

# Statistical Natural Language Processing

Lecture 11: Lexical Semantics

**Dr. Momtazi** Amirkabir University of Technology Lexical Semantics WordNet

2 Word Sense Disambiguation

Word Similarity

Lexical Semantics WordNet

2 Word Sense Disambiguation

Word Similarity

 Considering the meaning(s) of a word in addition to its written form



- Word Sense
  - A discrete representation of an aspect of the meaning of a word

- Lexeme
  - An entry in a lexicon consisting of a pair:
     a form with a single meaning representation
    - Camel (animal)
    - Camel (music band)

- Lemma
  - The grammatical form that is used to represent a lexeme
    - Camel

# **Homonymy**

6

Words which have similar form but different meanings

- Camel (animal)
- Camel (music band)



- Write
- Right



- /
- Realizing lexical relations among words' senses
  - □ Hyponymy (is a) {parent: hypernym, child: hyponym }
    - dog & animal



- 8
- Realizing lexical relations among words' senses
  - Meronymy (part of)
    - arm & body



- Realizing lexical relations among words' senses
  - Synonymy
    - fall & autumn

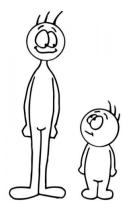


# **Semantics Relations**

- Realizing lexical relations among words' senses
  - Antonymy

10

• tall & short



# **Outline**

11

 Lexical Semantics WordNet

2 Word Sense Disambiguation

3 Word Similarity

- A hierarchical database of lexical relations
- Three Separate sub-databases
  - Nouns
  - Verbs
  - Adjectives and Adverbs
- Closed class words are not included
- Each word is annotated with a set of senses
- Available online
  - □ http://wordnetweb.princeton.edu/perl/webwn

### Number of words in WordNet 3.0

Category	Entry
Noun	117,097
Verb	11,488
Adjective	22,141
Adverb	4,061

Average number of senses in WordNet 3.0

Category	Sense
Noun	1.23
Verb	2.16

### Synset (synonym set)

- S: (n set, circle, band, lot an unofficial association of people or groups) "the smart set goes there; they were an angry lot"
- S: (n) band (instrumentalists not including string players)
- S: (n) band, banding, stria, striation (a stripe or stripes of contrasting color)
   "chromosomes exhibit characteristic bands"; "the black and yellow banding of bees
- <u>S.</u> (n) band, <u>banding</u>, <u>stripe</u> (an adornment consisting of a strip of a contrasting color
- or material)

  S: (n) dance band, band, dance orchestra (a group of musicians playing popular
  - music for dancing)
- S: (n) band (a range of frequencies between two limits)
- S: (n) band (a thin flat strip of flexible material that is worn around the body or one of the limbs (especially to decorate the body))
- S: (n) isthmus, band (a cord-like tissue connecting two larger parts of an anatomical
- S: (n) ring, band (jewelry consisting of a circlet of precious metal (often set with jewels) worn on the finger) "she had rings on every finger": "he noted that she wore
- jewels) worn on the finger) "she had rings on every finger"; "he noted that she wore a wedding band"
- S: (n) band (a driving belt in machinery)
- S: (n) band (a thin flat strip or loop of flexible material that goes around or over something else, typically to hold it together or as a decoration)
- S: (n) band, ring (a strip of material attached to the leg of a bird to identify it (as in studies of bird migration))
- S: (n) band (a restraint put around something to hold it together)

#### Verb

and wasps"

- S: (v) band (bind or tie together, as with a band)
- S: (v) ring, band (attach a ring to the foot of, in order to identify) "ring birds"; "band the

# Word Relations (Hypernym)

- S: (n) ring, band (jewelry consisting of a circlet of precious metal (often set with jewels) wom on the finger) "she had rings on every finger"; "he noted that she wore a wedding band"
  - direct hyponym / full hyponym
  - direct hypernym I inherited hypernym I sister term
    - S: (n) jewelry, jewellery (an adomment (as a bracelet or ring or necklace) made of precious metals and set with gems (or imitation gems))
      - S: (n) adornment (a decoration of color or interest that is added to relieve plainness)
        - S: (n) decoration, omament, ornamentation (something used to beautify)
          - S: (n) artifact, artefact (a man-made object taken as a whole)
            - S: (n) whole, unit (an assemblage of parts that is regarded as a single entity) "how big is that part compared to the whole?": "the team is a unit"
              - S: (n) object, physical object (a tangible and visible entity; an entity that can cast a shadow) "it was full of rackets, balls and other objects"
                - S: (n) physical entity (an entity that has physical existence)
                  - S: (n) entity (that which is perceived or known or inferred to have its own distinct existence (living or nonliving))

# Word Relations (Sister)

- S: (n) set, circle, band, lot (an unofficial association of people or groups) "the smart set goes there"; "they were an angry lot"
  - · direct hyponym / full hyponym
  - direct hypernym I inherited hypernym I sister term
    - S: (n) social group (people sharing some social relation)
      - S: (n) body (a group of persons associated by some common tie or occupation and regarded as an entity) "the whole body filed out of the auditorium": "the student body": "administrative body"
      - S: (n) society (an extended social group having a distinctive cultural and economic organization)
      - S: (n) minority (a group of people who differ racially or politically from a larger group of which it is a part)
      - S: (n) sector (a social group that forms part of the society or the
        - economy) "the public sector"
      - S: (n) <u>Interest, interest group</u> ((usually plural) a social group whose members control some field of activity and who have common aims) "the iron interests stepped up production"
      - S: (n) kin, kin group, kinship group, kindred, clan, tribe (group of people related by blood or marriage)
      - S: (n) kith (your friends and acquaintances) "all his kith and kin"
         S: (n) fringe (a social group holding marginal or extreme views)
      - "members of the fringe believe we should be armed with guns at all times"
      - S: (n) gathering, assemblage (a group of persons together in one place)
      - S: (n) congregation, fold, faithful (a group of people who adhere to a common faith and habitually attend a given church)
      - S: (n) organization, organisation (a group of people who work together)
      - S: (n) phylum ((linguistics) a large group of languages that are historically related)
      - S: (n) force (a group of people having the power of effective action)
         "he joined forces with a band of adventurers"
      - S: (n) platoon (a group of persons who are engaged in a common activity) "platoons of tourists poured out of the busses"; "the
      - activity) "platoons of tourists poured out of the busses"; "the defensive platoon of the football team"

        S:(n) revolving door (an organization or institution with a high rate
      - of tumover of personnel or membership)

        Si (n) set, circle, band, lot (an unofficial association of people or
      - groups) "the smart set goes there"; "they were an angry lot"
      - S: (n) organized crime, gangland, gangdom (underworld organizations)
      - S: (n) subculture (a social group within a national culture that has distinctive patterns of behavior and beliefs).

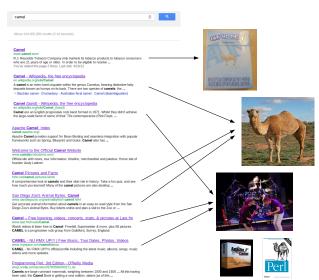
Lexical Semantics WordNet

2 Word Sense Disambiguation

3 Word Similarity

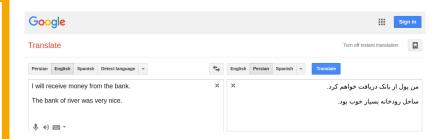
- Information retrieval
- Machine translation
- Speech recognition

## Information Retrieval



Momtazi | SNLP

20



- You have to process it write.
- You have to process it right.

22

- Input
  - A word
  - The context of the word
  - Set of potential senses for the word

- Output
  - The best sense of the word for this context

# **Example**

### Sense: band 532736 Music N

The band made copious recordings now regarded as classic from 1941 to 1950. These were to have a tremendous influence on the worldwide jazz revival to come During the war Lu led a 20 piece navy band in Hawaii.



# **Example**

### Sense: band 532838 Rubber-band N

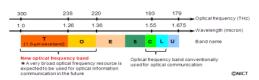
He had assumed that so famous and distinguished a professor would have been given the best possible medical attention it was the sort of assumption young men make. Here suspended from Lewis's person were pieces of tubing held on by rubber bands an old wooden peg a bit of cork.



# **Example**

### Sense: band 532734 Range N

There would be equal access to all currencies financial instruments and financial services dash and no major constitutional change. As realignments become more rare and exchange rates waver in narrower bands the system could evolve into one of fixed exchange rates.



- Thesaurus-based
- Supervised learning
- Semi-supervised learning

- Extracting sense definitions from existing sources
  - Dictionaries
  - Thesauri
  - Wikipedia





### Thesaurus-based



#### Band

From Wikipedia, the free encyclopedia

#### Band may refer to:

#### Clothing, jewelry, and accessories

- Bands (neckwear), two pieces of cloth fitted around the neck as part of formal clothing for clergy, academics, and lawyers
   Bandolier or bandoleer, an ammunition belt
- Belt (clothing)
- Wedding ring or wedding band
- · Strap, an elongated flap or ribbon, usually of fabric or leather

#### Science and technology

- · Band (radio), a range of frequencies or wavelengths used in radio transmission and radar
- Rubber band, a short length of rubber and latex formed in the shape of a loop
   Möbius strip or Möbius band, an artifact with interesting topological features
- Band (mathematics), an idempotent semigroup
- Spectral bands, part of the optical spectra of polyatomic systems
- Metals and semiconductors
  - Valence band
  - Conduction ban
     Band gap

#### Medicine and biology

- Bird ringing, or bird banding, placing a numbered bands of metal on birds' legs for identification
   A group of animals, such as parillas or covotes
- Herd
- Flocking (behavior)
- Band cell, a type of white blood cell
   Protein band, see Coomassie
- · Gastric band, a weight-control measure

#### Organizations

- Bands (Ralian Army irregulars), military units once in the service of the Italian Regio Esercito
- Brazilian broadcast television network Rede Bandeirantes, nicknamed Band or Band Network
   The Rand (wrestling), the Total Norston Westling name for the professional wrestling stable New World Order

#### Society and government

- Band society, a small group of humans in a simple form of society
- The primary unit of Native Americans in the United States
   Band (First Nations Canada), the primary unit of First Nations Government in Canada

#### People

#### Band (surname)

#### Places

Band, Mureş in Romania
 Bánd, a village in Hungary

#### Music

Band, a company of musicians—see Musical ensemble

Rock band

#### Rubber band

From Wikipedia, the free encyclopedia

This article is about the common household item. For other meanings, see Rubber band (disambiguation).

\*Elastic band\* redirects here. For the band and orchestra, see The Elastic Band. For the first aid bandage, see elastic bandage.

A rubber band (in some regions known as a binder, an elastic or elastic band, a lackey band, laggy band, lacka band or gumband) is a short length of rubber and latex formed in the shape

of a loop and is commonly used to hold multiple objects together. The rubber band was patented in England on March 17, 1845 by Stephen Perry [18283]

### Contents [hide] 1 Manufacturing

- 2 Material 3 Rubber band sizes
- 3.1 Measuring
- 3.1 Measuring 3.2 Rubber band size numbers
- 4 Thermodynamics 5 Red rubber bands
- 6 Ranger bands 7 Elastration
- 8 Model use
- 9 See also 10 References 11 External links



Rubber bands in different colors and sizes.

# The Lesk Algorithm

 Selecting the sense whose definition shares the most words with the word's context

### Simplified Algorithm [Kilgarriff and Rosenzweig, 2000]

```
function SIMPLIFIED LESK(word,sentence) returns best sense of word
best-sense <- most frequent sense for word
max-overlap <- 0
context <- set of words in sentence
for each sense in senses of word do
signature <- set of words in the gloss and examples of sense
overlap <- COMPUTEOVERLAP (signature,context)
if overlap > max-overlap then
max-overlap <- overlap
best-sense <- sense
end return (best-sense)
```

30

- Simple to implement
- No training data needed
- Relatively bad results

Training data:

A corpus in which each occurrence of the ambiguous word w is annotated by its correct sense

□ SemCor: 234,000 sense-tagged from Brown corpus

□ SENSEVAL-1: 34 target words

□ SENSEVAL-2: 73 target words

□ SENSEVAL-3: 57 target words (2081 sense-tagged)

- Using the words in the context with a specific window size
  - Collocation
    - Considering all words in a window (as well as their POS) and their position
  - Bag-of-word
    - Considering the frequent words regardless their position
    - Deriving a set of k most frequent words in the window from the training corpus
    - Representing each word in the data as a k-dimention vector
    - Finding the frequency of the selected words in the context of the current observation

### Sense: band 532734 Range N

There would be equal access to all currencies financial instruments and financial services dash and no major constitutional change. As realignments become more rare and exchange rates waver in narrower bands the system could evolve into one of fixed exchange rates.

- Window size: +/- 3
- Context: waver in narrower bands the system could  $\{W_{n-3}, P_{n-3}, W_{n-2}, P_{n-2}, W_{n-1}, P_{n-1}, W_{n+1}, P_{n+1}, W_{n+2}, P_{n+2}, W_{n+3}, P_{n+3}\}$  {waver, NN, in , IN , narrower, JJ, the, DT, system, NN , could, MD}

### Sense: band 532734 Range N

There would be equal access to all currencies financial instruments and financial services dash and no major constitutional change. As realignments become more rare and exchange rates waver in narrower bands the system could evolve into one of fixed exchange rates.

- Window size: +/- 3
- Context: waver in narrower bands the system could
- k frequent words for band: {circle, dance, group, jewelery, music, narrow, ring, rubber, wave} { 0 , 0 , 0 , 0 , 0 , 1 , 0 , 0 , 1 }

35

• Choosing the best sense  $\hat{s}$  out of all possible senses  $s_i$  for a feature vector  $\vec{f}$  of the word w

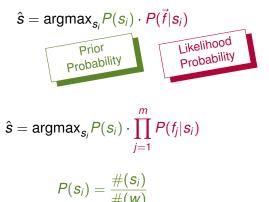
$$\hat{s} = \operatorname{argmax}_{s_i} P(s_i | \vec{f})$$

$$\hat{s} = \operatorname{argmax}_{s_i} \frac{P(\vec{f}|s_i) \cdot P(s_i)}{P(\vec{f})}$$

 $P(\vec{f})$  has no effect

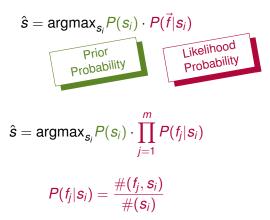
$$\hat{s} = \operatorname{argmax}_{s_i} P(\vec{f}|s_i) \cdot P(s_i)$$

# Naïve Bayes Classification



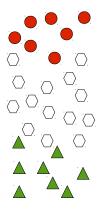
 $\#(s_i)$ : number of times the sense  $s_i$  is used for the word w in the training data #(w): the total number of samples for the word w

## Naïve Bayes Classification



 $\#(f_j, s_i)$ : the number of times the feature  $f_j$  occurred for the sense  $s_i$  of word w  $\#(s_i)$ : the total number of samples of w with the sense  $s_i$  in the training data

What is the best approach when we do not have enough data to train a model?



- A small amount of labeled data
- A large amount of unlabeled data
- Solution
  - Finding the similarity between the labeled and unlabeled data
  - □ Predicting the labels of the unlabeled data

■ For each sense,

- □ Select the most important word which frequently co-occurs with the target word only for this particular sense
- Example for Band

| sense  | selected word |
|--------|---------------|
| Music  | play          |
| Rubber | elastic       |
| Range  | spectrum      |

- For each sense,
  - □ Find the sentences from unlabeled data which contain the target word and the selected word

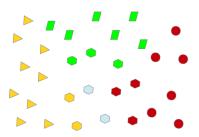
The band spectrum is the combination of many different spectral lines

For example the Jamaican reggae musician Bob Marley and his band The Wailers were known to play the concerts ....

A rubber band, also known as a binder, elastic band, lackey band, laggy band, "gum band", or elastic, is a short length of rubber and latex, elastic in nature and formed ...

For each sense,

- Label the sentence with the corresponding sense
- Add the new labeled sentences to the training data



## **Outline**

43

Lexical Semantics WordNet

2 Word Sense Disambiguation

Word Similarity

- Task
  - Finding the similarity between two words
  - Covering somewhat a wider range of relations in the meaning (different with synonymy)
  - □ Being defined with a score (degree of similarity)

## Example

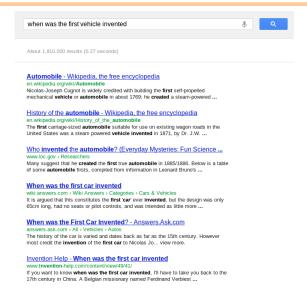
Bank (financial institute) & fund 0.8

car & bicycle 0.5

car & gasoline 0.2

- Information retrieval
- Question answering
- Document categorization
- Machine translation
- Language modeling
- Word clustering

# Information retrieval & Question Answering



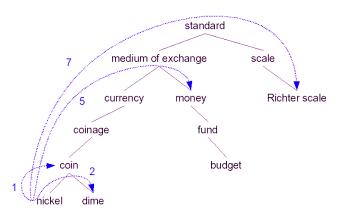
## **Language Modeling**

- Class-based models
  - "to London", "to Berlin", "to Tehran"
    - Class: CITY-NAME
  - □ ...
- Classes: AIRLINE, DAY-OF-WEEK, MONTH, etc.

- Thesaurus-based
  - Based on their distance in thesaurus
  - □ Based on their definition in thesaurus (gloss)

- Distributional
  - Based on the similarity between their contexts

■ Two concepts (sense) are similar if they are "nearby" (if there is a short path between them in the hypernym hierarchy)



# Path-base Similarity

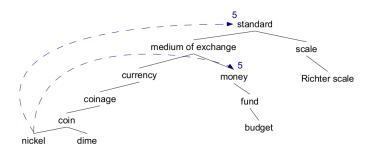
■  $pathlen(c_1, c_2) = 1 + number of edges in the shortest path between the sense nodes <math>c_1$  and  $c_2$ 

$$sim_{path}(c_1, c_2) = -\log pathlen(c_1, c_2)$$

 $wordsim(w_1, w_2) = \max_{\substack{c_1 \in senses(w_1) \\ c_2 \in senses(w_2)}} sim(c_1, c_2)$ 

when we have no knowledge about the exact sense (which is the case when processing general text)

- Shortcoming
  - Assumes that each link represents a uniform distance
    - Nickel to money seems closer than to standard



- Shortcoming
  - Assumes that each link represents a uniform distance
    - Nickel to money seems closer than to standard
  - Solution
    - Using a metric which represents the cost of each edge independently
      - ⇒ Words connected only through abstract nodes are less similar

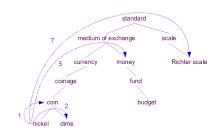
## Information Content Similarity

- Assigning a probability P(c) to each node of thesaurus
  - $\Box$  P(c) is the probability that a randomly selected word in a corpus is an instance of concept c
    - $\Rightarrow$  P(root) = 1, since all words are subsumed by the root concept
  - The probability is trained by counting the words in a corpus
  - □ The lower a concept in the hierarchy, the lower its probability

$$P(c) = \frac{\sum_{w \in words(c)} \# w}{N}$$

words(c) is the set of words subsumed by concept c N is the total number of words in the corpus that are available in thesaurus

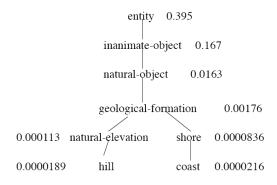
# **Information Content Similarity**

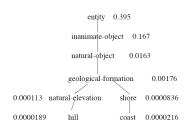


```
words(coin) = {nickel, dime}
words(coinage) = {nickel, dime, coin}
words(money) = {budget, fund}
```

words(medium of exchange) = {nickel, dime, coin, coinage, currency, budget, fund, money}

 Augmenting each concept in the WordNet hierarchy with a probability P(c)





Information Content:

$$IC(c) = -\log P(c)$$

Lowest common subsumer:

LCS(c1, c2) = the lowest node in the hierarchy that subsumes both  $c_1$  and  $c_2$ 

- Resnik similarity
  - Measuring the common amount of information by the information content of the lowest common subsumer of the two concepts

$$sim_{resnik}(c_1, c_2) = -\log P(LCS(c_1, c_2))$$

$$sim_{resnik}(hill,coast) = -\log P(geological-formation)$$

# **Information Content Similarity**

- Lin similarity
  - Measuring the difference between two concepts in addition to their commonality

$$sim_{Lin}(c_1, c_2) = \frac{2 \log P(LCS(c_1, c_2))}{\log P(c_1) + \log P(c_2)}$$

$$sim_{Lin}(hill, coast) = \frac{2 \log P(geological-formation)}{\log P(hill) + P(coast)}$$

Jiang-Conrath similarity

$$sim_{JC}(c_1, c_2) = \frac{1}{2 \log P(LCS(c_1, c_2)) - (\log P(c_1) + \log P(c_2))}$$

$$\textit{sim}_{\textit{JC}}(\textit{hill}, \textit{coast}) = \frac{1}{2 \log \textit{P}(\textit{geological-formation}) - (\log \textit{P}(\textit{hill}) + \log \textit{P}(\textit{coast}))}$$

- Looking at word definitions in thesaurus (gloss)
- Measuring the similarity base on the number of common words in their definition
- Adding a score of  $n^2$  for each n-word phrase that occurs in both glosses
- Computing overlap for other relations as well (gloss of hypernyms and hyponyms)

$$sim_{eLesk} = \sum_{r, q \in RELS} overlap(gloss(r(c_1)), gloss(q(c_2)))$$

- Computing overlap for other relations as well (gloss of hypernyms and hyponyms)
- Example:

$$\begin{split} sim_{eLesk} &= \sum_{r,q \in RELS} \mathsf{overlap}(gloss(r(c_1)), gloss(q(c_2))) \\ &= \mathsf{overlap}(gloss(c_1), gloss(c_2)) \\ &+ \mathsf{overlap}(gloss(Hypo(c_1)), gloss(Hypo(c_2))) \\ &+ \mathsf{overlap}(gloss(Hypo(c_1)), gloss(c_2)) \\ &+ \mathsf{overlap}(gloss(c_1), gloss(Hypo(c_2))) \end{split}$$

## **Extended Lesk**

## Drawing paper

paper that is specially prepared for use in drafting

#### Decal

the art of transferring designs from specially prepared paper to a wood or glass or metal surface

common phrases: specially prepared and paper

$$sim_{el \ esk} = 1 + 2^2 = 1 + 4 = 5$$

Overview

```
\begin{split} & \text{sim}_{\text{path}}(c_1, c_2) &= -\log \text{pathlen}(c_1, c_2) \\ & \text{sim}_{\text{Resnik}}(c_1, c_2) &= -\log P(\text{LCS}(c_1, c_2)) \\ & \text{sim}_{\text{Lin}}(c_1, c_2) &= \frac{2 \times \log P(\text{LCS}(c_1, c_2))}{\log P(c_1) + \log P(c_2)} \\ & \text{sim}_{\mathbf{jc}}(c_1, c_2) &= \frac{1}{2 \times \log P(\text{LCS}(c_1, c_2)) - (\log P(c_1) + \log P(c_2))} \\ & \text{sim}_{\text{eLesk}}(c_1, c_2) &= \sum_{r, q \in \text{RELS}} \text{overlap}(\text{gloss}(r(c_1)), \text{gloss}(q(c_2))) \end{split}
```

WordNet::Similarity

Source:

http://wn-similarity.sourceforge.net/

Web-based interface:

http://marimba.d.umn.edu/cgi-bin/similarity/
similarity.cgi

- Shortcomings
  - Many words are missing in thesaurus
  - Only use hyponym info
    - Might useful for nouns, but weak for adjectives, adverbs, and verbs
  - Many languages have no thesaurus
- Alternative
  - Using distributional methods for word similarity

- Using context information to find the similarity between words
- Guessing the meaning of a word based on its context

## ABC?

## ABC?

A plate full of *ABC* is on the table Everybody likes *ABC ABC* is cooked within 30 minutes We make *ABC* with potato

⇒ A kind of food

## **Context Representations**

- Considering a target term t
  - Building a vocabulary of M words ( $\{w_1, w_2, w_3, ..., w_M\}$ )
  - Creating a vector for t with M features ( $t = \{f_1, f_2, f_3, ..., f_M\}$ )
    - $\Box$   $f_i$  means the number of times the word  $w_i$  occurs in the context of t

## ABC?

A plate full of *ABC* is on the table Everybody likes *ABC ABC* is cooked within 30 minutes We make *ABC* with potato

```
t = ABC

vocab = \{book, plate, city, cook, like, water,...\}

t = \{ 0, 1, 0, 1, 1, 0, ...\}
```

## Term-term matrix

 The number of times the context word c appear close to the term t in within a window

|             | art | boil | data | function | large | sugar | summarize | water |
|-------------|-----|------|------|----------|-------|-------|-----------|-------|
| apricot     | 0   | 1    | 0    | 0        | 1     | 2     | 0         | 1     |
| pineapple   | 0   | 1    | 0    | 0        | 1     | 1     | 0         | 1     |
| digital     | 0   | 0    | 1    | 3        | 1     | 0     | 1         | 0     |
| information | 0   | 0    | 9    | 1        | 1     | 0     | 2         | 0     |

### Goal

- Finding a good metric that based on the vectors of these four words shows
  - apricot and pineapple to be hight similar
  - digital and information to be hight similar
  - the other four pairing (apricot & digital, apricot & information, pineapple & digital, pineapple & information) to be less similar

- Three parameters should be specified
  - ☐ How the co-occurrence terms are defined? (what is a neighbor?)
  - How terms are weighted?
  - What vector distance metric should be used?

## **Distributional Similarity**

- How the co-occurrence terms are defined? (what is a neighbor?)
  - □ Widow of k words
  - Sentence
  - Paragraph
  - Document

# **Distributional Similarity**

■ How terms are weighted?

- Binary
- Frequency
- Pointwise mutual information

/ |

- How terms are weighted?
  - Binary
    - 1, if two words co-occur (no matter how often)
    - 0, otherwise

#(t,c)

|             |     |      |      | 11 (-) -) |       |       |           |       |
|-------------|-----|------|------|-----------|-------|-------|-----------|-------|
|             | art | boil | data | function  | large | sugar | summarize | water |
| apricot     | 0   | 1    | 0    | 0         | 1     | 1     | 0         | 1     |
| pineapple   | 0   | 1    | 0    | 0         | 1     | 1     | 0         | 1     |
| digital     | 0   | 0    | 1    | 1         | 1     | 0     | 1         | 0     |
| information | 0   | 0    | 1    | 1         | 1     | 0     | 1         | 0     |

- How terms are weighted?
  - Frequency
    - Number of times two words co-occur with respect to the total size of the corpus

$$P(t,c) = \frac{\#(t,c)}{N}$$

| #(t,c)      |     |      |      |          |       |       |           |       |  |
|-------------|-----|------|------|----------|-------|-------|-----------|-------|--|
|             | art | boil | data | function | large | sugar | summarize | water |  |
| apricot     | 0   | 1    | 0    | 0        | 1     | 2     | 0         | 1     |  |
| pineapple   | 0   | 1    | 0    | 0        | 1     | 1     | 0         | 1     |  |
| digital     | 0   | 0    | 1    | 3        | 1     | 0     | 1         | 0     |  |
| information | 0   | 0    | 9    | 1        | 1     | 0     | 2         | 0     |  |

 $P(t, c) \{N = 28\}$ 

|             |     |       |       | ( / / (  | ,     |       |           |       |
|-------------|-----|-------|-------|----------|-------|-------|-----------|-------|
|             | art | boil  | data  | function | large | sugar | summarize | water |
| apricot     | 0   | 0.035 | 0     | 0        | 0.035 | 0.071 | 0         | 0.035 |
| pineapple   | 0   | 0.035 | 0     | 0        | 0.035 | 0.035 | 0         | 0.035 |
| digital     | 0   | 0     | 0.035 | 0.107    | 0.035 | 0     | 0.035     | 0     |
| information | 0   | 0     | 0.321 | 0.035    | 0.035 | 0     | 0.071     | 0     |

- How terms are weighted?
  - Pointwise mutual information
    - Number of times two words co-occur, compared with what we would expect if they were independent

$$PMI(t, c) = log \frac{P(t, c)}{P(t) \cdot P(c)}$$

| 7 | ^ |  |
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| 1 | u |  |

|             | art  | boil  | data   | function | large | sugar | summarize     | water |
|-------------|------|-------|--------|----------|-------|-------|---------------|-------|
|             | Δ1 ι |       | - data | 0        |       | 3     | 3dillillarize |       |
| apricot     | 0    | 0.035 | 0      | 0        | 0.035 | 0.071 | 0             | 0.035 |
| pineapple   | 0    | 0.035 | 0      | 0        | 0.035 | 0.035 | 0             | 0.035 |
| digital     | 0    | 0     | 0.035  | 0.107    | 0.035 | 0     | 0.035         | 0     |
| information | 0    | 0     | 0.321  | 0.035    | 0.035 | 0     | 0.071         | 0     |

P(digital, summarize) = 0.035P(information, function) = 0.035

P(digital, summarize) = P(information, function)

PMI(digital, summarize) =?
PMI(information, function) =?

|             | art | boil  | data  | function | large | sugar | summarize | water |
|-------------|-----|-------|-------|----------|-------|-------|-----------|-------|
| apricot     | 0   | 0.035 | 0     | 0        | 0.035 | 0.071 | 0         | 0.035 |
| pineapple   | 0   | 0.035 | 0     | 0        | 0.035 | 0.035 | 0         | 0.035 |
| digital     | 0   | 0     | 0.035 | 0.107    | 0.035 | 0     | 0.035     | 0     |
| information | 0   | 0     | 0.321 | 0.035    | 0.035 | 0     | 0.071     | 0     |

P(digital, summarize) = 0.035P(information, function) = 0.035

$$P(digital) = 0.212$$
  
 $P(information) = 0.462$ 

$$P(summarize) = 0.106$$
  
 $P(function) = 0.142$ 

$$PMI(digital, summarize) = \frac{P(digital, summarize)}{P(digital) \cdot P(summarize)} = \frac{0.035}{0.212 \times 0.106} = 1.557$$

$$PMI(information, function) = \frac{P(information, function)}{P(information) \cdot P(function)} = \frac{0.035}{0.462 \times 0.142} = 0.533$$

P(digital, summarize) > P(information, function)

- What vector distance metric should be used?
  - Cosine

• 
$$Sim_{cosine}(\vec{v},\vec{w}) = rac{\sum_i v_i imes w_i}{\sqrt{\sum_i v_i^2} \sqrt{\sum_i w_i^2}}$$

Jaccard

• 
$$Sim_{jaccard}(\vec{v},\vec{w}) = rac{\sum_{i} min(v_i,w_i)}{\sum_{i} max(v_i,w_i)}$$

- Dice
  - $Sim_{dice}(\vec{v},\vec{w}) = rac{2 imes \sum_i min(v_i,w_i)}{\sum_i (v_i + w_i)}$

## **Further Reading**

- Speech and Language Processing
  - □ Chapters 19, 20