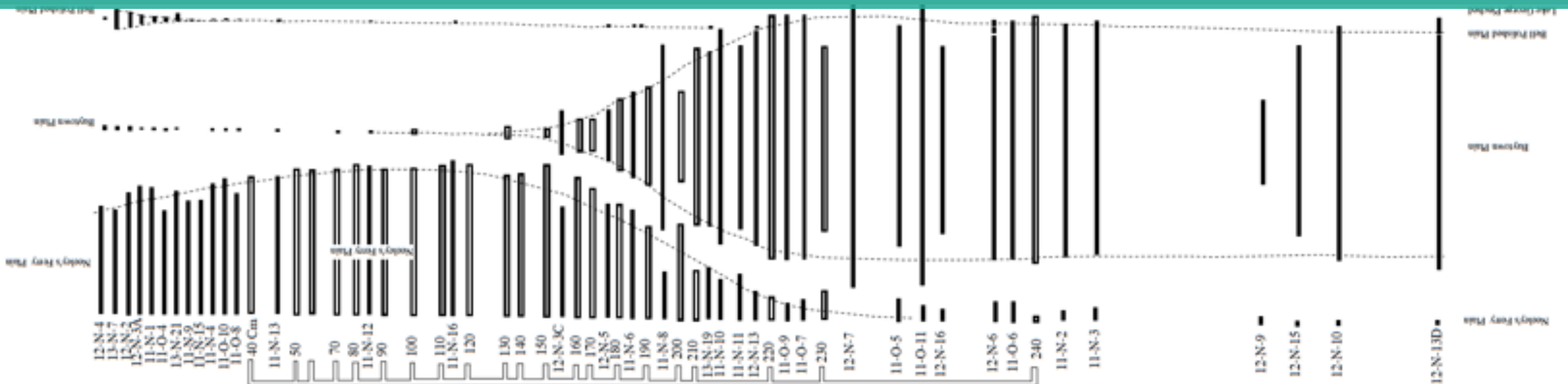




UNIVERSITY of WASHINGTON

BINGHAMTON  
UNIVERSITY

The State University of New York



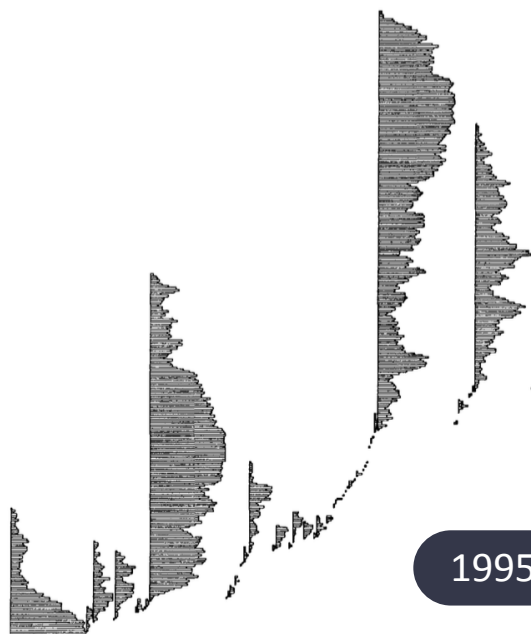
# Frequency Seriation and Unimodality

30s - 40s

Ford and Krieger

Historical types are constructed  
and tested for chronological  
significance

Unimodality served as a “signature”  
for chronologically useful types



1995

Neiman and others

Unimodality is an outcome of  
cultural transmission, but one kind of  
pattern — albeit a useful one!

1916

TABLE 5.  
PERCENTAGES.

Period	Site	Corrugated	Three Colors	Black on Red	Any Red	“Black” ware
PRESENT	Zufi	0 <sup>a</sup>	0	1		
LATE A	Towwayallanna	1	8	3		
	Kolliwa	—	7	2		
	Shunntekkya	2	7	2		
	Wimmayawa	2	4	1	22 <sup>b</sup>	53 <sup>b</sup>
	Mattsakya	3	4	3		
EARLY A	Kyakkima	4	3	2		
	Pinnawa	10	1	8		
	Site W	24	—	1		
LATE B	Hattsinawa	27	—	5	10	19
	Kyakkima West	12 <sup>c</sup>	—	4	8	— <sup>c</sup>
MIDDLE B	Shoptlawwayala	40	—	2	3	7
	“Hawwikku B”	49	—	6	12	9
EARLY B	Te'allatashshanna	66	—	—	—	5
	Site X	71	—	—	3	1
	Tetlnatluwayala	72	—	—	2	—
? — B	He'i'tli'annanna	—	—	—	—	3
	Site Y	—	—	—	—	—

<sup>a</sup> Present, but less than half of one percent.  
<sup>b</sup> The variation between sites here lumped seems due more to accident or selection in collecting than to differences typical of period.  
<sup>c</sup> Unfortunately only 25 pieces are available from this site.



Kroeber

Stylistic types change  
according to “normal  
curves” and the popularity  
principle

Lipo, Madsen, and Dunnell

2015



OPEN ACCESS

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RESEARCH ARTICLE

## A Theoretically-Sufficient and Computationally-Practical Technique for Deterministic Frequency Seriation

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# Distance Minimization in Seriation

**Method:** arrange assemblages by minimizing pairwise inter-assemblage distance according to some distance metric, forming a graph by agglomeration of assemblages by edges, without enforcing linearity

1

## Global criterion

Unimodality was sufficient and convenient, but not necessary, and restricted seriations to a subset of the total variation. It was essential prior to good computing support, but is **optional** today.

2

## Theoretically sound

CT models are generally AR(1) processes and Markov chains. Large jumps are possible but rare, spatiotemporal smoothness in frequencies is the rule, not the exception. Assemblages closer together in space and time will tend to have **smaller** pairwise distance metrics

3

## Builds on existing work

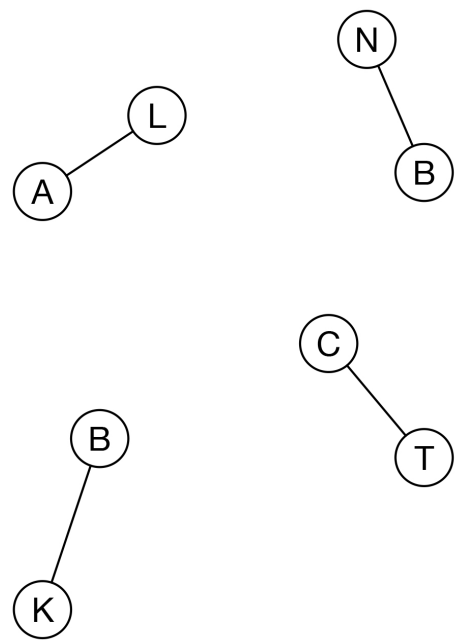
Kadane (1971) and Shepherdson (2006) examined total path length approaches, but with the requirement of a single linear solution, treating departures as error rather than information

4

## Full spatiotemporal order

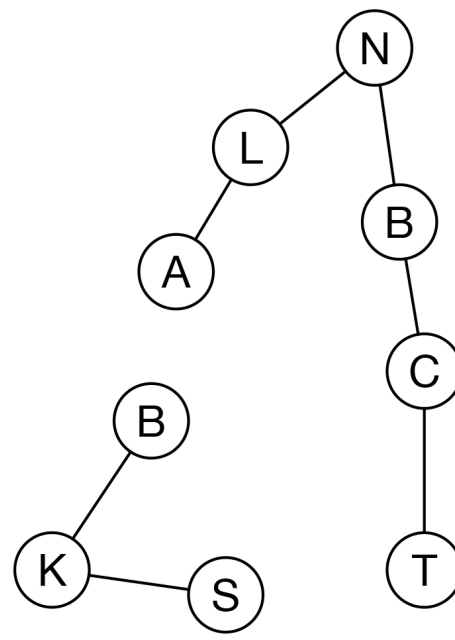
By finding the network with minimum total path distance, whether linear or not, we allow **spatial variation** in trait evolution into the solution along with **temporal ordering**.

# “Continuity” seriation: exact distance minimization



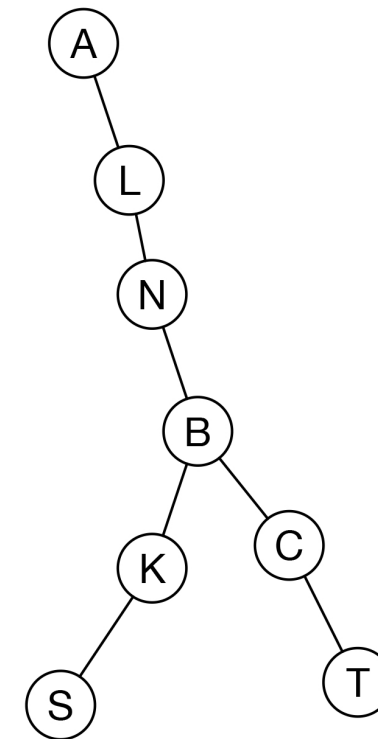
Find shortest pairwise distances

Distance can be any metric, but we began with Euclidean distance (L2 norm)



Iteratively add vertices by distance

Keep all partial solutions because each may measure change in a different region or direction over time



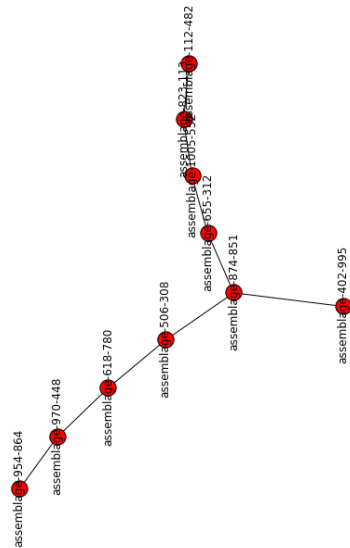
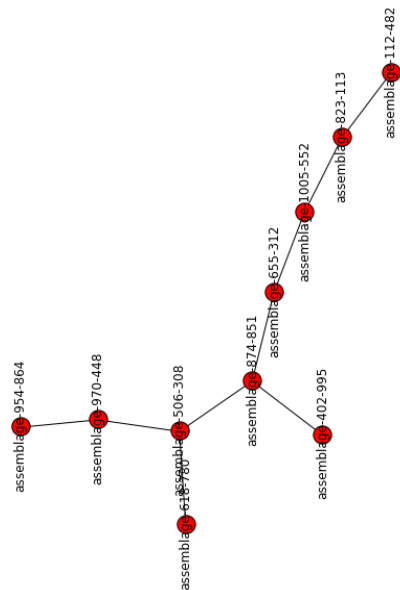
Coalesce partial solutions

Overlay partial solutions using overlapping vertices to form seriation networks. Linear orders still occur, but spatial variation or other mesoscale structure induces tree structure

# Comparing Frequency and Continuity Seriation

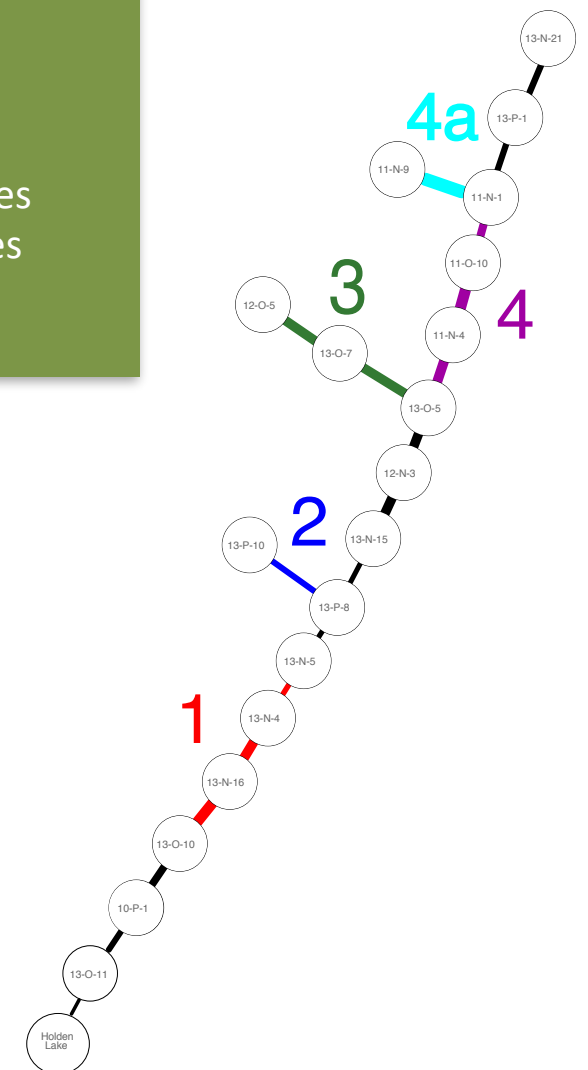
Simulated cultural transmission in a fully spatiotemporal network of communities, with time averaging and typical sampling and filtering techniques.

Frequency (unimodal) and continuity (exact distance minimization) give identical results in most cases, and differ in specific assignments when there are disagreements, given that small differences in directionality vs. distance determine the order.



## Empirical

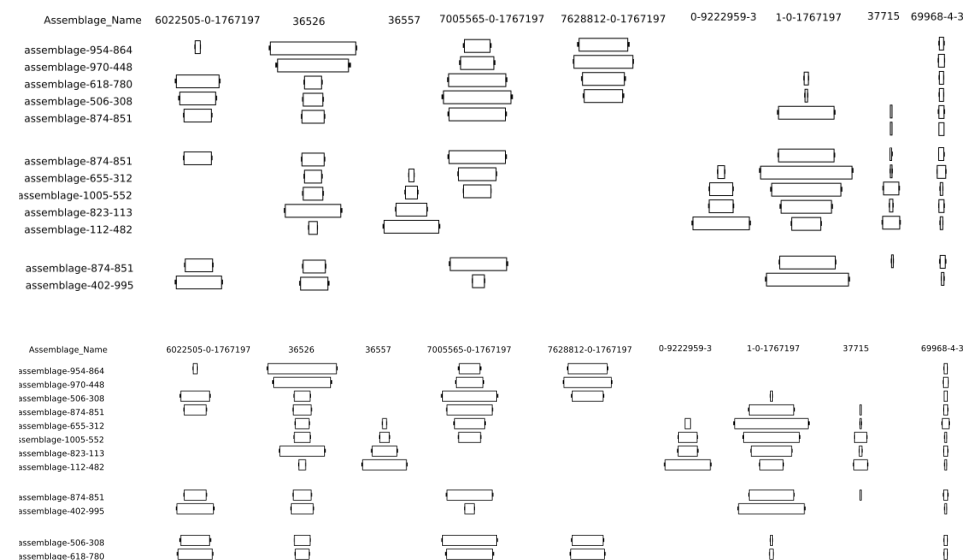
Phillips et al. 1951  
pottery assemblages  
show no differences  
between methods



## Simulation

Continuity (left) and Frequency (right) are identical other than the placement of one community, which forms a separate solution in continuity.

Bar charts: freq (top) & continuity (bottom)



# Why do we need better seriation methods?

1

## Global criterion

Unimodality was sufficient and convenient, but not necessary, and restricted seriations to a subset of the total variation. We should be able to apply seriation to any cultural transmission problem, whether unimodal types can be found or not.

2

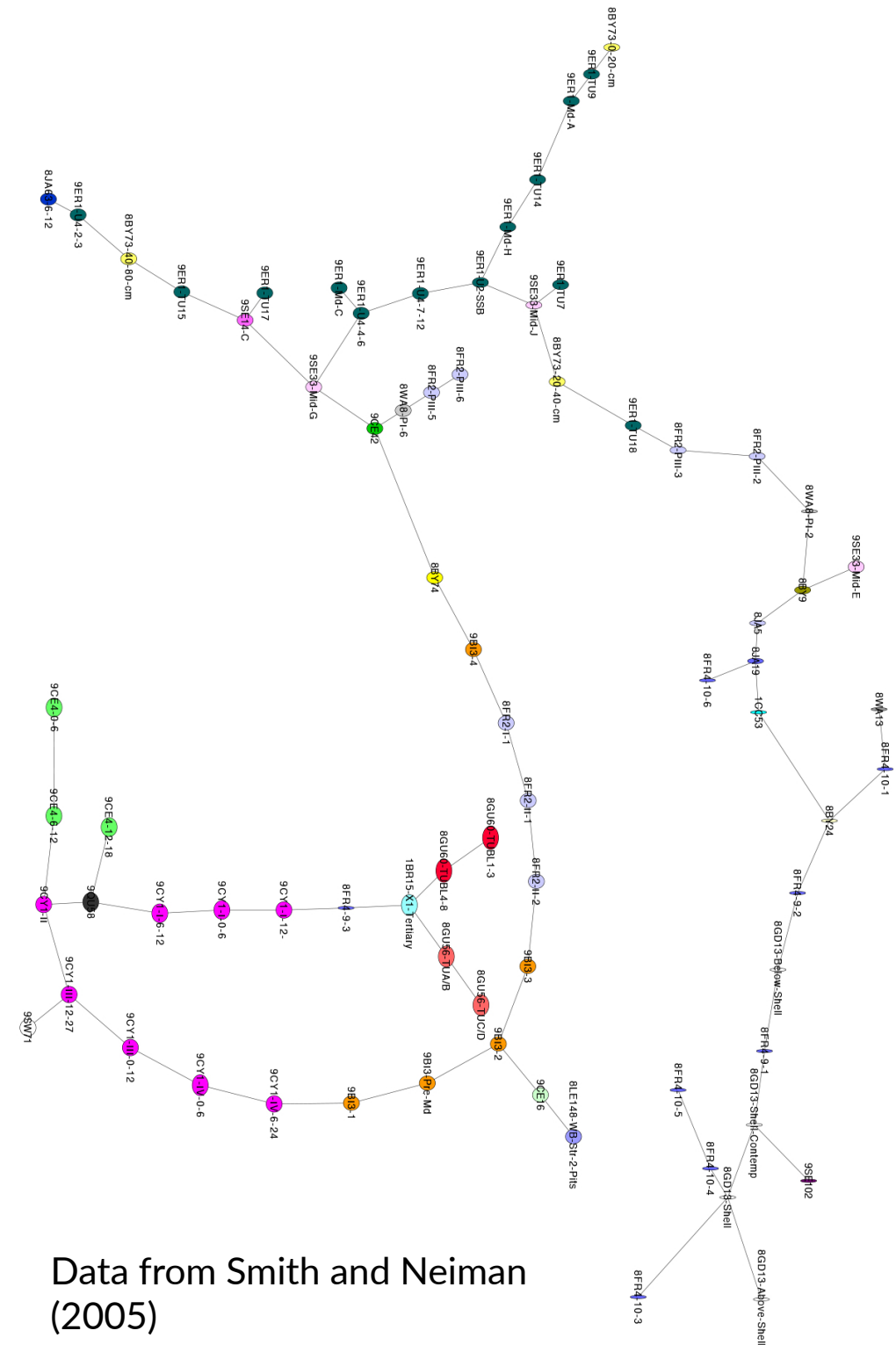
## Targets mesoscale problems

Cladistics tends to operate at particular scales given presence/absence of synapomorphic traits. Little work on polymorphic populations has been done, while polymorphism is key to understanding mesoscale, rather than macroscale, evolution.

3

## Performance and scalability

Even with advances in technique in our 2015 paper, frequency seriation of large datasets is hard. Exact distance minimization as shown here performed 26x faster than unimodality analysis, while using 1/4th of the CPU count, for an effective speedup of 104x. This allows us to seriate large datasets and attack contemporary, not just archaeological, data.



Data from Smith and Neiman (2005)



# Thank You!

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