

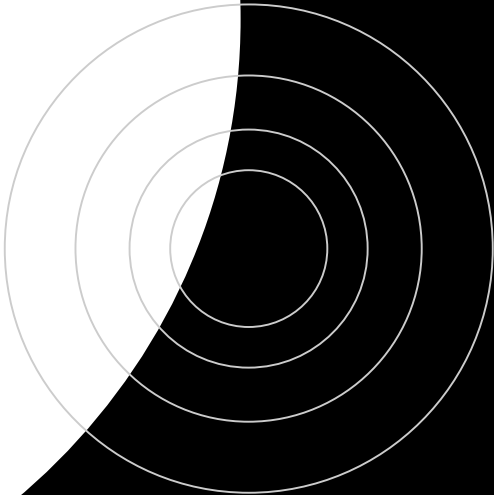
# ILP-based Scheduler





1

# Results

- Task Graph 1
  - Task Graph 2
  - Task Graph 3
  - Task Graph 4
  - Task Graph 5
- 

# 1

- For each task graph

- Task Graph Description
- Example - 1 (**Tmax only**)
  - Intlinprog scheduling
  - Cplexmilp scheduling
- Example - 2 (**Tmax only**)
  - Intlinprog scheduling
  - Cplexmilp scheduling
- Example - 1" (**Tmax + Energy**)
  - Intlinprog scheduling
  - Cplexmilp scheduling
- Example - 2" (**Tmax + Energy**)
  - Intlinprog scheduling
  - Cplexmilp scheduling



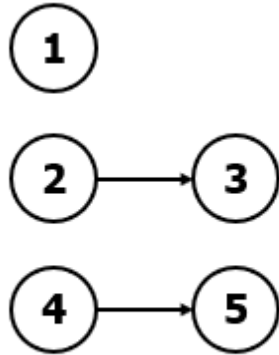
**Communication  
Time differs!**



**Communication  
Time and Power  
differs!**

# Task Graph 1

- CTG 1



- CTG 1 Description

```
add_new_tasks 5
task_1 1
task_1 earliest_start 0 deadline 9
task_2 2
task_2 earliest_start 0 deadline 9
task_3 3 2
task_3 earliest_start 0 deadline 9
task_4 4
task_4 earliest_start 0 deadline 9
task_5 5 4
task_5 earliest_start 0 deadline 9
```

- Resource Description

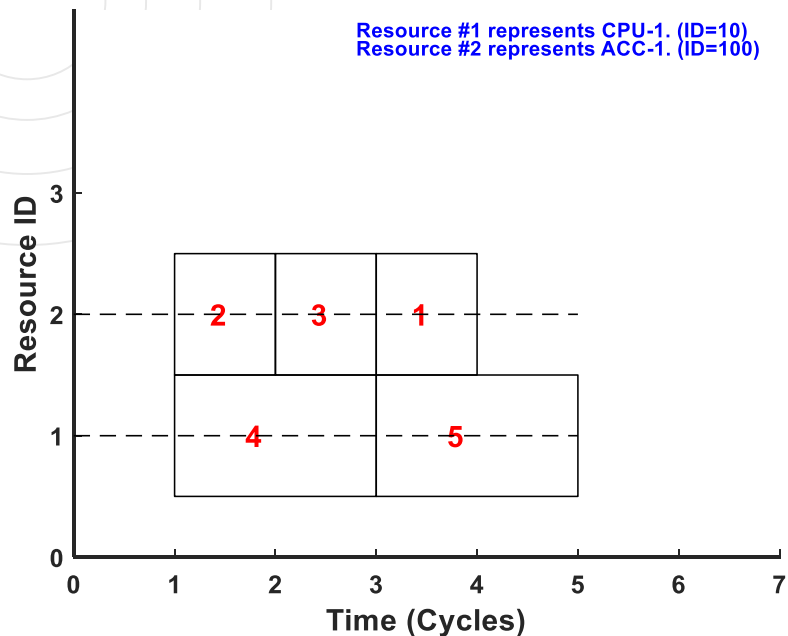
```
add_new_resource ACCa_0 0 5
task_1 10 5
task_2 10 4
task_3 10 3
task_4 10 2
task_5 10 1

add_new_resource CPUa_1 1 2
task_4 20 4
task_5 20 2
```

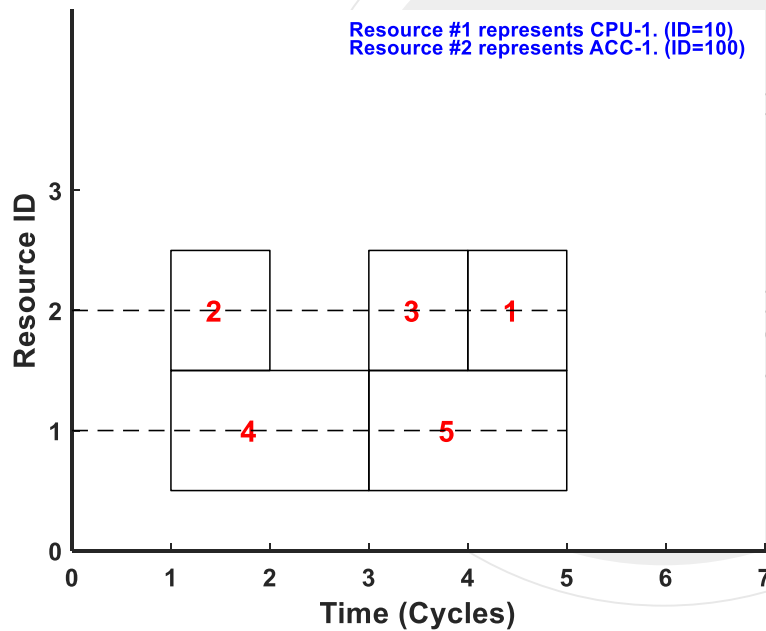
# Task Graph 1 Scheduling

(obj = tmax)

- Communication Time:
  - 0 for same type
  - 2 cycles for different type



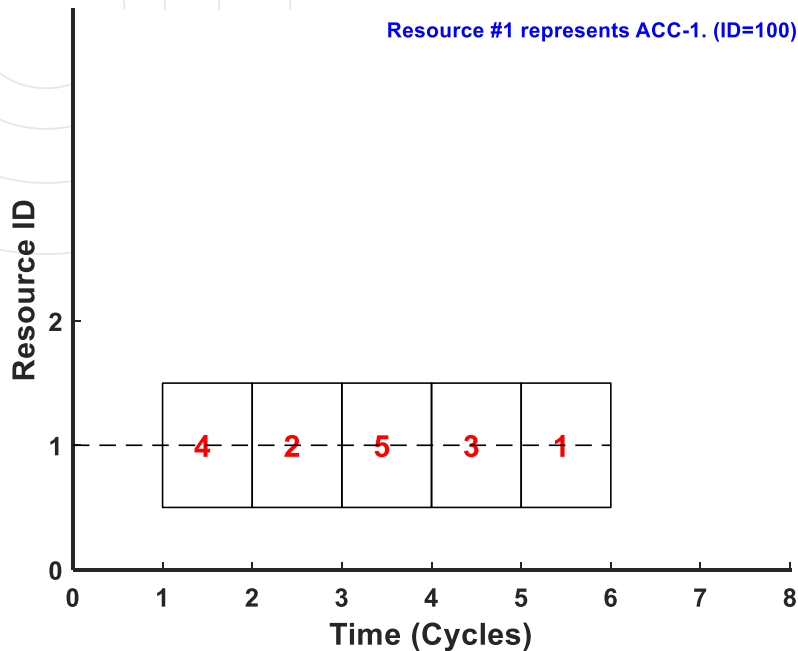
**Intlinprog:** 4 cycles



**cplexmilp:** 4 cycles

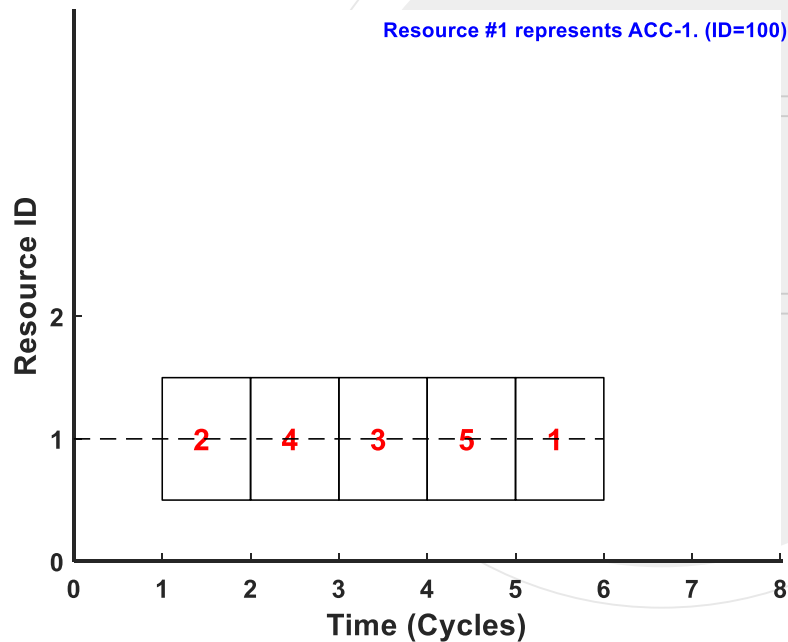
# Task Graph 1 Scheduling

(obj = tmax)



**Intlinprog:** 5 cycles

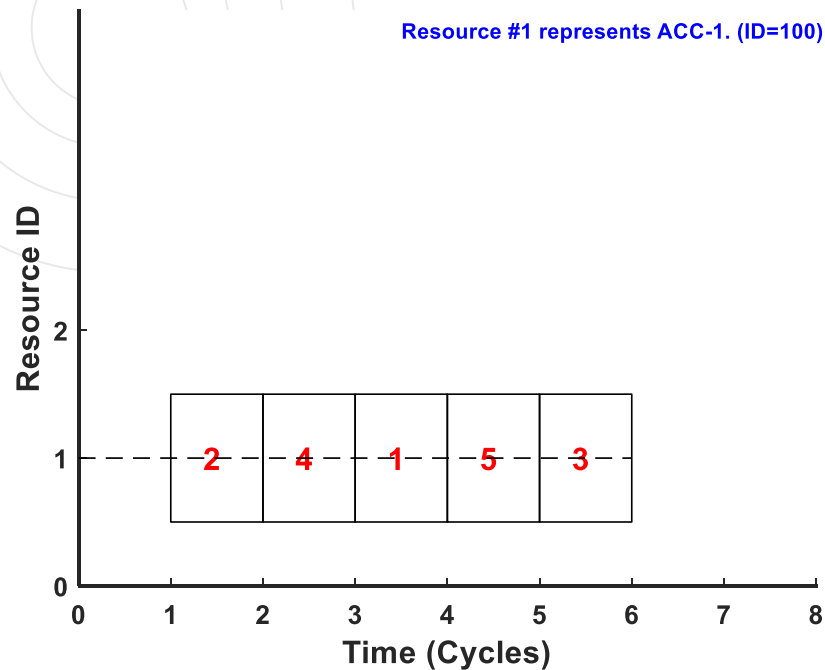
- Communication Time:
  - 1 for same type
  - 2 cycles for different type



**cplexmilp:** 5 cycles

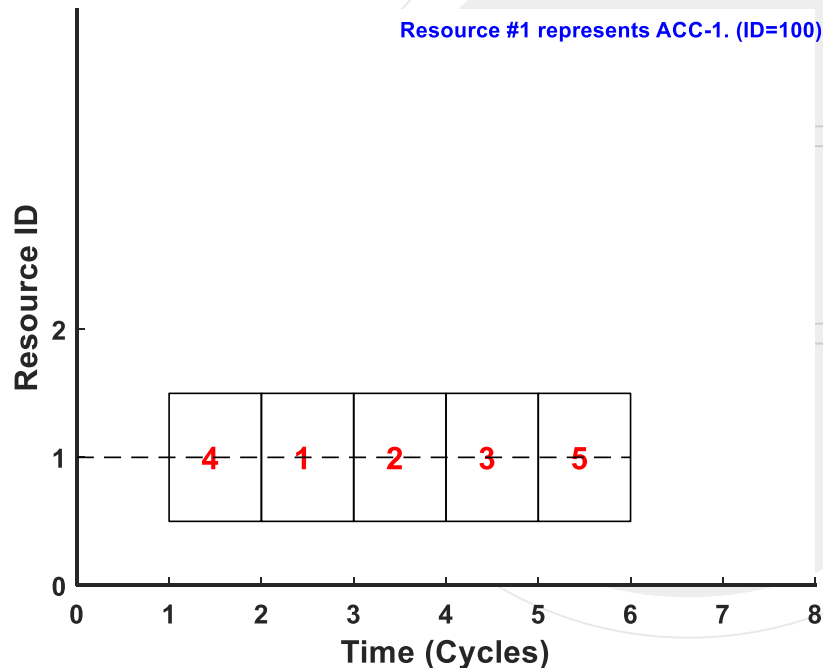
# Task Graph 1 Scheduling

(obj = tmax + energy)



**Intlinprog:** 5 cycles, 15 units energy

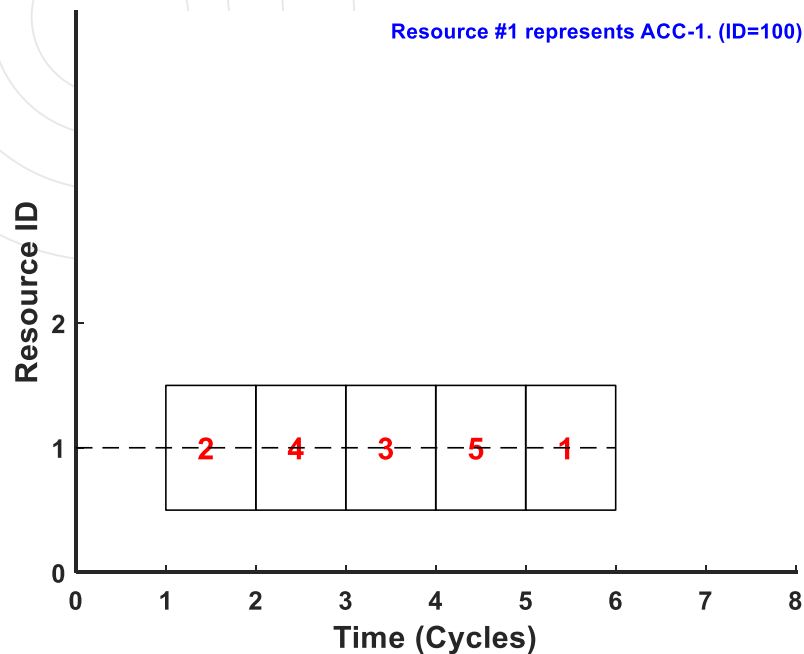
- Communication Power, Time:
  - 0 for same type
  - 2 for different type



**Cplexmilp:** 5 cycles, 15 units energy

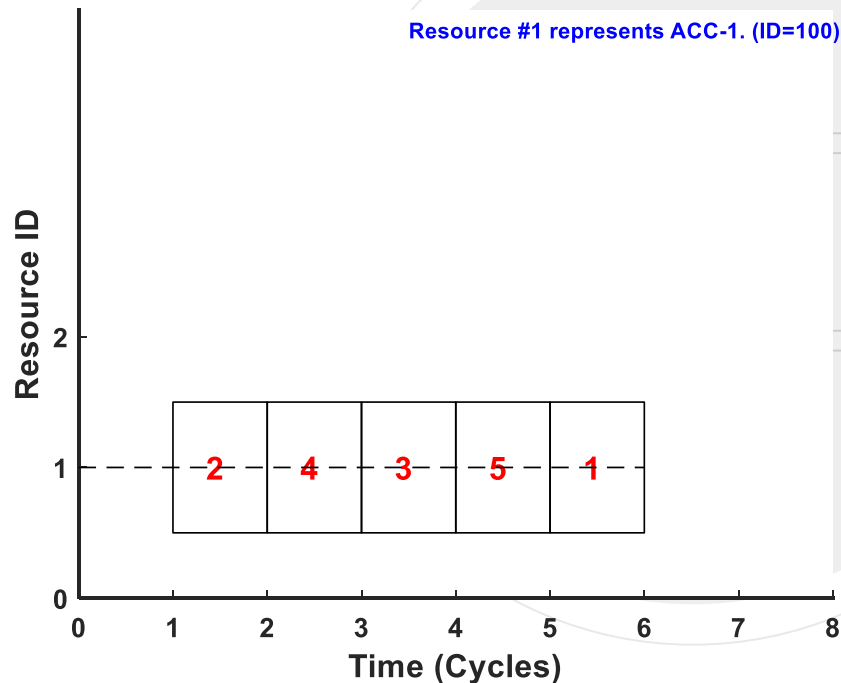
# Task Graph 1 Scheduling

(obj = tmax + energy)



**Intlinprog:** 5 cycles, 17 units energy

- Communication Power, Time:
  - 1 for same type
  - 2 for different type

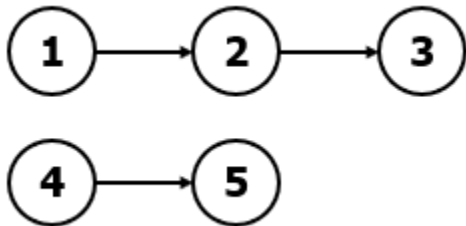


**Cplexmilp:** 5 cycles, 17 units energy



# Task Graph 2

- CTG 2



- CTG 2 Description

```
add_new_tasks 5
task_1 1
task_1 earliest_start 0 deadline 100
task_2 2 1
task_2 earliest_start 0 deadline 100
task_3 3 2
task_3 earliest_start 0 deadline 100
task_4 4
task_4 earliest_start 0 deadline 100
task_5 5 4
task_5 earliest_start 0 deadline 100
```

- Resource Description

```
add_new_resource CPUa_0 0 5
task_1 30 10
task_2 32 10
task_3 25 10
task_4 20 10
task_5 20 10

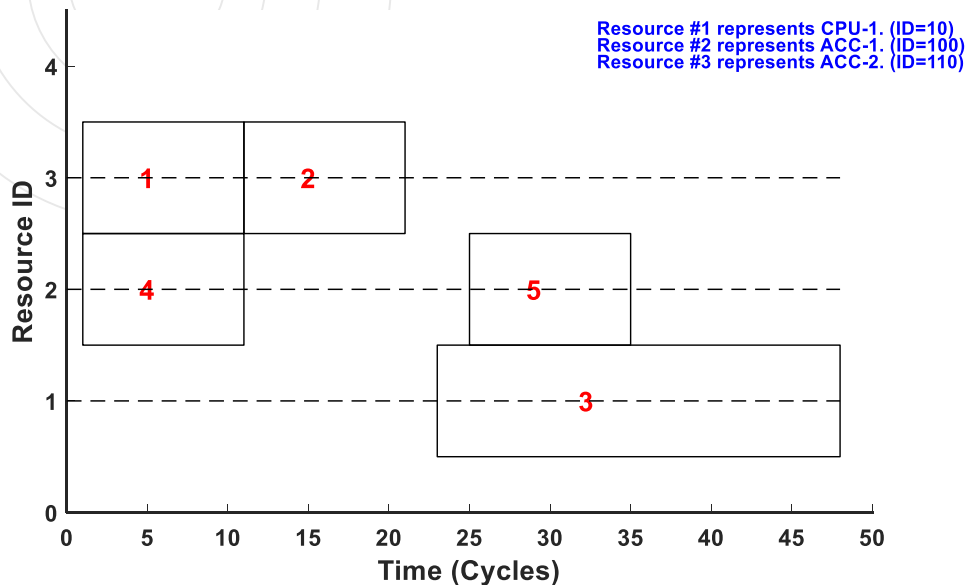
add_new_resource ACCa_1 1 2
task_4 10 20
task_5 10 20

add_new_resource ACCb_1 1 2
task_1 10 10
task_2 10 10
```

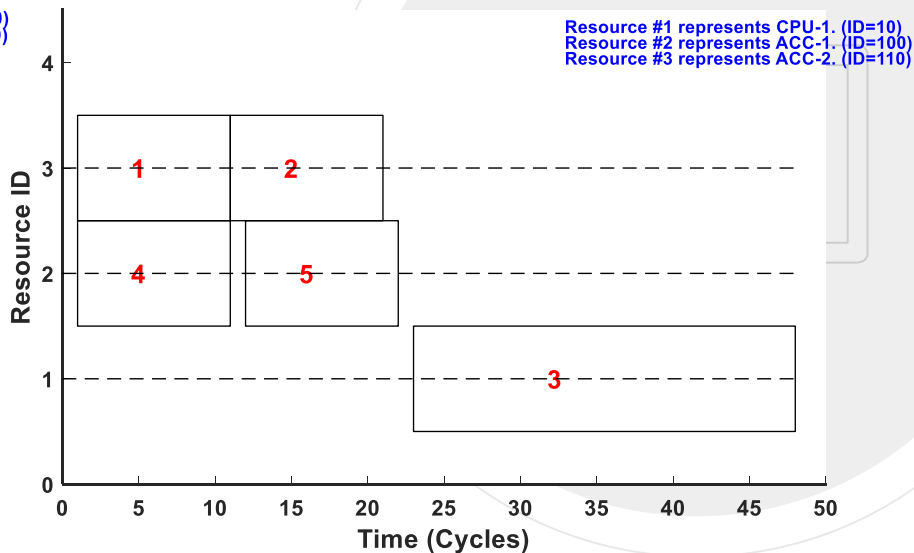
# Task Graph 2 Scheduling

(obj = tmax)

- Communication Time:
  - 0 for same type
  - 2 cycles for different type



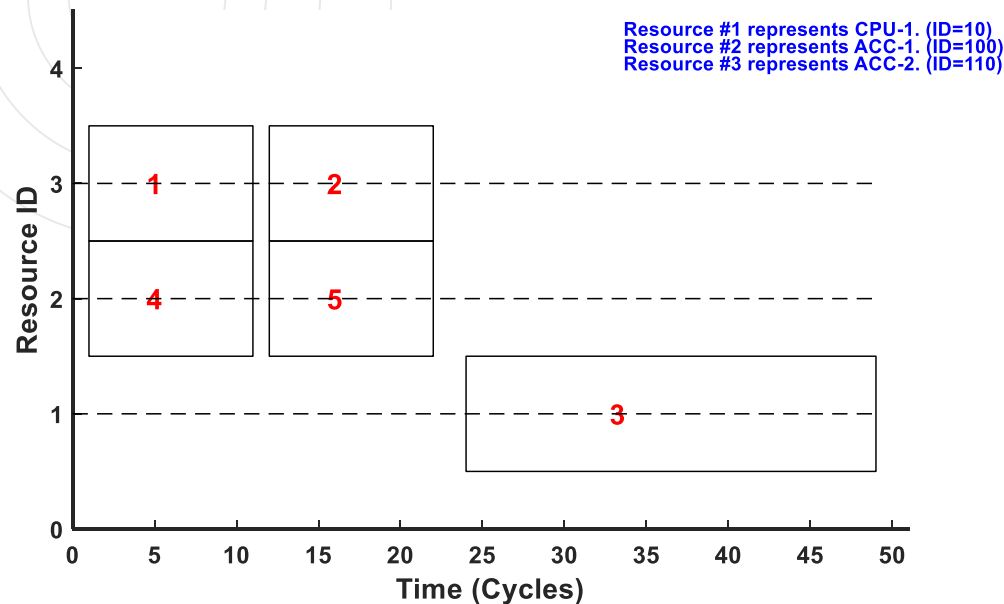
**Intlinprog:** 47 cycles



**cplexmilp:** 47 cycles

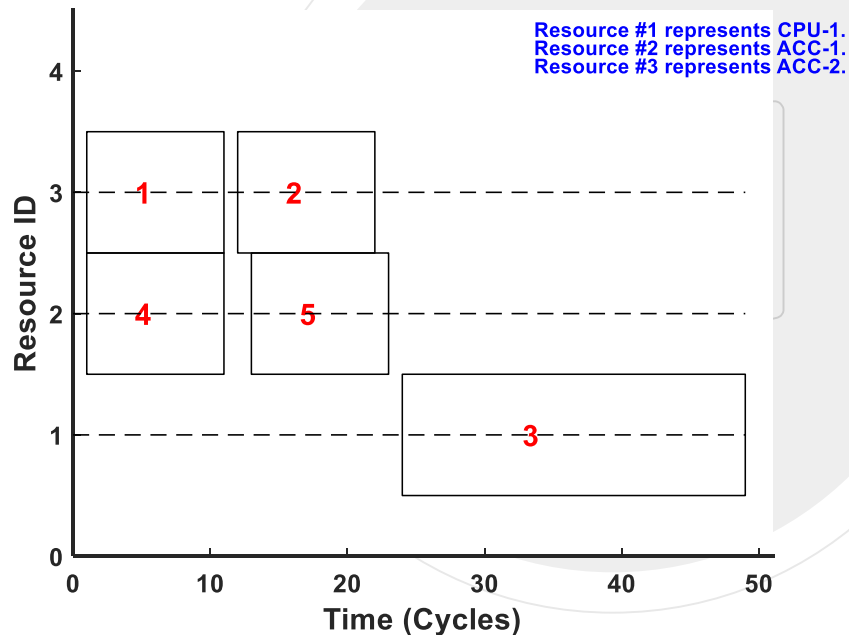
# Task Graph 2 Scheduling

(obj = tmax)



**Intlinprog:** 48 cycles

- Communication Time:
  - 1 for same type
  - 2 cycles for different type



**cplexmilp:** 48 cycles

# Task Graph 2 Scheduling

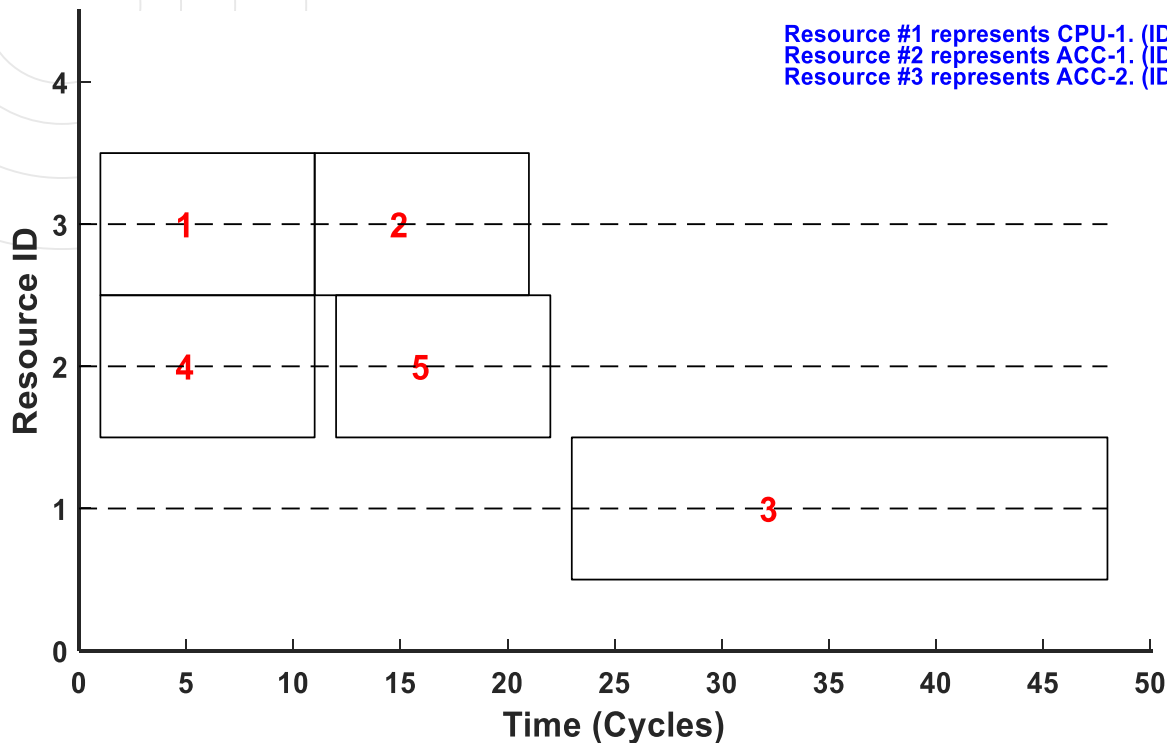
(obj = tmax + energy)

- Communication Power, Time:

-- 0 for same type

-- 2 for different type

Resource #1 represents CPU-1. (ID=10)  
Resource #2 represents ACC-1. (ID=100)  
Resource #3 represents ACC-2. (ID=110)



**Cplexmilp:**

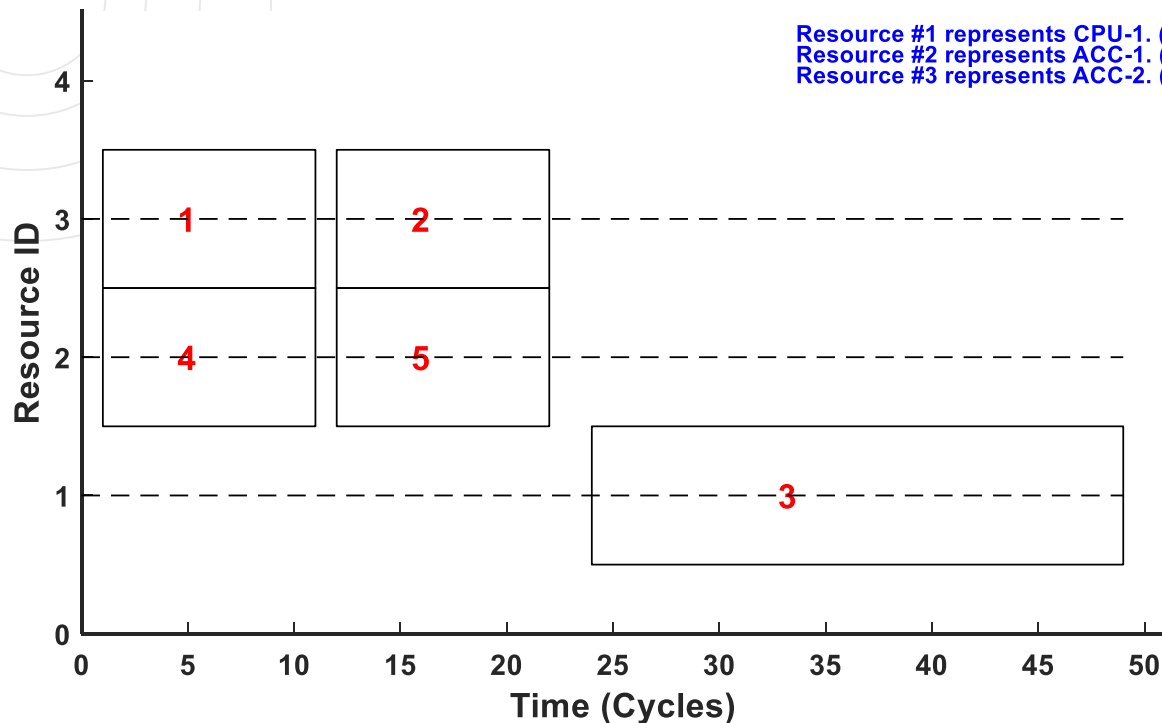
47 cycles,

854 units energy

# Task Graph 2 Scheduling

(obj = tmax + energy)

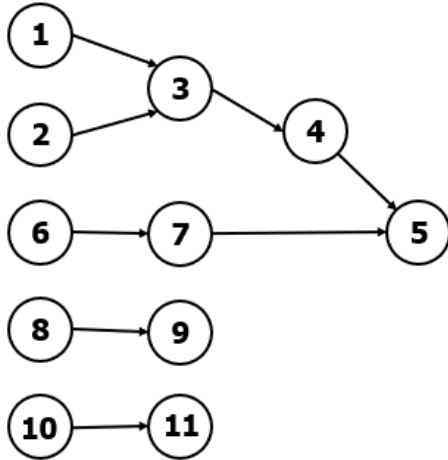
- Communication Power, Time:
  - 1 for same type
  - 2 for different type



**Cplexmilp:**  
48 cycles,  
856 units energy

# Task Graph 3

- CTG 3



- CTG 3 Description

```
add_new_tasks 11
task_1 1
task_1 earliest_start 0 deadline 13
task_2 2
task_2 earliest_start 0 deadline 13
task_3 3 1 2
task_3 earliest_start 0 deadline 14
task_4 4 3
task_4 earliest_start 0 deadline 14
task_5 5 4 7
task_5 earliest_start 0 deadline 15
task_6 6
task_6 earliest_start 0 deadline 13
task_7 7 6
task_7 earliest_start 0 deadline 14
task_8 8
task_8 earliest_start 0 deadline 16
task_9 9 8
task_9 earliest_start 0 deadline 16
task_10 10
task_10 earliest_start 0 deadline 13
task_11 11 10
task_11 earliest_start 0 deadline 14
```

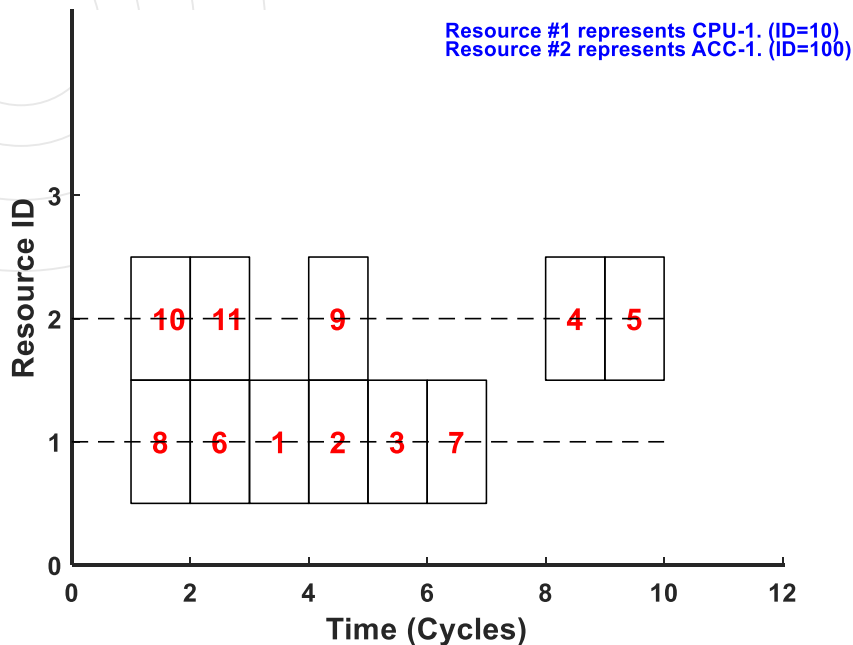
- Resource Description

```
add_new_resource MULTIPLIER_0 0 6
task_1 10 15
task_2 10 15
task_3 10 15
task_6 10 15
task_7 10 15
task_8 10 15

add_new_resource ALU_1 1 5
task_4 10 10
task_5 10 10
task_9 10 10
task_10 10 10
task_11 10 10
```

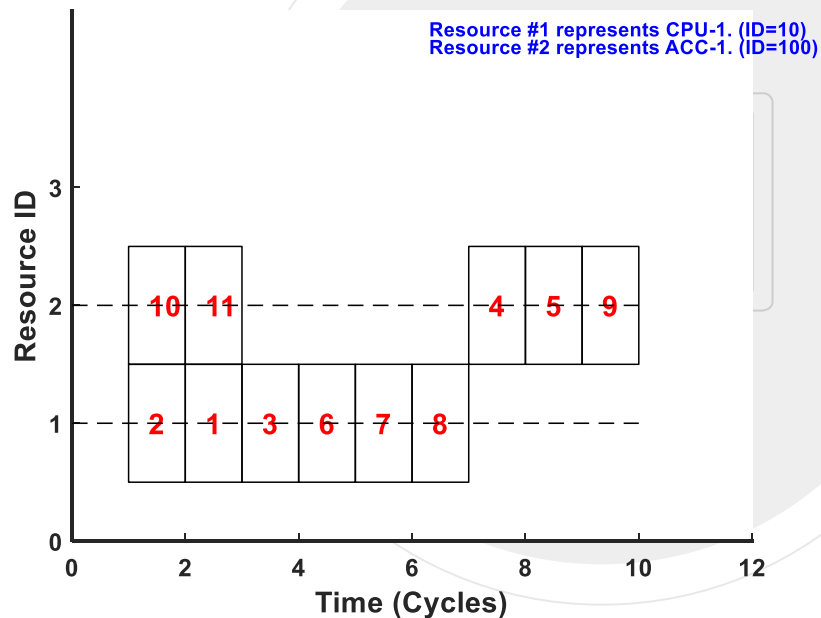
# Task Graph 3 Scheduling

(obj = tmax)



**Intlinprog:** 9 cycles

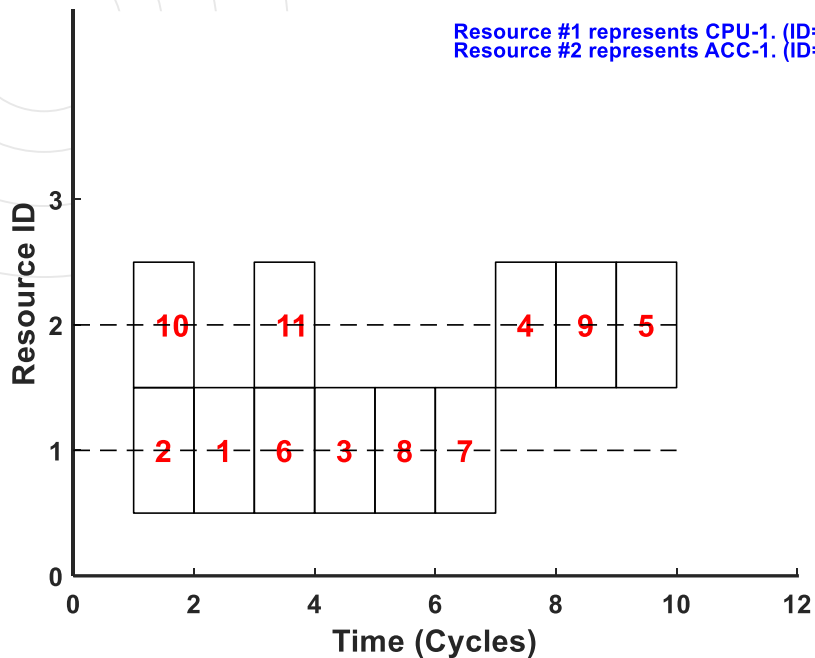
- Communication Time:
  - 0 for same type
  - 2 cycles for different type



**cplexmilp:** 9 cycles

# Task Graph 3 Scheduling

## (obj = tmax)

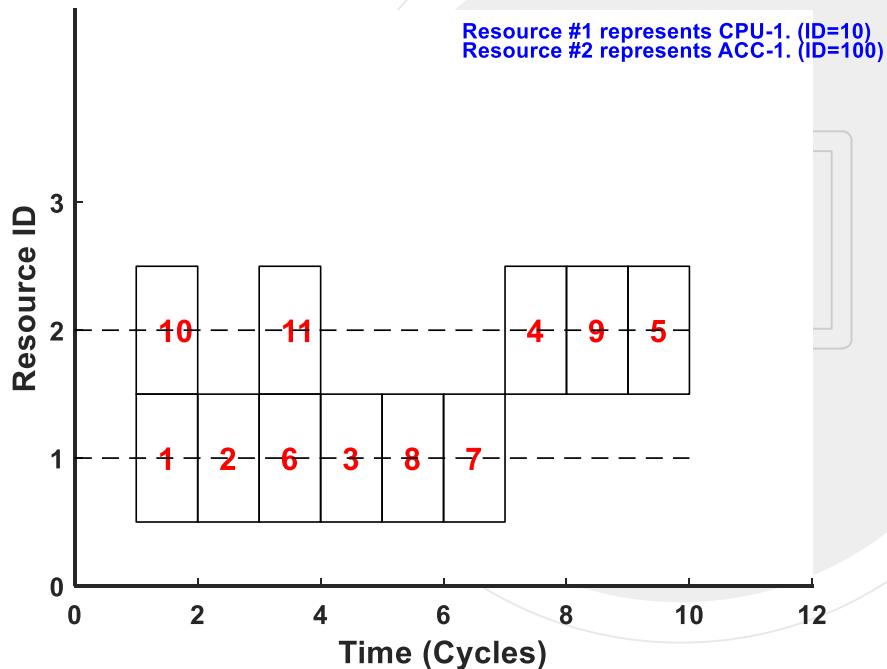


**Intlinprog:** 9 cycles

- Communication Time:

-- 1 for same type

-- 2 cycles for different type

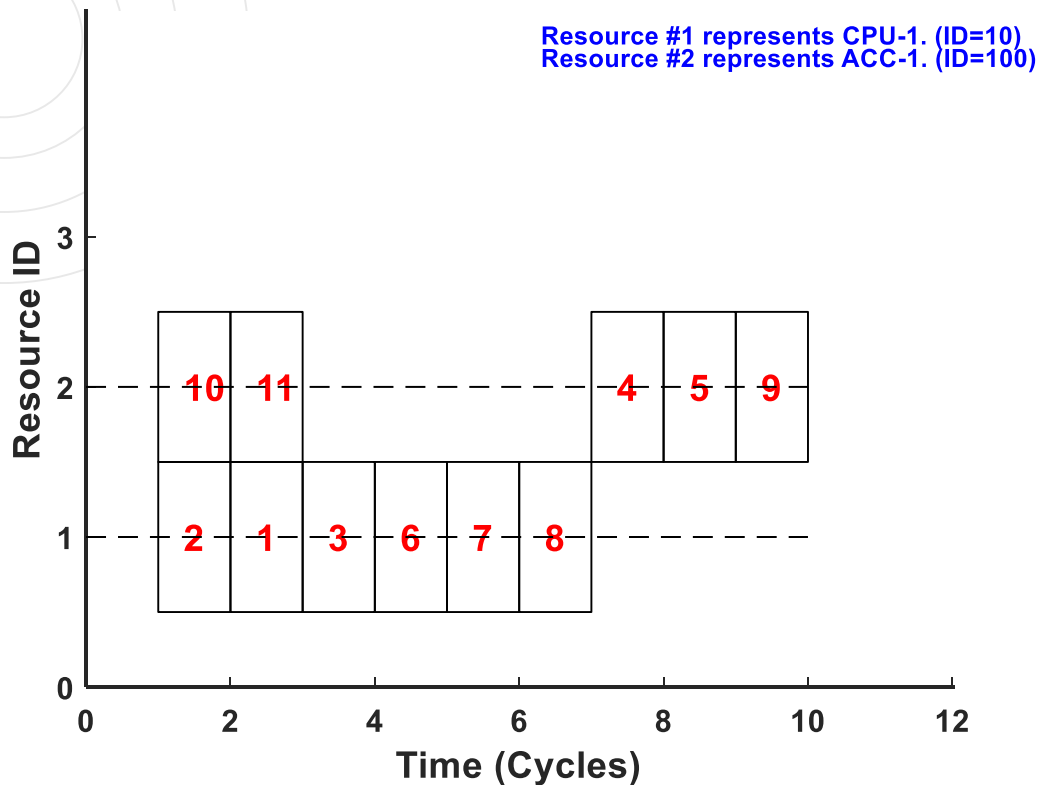


**cplexmilp:** 9 cycles



# Task Graph 3 Scheduling

(obj = tmax + energy)



- Communication Power, Time:
  - 0 for same type
  - 2 for different type

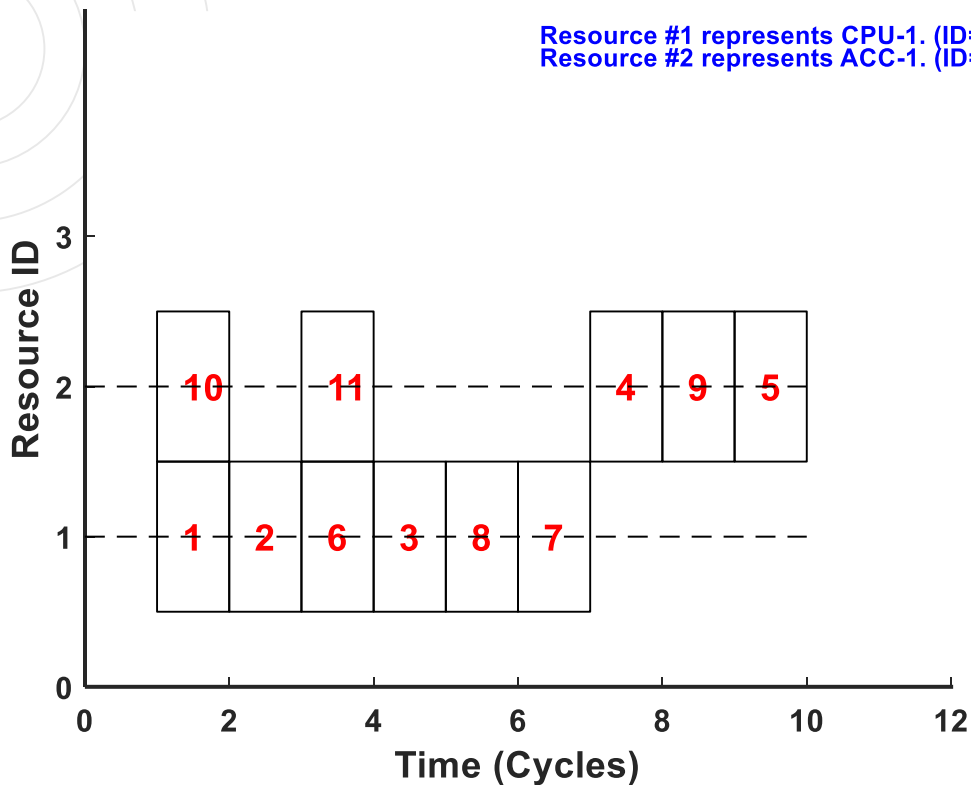
**Cplexmilp:**

9 cycles,

152 units energy

# Task Graph 3 Scheduling

(obj = tmax + energy)

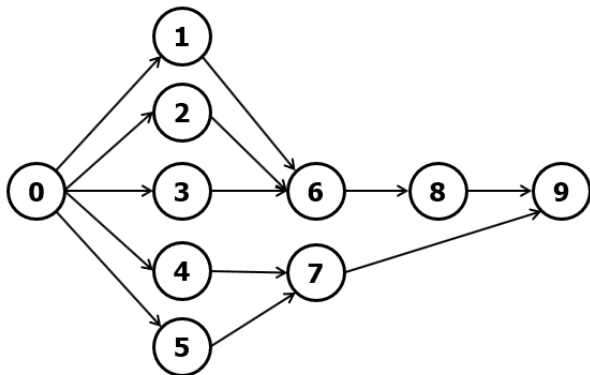


- Communication Power, Time:
  - 1 for same type
  - 2 for different type

**Cplexmilp:**  
9 cycles,  
157 units energy

# Task Graph 4

- CTG 4



- CTG 4 Description

```
add_new_tasks 10
task_1 1
task_1 earliest_start 0 deadline 250
task_2 2 1
task_2 earliest_start 0 deadline 250
task_3 3 1
task_3 earliest_start 0 deadline 250
task_4 4 1
task_4 earliest_start 0 deadline 250
task_5 5 1
task_5 earliest_start 0 deadline 250
task_6 6 1
task_6 earliest_start 0 deadline 250
task_7 7 2 3 4
task_7 earliest_start 0 deadline 250
task_8 8 5 6
task_8 earliest_start 0 deadline 250
task_9 9 7
task_9 earliest_start 0 deadline 250
task_10 10 8 9
task_10 earliest_start 0 deadline 250
```

- Resource Description

```
add_new_resource CPUa_0 0 10
task_1 30 22
task_2 25 23
task_3 23 24
task_4 16 20
task_5 20 18
task_6 25 17
task_7 18 20
task_8 32 29
task_9 14 15
task_10 29 18

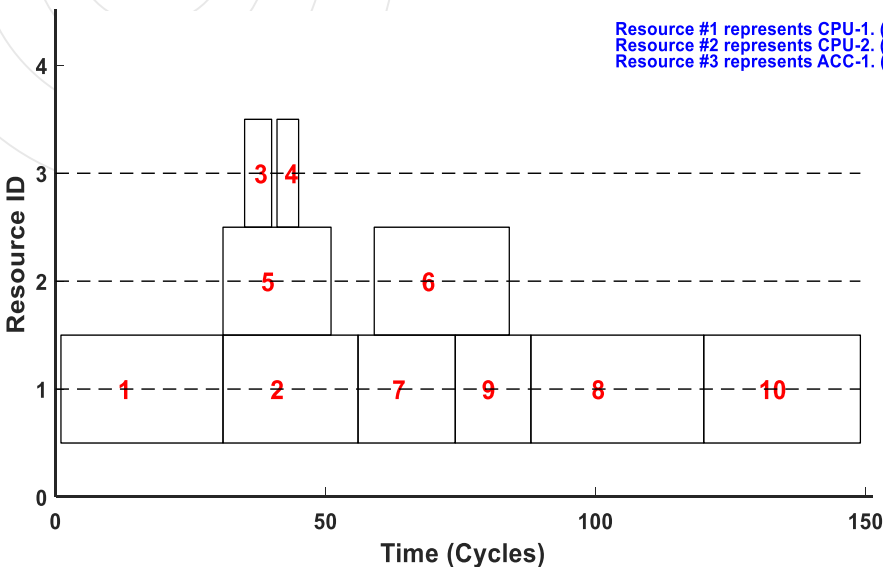
add_new_resource ACCa_1 1 2
task_4 10 18
task_5 12 17

add_new_resource ACCb_1 1 2
task_2 5 4
task_3 4 5
```

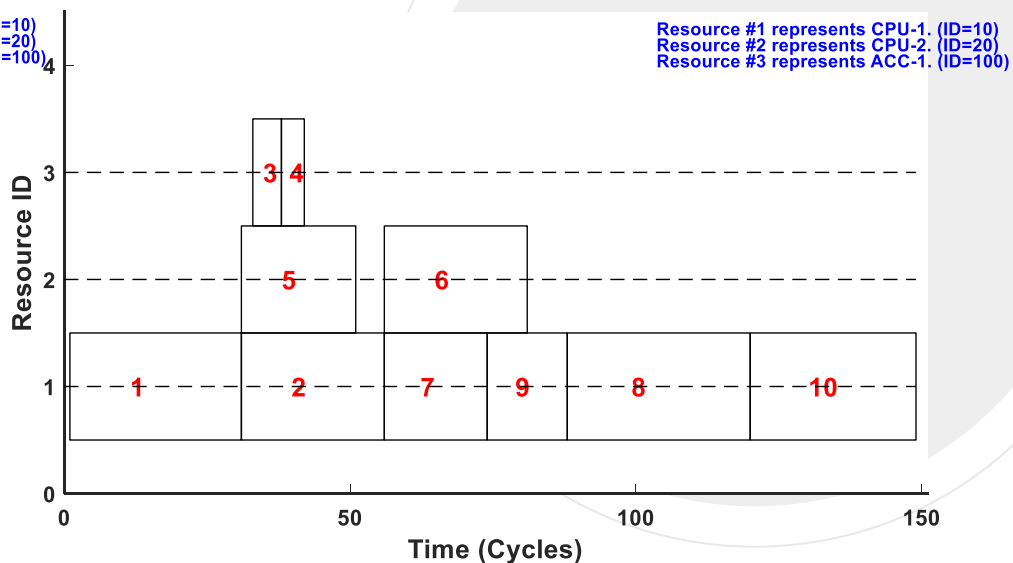
# Task Graph 4 Scheduling

## (obj = tmax)

- Communication Time:
  - 0 for same type
  - 2 cycles for different type



**Intlinprog:** 148 cycles



**cplexmilp:** 148 cycles

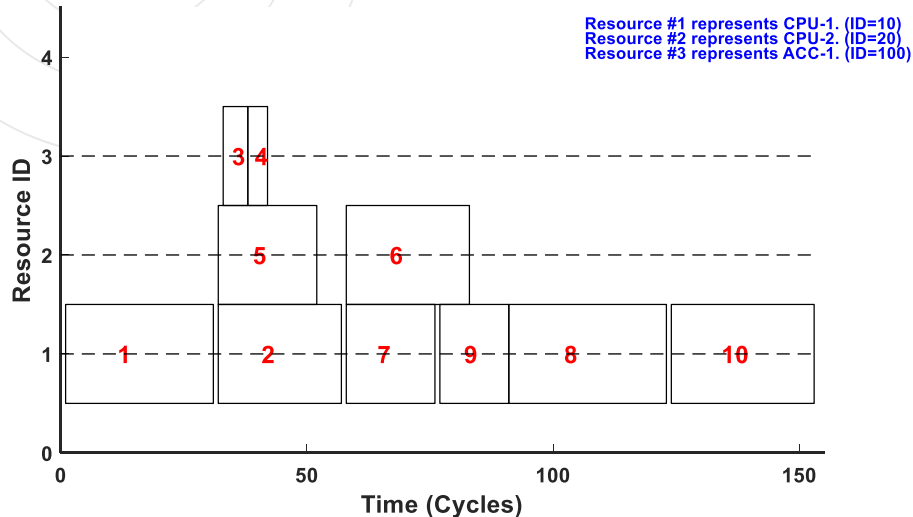
# Task Graph 4 Scheduling

(obj = tmax)

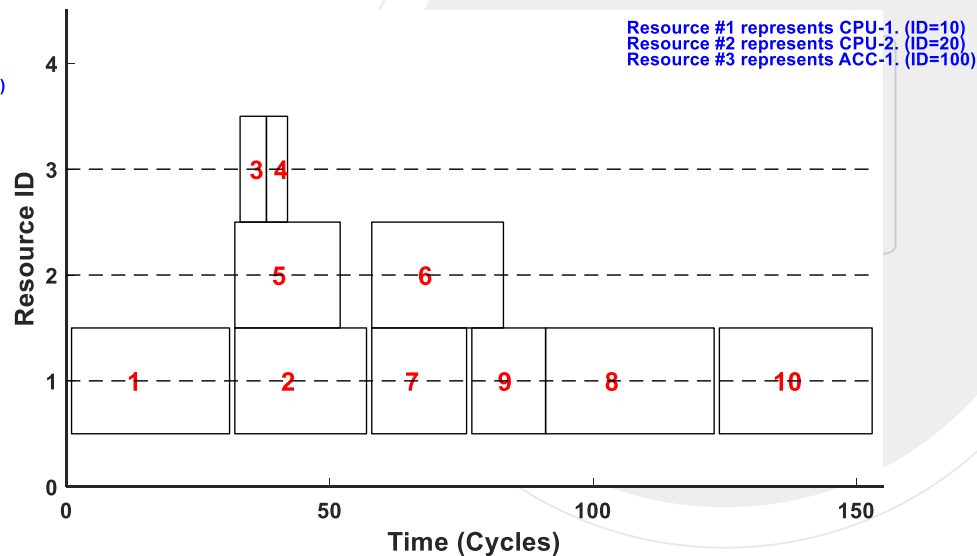
- Communication Time:

-- 1 for same type

-- 2 cycles for different type



**Intlinprog:** 152 cycles

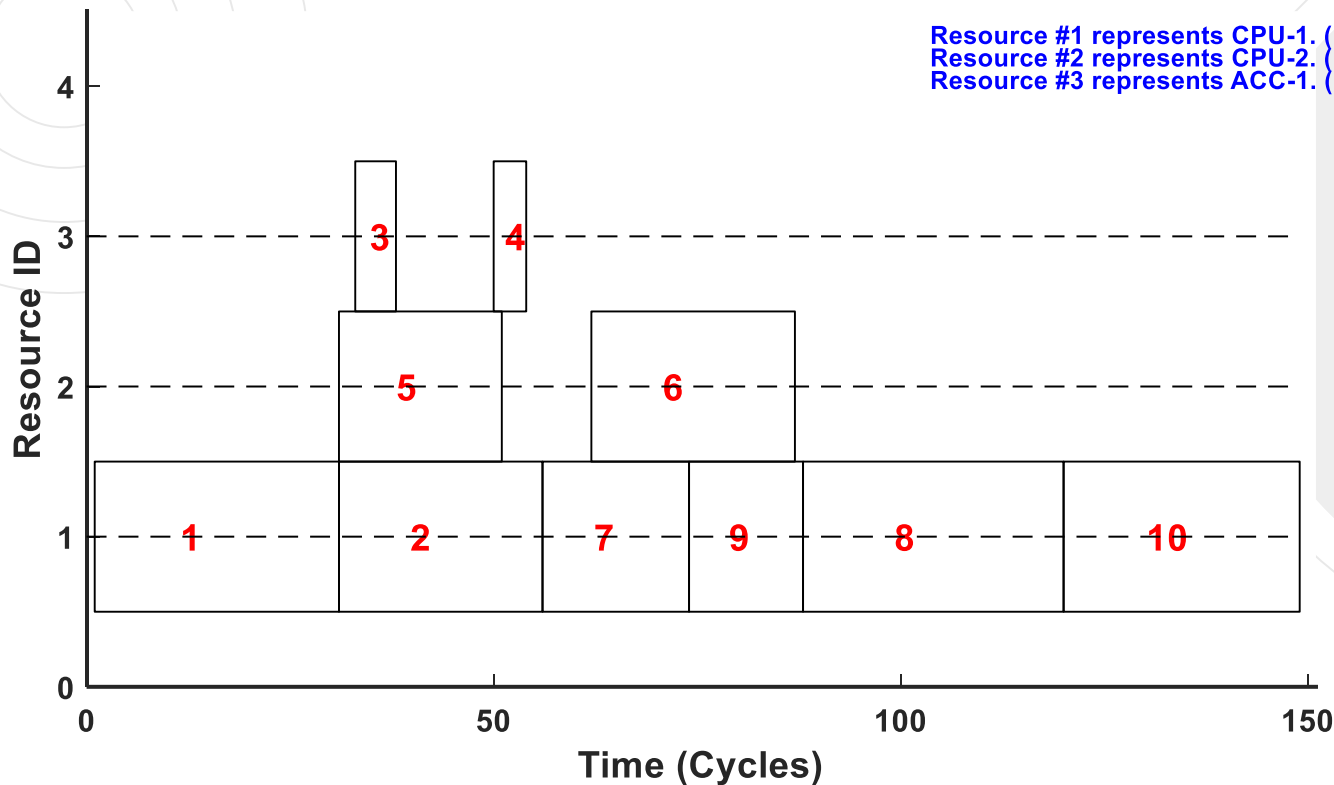


**cplexmilp:** 152 cycles

# Task Graph 4 Scheduling

(obj = tmax + energy)

- Communication Power, Time:
  - 0 for same type
  - 2 for different type



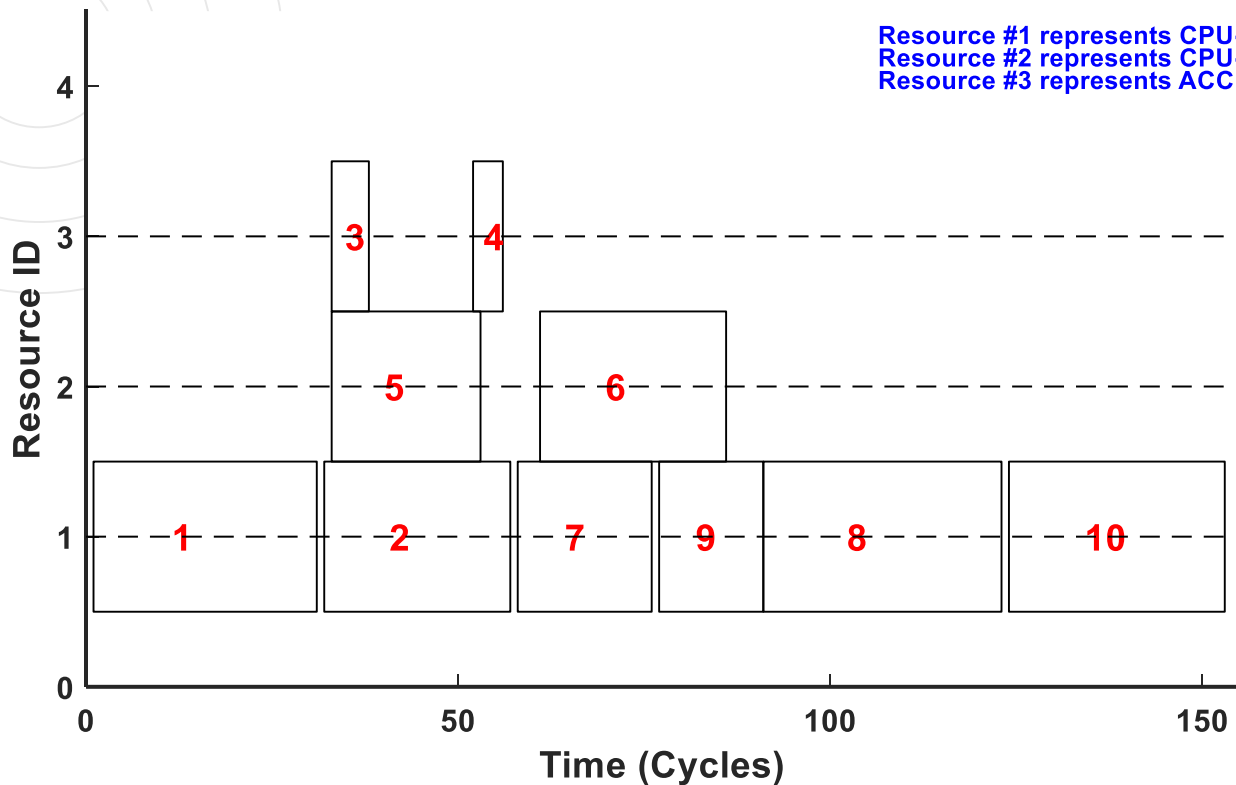
**Cplexmilp:**  
148 cycles,  
4100 units energy

# Task Graph 4 Scheduling

(obj = tmax + energy)

- Communication Power, Time:
  - 1 for same type
  - 2 for different type

Resource #1 represents CPU-1. (ID=10)  
Resource #2 represents CPU-2. (ID=20)  
Resource #3 represents ACC-1. (ID=100)

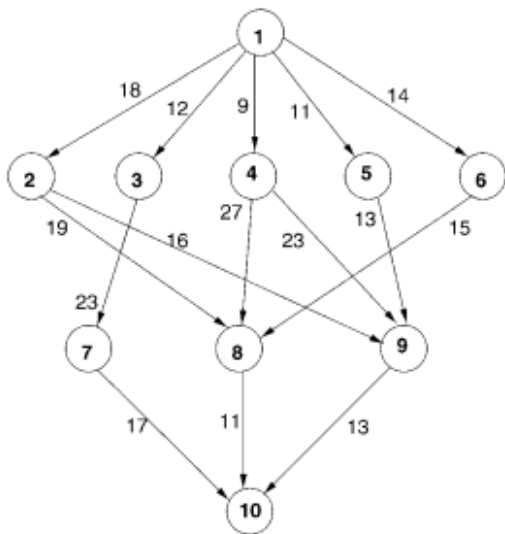


**Cplexmilp:**

152 cycles,  
4110 units energy

# Task Graph 5

- CTG 5



- CTG 5 Description

```

add_new_tasks 10
task_1 1
task_1 earliest_start 0 deadline 90
task_2 2 1
task_2 earliest_start 0 deadline 90
task_3 3 1
task_3 earliest_start 0 deadline 90
task_4 4 1
task_4 earliest_start 0 deadline 90
task_5 5 1
task_5 earliest_start 0 deadline 90
task_6 6 1
task_6 earliest_start 0 deadline 90
task_7 7 3
task_7 earliest_start 0 deadline 90
task_8 8 2 4 6
task_8 earliest_start 0 deadline 90
task_9 9 2 4 5
task_9 earliest_start 0 deadline 90
task_10 10 7 8 9
task_10 earliest_start 0 deadline 90
    
```

- Resource Description

```

add_new_resource CPUa_0 0 10
task_1 14 2
task_2 13 2
task_3 11 3
task_4 13 3
task_5 12 4
task_6 13 4
task_7 7 5
task_8 5 5
task_9 18 7
task_10 21 7
    
```

```

add_new_resource ACCa_1 1 10
task_1 16 4
task_2 19 4
task_3 13 3
task_4 8 3
task_5 13 2
task_6 16 2
task_7 15 1
task_8 11 1
task_9 12 3
task_10 7 3
    
```

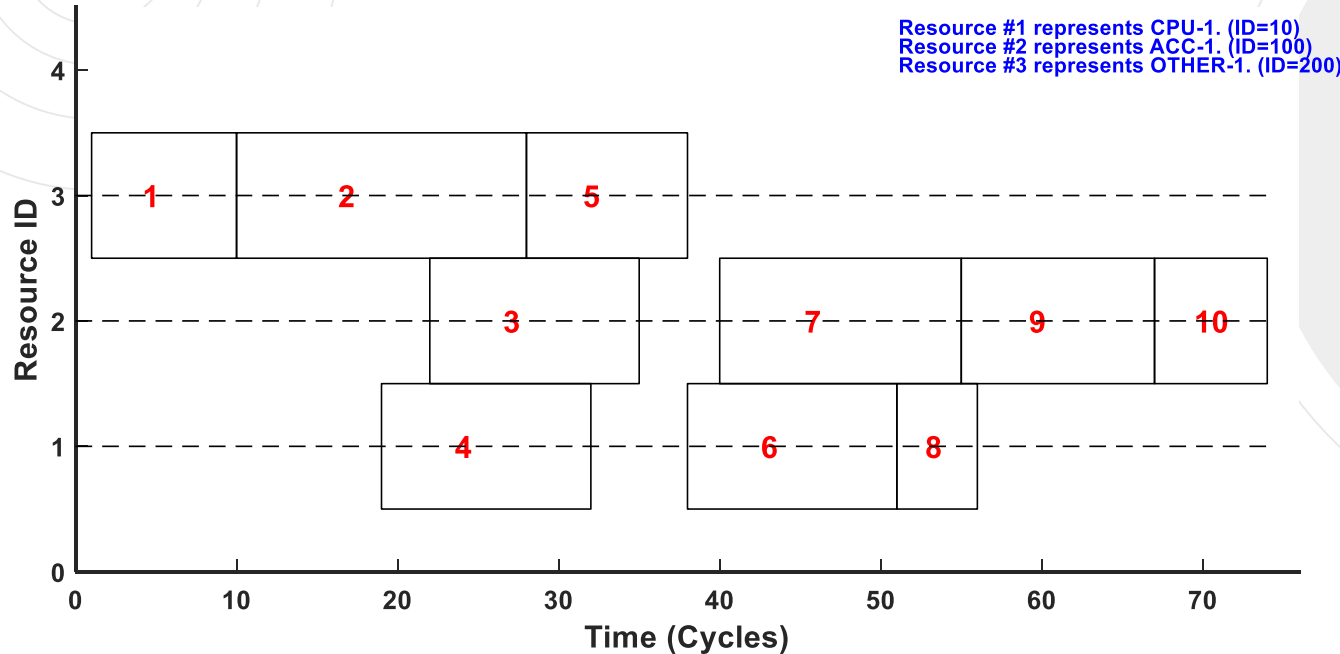
```

add_new_resource OTHERa_1 1 10
task_1 9 12
task_2 18 12
task_3 19 11
task_4 17 11
task_5 10 5
task_6 9 5
task_7 11 7
task_8 14 7
task_9 20 9
task_10 16 9
    
```



# Task Graph 5 Scheduling (cplexmilp)

(obj = tmax)



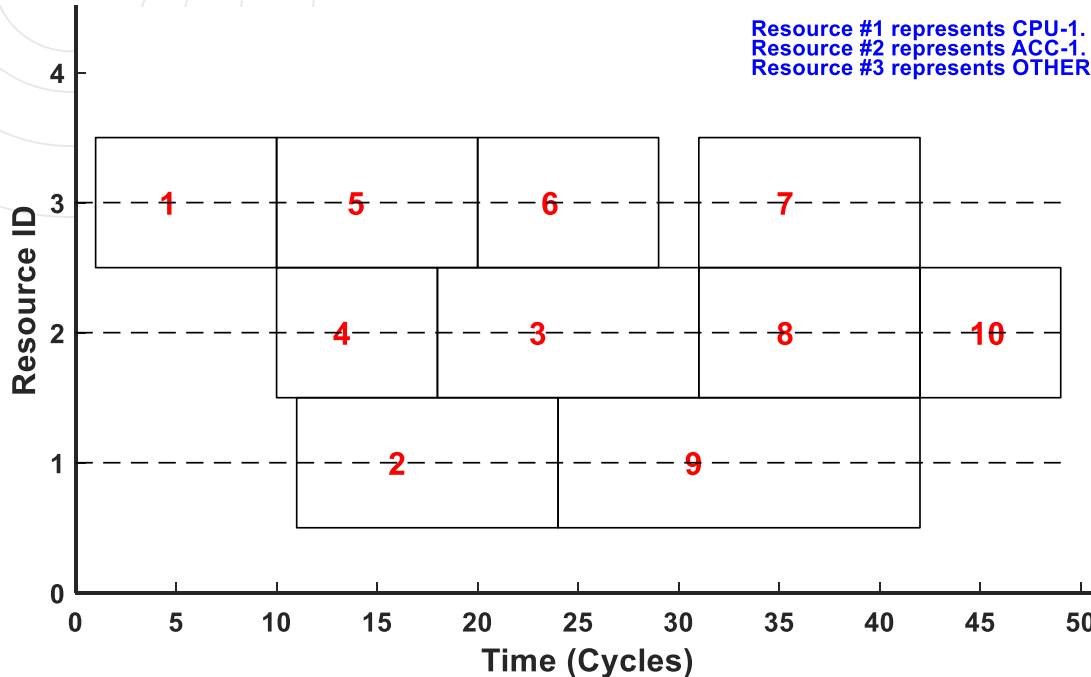
ILP: 73 cycles  
HEFT: 80 cycles

# Task Graph 5 Scheduling (cplexmilp)

(obj = tmax)

- Communication Time: 0!

Resource #1 represents CPU-1. (ID=10)  
Resource #2 represents ACC-1. (ID=100)  
Resource #3 represents OTHER-1. (ID=200)



- ILP: 48 cycles
- HEFT: ?? cycles

# Task Graph 5 Scheduling (**cplexmilp**)

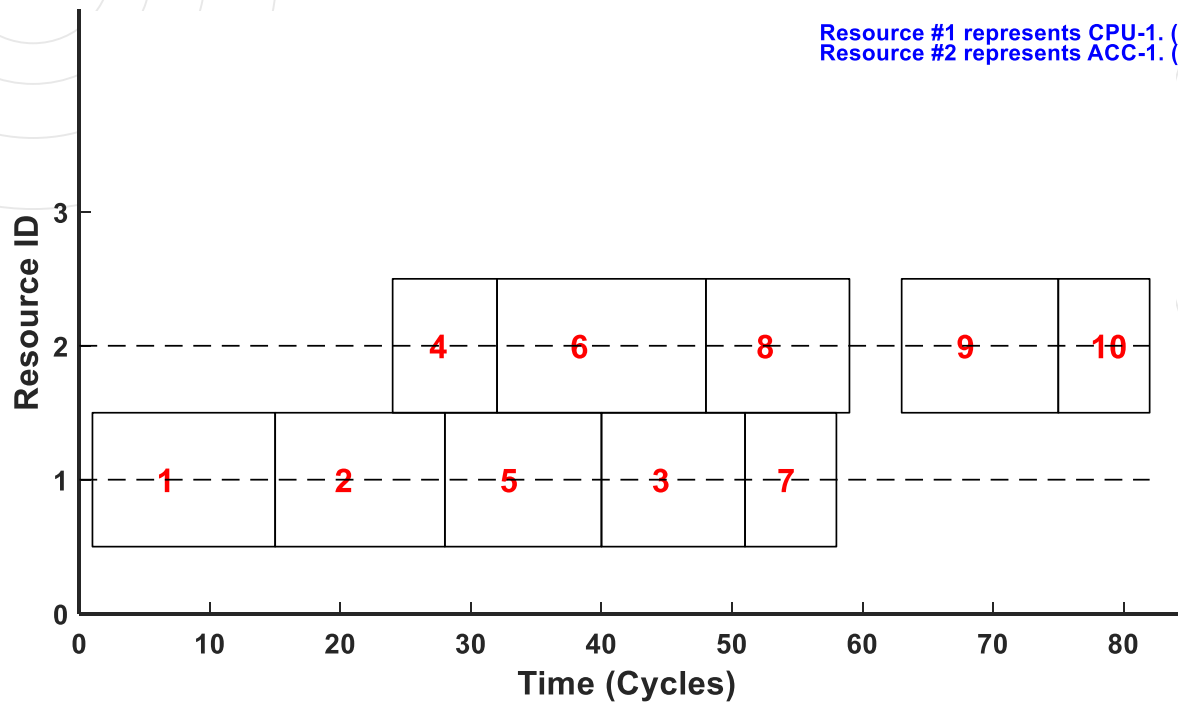
(**obj = tmax + energy**)

- Communication Power:

-- 0 for same type

-- 2 for different type

Resource #1 represents CPU-1. (ID=10)  
Resource #2 represents ACC-1. (ID=100)



**Cplexmilp:**  
81 cycles,  
470 units energy

# Task Graph 5 Scheduling (**cplexmilp**)

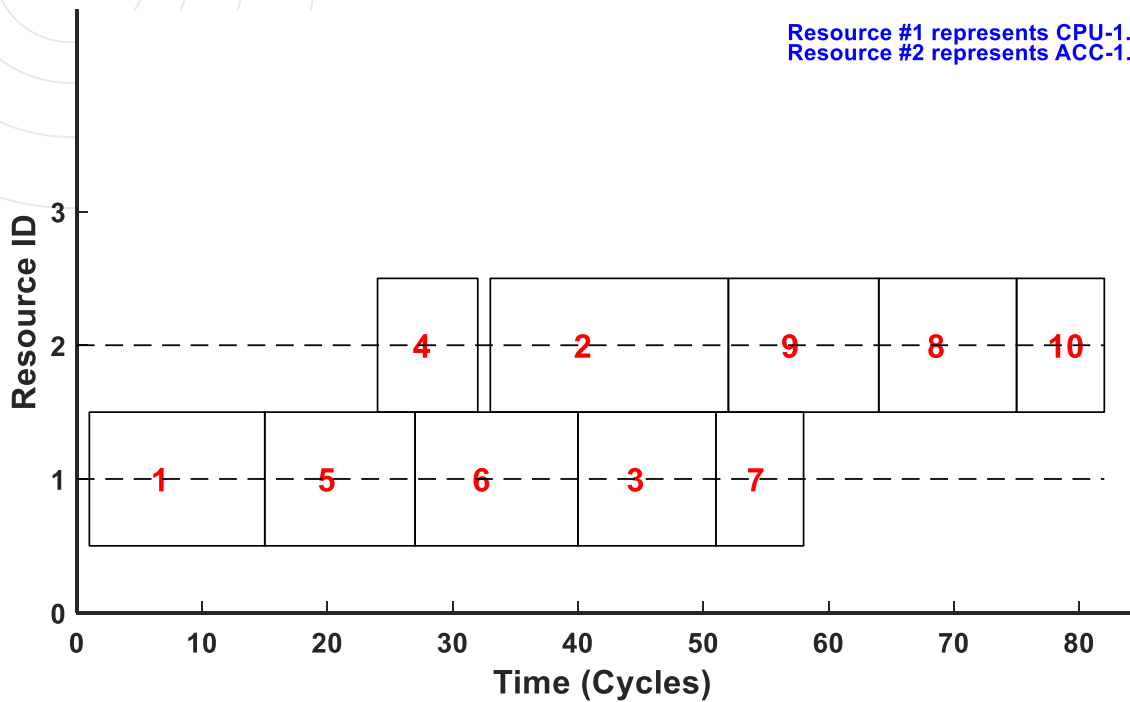
(**obj = tmax + energy**)

- Communication Power:

-- 0 for same type

-- 5 for different type

Resource #1 represents CPU-1. (ID=10)  
Resource #2 represents ACC-1. (ID=100)



**Cplexmilp:**

81 cycles,

724 units energy

# Task Graph 5 Scheduling (cplexmilp)

(obj = tmax + energy)

Performance Budget	Energy
< 73	NA
73	994
74	790
76	761
85	672
100	645

