

Q12

given weight vector:  $w = [1, -2, 3, -4]$

Bias term  $w_0 = 25$

Feature  $x = [10, 20, 30, 40]$

(a) Predicted output:-

The linear regression prediction formula is

$$y = w_0 + w_1x_1 + w_2x_2 + w_3x_3 + w_4x_4$$

plugging the value in:-

$$y = 25 + (1 \times 10) + (-2 \times 20) + (3 \times 30) + (-4 \times 40)$$

This will give:-

$$25 + 10 - 40 + 90 - 160$$

Combine terms:  $25 + 10 = 35$ ;  $35 - 40 = -5$ ;  $-5 + 90 = 85$

$$85 - 160 = \boxed{-75}$$

(b) Penalty term of Regression:

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[R] formula for ridge penalty term

$$2C = \frac{\lambda}{2} \sum_{i=1}^n w_i^2$$

given  $\lambda = 0.6$ ,  $w = [1, -2, 3, -4]$ :

Calculating sum of squared weights:

$$(1)^2 + (-2)^2 + (3)^2 + (-4)^2$$

$$= 1 + 4 + 9 + 16$$

$$= 30$$

$$1^2 + 2^2 + 3^2 + 4^2 = 30$$

now, multiply by  $\lambda$ :  $0.6 \times 30 = 18.0$

and now  $\frac{\lambda}{2} = \frac{18}{2} = 9.0$

$$2C = 18.0$$