

# INFORMATION RETRIEVAL – SHORT EXERCISES III – EVALUATION IN INFORMATION RETRIEVAL AND PAGERANK

I. Consider an information need for which there are 4 relevant documents in the collection. A system run on this collection returned the top 10 results for which the relevance is judged as follows (R – relevant; N – non-relevant):

k=	1	2	3	4	5	6	7	8	9	10
	R	N	R	N	N	N	N	N	R	R
$P@k$	$\frac{1}{1}$	$\frac{1}{2}$	$\frac{2}{3}$	$\frac{2}{4}$	$\frac{2}{5}$	$\frac{2}{6}$	$\frac{2}{7}$	$\frac{2}{8}$	$\frac{3}{9}$	$\frac{4}{10}$

What is the recall at 6 (R@6)? Answer:  $\frac{2}{4}$

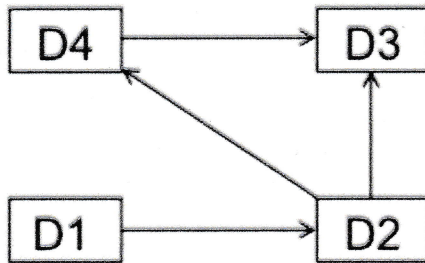
$$P@k = \frac{1}{k} \sum_{i=1}^k r_i$$

$$R@k = \frac{1}{\#rel} \sum_{i=1}^k r_i$$

$$MAP(q) = \frac{1}{\#rel} \sum_{i=1}^{\#rel} P@i$$

What is the Mean Average Precision? Answer:  $\frac{1}{4} \left( \frac{1}{1} + \frac{2}{3} + \frac{3}{9} + \frac{4}{10} \right) = \frac{1}{4} \cdot \frac{24}{10} = \frac{6}{10} = \frac{3}{5}$

II. Consider the web graph presented below to the left. It involves four pages D1-D4 and four links. Fill in the stochastic matrix M given to the right.



	D1	D2	D3	D4
D1	0	0	0	0
D2	1	0	0	0
D3	0	$\frac{1}{2}$	0	1
D4	0	$\frac{1}{2}$	0	0

Write the equation for PR(D3) without dumping factor  $q$ ? Answer:  $PR(D3) = \frac{1}{2} PR(D2) + PR(D4)$

Which page has the greatest PageRank (without computing the exact PR values)? Answer: D3

An oracle has evaluated D2 as trusted and D4 as spam. What is the starting vector  $d$  for TrustRank?

Answer:  $d = [ \overset{D1}{0}, \overset{D2}{1}, \overset{D3}{0}, \overset{D4}{0} ]$