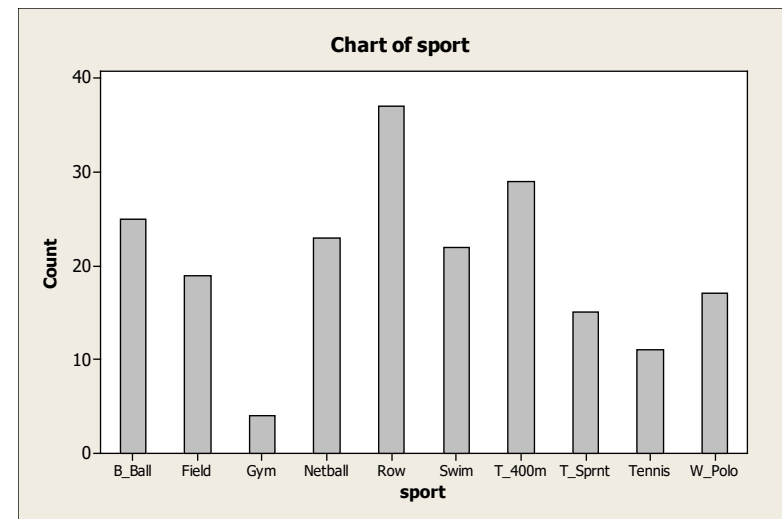
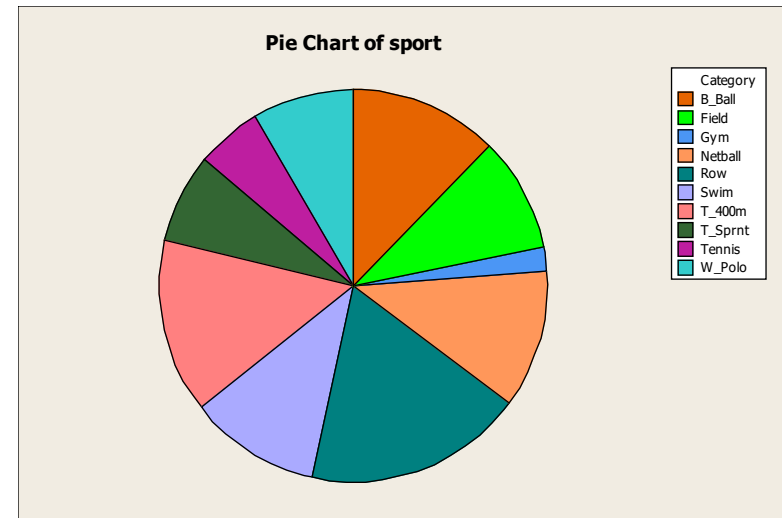
| Variable | Description                      |
|----------|----------------------------------|
| sex      | sex                              |
| sport    | sport                            |
| rcc      | red cell count                   |
| wcc      | white cell count                 |
| Hc       | Hematocrit                       |
| Hg       | Hemoglobin                       |
| Fe       | plasma ferritin concentration    |
| bmi      | body mass index, weight/(height) |
| ssf      | sum of skin folds                |
| Bfat     | body fat percentage              |
| lbm      | lean body mass                   |
| Ht       | height (cm)                      |
| Wt       | weight (Kg)                      |

# SUMMARIZING A SINGLE CATEGORICAL VARIABLE



- **Frequency (Count)** - number of times the value occurs in the data
- **Relative frequency (Percent)** - proportion of the data with the value
- **ais.xls (D2L/Content/Datasets)**

| sport   | Count | Percent |
|---------|-------|---------|
| B_Ball  | 25    | 12.38   |
| Field   | 19    | 9.41    |
| Gym     | 4     | 1.98    |
| Netball | 23    | 11.39   |
| Row     | 37    | 18.32   |
| Swim    | 22    | 10.89   |
| T_400m  | 29    | 14.36   |
| T_Sprnt | 15    | 7.43    |
| Tennis  | 11    | 5.45    |
| W_Polo  | 17    | 8.42    |
| N=      | 202   |         |

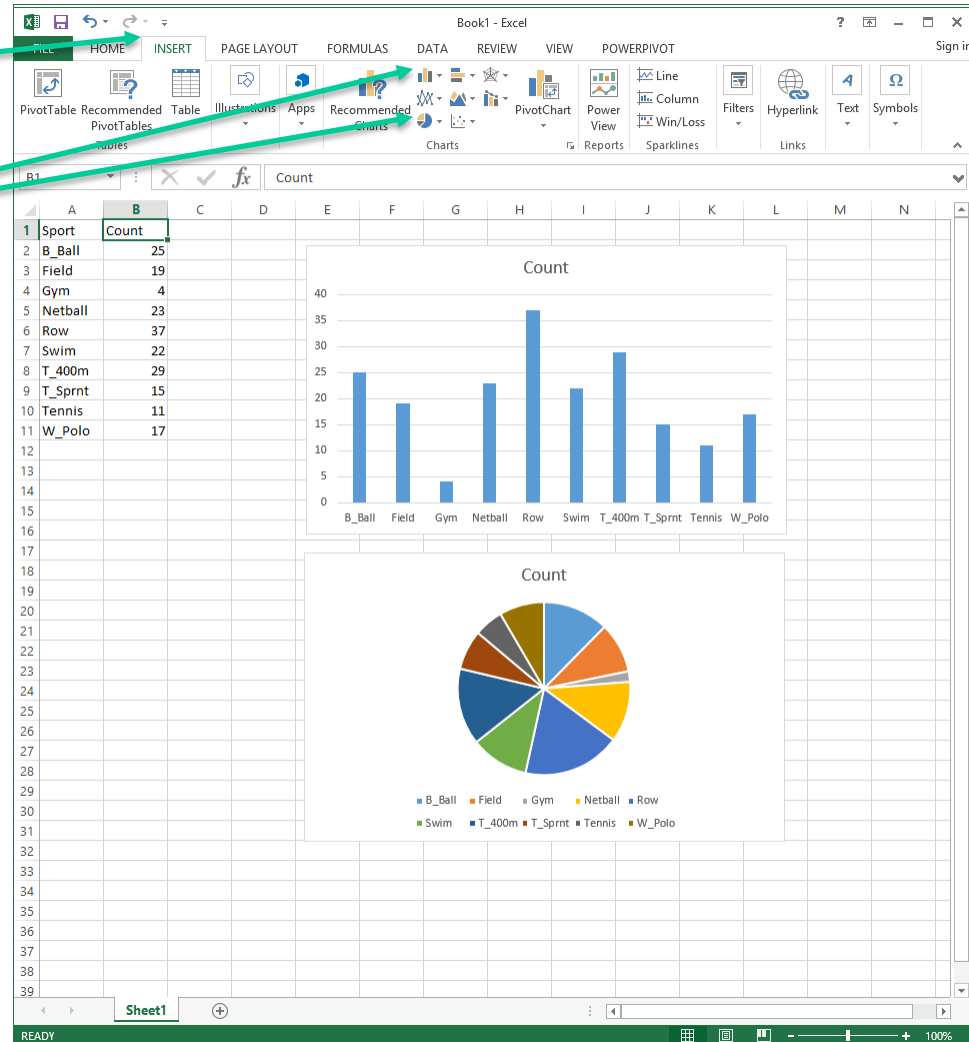






# HOW TO?

- Enter the Data in Excel:
- Select Insert
- Select Pie or Bar Charts
- JAMM: STAT-Calculator





# GRAPHING QUANTITATIVE DATA

- **Distribution** The pattern of variability displayed by the data of a variable. The distribution displays the frequency of each value of the variable.
- **Dotplot display** Displays the data of a sample by representing each data value with a dot positioned along a scale. The frequency of the values is represented along the other scale.

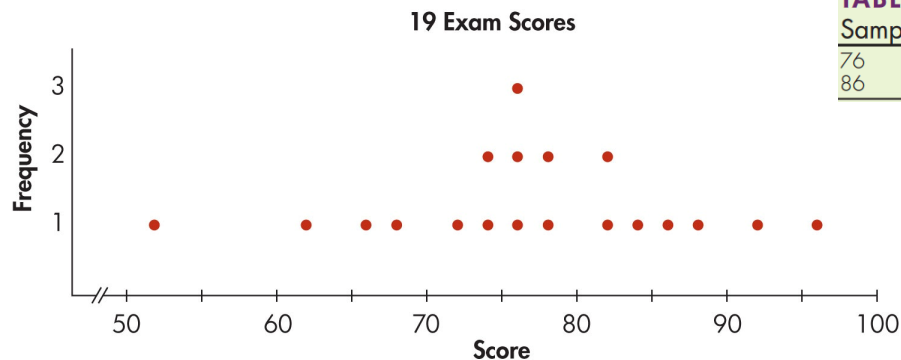


Table 2.2 provides a sample of 19 exam grades randomly selected from a large class.

**TABLE 2.2**

Sample of 19 Exam Grades [\[TA02-02\]](#)

|    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|
| 76 | 74 | 82 | 96 | 66 | 76 | 78 | 72 | 52 |    |
| 86 | 84 | 62 | 76 | 78 | 92 | 82 | 74 | 88 | 68 |

# GRAPHING QUANTITATIVE DATA

- **Stem-and-leaf display** Displays the data of a sample using the actual digits that make up the data values. Each numerical value is divided into two parts: The **leading** digit(s) becomes the **stem**, and the **trailing** digit(s) becomes the **leaf**.

Table 2.2 provides a sample of 19 exam grades randomly selected from a large class.

**TABLE 2.2**

Sample of 19 Exam Grades [TA02-02]

|    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|
| 76 | 74 | 82 | 96 | 66 | 76 | 78 | 72 | 52 | 68 |
| 86 | 84 | 62 | 76 | 78 | 92 | 82 | 74 | 88 |    |

**19 Exam Scores**

|   |                 |
|---|-----------------|
| 5 | 2               |
| 6 | 6 8 2           |
| 7 | 6 4 6 8 2 6 8 4 |
| 8 | 2 6 4 2 8       |
| 9 | 6 2             |

**Or**

**19 Exam Scores**

|   |                 |
|---|-----------------|
| 5 | 2               |
| 6 | 2 6 8           |
| 7 | 2 4 4 6 6 6 8 8 |
| 8 | 2 2 4 6 8       |
| 9 | 2 6             |



## EXAMPLE 3

### OVERLAPPING DISTRIBUTIONS

- A random sample of 50 college students was selected. Their weights were obtained from their medical records. The resulting data are listed in Table 2.3.**

|             |     |     |     |     |     |     |     |     |     |     |
|-------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| Student     | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | 10  |
| Male/Female | F   | M   | F   | M   | M   | F   | F   | M   | M   | F   |
| Weight      | 98  | 150 | 108 | 158 | 162 | 112 | 118 | 167 | 170 | 120 |
| Student     | 11  | 12  | 13  | 14  | 15  | 16  | 17  | 18  | 19  | 20  |
| Male/Female | M   | M   | M   | F   | F   | M   | F   | M   | M   | F   |
| Weight      | 177 | 186 | 191 | 128 | 135 | 195 | 137 | 205 | 190 | 120 |
| Student     | 21  | 22  | 23  | 24  | 25  | 26  | 27  | 28  | 29  | 30  |
| Male/Female | M   | M   | F   | M   | F   | F   | M   | M   | M   | M   |
| Weight      | 188 | 176 | 118 | 168 | 115 | 115 | 162 | 157 | 154 | 148 |
| Student     | 31  | 32  | 33  | 34  | 35  | 36  | 37  | 38  | 39  | 40  |
| Male/Female | F   | M   | M   | F   | M   | F   | M   | F   | M   | M   |
| Weight      | 101 | 143 | 145 | 108 | 155 | 110 | 154 | 116 | 161 | 165 |
| Student     | 41  | 42  | 43  | 44  | 45  | 46  | 47  | 48  | 49  | 50  |
| Male/Female | F   | M   | F   | M   | M   | F   | F   | M   | M   | M   |
| Weight      | 142 | 184 | 120 | 170 | 195 | 132 | 129 | 215 | 176 | 183 |

Weights of 50 College Students [TA02-03]

Table 2.3



## EXAMPLE 3

### OVERLAPPING DISTRIBUTIONS

- Notice that the weights range from 98 to 215 pounds. Let's group the weights on stems of 10 units using the hundreds and the tens digits as stems and the units digit as the leaf (see Figure 2.7).
- The leaves have been arranged in numerical order. Close inspection of Figure 2.7 suggests that two overlapping distributions may be involved.

| Weights of<br>50 College Students (lb) |                 |
|--|-----------------|
| $N = 50$                               | Leaf Unit = 1.0 |
| 9                                      | 8               |
| 10                                     | 1 8 8           |
| 11                                     | 0 2 5 5 6 8 8   |
| 12                                     | 0 0 0 8 9       |
| 13                                     | 2 5 7           |
| 14                                     | 2 3 5 8         |
| 15                                     | 0 4 4 5 7 8     |
| 16                                     | 1 2 2 5 7 8     |
| 17                                     | 0 0 6 6 7       |
| 18                                     | 3 4 6 8         |
| 19                                     | 0 1 5 5         |
| 20                                     | 5               |
| 21                                     | 5               |

Stem-and-Leaf Display

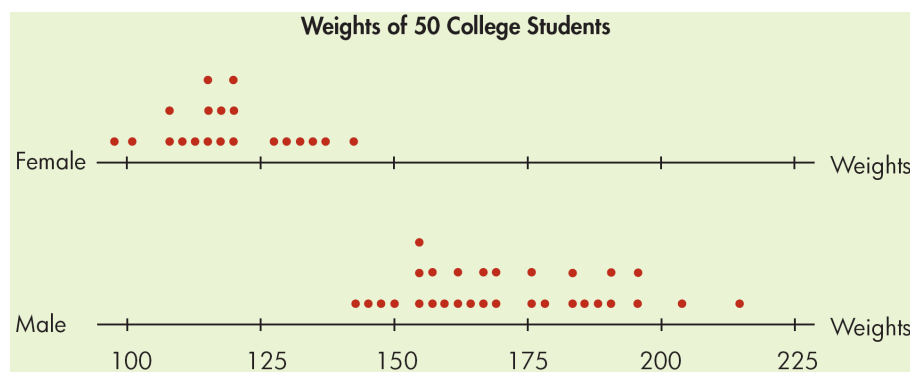
Figure 2.7

# EXAMPLE 3

## OVERLAPPING DISTRIBUTIONS

cont'd

- That is exactly what we have: a distribution of female weights and a distribution of male weights.
- Figure 2.8 shows a “back-to-back” stem-and-leaf display of this set of data and makes it obvious that two distinct distributions are involved.



| Weights of 50 College Students (lb) |       |    |             |
|-------------------------------------|-------|----|-------------|
| Female                              |       |    | Male        |
|                                     | 8     | 09 |             |
|                                     | 1 8 8 | 10 |             |
| 0 2 5 5 6 8 8                       |       | 11 |             |
| 0 0 0 8 9                           |       | 12 |             |
| 2 5 7                               |       | 13 |             |
| 2                                   |       | 14 | 3 5 8       |
|                                     |       | 15 | 0 4 4 5 7 8 |
|                                     |       | 16 | 1 2 2 5 7 8 |
|                                     |       | 17 | 0 0 6 6 7   |
|                                     |       | 18 | 3 4 6 8     |
|                                     |       | 19 | 0 1 5 5     |
|                                     |       | 20 | 5           |
|                                     |       | 21 | 5           |

“Back-to-Back” Stem-and-Leaf Display

Figure 2.8

# FREQUENCY DISTRIBUTIONS AND HISTOGRAMS

- **Frequency distribution** A listing, often expressed in chart form, that pairs values of a variable with their frequency.
- **Let's use a sample of 50 final exam scores taken from last semester's elementary statistics class.**

|    |    |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 60 | 47 | 82 | 95 | 88 | 72 | 67 | 66 | 68 | 98 | 90 | 77 | 86 |
| 58 | 64 | 95 | 74 | 72 | 88 | 74 | 77 | 39 | 90 | 63 | 68 | 97 |
| 70 | 64 | 70 | 70 | 58 | 78 | 89 | 44 | 55 | 85 | 82 | 83 |    |
| 72 | 77 | 72 | 86 | 50 | 94 | 92 | 80 | 91 | 75 | 76 | 78 |    |

Statistics Exam Scores [TA02-06]

Table 2.6

# FORM A FREQUENCY DISTRIBUTION AND HISTOGRAM



|    |    |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 60 | 47 | 82 | 95 | 88 | 72 | 67 | 66 | 68 | 98 | 90 | 77 | 86 |
| 58 | 64 | 95 | 74 | 72 | 88 | 74 | 77 | 39 | 90 | 63 | 68 | 97 |
| 70 | 64 | 70 | 70 | 58 | 78 | 89 | 44 | 55 | 85 | 82 | 83 |    |
| 72 | 77 | 72 | 86 | 50 | 94 | 92 | 80 | 91 | 75 | 76 | 78 |    |

1. **Identify the high score ( $H = 98$ ) and the low score ( $L = 39$ ), and find the range:**
  - **range** =  $H - L = 98 - 39 = 59$
2. **Select a number of classes ( $m = 7$ ) and a class width ( $c = 10$ ) so that the product ( $mc = 70$ ) is a bit larger than the range (range = 59).**
3. **Pick a starting point. This starting point should be a little smaller than the lowest score,  $L$ .**



# FORM A FREQUENCY DISTRIBUTION AND HISTOGRAM



|    |    |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 60 | 47 | 82 | 95 | 88 | 72 | 67 | 66 | 68 | 98 | 90 | 77 | 86 |
| 58 | 64 | 95 | 74 | 72 | 88 | 74 | 77 | 39 | 90 | 63 | 68 | 97 |
| 70 | 64 | 70 | 70 | 58 | 78 | 89 | 44 | 55 | 85 | 82 | 83 |    |
| 72 | 77 | 72 | 86 | 50 | 94 | 92 | 80 | 91 | 75 | 76 | 78 |    |

- Let the starting point to be 35. Given class width ( $c = 10$ )

| Class Number | Class Tallies | Boundaries           | Frequency |
|--------------|---------------|----------------------|-----------|
| 1            |               | $35 \leq x < 45$     | 2         |
| 2            |               | $45 \leq x < 55$     | 2         |
| 3            |               | $55 \leq x < 65$     | 7         |
| 4            |               | $65 \leq x < 75$     | 13        |
| 5            |               | $75 \leq x < 85$     | 11        |
| 6            |               | $85 \leq x < 95$     | 11        |
| 7            |               | $95 \leq x \leq 105$ | 4         |
|              |               |                      | 50        |

Standard Chart for Frequency Distribution

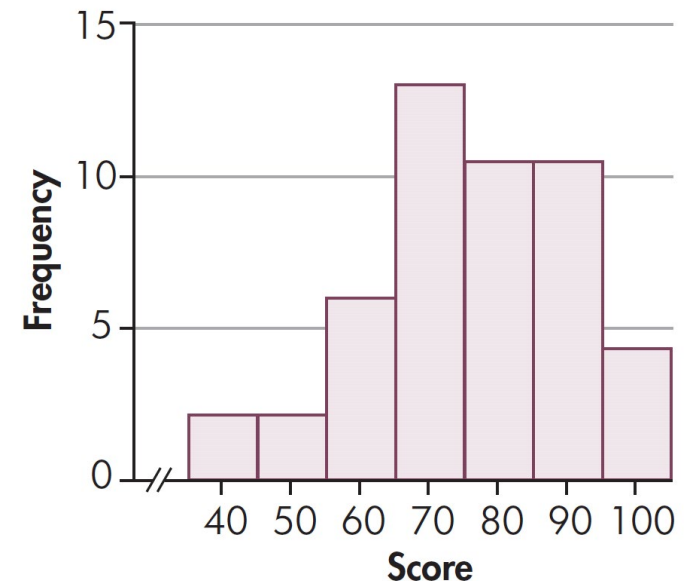
# FORM A FREQUENCY DISTRIBUTION AND HISTOGRAM



| Class Number | Class Tallies | Boundaries           | Frequency |
|--------------|---------------|----------------------|-----------|
| 1            |               | $35 \leq x < 45$     | 2         |
| 2            |               | $45 \leq x < 55$     | 2         |
| 3            |               | $55 \leq x < 65$     | 7         |
| 4            |               | $65 \leq x < 75$     | 13        |
| 5            |               | $75 \leq x < 85$     | 11        |
| 6            |               | $85 \leq x < 95$     | 11        |
| 7            |               | $95 \leq x \leq 105$ | 4         |
|              |               |                      | 50        |

- **Histogram** A bar graph that represents a frequency distribution of a quantitative variable.

50 Final Exam Scores  
in Elementary Statistics



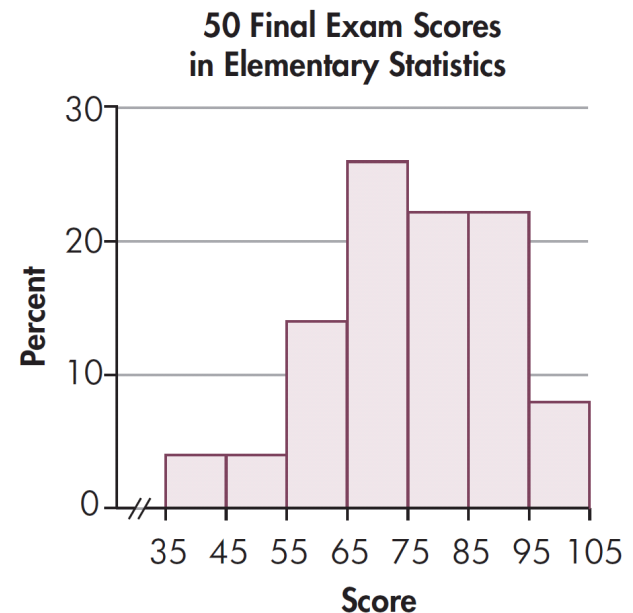
# FORM A FREQUENCY DISTRIBUTION AND HISTOGRAM



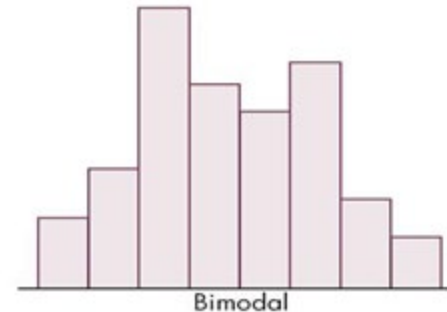
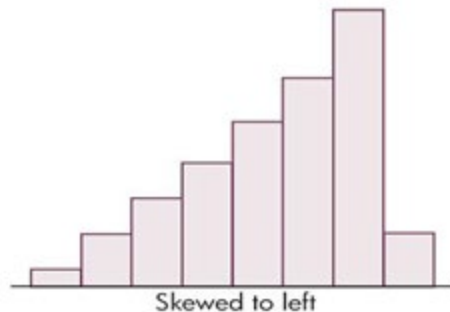
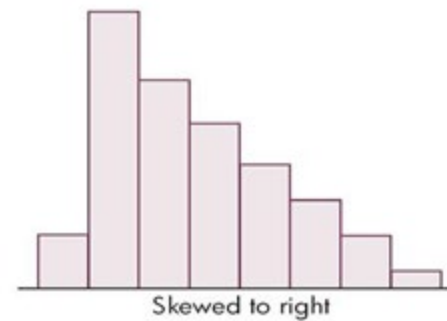
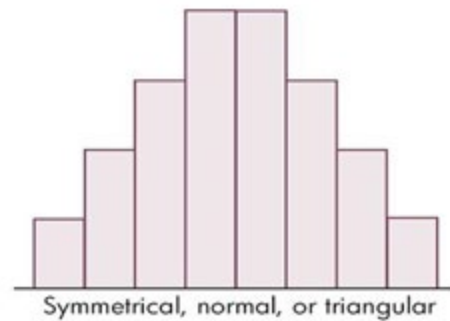
| Class Number | Class Tallies | Boundaries           | Frequency | Percentage |
|--------------|---------------|----------------------|-----------|------------|
| 1            |               | $35 \leq x < 45$     | 2         | 4%         |
| 2            |               | $45 \leq x < 55$     | 2         | 4%         |
| 3            |               | $55 \leq x < 65$     | 7         | 14%        |
| 4            |               | $65 \leq x < 75$     | 13        | 26%        |
| 5            |               | $75 \leq x < 85$     | 11        | 22%        |
| 6            |               | $85 \leq x < 95$     | 11        | 22%        |
| 7            |               | $95 \leq x \leq 105$ | 4         | 8%         |
|              |               |                      | 50        | 100%       |

Divide all by 50

- The **relative frequency (percentage)** is a proportional measure of the frequency for an occurrence.
- It is found by dividing the class frequency by the total number of observations.



# FREQUENCY DISTRIBUTIONS AND HISTOGRAMS



- **Symmetrical** Both sides of this distribution are identical (halves are mirror images).
- **Skewed** One tail is stretched out longer than the other. The direction of skewness is on the side of the longer tail.

# FREQUENCY DISTRIBUTIONS AND HISTOGRAMS



**Bimodal** The two most populous classes are separated by one or more classes. This situation often implies that two populations are being sampled. (See Figure 2.7)

| Weights of<br>50 College Students (lb) |                 |
|--|-----------------|
| $N = 50$                               | Leaf Unit = 1.0 |
| 9                                      | 8               |
| 10                                     | 1 8 8           |
| 11                                     | 0 2 5 5 6 8 8   |
| 12                                     | 0 0 0 8 9       |
| 13                                     | 2 5 7           |
| 14                                     | 2 3 5 8         |
| 15                                     | 0 4 4 5 7 8     |
| 16                                     | 1 2 2 5 7 8     |
| 17                                     | 0 0 6 6 7       |
| 18                                     | 3 4 6 8         |
| 19                                     | 0 1 5 5         |
| 20                                     | 5               |
| 21                                     | 5               |

Stem-and-Leaf Display

Figure 2.7



$$\text{midrange} = \frac{\text{low value} + \text{high value}}{2}$$

$$\text{midrange} = \frac{L + H}{2} \quad (2.3)$$

Sample mean:  $\bar{x} = \frac{\text{sum of all } x}{\text{number of } x}$

$$\bar{x} = \frac{\sum x}{n} \quad (2.1)$$

# Numerical Summaries

$$s^2 = \frac{(\text{sum of } x^2) - \left[ \frac{(\text{sum of } x)^2}{\text{number}} \right]}{\text{number} - 1}$$

$$\text{sample variance: } s^2 = \frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n - 1} \quad (2.9)$$

sample variance:  $s^2 = \frac{\text{sum of (deviations squared)}}{\text{number} - 1}$

$$s^2 = \frac{\sum (x - \bar{x})^2}{n - 1} \quad (2.5)$$

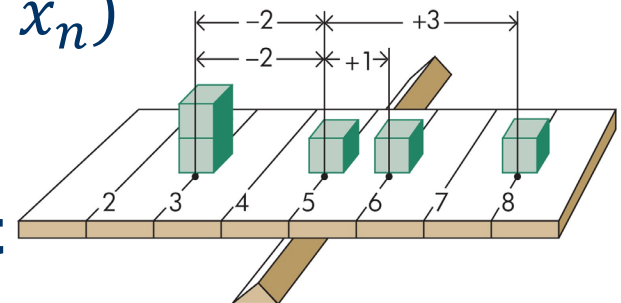
# MEASURES OF CENTRAL TENDENCY

- The measures of central tendency characterize the center of the distribution of data values. The term *average* is often associated with all measures of central tendency.
- **Mean (arithmetic mean)** The average with which you are probably most familiar. The sample mean is represented by  $\bar{x}$  (read “*x*-bar” or “sample mean”).

$$\text{Sample mean: } \bar{x} = \frac{\text{sum of all } x}{\text{number of } x}$$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i = \frac{1}{n} (x_1 + x_2 + \cdots + x_n)$$

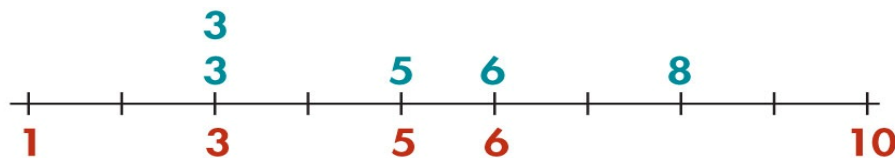
- The center of gravity or balance point





# MEASURES OF CENTRAL TENDENCY

- **Sample Median:** Middle value when data ordered. 50% above, 50% below. Represented by  $\tilde{x}$  called “*x-tilde*.”
  - Order data from smallest to largest.
  - If  $n$  odd,  $\tilde{x}$  = middle value
  - If  $n$  even,  $\tilde{x}$  = average of middle two values
- **Sample Mode:** The value that happens most often in sample.
- Represented by  $\hat{x}$  called “*x-hat*.”
  - If two or more values in a sample are tied for the highest frequency, we say that there is **no mode**.



$$\text{midrange} = \frac{\text{low value} + \text{high value}}{2}$$

$$\text{midrange} = \frac{L + H}{2}$$

- **Sample Midrange:** The number exactly midway between a lowest-valued data,  $L$ , and a highest-valued data,  $H$ .
- There are other measures called **measures of dispersion** that characterize the spread or variability in the data.



# MEASURES OF DISPERSION

- **Range** The difference in value between the highest-valued data,  $H$ , and the lowest-valued data,  $L$ :
  - *Range = high value – low value =  $H - L$*
- **Deviation from the mean:** The difference between the data value  $x_i$  and the sample mean  $\bar{x}$ 
  - $i^{th}$  deviation from the mean =  $x_i - \bar{x}$
- **The sum of the deviations,  $\sum_{i=1}^n (x_i - \bar{x})$  is always zero because the deviations of  $x_i$  values smaller than the mean (which are negative) cancel out those  $x_i$  values larger than the mean (which are positive).**

# MEASURES OF DISPERSION

- **Sample Variance:** The mean of the squared deviations using  $n - 1$  as a divisor.

$$s^2 = \frac{1}{n - 1} \sum_{i=1}^n (x_i - \bar{x})^2$$

- where  $x_i$  is the  $i^{th}$  data value,  $\bar{x}$  is the sample mean, and  $n$  is the sample size.

$SS(x)$ : *sum of squares for x*

- **This is equivalent to:**

$$s^2 = \frac{1}{n - 1} \left\{ \sum_{i=1}^n x_i^2 - \left[ \frac{(\sum_{i=1}^n x_i)^2}{n} \right] \right\}$$

- **Therefore**

$$s^2 = \frac{1}{n - 1} SS(x)$$

# MEASURES OF **DISPERSION**

- **Sample Standard Deviation: Square root of the sample variance.**

- Has **same units** data values and sample mean.

$$s = \sqrt{s^2}, \quad \text{where} \quad s^2 = \frac{1}{n-1} SS(x)$$

- **Example: Consider a second set of data: {6, 3, 8, 5, 2}. Find the followings:**
- **Measures of Central Tendency**
  - **Mean**  $\bar{x} = \frac{1}{5}(6 + 3 + 8 + 5 + 2) = 4.8$
  - **Median**  $\tilde{x} = \text{middle value} = 5$
  - **Mode**  $\hat{x} = \text{the value with the highest count} \Rightarrow \text{There is no mode}$
- **Measures of Dispersion**
  - **Range**  $\text{range} = H - L = 8 - 2 = 6$
  - **Sample Variance and Sample Standard Deviation**

## EXAMPLE (SAMPLE VARIANCE)

- Consider a second set of data: {6, 3, 8, 5, 2}

- $s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$

| Step 1. Find $\sum x$ | Step 2. Find $\bar{x}$       | Step 3. Find each $x - \bar{x}$ | Step 4. Find $\sum (x - \bar{x})^2$ | Step 5. Find $s^2$                         |
|-----------------------|------------------------------|---------------------------------|-------------------------------------|--|
| 6                     | $\bar{x} = \frac{\sum x}{n}$ | $6 - 4.8 = 1.2$                 | $(1.2)^2 = 1.44$                    | $s^2 = \frac{\sum (x - \bar{x})^2}{n - 1}$ |
| 3                     |                              | $3 - 4.8 = -1.8$                | $(-1.8)^2 = 3.24$                   |  |
| 8                     |                              | $8 - 4.8 = 3.2$                 | $(3.2)^2 = 10.24$                   |  |
| 5                     | $\bar{x} = \frac{24}{5}$     | $5 - 4.8 = 0.2$                 | $(0.2)^2 = 0.04$                    | $s^2 = \frac{22.80}{4}$                    |
| 2                     |                              | $2 - 4.8 = -2.8$                | $(-2.8)^2 = 7.84$                   |  |
| $\sum x = 24$         | $\bar{x} = 4.8$              | $\sum (x - \bar{x}) = 0$        | $\sum (x - \bar{x})^2 = 22.80$      | $s^2 = 5.7$                                |

- Or  $s^2 = \frac{1}{n-1} \left\{ \sum_{i=1}^n x_i^2 - \frac{1}{n} (\sum_{i=1}^n x_i)^2 \right\}$

$$s = \sqrt{s^2} = \sqrt{5.7}$$

| Step 1. Find $\sum x$ | Step 2. Find $\sum x^2$ | Step 3. Find $SS(x)$                      | Step 4. Find $s^2$                                    | Step 5. Find $s$ |
|-----------------------|-------------------------|---|---|------------------|
| 6                     | $6^2 = 36$              | $SS(x) = \sum x^2 - \frac{(\sum x)^2}{n}$ | $s^2 = \frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n - 1}$ | $s = \sqrt{s^2}$ |
| 3                     | $3^2 = 9$               |   |   | $s = \sqrt{5.7}$ |
| 8                     | $8^2 = 64$              | $SS(x) = 138 - \frac{(24)^2}{5}$          | $s^2 = \frac{22.8}{4}$                                | $s = 2.4$        |
| 5                     | $5^2 = 25$              |   |   |                  |
| 2                     | $2^2 = 4$               | $SS(x) = 138 - 115.2$                     | $s^2 = 5.7$   |                  |
| $\sum x = 24$         | $\sum x^2 = 138$        | $SS(x) = 22.8$                            |   |                  |



# EXAMPLE IN MICROSOFT EXCEL

Book2 - Excel

FILE HOME INSERT PAGE LAYOUT FORMULAS DATA REVIEW VIEW POWERPIVOT

Clipboard Font Alignment Number Styles Cells Editing

fx =AVERAGE(A1:A5) Enter the formula

|    | A | B | C | D | E | F                         | G | H | I        | J | K | L | M | N |
|----|---|---|---|---|---|---------------------------|---|---|----------|---|---|---|---|---|
| 1  | 6 |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 2  | 3 |   |   |   |   | Mean                      |   |   | 4.8      |   |   |   |   |   |
| 3  | 8 |   |   |   |   | Median                    |   |   | 5        |   |   |   |   |   |
| 4  | 5 |   |   |   |   | Mode                      |   |   | #N/A     |   |   |   |   |   |
| 5  | 2 |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 6  |   |   |   |   |   | Sample variance           |   |   | 5.7      |   |   |   |   |   |
| 7  |   |   |   |   |   | Sample standard deviation |   |   | 2.387467 |   |   |   |   |   |
| 8  |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 9  |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 10 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 11 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 12 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 13 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 14 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 15 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 16 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 17 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 18 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 19 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 20 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 21 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 22 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 23 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 24 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 25 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 26 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 27 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 28 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 29 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |
| 30 |   |   |   |   |   |                           |   |   |          |   |   |   |   |   |

Enter the data values

=MEDIAN(A1:A5)

=MODE(A1:A5)

=VAR(A1:A5)

=STDEV(A1:A5)

# QUESTIONS?

- **ANY QUESTION?**