

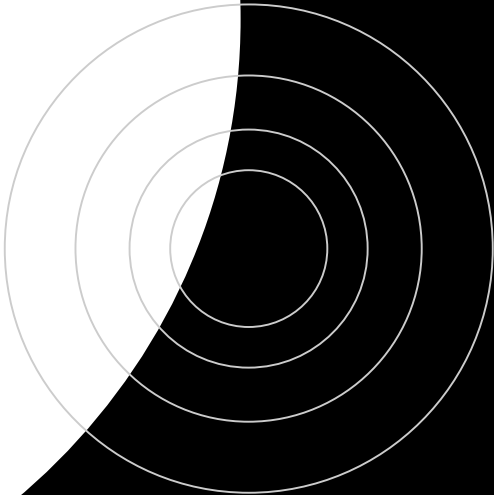
# ILP-based Footprint Arrangement





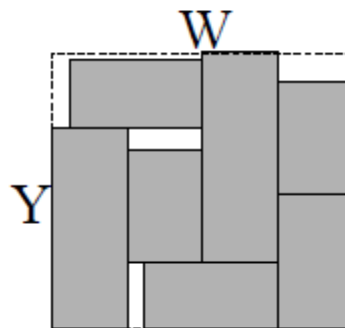
1

# Results

- Block Graph 1
  - Block Graph 2
  - Block Graph 3
  - Block Graph 4
  - Block Graph 5
- 

# Formulation

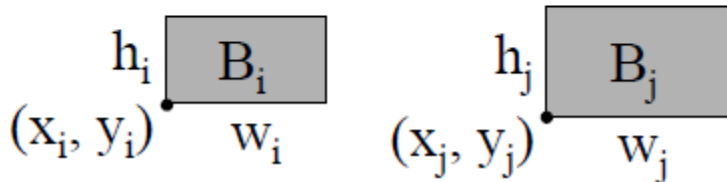
- Minimize the packing area:
  - Assume that one dimension  $W$  is fixed.
  - Minimize the other dimension  $Y$ .
- Need to have constraints so that blocks do not overlap.
- Associate each block  $B_i$  with 4 variables:
  - $x_i$  and  $y_i$ : coordinates of its lower left corner.
  - $w_i$  and  $h_i$ : width and height.



# Non-overlapping Constraints

For two non-overlapping blocks  $B_i$  and  $B_j$ , at least one of the following four linear constraints must be satisfied:

- |        |                      |                                   |
|--------|----------------------|-----------------------------------|
| (1)    | $x_i + w_i \leq x_j$ | if $B_i$ is to the left of $B_j$  |
| or (2) | $x_i - w_j \geq x_j$ | if $B_i$ is to the right of $B_j$ |
| or (3) | $y_i + h_i \leq y_j$ | if $B_i$ is below $B_j$           |
| or (4) | $y_i - h_j \geq y_j$ | if $B_i$ is above $B_j$           |



# Non-overlapping Constraints (hard blocks)

- Use integer (0 or 1) variables  $x_{ij}$  and  $y_{ij}$ :  
 $x_{ij}=0$  and  $y_{ij}=0$  if (1) is true.  
 $x_{ij}=0$  and  $y_{ij}=1$  if (2) is true.  
 $x_{ij}=1$  and  $y_{ij}=0$  if (3) is true.  
 $x_{ij}=1$  and  $y_{ij}=1$  if (4) is true.
- Let  $W$  and  $H$  be upper bounds on the total width and height. Non-overlapping constraints:

$$\begin{aligned}
 (1') \quad & x_i + w_i \leq x_j + W(x_{ij} + y_{ij}) \\
 (2') \quad & x_i - w_j \geq x_j - W(1 + x_{ij} - y_{ij}) \\
 (3') \quad & y_i + h_i \leq y_j + H(1 - x_{ij} + y_{ij}) \\
 (4') \quad & y_i - h_j \geq y_j - H(2 - x_{ij} - y_{ij})
 \end{aligned}$$

$$\begin{aligned}
 \text{Min. } & Y \\
 \text{s.t. } & 0 \leq x_i, x_i + w_i \leq W & 1 \leq i \leq n \\
 & 0 \leq y_i, y_i + h_i \leq Y & 1 \leq i \leq n \\
 & x_i + w_i \leq x_j + W(x_{ij} + y_{ij}) & 1 \leq i < j \leq n \\
 & x_i - w_j \geq x_j - W(1 + x_{ij} - y_{ij}) & 1 \leq i < j \leq n \\
 & y_i + h_i \leq y_j + H(1 - x_{ij} + y_{ij}) & 1 \leq i < j \leq n \\
 & y_i - h_j \geq y_j - H(2 - x_{ij} - y_{ij}) & 1 \leq i < j \leq n \\
 & x_{ij} = 0 \text{ or } 1 & 1 \leq i < j \leq n \\
 & y_{ij} = 0 \text{ or } 1 & 1 \leq i < j \leq n
 \end{aligned}$$

# Block Graph 1

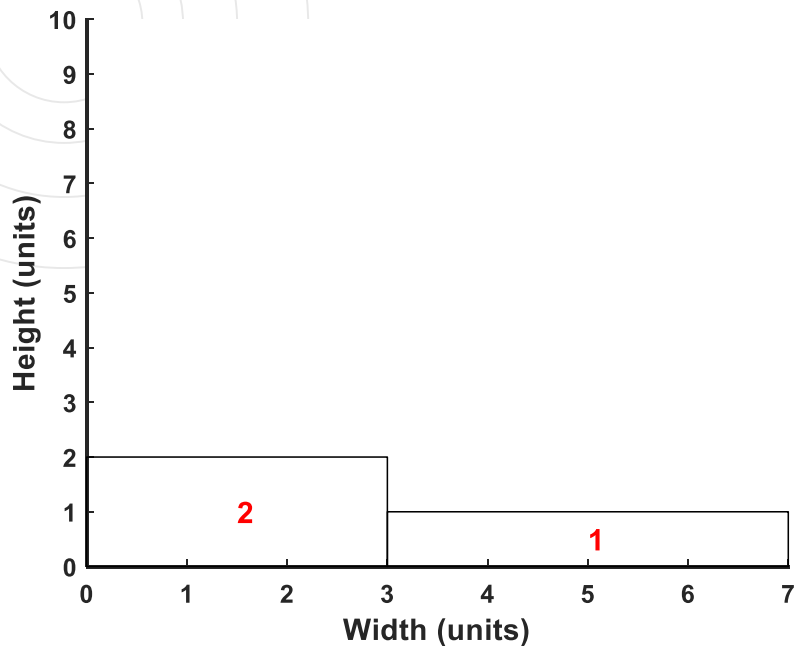
- Block Area Info 1

```
num_blocks 2
block_1 1
block_1 width 4 height 1 area 4
block_2 1
block_2 width 3 height 2 area 6
```

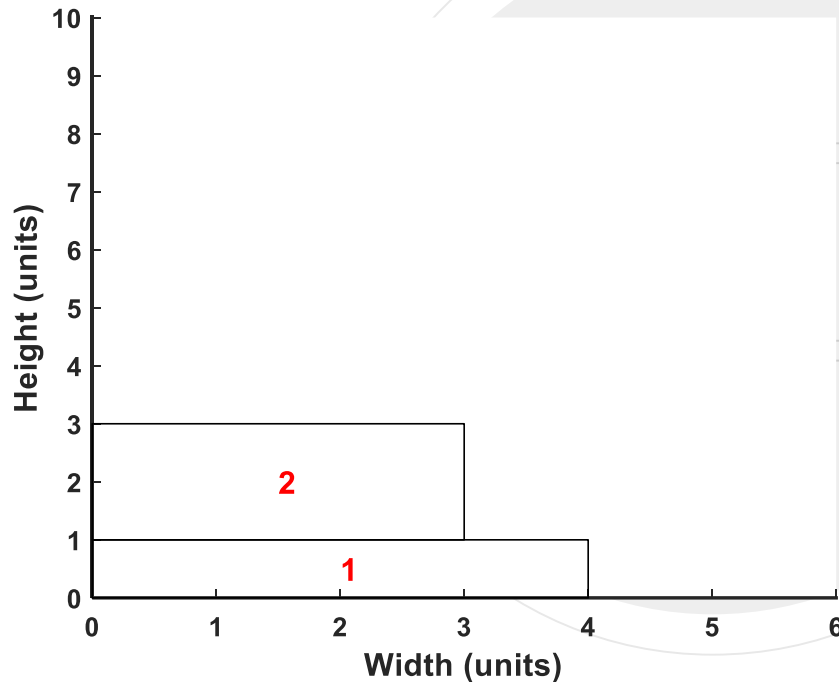
- Two hard blocks.
- We **decreases** width from **7 to 2** and see how minimized height changes.



# Footprint Graph 1

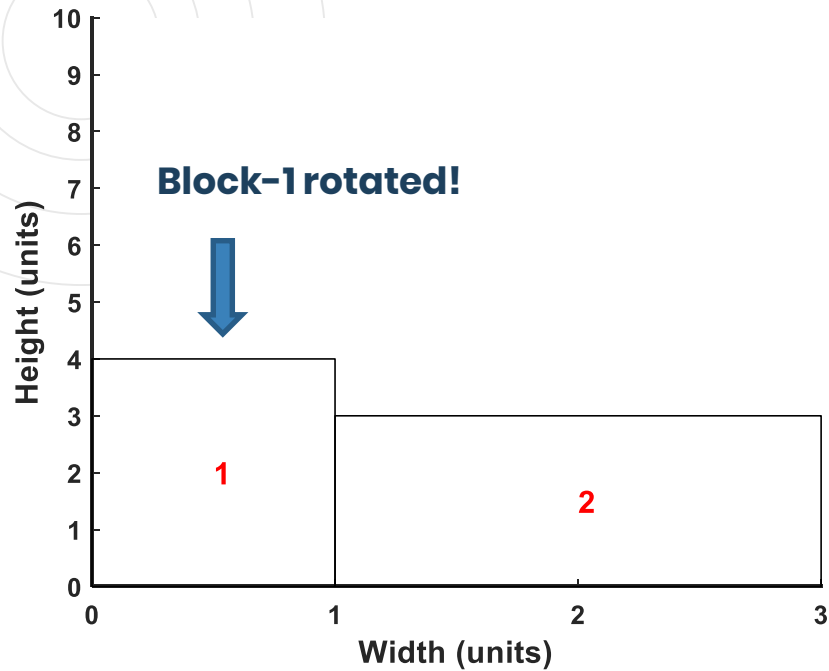


**Width = 7 → Y = 2**

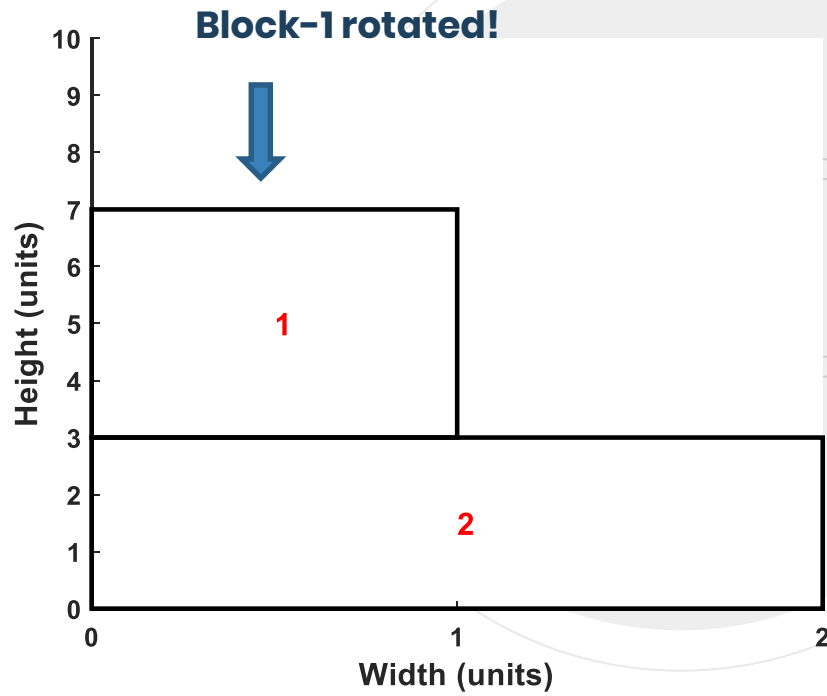


**Width = 6, 5, 4 → Y = 3**

# Footprint Graph 1



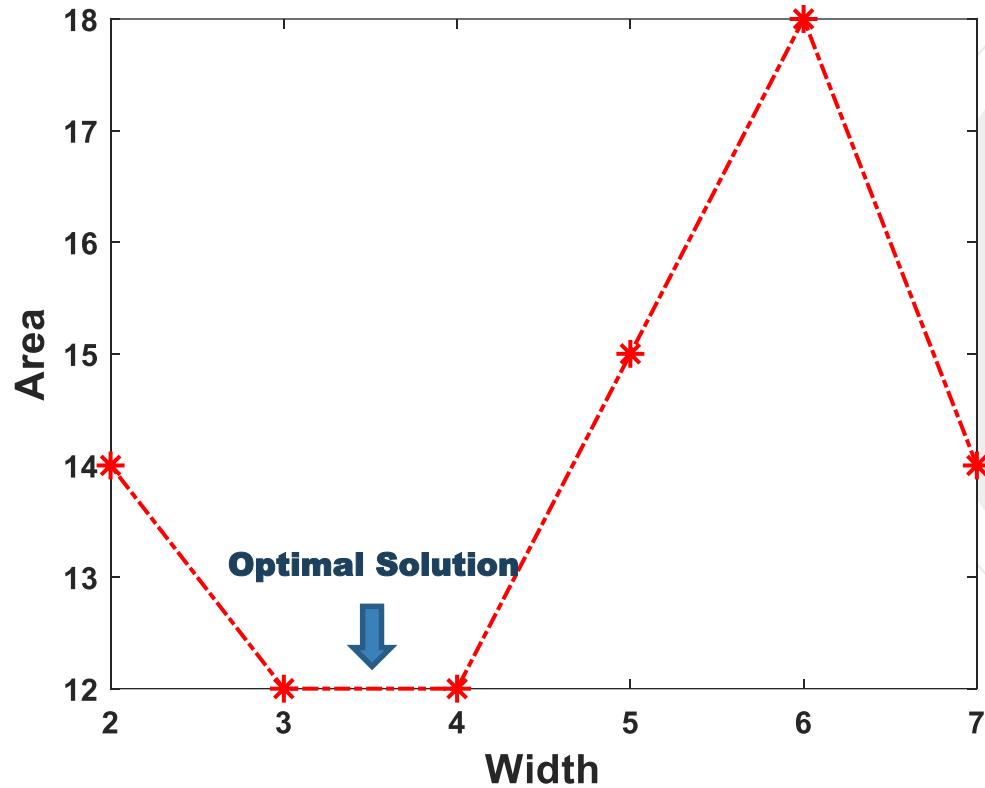
**Width = 3 → Y = 4**



**Width = 2 → Y = 7**



# Footprint Graph 1



# Block Graph 2

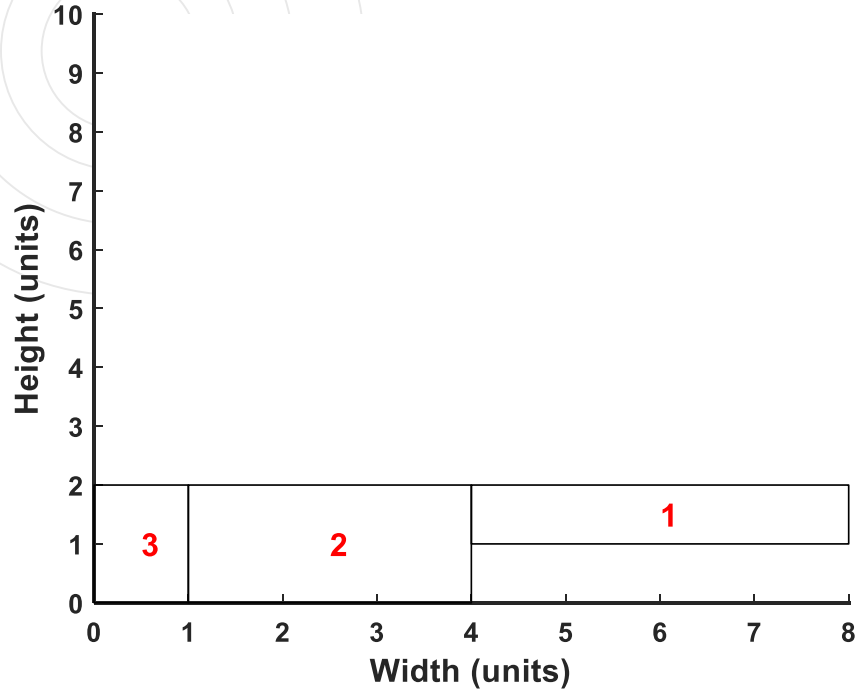
- Block Area Info 2

```
num_blocks 3
block_1 1
block_1 width 4 height 1 area 4
block_2 1
block_2 width 3 height 2 area 6
block_3 1
block_3 width 1 height 2 area 2
```

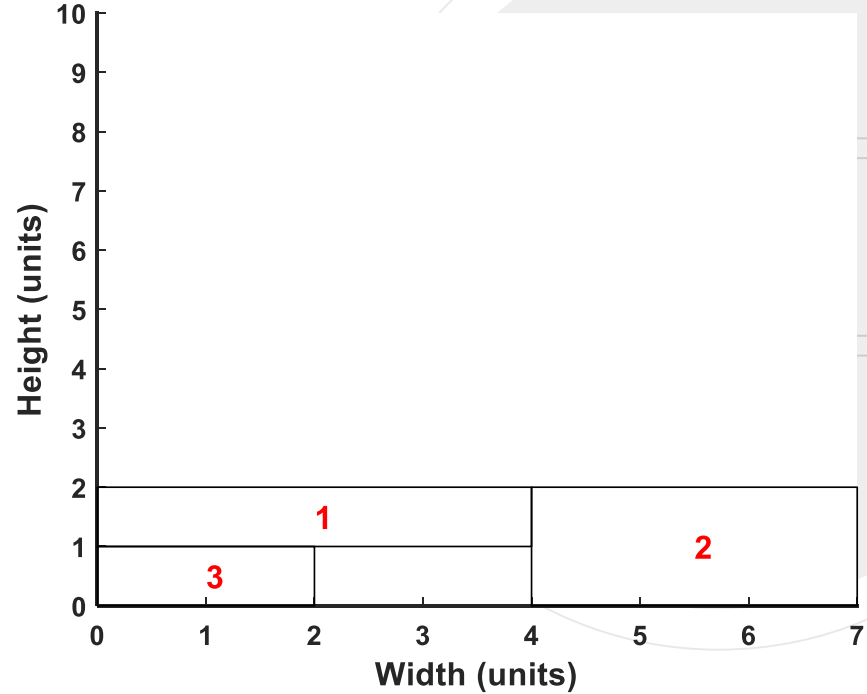
- Three hard blocks
- We **decreases** width from **8 to 2** and see how minimized height changes.



# Footprint Graph 2

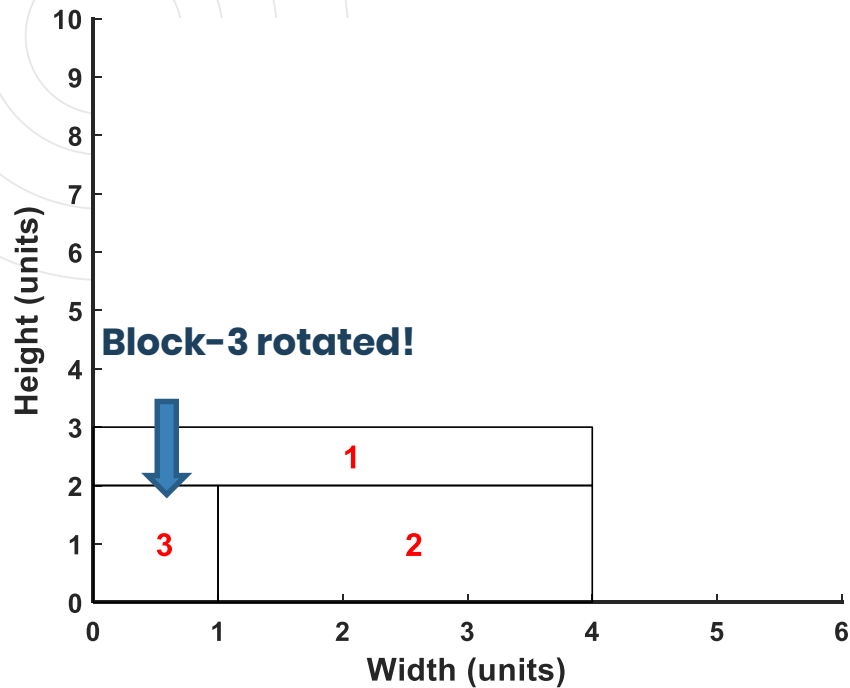


**Width = 8 → Y = 2**

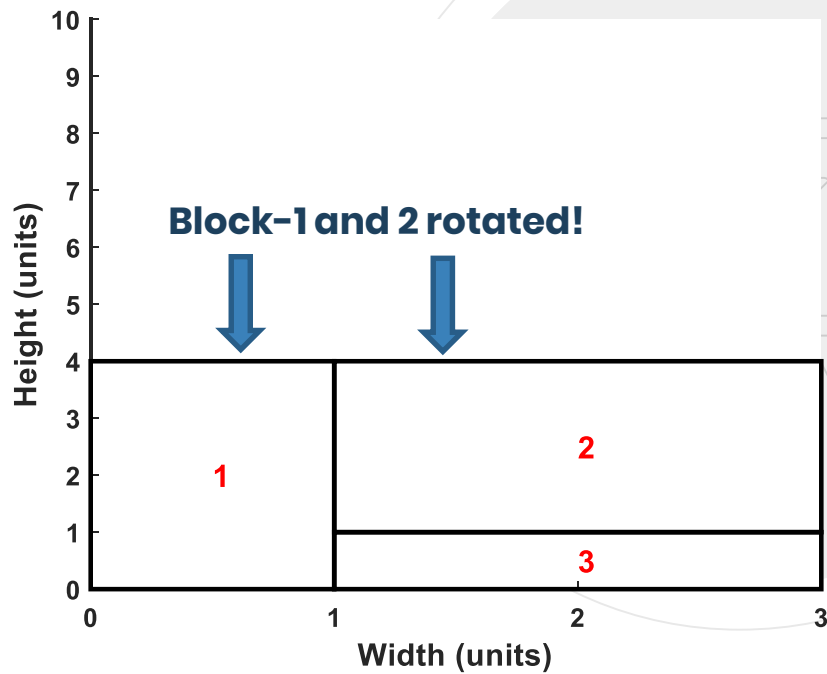


**Width = 7 → Y = 2**

# Footprint Graph 2



**Width = 6, 5, 4 → Y = 3**



**Width = 3 → Y = 4**

# Footprint Graph 2



**Width = 2 → Y = 7**

