

To Professor Professor Nicola Bellomo and Professor Franco Brezzi
Managing Editors of Mathematical Models and Methods in Applied
Sciences



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Numerische Analysis

Object: Submission of the paper “Inferring Interaction Rules from
Observations of Evolutive Systems I: The Variational Approach”

Dear Professor Bellomo and Professor Brezzi,

with this letter and on behalf of my coauthors, I wish to submit the paper

“Inferring Interaction Rules from Observations of Evolutive Systems I:
The Variational Approach”

a joint work with Mattia Bongini, Markus Hansen, and Mauro Maggioni,
for publication on Mathematical Models and Methods in Applied
Sciences.

Let me briefly describe the main content of the paper. We are concerned
with the learnability of nonlocal interaction kernels for first order systems
modeling certain social interactions, from observations of realizations of
their dynamics. This paper is the first of a series on learnability of
nonlocal interaction kernels and presents a variational approach to the
problem. In particular, we assume here that the kernel to be learned is
bounded and locally Lipschitz continuous and that the initial conditions of
the systems are drawn identically and independently at random
according to a given initial probability distribution. Then the minimization
over a rather arbitrary sequence of (finite dimensional) subspaces of a
least square functional measuring the discrepancy from observed
trajectories produces uniform approximations to the kernel on compact
sets. The convergence result is obtained by combining mean-field limits,
transport methods, and a Gamma-convergence argument. A crucial
condition for the learnability is a certain coercivity property of the least
square functional, majoring an energy-norm discrepancy to the kernel
with respect to a probability measure, depending on the given initial
probability distribution by suitable push forwards and transport maps.
We illustrate the convergence result by means of several numerical
experiments.

As this paper addresses a very relevant learning problem, combining
several tools from approximation theory, dynamical systems, mean-field
equations, measure theory, and variational methods, we consider
Mathematical Models and Methods in Applied Sciences a very suitable
journal for a potential publication.

Sincerely yours

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