

5.12 Increase sample size by four times.

$$5.13 \quad \hat{\sigma} = 13, E = 3, \alpha = 0.01 \Rightarrow n = \frac{(2.58)^2 (13)^2}{(3)^2} = 124.99 \Rightarrow n = 125$$

5.16

a.  $z = \frac{25.9 - 26}{7.6/\sqrt{50}} = -0.09 \geq -1.645 = z_{0.05}$  Because the observed value of  $\bar{y}$  lies less than 1.645 ( $\alpha = 0.05$ ) standard deviations below the hypothesized mean of 26, we fail to reject  $H_0$  and conclude that there is not significant evidence that the mean is less than 26.

$$b. \quad \beta(24) = P\left(z \leq 1.645 - \frac{|24 - 26|}{7.6/\sqrt{50}}\right) = P(z \leq -0.22) = 0.4129$$

$$c. \quad \beta(24) = P\left(z \leq 1.645 - \frac{|24 - 26|}{7.6/\sqrt{100}}\right) = P(z \leq -0.99) = 0.1611$$

5.21  $H_0 : \mu \leq 2$  vs  $H_a : \mu > 2$ ,  $\bar{y} = 2.17$ ,  $s = 1.05$ ,  $n = 90$

a.  $z = \frac{2.17 - 2}{1.05/\sqrt{90}} = 1.54 < 1.645 = z_{0.05} \Rightarrow$  fail to reject  $H_0$ . The data does not support the hypothesis that the mean has been decreased from 2.

$$b. \quad \beta(2.1) = P\left(z \leq 1.645 - \frac{|2 - 2.1|}{1.05/\sqrt{90}}\right) = P(z \leq 0.74) = 0.7704$$

$$5.24 \quad n = \frac{(80)^2 (1.645 + 1.96)^2}{(525 - 550)^2} = 133.08 \Rightarrow n = 134$$

5.26  $H_0 : \mu \geq 16$  vs  $H_a : \mu < 16$

$\alpha = 0.05$ ,  $\beta = 0.10$ , whenever  $\mu \leq 12$ ,  $\sigma = 7.64$

$$z_{0.05} = 1.645, z_{0.10} = 1.28, n = \frac{(7.64)^2 (1.645 + 1.28)^2}{(12 - 16)^2} = 31.2 \Rightarrow n = 32$$

$$5.29 \quad p\text{-value} = P(z \leq -1.08) = 0.1401 > 0.10 = \alpha$$

No, there is still not significant evidence that the mean is less than 35 at the 0.10 level.

5.30 In testing  $H_0 : \mu = 21.7$  versus  $H_a : \mu \neq 21.7$ ,

$$p\text{-value} = 2P\left(z \geq \frac{|18.8 - 21.7|}{15.3/\sqrt{90}}\right) = 2P(z \geq 1.80) = 2(0.0359) = 0.0719 > 0.05 = \alpha$$

There is not significant evidence that the mean number of Type 2 fibers is different from 21.7.