

Formula Card for Johnson & Kuby, ELEMENTARY STATISTICS, Eleventh Edition

Sample mean:

$$\bar{x} = \frac{\sum x}{n} \quad (2.1)$$

Depth of sample median:

$$d(\tilde{x}) = (n + 1)/2 \quad (2.2)$$

Range: $H - L$

Sample variance:

$$s^2 = \frac{\sum (x - \bar{x})^2}{n - 1} \quad (2.5)$$

or

$$s^2 = \frac{\sum x^2 - \frac{(\sum x)^2}{n}}{n - 1} \quad (2.9)$$

Sample standard deviation:

$$s = \sqrt{s^2} \quad (2.6)$$

Chebyshev's theorem: at least $1 - (1/k^2)$ (p. 99)

Sum of squares of x :

$$SS(x) = \sum x^2 - ((\sum x)^2/n) \quad (2.8)$$

Sum of squares of y :

$$SS(y) = \sum y^2 - ((\sum y)^2/n) \quad (3.3)$$

Sum of squares of xy :

$$SS(xy) = \sum xy - ((\sum x \cdot \sum y)/n) \quad (3.4)$$

Pearson's correlation coefficient:

$$r = SS(xy) / \sqrt{SS(x) \cdot SS(y)} \quad (3.2)$$

Equation for line of best fit: $\hat{y} = b_0 + b_1x$ (p. 146)

Slope for line of best fit: $b_1 = SS(xy)/SS(x)$ (3.6)

y-intercept for line of best fit:

$$b_0 = [\sum y - (b_1 \cdot \sum x)]/n \quad (3.7)$$

Empirical (observed) probability:

$$P'(A) = n(A)/n \quad (4.1)$$

Theoretical probability for equally likely sample space:

$$P(A) = n(A)/n(S) \quad (4.2)$$

Complement rule:

$$P(\text{not } A) = P(\bar{A}) = 1 - P(A) \quad (4.3)$$

General addition rule:

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) \quad (4.4)$$

General multiplication rule:

$$P(A \text{ and } B) = P(A) \cdot P(B | A) \quad (4.5)$$

Special addition rule for mutually exclusive events:

$$P(A \text{ or } B \text{ or } \dots \text{ or } E) = P(A) + P(B) + \dots + P(E) \quad (4.6)$$

Special multiplication rule for independent events:

$$P(A \text{ and } B \text{ and } \dots \text{ and } E) = P(A) \cdot P(B) \cdot \dots \cdot P(E) \quad (4.7)$$

Mean of discrete random variable:

$$\mu = \sum [xP(x)] \quad (5.1)$$

Variance of discrete random variable:

$$\sigma^2 = \sum [x^2P(x)] - \{\sum [xP(x)]\}^2 \quad (5.3a)$$

Standard deviation of discrete random variable:

$$\sigma = \sqrt{\sigma^2} \quad (5.4)$$

Factorial: $n! = (n)(n-1)(n-2) \cdots 2 \cdot 1$ (p. 248)

Binomial coefficient:

$$\binom{n}{x} = \frac{n!}{x!(n-x)!} \quad (5.6)$$

Binomial probability function:

$$P(x) = \binom{n}{x} \cdot p^x \cdot q^{n-x}, x = 0, 1, 2, \dots, n \quad (5.5)$$

Mean of binomial random variable: $\mu = np$ (5.7)

Standard deviation, binomial random variable:

$$\sigma = \sqrt{npq} \quad (5.8)$$

Standard score: $z = (x - \mu)/\sigma$ (6.3)

Standard score for \bar{x} : $z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$ (7.2)

Confidence interval for mean, μ (σ known):

$$\bar{x} \pm z(\alpha/2) \cdot (\sigma/\sqrt{n}) \quad (8.1)$$

Sample size for $1 - \alpha$ confidence estimate for μ :

$$n = [z(\alpha/2) \cdot \sigma/E]^2 \quad (8.3)$$

Calculated test statistic for $H_0: \mu = \mu_0$ (σ known):

$$z^* = (\bar{x} - \mu_0)/(\sigma/\sqrt{n}) \quad (8.4)$$

Confidence interval estimate for mean, μ (σ unknown):

$$\bar{x} \pm t(df, \alpha/2) \cdot (s/\sqrt{n}) \text{ with } df = n - 1 \quad (9.1)$$

Calculated test statistic for $H_0: \mu = \mu_0$ (σ unknown):

$$t^* = \frac{\bar{x} - \mu_0}{s/\sqrt{n}} \text{ with } df = n - 1 \quad (9.2)$$

Confidence interval estimate for proportion, p :

$$p' \pm z(\alpha/2) \cdot \sqrt{p'q'/n}, p' = x/n \quad (9.6)$$

Sample Size for $1 - \alpha$ Confidence Interval of p

$$n = \frac{[z(\alpha/2)]^2 p^* q^*}{E^2} \quad (9.8)$$

Calculated test statistic for $H_0: p = p_0$:

$$z^* = (p' - p_0)/\sqrt{p_0q_0/n}, p' = x/n \quad (9.9)$$

Calculated test statistic for $H_0: \sigma^2 = \sigma_0^2$ or $\sigma = \sigma_0$:

$$\chi^2 = (n-1)s^2/\sigma_0^2, df = n - 1 \quad (9.10)$$

Mean difference between two dependent samples:

$$\text{Paired difference: } d = x_1 - x_2 \quad (10.1)$$

Confidence interval for mean difference, μ_d :

$$\bar{d} \pm t(df, \alpha/2) \cdot s_d/\sqrt{n} \text{ with } df = n - 1 \quad (10.2)$$

Sample mean of paired differences:

$$\bar{d} = \sum d/n \quad (10.3)$$

Sample standard deviation of paired differences:

$$s_d = \sqrt{\frac{\sum d^2 - \frac{(\sum d)^2}{n}}{n-1}} \quad (10.4)$$

Calculated test statistic for $H_0: \mu_d = \mu_0$:

$$t^* = (\bar{d} - \mu_0) / (s_d / \sqrt{n}), \quad df = n - 1 \quad (10.5)$$

Difference between means of two independent samples:

Degrees of freedom:

$$df = \text{smaller of } (n_1 - 1) \text{ or } (n_2 - 1) \quad (\text{p. 496})$$

Confidence interval estimate for $\mu_1 - \mu_2$:

$$(\bar{x}_1 - \bar{x}_2) \pm t(df, \alpha/2) \sqrt{(s_1^2/n_1) + (s_2^2/n_2)} \quad (10.8)$$

Calculated test statistic for $H_0: \mu_1 - \mu_2 = (\mu_1 - \mu_2)_0$:

$$t^* = [(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)_0] / \sqrt{(s_1^2/n_1) + (s_2^2/n_2)} \quad (10.9)$$

Difference between proportions of two independent samples:

Confidence interval for $p_1 - p_2$:

$$(p'_1 - p'_2) \pm z(\alpha/2) \cdot \sqrt{\frac{p'_1 q'_1}{n_1} + \frac{p'_2 q'_2}{n_2}} \quad (10.11)$$

Pooled observed probability:

$$p'_p = (x_1 + x_2) / (n_1 + n_2) \quad (10.13)$$

$$q'_p = 1 - p'_p \quad (10.14)$$

Calculated test statistic for $H_0: p_1 - p_2 = 0$:

$$z^* = \frac{p'_1 - p'_2}{\sqrt{(p'_p)(q'_p) \left[\left(\frac{1}{n_1} + \frac{1}{n_2} \right) \right]}} \quad (10.15)$$

Ratio of variances between two independent samples:

Calculated test statistic for $H_0: \sigma_1^2 / \sigma_2^2 = 1$:

$$F^* = s_1^2 / s_2^2 \quad (10.16)$$

Calculated test statistic for enumerative data:

$$\chi^2^* = \sum [(O - E)^2 / E] \quad (11.1)$$

Multinomial experiment:

$$\text{Degrees of freedom: } df = k - 1 \quad (11.2)$$

$$\text{Expected frequency: } E = n \cdot p \quad (11.3)$$

Test for independence or Test of homogeneity:

Degrees of freedom:

$$df = (r - 1) \cdot (c - 1) \quad (11.4)$$

$$\text{Expected value: } E = (R \cdot C) / n \quad (11.5)$$

Mathematical model:

$$x_{c,k} = \mu + F_c + \epsilon_{k(c)} \quad (12.13)$$

Total sum of squares:

$$SS(\text{total}) = \sum (x^2) - \frac{(\sum x)^2}{n} \quad (12.2)$$

Sum of squares due to factor:

$$\left[\left(\frac{C_1^2}{k_1} \right) + \left(\frac{C_2^2}{k_2} \right) + \left(\frac{C_3^2}{k_3} \right) + \dots \right] - \left[\frac{(\sum x)^2}{n} \right] \quad (12.3)$$

Sum of squares due to error:

$$SS(\text{error}) = \sum (x^2) - [(C_1^2/k_1) + (C_2^2/k_2) + (C_3^2/k_3) + \dots] \quad (12.4)$$

Degrees of freedom for total:

$$df(\text{total}) = n - 1 \quad (12.6)$$

Degrees of freedom for factor:

$$df(\text{factor}) = c - 1 \quad (12.5)$$

Degrees of freedom for error:

$$df(\text{error}) = n - c \quad (12.7)$$

Mean square for factor:

$$MS(\text{factor}) = SS(\text{factor}) / df(\text{factor}) \quad (12.10)$$

Mean square for error:

$$MS(\text{error}) = SS(\text{error}) / df(\text{error}) \quad (12.11)$$

Calculated test statistic for H_0 : Mean value is same at all levels:

$$F^* = MS(\text{factor}) / MS(\text{error}) \quad (12.12)$$

Covariance of x and y :

$$\text{covar}(x, y) = \sum [(x - \bar{x})(y - \bar{y})] / (n - 1) \quad (13.1)$$

Pearson's correlation coefficient:

$$r = \text{covar}(x, y) / (s_x \cdot s_y) \quad (13.2)$$

or

$$r = SS(xy) / \sqrt{SS(x) \cdot SS(y)} \quad (3.2) \text{ or } (13.3)$$

$$\text{Experimental error: } e = y - \hat{y} \quad (13.5)$$

$$\text{Estimated variance of error: } s_e^2 = \sum (y - \hat{y})^2 / (n - 2) \quad (13.6)$$

or

$$s_e^2 = \frac{(\sum y^2) - (b_0)(\sum y) - (b_1)(\sum xy)}{n - 2} \quad (13.8)$$

Standard deviation about the line of best fit:

$$s_e = \sqrt{s_e^2} \quad (13.9)$$

Estimate for variance of slope:

$$s_{b_1}^2 = \frac{s_e^2}{SS(x)} = \frac{s_e^2}{\sum x^2 - [(\sum x)^2 / n]} \quad (13.12)$$

Confidence interval for β_1 :

$$b_1 \pm t(df, \alpha/2) \cdot s_{b_1} \quad (13.14)$$

Calculated test statistic for $H_0: \beta_1 = 0$:

$$t^* = (b_1 - \beta_1) / s_{b_1} \text{ with } df = n - 2 \quad (13.15)$$

Confidence interval for mean value of y at x_0 :

$$\hat{y} \pm t(n - 2, \alpha/2) \cdot s_e \cdot \sqrt{\frac{1}{n} + \frac{(x_0 - \bar{x})^2}{SS(x)}} \quad (13.17)$$

Prediction interval for y at x_0 :

$$\hat{y} \pm t(n - 2, \alpha/2) \cdot s_e \cdot \sqrt{1 + \frac{1}{n} + \frac{(x_0 - \bar{x})^2}{SS(x)}} \quad (13.16)$$

Mann-Whitney U test:

$$U_a = n_a \cdot n_b + [(n_b) \cdot (n_b + 1) / 2] - R_b \quad (14.3)$$

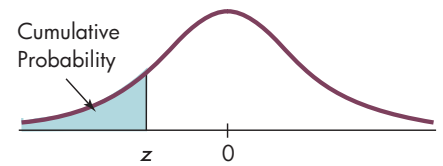
$$U_b = n_a \cdot n_b + [(n_a) \cdot (n_a + 1) / 2] - R_a \quad (14.4)$$

Spearman's rank correlation coefficient:

$$r_s = 1 - \left[\frac{6 \sum d^2}{n(n^2 - 1)} \right] \quad (14.11)$$

z-Table

negative z-values

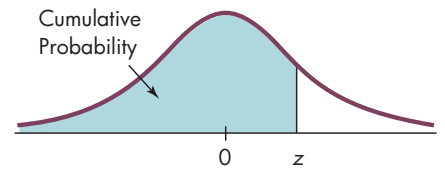


z-value in the **left-hand tail**. **z**

	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
-5.0	0.0000003									
-4.5	0.000003									
-4.0	0.00003	0.00003	0.00003	0.00003	0.00003	0.00003	0.00002	0.00002	0.00002	0.00002
-3.9	0.00005	0.00005	0.00004	0.00004	0.00004	0.00004	0.00004	0.00004	0.00003	0.00003
-3.8	0.00007	0.00007	0.00007	0.00006	0.00006	0.00006	0.00006	0.00005	0.00005	0.00005
-3.7	0.00011	0.00010	0.00010	0.00010	0.00009	0.00009	0.00008	0.00008	0.00008	0.00008
-3.6	0.0002	0.0002	0.0002	0.00014	0.00014	0.00013	0.00013	0.00012	0.00012	0.00011
-3.5	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002	0.0002
-3.4	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0002
-3.3	0.0005	0.0005	0.0005	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004
-3.2	0.0007	0.0007	0.0006	0.0006	0.0006	0.0006	0.0006	0.0005	0.0005	0.0005
-3.1	0.0010	0.0009	0.0009	0.0009	0.0008	0.0008	0.0008	0.0008	0.0007	0.0007
-3.0	0.0014	0.0013	0.0013	0.0012	0.0012	0.0011	0.0011	0.0011	0.0010	0.0010
-2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
-2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
-2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
-2.6	0.0047	0.0045	0.0044	0.0043	0.0042	0.0040	0.0039	0.0038	0.0037	0.0036
-2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
-2.4	0.0082	0.0080	0.0078	0.0076	0.0073	0.0071	0.0070	0.0068	0.0066	0.0064
-2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
-2.2	0.0139	0.0136	0.0132	0.0129	0.0126	0.0122	0.0119	0.0116	0.0113	0.0110
-2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
-2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
-1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
-1.8	0.0359	0.0352	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
-1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
-1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
-1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
-1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
-1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
-1.2	0.1151	0.1131	0.1112	0.1094	0.1075	0.1057	0.1038	0.1020	0.1003	0.0985
-1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
-1.0	0.1587	0.1563	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
-0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
-0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
-0.7	0.2420	0.2389	0.2358	0.2327	0.2297	0.2266	0.2236	0.2207	0.2177	0.2148
-0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
-0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
-0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
-0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
-0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
-0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641

z-Table

positive z-values



z-value in the **left-hand tail**. z

	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5754
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7258	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7518	0.7549
0.7	0.7580	0.7612	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7996	0.8023	0.8051	0.8079	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9430	0.9441
1.6	0.9452	0.9463	0.9474	0.9485	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9700	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9762	0.9767
2.0	0.9773	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9865	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9980	0.9981
2.9	0.9981	0.9982	0.9983	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998	0.9998
3.5	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998
3.6	0.99984	0.99985	0.99985	0.99986	0.99986	0.99987	0.99987	0.99988	0.99988	0.99989
3.7	0.99989	0.99990	0.99990	0.99990	0.99991	0.99991	0.99992	0.99992	0.99992	0.99992
3.8	0.99993	0.99993	0.99993	0.99994	0.99994	0.99994	0.99994	0.99995	0.99995	0.99995
3.9	0.99995	0.99995	0.99996	0.99996	0.99996	0.99996	0.99996	0.99996	0.99997	0.99997
4.0	0.99997	0.99997	0.99997	0.99997	0.99997	0.99997	0.99998	0.99998	0.99998	0.99998
4.5	0.999997									
5.0	0.9999997									

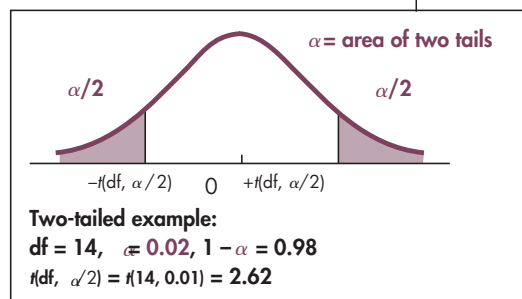
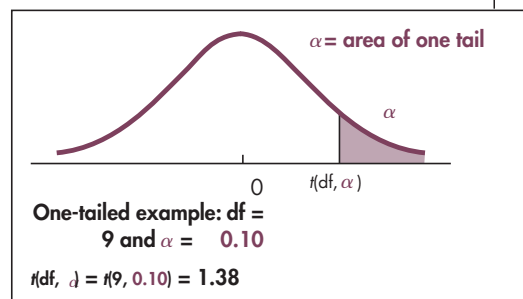
t-Table

Area in One Tail

	0.25	0.10	0.05	0.025	0.01	0.005
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Area in Two Tails

df	0.50	0.20	0.10	0.05	0.02	0.01
3	0.765	1.64	2.35	3.18	4.54	5.84
4	0.741	1.53	2.13	2.78	3.75	4.60
5	0.727	1.48	2.02	2.57	3.36	4.03
6	0.718	1.44	1.94	2.45	3.14	3.71
7	0.711	1.41	1.89	2.36	3.00	3.50
8	0.706	1.40	1.86	2.31	2.90	3.36
9	0.703	1.38	1.83	2.26	2.82	3.25
10	0.700	1.37	1.81	2.23	2.76	3.17
11	0.697	1.36	1.80	2.20	2.72	3.11
12	0.695	1.36	1.78	2.18	2.68	3.05
13	0.694	1.35	1.77	2.16	2.65	3.01
14	0.692	1.35	1.76	2.14	2.62	2.98
15	0.691	1.34	1.75	2.13	2.60	2.95
16	0.690	1.34	1.75	2.12	2.58	2.92
17	0.689	1.33	1.74	2.11	2.57	2.90
18	0.688	1.33	1.73	2.10	2.55	2.88
19	0.688	1.33	1.73	2.09	2.54	2.86
20	0.687	1.33	1.72	2.09	2.53	2.85
21	0.686	1.32	1.72	2.08	2.52	2.83
22	0.686	1.32	1.72	2.07	2.51	2.82
23	0.685	1.32	1.71	2.07	2.50	2.81
24	0.685	1.32	1.71	2.06	2.49	2.80
25	0.684	1.32	1.71	2.06	2.49	2.79
26	0.684	1.31	1.70	2.05	2.47	2.77
27	0.684	1.31	1.70	2.05	2.47	2.77
28	0.683	1.31	1.70	2.05	2.47	2.76
29	0.683	1.31	1.70	2.05	2.46	2.76
30	0.683	1.31	1.70	2.04	2.46	2.75
35	0.682	1.31	1.69	2.03	2.44	2.72
40	0.681	1.30	1.68	2.02	2.42	2.70
50	0.679	1.30	1.68	2.01	2.40	2.68
70	0.678	1.29	1.67	1.99	2.38	2.65
100	0.677	1.29	1.66	1.98	2.36	2.63
df > 100	0.675	1.28	1.65	1.96	2.33	2.58



χ^2 -Table

a) Area to the Right

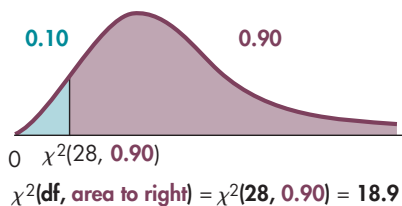
	0.995	0.99	0.975	0.95	0.90	0.75	0.50	0.25	0.10	0.05	0.025	0.01	0.005
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b) Area to the Left (the Cumulative Area)

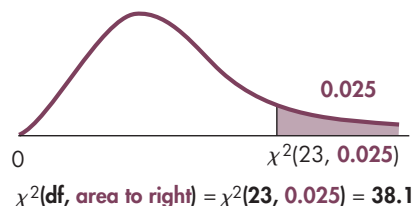
Median

df	0.005	0.01	0.025	0.05	0.10	0.25	0.50	0.75	0.90	0.95	0.975	0.99	0.995
1	0.0000393	0.000157	0.000982	0.00393	0.0158	0.102	0.455	1.32	2.71	3.84	5.02	6.63	7.88
2	0.0100	0.0201	0.0506	0.103	0.211	0.575	1.39	2.77	4.61	5.99	7.38	9.21	10.6
3	0.0717	0.115	0.216	0.352	0.584	1.21	2.37	4.11	6.25	7.81	9.35	11.3	12.8
4	0.207	0.297	0.484	0.711	1.06	1.92	3.36	5.39	7.78	9.49	11.1	13.3	14.9
5	0.412	0.554	0.831	1.15	1.61	2.67	4.35	6.63	9.24	11.1	12.8	15.1	16.7
6	0.676	0.872	1.24	1.64	2.20	3.45	5.35	7.84	10.6	12.6	14.4	16.8	18.5
7	0.989	1.24	1.69	2.17	2.83	4.25	6.35	9.04	12.0	14.1	16.0	18.5	20.3
8	1.34	1.65	2.18	2.73	3.49	5.07	7.34	10.2	13.4	15.5	17.5	20.1	22.0
9	1.73	2.09	2.70	3.33	4.17	5.90	8.34	11.4	14.7	16.9	19.0	21.7	23.6
10	2.16	2.56	3.25	3.94	4.87	6.74	9.34	12.5	16.0	18.3	20.5	23.2	25.2
11	2.60	3.05	3.82	4.57	5.58	7.58	10.34	13.7	17.3	19.7	21.9	24.7	26.8
12	3.07	3.57	4.40	5.23	6.30	8.44	11.34	14.8	18.5	21.0	23.3	26.2	28.3
13	3.57	4.11	5.01	5.89	7.04	9.30	12.34	16.0	19.8	22.4	24.7	27.7	29.8
14	4.07	4.66	5.63	6.57	7.79	10.2	13.34	17.1	21.1	23.7	26.1	29.1	31.3
15	4.60	5.23	6.26	7.26	8.55	11.0	14.34	18.2	22.3	25.0	27.5	30.6	32.8
16	5.14	5.81	6.91	7.96	9.31	11.9	15.34	19.4	23.5	26.3	28.8	32.0	34.3
17	5.70	6.41	7.56	8.67	10.1	12.8	16.34	20.5	24.8	27.6	30.2	33.4	35.7
18	6.26	7.01	8.23	9.39	10.9	13.7	17.34	21.6	26.0	28.9	31.5	34.8	37.2
19	6.84	7.63	8.91	10.1	11.7	14.6	18.34	22.7	27.2	30.1	32.9	36.2	38.6
20	7.43	8.26	9.59	10.9	12.4	15.5	19.34	23.8	28.4	31.4	34.2	37.6	40.0
21	8.03	8.90	10.3	11.6	13.2	16.3	20.34	24.9	29.6	32.7	35.5	38.9	41.4
22	8.64	9.54	11.0	12.3	14.0	17.2	21.34	26.0	30.8	33.9	36.8	40.3	42.8
23	9.26	10.2	11.7	13.1	14.8	18.1	22.34	27.1	32.0	35.2	38.1	41.6	44.2
24	9.89	10.9	12.4	13.8	15.7	19.0	23.34	28.2	33.2	36.4	39.4	43.0	45.6
25	10.5	11.5	13.1	14.6	16.5	19.9	24.34	29.3	34.4	37.7	40.6	44.3	46.9
26	11.2	12.2	13.8	15.4	17.3	20.8	25.34	30.4	35.6	38.9	41.9	45.6	48.3
27	11.8	12.9	14.6	16.2	18.1	21.7	26.34	31.5	36.7	40.1	43.2	47.0	49.6
28	12.5	13.6	15.3	16.9	18.9	22.7	27.34	32.6	37.9	41.3	44.5	48.3	51.0
29	13.1	14.3	16.0	17.7	19.8	23.6	28.34	33.7	39.1	42.6	45.7	49.6	52.3
30	13.8	15.0	16.8	18.5	20.6	24.5	29.34	34.8	40.3	43.8	47.0	50.9	53.7
40	20.7	22.2	24.4	26.5	29.1	33.7	39.34	45.6	51.8	55.8	59.3	63.7	66.8
50	28.0	29.7	32.4	34.8	37.7	42.9	49.33	56.3	63.2	67.5	71.4	76.2	79.5
60	35.5	37.5	40.5	43.2	46.5	52.3	59.33	67.0	74.4	79.1	83.3	88.4	92.0
70	43.3	45.4	48.8	51.7	55.3	61.7	69.33	77.6	85.5	90.5	95.0	100.4	104.2
80	51.2	53.5	57.2	60.4	64.3	71.1	79.33	88.1	96.6	101.9	106.6	112.3	116.3
90	59.2	61.8	65.6	69.1	73.3	80.6	89.33	98.6	107.6	113.1	118.1	124.1	128.3
100	67.3	70.1	74.2	77.9	82.4	90.1	99.33	109.1	118.5	124.3	129.6	135.8	140.2

Left-tail example:
Find χ^2 with df = 28; area in left-tail = 0.10.



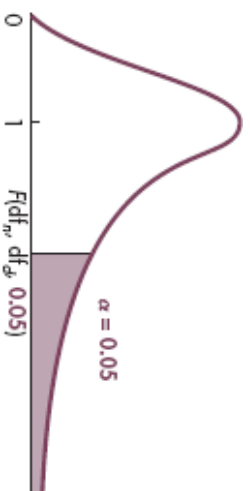
Right-tail example:
Find χ^2 with df = 23; area in right-tail = 0.025



For specific details about using this table to find p -values, see pages 458–461; critical values, pages 454–455.
Table 8 was generated using Minitab.

F - Table

$\alpha = 0.05$



		Degrees of Freedom for Numerator																		
		1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	10,000
Degrees of Freedom for Denominator	1	161.	200.	216.	225.	230.	234.	237.	239.	241.	242.	244.	246.	248.	249.	250.	251.	252.	253.	254.
	2	18.5	19.0	19.2	19.2	19.3	19.3	19.4	19.4	19.4	19.4	19.4	19.4	19.4	19.5	19.5	19.5	19.5	19.5	19.5
	3	10.1	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.70	8.66	8.64	8.62	8.59	8.57	8.55	8.53
	4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.69	5.66	5.63
	5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.68	4.62	4.56	4.53	4.50	4.46	4.43	4.40	4.37
	6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.94	3.87	3.84	3.81	3.77	3.74	3.70	3.67
	7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.51	3.44	3.41	3.38	3.34	3.30	3.27	3.23
	8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.28	3.22	3.15	3.12	3.08	3.04	3.01	2.97	2.93
	9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.01	2.94	2.90	2.86	2.83	2.79	2.75	2.71
	10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.91	2.85	2.77	2.74	2.70	2.66	2.62	2.58	2.54
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	3.01	2.95	2.90	2.85	2.79	2.72	2.65	2.61	2.57	2.53	2.49	2.45	2.41
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.91	2.85	2.80	2.75	2.69	2.62	2.54	2.51	2.47	2.43	2.38	2.34	2.30
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.83	2.77	2.71	2.67	2.60	2.53	2.46	2.42	2.38	2.34	2.30	2.25	2.21
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.76	2.70	2.65	2.60	2.53	2.46	2.39	2.35	2.31	2.27	2.22	2.18	2.13
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.71	2.64	2.59	2.54	2.48	2.40	2.33	2.29	2.25	2.20	2.16	2.11	2.07
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.66	2.59	2.54	2.49	2.42	2.35	2.28	2.24	2.19	2.15	2.11	2.06	2.01
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.61	2.55	2.49	2.45	2.38	2.31	2.23	2.19	2.15	2.10	2.06	2.01	1.96
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.58	2.51	2.46	2.41	2.34	2.27	2.20	2.15	2.11	2.06	2.02	1.97	1.92
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.54	2.48	2.42	2.38	2.31	2.23	2.16	2.11	2.07	2.03	1.98	1.93	1.88
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.51	2.45	2.39	2.35	2.28	2.20	2.12	2.08	2.04	1.99	1.95	1.90	1.84
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.49	2.42	2.37	2.32	2.25	2.18	2.10	2.05	2.01	1.96	1.92	1.87	1.81
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.46	2.40	2.34	2.30	2.23	2.15	2.07	2.03	1.98	1.94	1.89	1.84	1.78
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.44	2.37	2.32	2.27	2.20	2.13	2.05	2.01	1.96	1.91	1.86	1.81	1.76
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.42	2.36	2.30	2.25	2.18	2.11	2.03	1.98	1.94	1.89	1.84	1.79	1.73
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.40	2.34	2.28	2.24	2.16	2.09	2.01	1.96	1.92	1.87	1.82	1.77	1.71
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.33	2.27	2.21	2.16	2.09	2.01	1.93	1.89	1.84	1.79	1.74	1.68	1.62
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.25	2.18	2.12	2.08	2.00	1.92	1.84	1.79	1.74	1.69	1.64	1.58	1.51
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.17	2.10	2.04	1.99	1.92	1.84	1.75	1.70	1.65	1.59	1.53	1.47	1.39
120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.09	2.02	1.96	1.91	1.83	1.75	1.66	1.61	1.55	1.50	1.43	1.35	1.26
10,000	3.84	3.00	2.61	2.37	2.21	2.10	2.01	2.01	1.94	1.88	1.83	1.75	1.67	1.57	1.52	1.46	1.40	1.32	1.22	1.03

$\alpha=0.01$ 

Degrees of Freedom for Numerator																			
	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	10,000
Degrees of Freedom for Denominator	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	10,000
1	4052.	5000.	5403.	5625.	5764.	5859.	5928.	5981.	6022.	6056.	6106.	6157.	6209.	6235.	6261.	6287.	6313.	6339.	6366.
2	98.5	99.0	99.2	99.2	99.3	99.3	99.4	99.4	99.4	99.4	99.4	99.4	99.4	99.5	99.5	99.5	99.5	99.5	99.5
3	34.1	30.8	29.5	28.7	28.2	27.9	27.7	27.5	27.3	27.2	27.1	26.9	26.7	26.6	26.5	26.4	26.3	26.2	26.1
4	21.2	18.0	16.7	16.0	15.5	15.2	15.0	14.8	14.7	14.5	14.4	14.2	14.0	13.9	13.8	13.7	13.7	13.6	13.5
5	16.3	13.3	12.1	11.4	11.0	10.7	10.5	10.3	10.2	10.1	9.89	9.72	9.55	9.47	9.38	9.29	9.20	9.11	9.02
6	13.7	10.9	9.78	9.15	8.75	8.47	8.26	8.10	7.98	7.87	7.72	7.56	7.40	7.31	7.23	7.14	7.06	6.97	6.88
7	12.2	9.55	8.45	7.85	7.46	7.19	6.99	6.84	6.72	6.62	6.47	6.31	6.16	6.07	5.99	5.91	5.82	5.74	5.65
8	11.3	8.65	7.59	7.01	6.63	6.37	6.18	6.03	5.91	5.81	5.67	5.52	5.36	5.28	5.20	5.12	5.03	4.95	4.86
9	10.6	8.02	6.99	6.42	6.06	5.80	5.61	5.47	5.35	5.26	5.11	4.96	4.81	4.73	4.65	4.57	4.48	4.40	4.31
10	10.0	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.94	4.85	4.71	4.56	4.41	4.33	4.25	4.17	4.08	4.00	3.91
11	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74	4.63	4.54	4.40	4.25	4.10	4.02	3.94	3.86	3.78	3.69	3.60
12	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.50	4.39	4.30	4.16	4.01	3.86	3.78	3.70	3.62	3.54	3.45	3.36
13	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.19	4.10	3.96	3.82	3.66	3.59	3.51	3.43	3.34	3.25	3.17
14	8.86	6.51	5.56	5.04	4.70	4.46	4.28	4.14	4.03	3.94	3.80	3.66	3.51	3.43	3.35	3.27	3.18	3.09	3.01
15	8.68	6.36	5.42	4.89	4.56	4.32	4.14	4.00	3.89	3.80	3.67	3.52	3.37	3.29	3.21	3.13	3.05	2.96	2.87
16	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.78	3.69	3.55	3.41	3.26	3.18	3.10	3.02	2.93	2.84	2.75
17	8.40	6.11	5.19	4.67	4.34	4.10	3.93	3.79	3.68	3.59	3.46	3.31	3.16	3.08	3.00	2.92	2.83	2.75	2.65
18	8.29	6.01	5.09	4.58	4.25	4.01	3.84	3.71	3.60	3.51	3.37	3.23	3.08	3.00	2.92	2.84	2.75	2.66	2.57
19	8.18	5.93	5.01	4.50	4.17	3.94	3.77	3.63	3.52	3.43	3.30	3.15	3.00	2.92	2.84	2.76	2.67	2.58	2.49
20	8.10	5.85	4.94	4.43	4.10	3.87	3.70	3.56	3.46	3.37	3.23	3.09	2.94	2.86	2.78	2.69	2.61	2.52	2.42
21	8.02	5.78	4.87	4.37	4.04	3.81	3.64	3.51	3.40	3.31	3.17	3.03	2.88	2.80	2.72	2.64	2.55	2.46	2.36
22	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35	3.26	3.12	2.98	2.83	2.75	2.67	2.58	2.50	2.40	2.31
23	7.88	5.66	4.76	4.26	3.94	3.71	3.54	3.41	3.30	3.21	3.07	2.93	2.78	2.70	2.62	2.54	2.45	2.35	2.26
24	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26	3.17	3.03	2.89	2.74	2.66	2.58	2.49	2.40	2.31	2.21
25	7.77	5.57	4.68	4.18	3.86	3.63	3.46	3.32	3.22	3.13	2.99	2.85	2.70	2.62	2.54	2.45	2.36	2.27	2.17
30	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07	2.98	2.84	2.70	2.55	2.47	2.39	2.30	2.21	2.11	2.01
40	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89	2.80	2.66	2.52	2.37	2.29	2.20	2.11	2.02	1.92	1.80
60	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72	2.63	2.50	2.35	2.20	2.12	2.03	1.94	1.84	1.73	1.60
120	6.85	4.79	3.95	3.48	3.17	2.96	2.79	2.66	2.56	2.47	2.34	2.19	2.03	1.95	1.86	1.76	1.66	1.53	1.38
10,000	6.64	4.61	3.78	3.32	3.02	2.80	2.64	2.51	2.41	2.32	2.19	2.04	1.88	1.79	1.70	1.59	1.48	1.33	1.05

$$\alpha=0.025$$


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120
10,000

1	648.	800.	864.	900.	922.	937.	948.	957.	963.	969.	977.	985.	993.	997.	1001.	1006.	1010.	1014.	1018.
2	38.5	39.0	39.2	39.2	39.3	39.3	39.4	39.4	39.4	39.4	39.4	39.4	39.4	39.5	39.5	39.5	39.5	39.5	39.5
3	17.4	16.0	15.4	15.1	14.9	14.7	14.6	14.5	14.5	14.4	14.3	14.3	14.2	14.1	14.1	14.0	14.0	13.9	13.9
4	12.2	10.6	9.98	9.60	9.36	9.20	9.07	8.98	8.90	8.84	8.75	8.66	8.56	8.51	8.46	8.41	8.36	8.31	8.26
5	10.0	8.43	7.76	7.39	7.15	6.98	6.85	6.76	6.68	6.62	6.52	6.43	6.33	6.28	6.23	6.18	6.12	6.07	6.02
6	8.81	7.26	6.60	6.23	5.99	5.82	5.70	5.60	5.52	5.46	5.37	5.27	5.17	5.12	5.07	5.01	4.96	4.90	4.85
7	8.07	6.54	5.89	5.52	5.29	5.12	4.99	4.90	4.82	4.76	4.67	4.57	4.47	4.42	4.36	4.31	4.25	4.20	4.14
8	7.57	6.06	5.42	5.05	4.82	4.65	4.53	4.43	4.36	4.30	4.20	4.10	4.00	3.95	3.89	3.84	3.78	3.73	3.67
9	7.21	5.71	5.08	4.72	4.48	4.32	4.20	4.10	4.03	3.96	3.87	3.77	3.67	3.61	3.56	3.51	3.45	3.39	3.33
10	6.94	5.46	4.83	4.47	4.24	4.07	3.95	3.85	3.78	3.72	3.62	3.52	3.42	3.37	3.31	3.26	3.20	3.14	3.08
11	6.72	5.26	4.63	4.28	4.04	3.88	3.76	3.66	3.59	3.53	3.43	3.33	3.23	3.17	3.12	3.06	3.00	2.94	2.88
12	6.55	5.10	4.47	4.12	3.89	3.73	3.61	3.51	3.44	3.37	3.28	3.18	3.07	3.02	2.96	2.91	2.85	2.79	2.73
13	6.41	4.97	4.35	4.00	3.77	3.60	3.48	3.39	3.31	3.25	3.15	3.05	2.95	2.89	2.84	2.78	2.72	2.66	2.60
14	6.30	4.86	4.24	3.89	3.66	3.50	3.38	3.28	3.21	3.15	3.05	2.95	2.84	2.79	2.73	2.67	2.61	2.55	2.49
15	6.20	4.77	4.15	3.80	3.58	3.41	3.29	3.20	3.12	3.06	2.96	2.86	2.76	2.70	2.64	2.59	2.52	2.46	2.40
16	6.12	4.69	4.08	3.73	3.50	3.34	3.22	3.12	3.05	2.99	2.89	2.79	2.68	2.63	2.57	2.51	2.45	2.38	2.32
17	6.04	4.62	4.01	3.66	3.44	3.28	3.16	3.06	2.98	2.92	2.82	2.72	2.62	2.56	2.50	2.44	2.38	2.32	2.25
18	5.98	4.56	3.95	3.61	3.38	3.22	3.10	3.01	2.93	2.87	2.77	2.67	2.56	2.50	2.44	2.38	2.32	2.26	2.19
19	5.92	4.51	3.90	3.56	3.33	3.17	3.05	2.96	2.88	2.82	2.72	2.62	2.51	2.45	2.39	2.33	2.27	2.20	2.13
20	5.87	4.46	3.86	3.51	3.29	3.13	3.01	2.91	2.84	2.77	2.68	2.57	2.46	2.41	2.35	2.29	2.22	2.16	2.09
21	5.83	4.42	3.82	3.48	3.25	3.09	2.97	2.87	2.80	2.73	2.64	2.53	2.42	2.37	2.31	2.25	2.18	2.11	2.04
22	5.79	4.38	3.78	3.44	3.22	3.05	2.93	2.84	2.76	2.70	2.60	2.50	2.39	2.33	2.27	2.21	2.14	2.08	2.00
23	5.75	4.35	3.75	3.41	3.18	3.02	2.90	2.81	2.73	2.67	2.57	2.47	2.36	2.30	2.24	2.18	2.11	2.04	1.97
24	5.72	4.32	3.72	3.38	3.15	2.99	2.87	2.78	2.70	2.64	2.54	2.44	2.33	2.27	2.21	2.15	2.08	2.01	1.94
25	5.69	4.29	3.69	3.35	3.13	2.97	2.85	2.75	2.68	2.61	2.51	2.41	2.30	2.24	2.18	2.12	2.05	1.98	1.91
30	5.57	4.18	3.59	3.25	3.03	2.87	2.75	2.65	2.57	2.51	2.41	2.31	2.20	2.14	2.07	2.01	1.94	1.87	1.79
40	5.42	4.05	3.46	3.13	2.90	2.74	2.62	2.53	2.45	2.39	2.29	2.18	2.07	2.01	1.94	1.88	1.80	1.72	1.64
60	5.29	3.93	3.34	3.01	2.79	2.63	2.51	2.41	2.33	2.27	2.17	2.06	1.94	1.88	1.82	1.74	1.67	1.58	1.48
120	5.15	3.80	3.23	2.89	2.67	2.52	2.39	2.30	2.22	2.16	2.05	1.95	1.82	1.76	1.69	1.61	1.53	1.43	1.31
10,000	5.03	3.69	3.12	2.79	2.57	2.41	2.29	2.19	2.11	2.05	1.95	1.83	1.71	1.64	1.57	1.49	1.39	1.27	1.04

Case 1: One Variable (Population)

Assumptions	σ is known	σ is unknown	$n(p_0) > 5$ and $n(1 - p_0) > 5$	Data comes from Normal Population
Parameter of interest:	Mean, μ	Mean, μ	Proportion, p	Variance, σ^2
Confidence Interval Formula:	$\bar{x} \pm z(\alpha/2) \frac{\sigma}{\sqrt{n}}$	$\bar{x} \pm t(df, \alpha/2) \frac{s}{\sqrt{n}}$ with $df = n - 1$	$p' \pm z(\alpha/2) \sqrt{\frac{p'q'}{n}}$	$\frac{(n-1)s^2}{\chi^2(df, \alpha/2)} < \sigma^2 < \frac{(n-1)s^2}{\chi^2(df, 1 - \alpha/2)}$ with $df = n - 1$
Name of Hypothesis Test, H_0	One sample z-test, $H_0: \mu = \mu_0$	One sample t-test, $H_0: \mu = \mu_0$	One sample test of proportion $H_0: p = p_0$	One sample test for Variance $H_0: \sigma^2 = \sigma_0^2$
Test Statistic Formula:	$z^* = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}}$	$t^* = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$ with $df = n - 1$	$z^* = \frac{p' - p_0}{\sqrt{\frac{p_0q_0}{n}}}$	$\chi^{2*} = \frac{(n-1)s^2}{\sigma_0^2}$ with $df = n - 1$
p-value:	$H_a: \mu > \mu_0$, p-value= $P(z \geq z^*)$ $H_a: \mu < \mu_0$, p-value= $P(z \leq z^*)$ $H_a: \mu \neq \mu_0$, p-value= $2 \times P(z \geq z^*)$	$H_a: \mu > \mu_0$, p-value= $P(t(df) \geq t^*)$ $H_a: \mu < \mu_0$, p-value= $P(t(df) \leq t^*)$ $H_a: \mu \neq \mu_0$, p-value= $2 \times P(t(df) \geq t^*)$	$H_a: p > p_0$, p-value= $P(z \geq z^*)$ $H_a: p < p_0$, p-value= $P(z \leq z^*)$ $H_a: p \neq p_0$, p-value= $2 \times P(z \geq z^*)$	$H_a: \sigma^2 > \sigma_0^2$, p-value= $P(\chi^2(df) \geq \chi^{2*})$ $H_a: \sigma^2 < \sigma_0^2$, p-value= $P(\chi^2(df) \leq \chi^{2*})$ $H_a: \sigma^2 \neq \sigma_0^2$, p-value= $2 \times P(\chi^2(df) \geq \chi^{2*})$

Case 2: Two Numerical Variables (Populations)

	Dependent Samples (Paired Samples)	Independent Samples		Two Normal Populations Independent Samples
Parameter of interest:	Mean Difference, $\mu_d = \mu_1 - \mu_2$	Mean Difference, $\mu_1 - \mu_2$	Proportion Difference, $p_1 - p_2$	Ratio of variances, σ_n^2 / σ_d^2
Confidence Interval Formula:	$\bar{d} \pm t(df, \alpha/2) \frac{s_d}{\sqrt{n}}$ with $df = n - 1$ where $d = x_1 - x_2$	$(\bar{x}_1 - \bar{x}_2)$ $\pm t(df, \alpha/2) \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$ with $df = \min(n_1 - 1, n_2 - 1)$	$(p'_1 - p'_2)$ $\pm z(\alpha/2) \sqrt{\frac{p'_1 q'_1}{n_1} + \frac{p'_2 q'_2}{n_2}}$	$\frac{1}{F(df_n, df_d, \alpha/2)} \frac{s_n^2}{s_m^2} < \frac{\sigma_n^2}{\sigma_d^2}$ $< F(df_d, df_n, \alpha/2) \frac{s_n^2}{s_m^2}$ with $df_n = n_{num} - 1$ and $df_d = n_{den} - 1$
Name of Hypothesis Test, H_0	Paired samples t -test, $H_0: \mu_1 = \mu_2$	Two independent samples t -test, $H_0: \mu_1 = \mu_2$	Two sample test of proportion $H_0: p_1 = p_2$	Two sample test for variance $H_0: \sigma_n^2 = \sigma_d^2$
Test Statistic Formula:	$t^* = \frac{\bar{d}}{s_d / \sqrt{n}}$ with $df = n - 1$	$t^* = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$ with $df = \min(n_1 - 1, n_2 - 1)$	$z^* = \frac{p'_1 - p'_2}{\sqrt{p'_p q'_p \left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$ where $p'_p = \frac{x_1 + x_2}{n_1 + n_2}$ and $q'_p = 1 - p'_p$	$F^* = \frac{s_n^2}{s_m^2}$ with $df_n = n_{num} - 1$ and $df_d = n_{den} - 1$
p-value:	$H_a: \mu_1 > \mu_2$, p-value= $P(t(df) \geq t^*)$ $H_a: \mu_1 < \mu_2$, p-value= $P(t(df) \leq t^*)$ $H_a: \mu_1 \neq \mu_2$, p-value= $2 \times P(t(df) \geq t^*)$	$H_a: p_1 > p_2$, p-value= $P(z \geq z^*)$ $H_a: p_1 < p_2$, p-value= $P(z \leq z^*)$ $H_a: p_1 \neq p_2$, p-value= $2 \times P(z \geq z^*)$	$H_a: \sigma_n^2 > \sigma_d^2$, p-value= $P(F(df_n, df_d) \geq F^*)$ $H_a: \sigma_n^2 \neq \sigma_d^2$, p-value= $2 \times P(F(df_n, df_d) \geq F^*)$	

Case 3: More than Two Populations (Multinomial Experiment, Contingency Table, Test of Homogeneity - ANOVA)

	Multinomial Experiment, Contingency Table, Homogeneity		Analysis of Variance (ANOVA)
Parameter of interest:	Probability: p_1, p_2, \dots, p_k	Probability	Mean: $\mu_1, \mu_2, \dots, \mu_c$
H_0	$H_0: p_1 = p_{10}, \dots, p_k = p_{k0}$	H_0 : Independency (Homogeneity)	$H_0: \mu_1 = \mu_2 = \dots = \mu_c$
Test Statistic Formula:	$\chi^{2*} = \sum_{\text{all cells}} \frac{(O - E)^2}{E}$		$F^* = \frac{\text{MS(factor)}}{\text{MS(error)}} = \frac{\text{SS(factor)}/\text{df(factor)}}{\text{SS(error)}/\text{df(error)}}$
df and other items	$df = k - 1$ $E_i = n \times p_{i0}$	$df = (r - 1)(c - 1)$ $E_{ij} = \frac{R_i \times C_j}{n}$	$\text{df(factor)} = c - 1, \text{df(error)} = n - c$ $\text{SS(factor)} = \left(\frac{C_1^2}{k_1} + \frac{C_2^2}{k_2} + \dots + \frac{C_c^2}{k_c} \right) - \frac{(\sum x)^2}{n}$ $\text{SS(error)} = \sum (x^2) - \left(\frac{C_1^2}{k_1} + \frac{C_2^2}{k_2} + \dots + \frac{C_c^2}{k_c} \right)$
p-value:	p-value= $P(\chi^2(df) \geq \chi^{2*})$		p-value= $P(F(df_n, df_d) \geq F^*)$