

# INFORMATION RETRIEVAL – SHORT EXERCISES V – COLLABORATIVE FILTERING AND ADWORDS

I. Given the below user-item rating matrix, predict rating of user U7 for item I4:

	I1	I2	I3	I4	$sim(U7, U \cdot)$
U1	5	4	4	4	0.0
U2	5	3	7	3	1.0
U3	4	3	2	3	-0.5
U4	6	4	5	4	0.5
U5	3	4	2	4	-1.0
U6	4	3	5	3	1.0
U7	4	3	5	?	

Average

$$\frac{5+3+7}{3} = 5$$

$$\frac{4+3+5}{3} = 4$$

$$\bar{r}_{U7} = \frac{4+3+5}{3} = 4$$

a) Employ user-based CF with  $k=2$  and either simple average or weighted average?

Answer:  $U7(I4) = \bar{r}_{U7, I4} = \frac{3+3}{2} = 3$  here simple average and weighted average give the same result since both  $k=2$  users have the same similarity with user 7.

b) Employ user-based CF with  $k=2$  and modify U7's average rating by the weighted modification of its nearest neighbors averages:

$$\bar{r}_{a, i} = \bar{r}_a + \frac{\sum (r_{u, i} - \bar{r}_u) \cdot sim(a, u)}{\sum sim(a, u)}$$

$$\text{Answer: } U7(I4) = \bar{r}_{U7, I4} = 4 + \frac{1 \cdot (3-5) + 1 \cdot (3-4)}{2} = 4 + \frac{-2-1}{2} = 4 - \frac{3}{2} = \frac{5}{2} = 2,5$$

c) Which item should be analyzed to predict the rating when using item-based CF with  $k=1$ ? What would be the predicted rating?

they have the same ratings user-wise, so they have the highest possible cosine similarity = 1.

Answer: item <sup>1</sup>2 and prediction <sup>3</sup>

II. Four advertisers A, B, C, and D with a daily budget of \$2 bid for the following keywords (\$1 each):

A: w, x; B: x, z; C: x, y; D: y, z. Use a simplified version of BALANCE to select the ads for the following query stream (in the case of a tie use the following order for breaking it  $A > B > C > D$ ):

query stream	x	y	w	z	z	w	y	x
BALANCE	A	C	A	?B	?D	?—	?C	?B

A: 2	A: 1	A: 1	B: 2	B: 1	B: 1	B: 1	B: 1	B: 1
B: 2	B: 2	B: 2	C: 1	C: 1	C: 1	C: 1	C: 1	C: 1
C: 2	C: 2	C: 1	D: 2	D: 2	D: 1	D: 1	D: 1	D: 1
D: 2	D: 2	D: 2						

A: w, x  
B: x, z  
C: x, y  
D: y, z

no possible option using BALANCE here

$$\text{competitive ratio} = \frac{7}{8} \rightarrow 87,5\%$$