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import time
import heapq
import copy

In [2]:
UNIFORM_COST = 'Uniform Cost'
MISPLACED_TILES = 'Misplaced Tiles heuristic'
MANHATTAN_DIST = 'Manhattan distance heuristic'

heuristic_choices = {
    '1': UNIFORM_COST,
    '2': MISPLACED_TILES,
    '3': MANHATTAN_DIST
}

test_cases = [
    [[1, 2, 3],
     [4, 5, 6],
     [7, 8, 0]],

    [[1, 2, 3],
     [4, 5, 6],
     [0, 7, 8]],

    [[1, 2, 3],
     [5, 0, 6],
     [4, 7, 8]],

    [[1, 3, 6],
     [5, 0, 2],
     [4, 8, 2]],

    [[1, 3, 6],
     [5, 0, 7],
     [4, 8, 2]],

    [[1, 6, 7],
     [5, 0, 3],
     [4, 8, 2]],

    [[7, 1, 2],
     [4, 8, 5],
     [6, 3, 0]],

    [[0, 7, 2],
     [4, 6, 1],
     [3, 5, 8]],
]

In [3]:
print(test_cases)

[[[1, 2, 3], [4, 5, 6], [7, 8, 0]], [[1, 2, 3], [4, 5, 6], [0, 7, 8]], [[1, 2, 3], [5, 0, 6], [4, 7, 8]]]

In [4]:
# The class is used to maintain the state of any orientation during the Eight Puzzle simulation
class EightPuzzleNode:
    def __init__(self, board, heuristic, depth):
        self.board = board
        self.heuristic = heuristic
        self.goal_state = \
            [[1, 2, 3],
             [4, 5, 6],
             [7, 8, 0]]
        self.value_position_mapping = self._getValuePositionMapping()
        self_blankCellIndex = self._getBlankCellIndex()
        self_depth = depth
        self_calculateTotalCost()

    def getBoard(self):
        return copy.deepcopy(self._board)

    # maps the goal position of a tile with a number from 1-8
    def _getValuePositionMapping(self):
        value_position_mapping = {}
        for row_idx in range(3):
            for col_idx in range(3):
                value_position_mapping[self_goal_state[row_idx][col_idx]] = \
                    (row_idx, col_idx)

        return value_position_mapping

    # returns the depth of the state
    def getDepth(self):
        return self._depth

    # returns the heuristic used
    def getHeuristic(self):
        return self._heuristic

    # sets the blank cell index of the state
    def _getBlankCellIndex(self):
        for row_idx in range(3):
            for col_idx in range(3):
                if self._board[row_idx][col_idx] == 0:
                    return row_idx, col_idx

        # returns the blank cell index of the state
    def getBlankCellIndex(self):
        return self._blankCellIndex

    # checks if the state is in a solved/goal orientation
    def isSolved(self):
        for row_idx in range(3):
            if self._board[row_idx] != self_goal_state[row_idx]:
                return False

        return True

    # prints the current state
    def printCurrentState(self):
        for row_idx in range(3):
            print(self._board[row_idx])

    # calculates the number of misplaced tiles
    def _findMisplacedTilesCount(self):
        misplaced_tiles_count = 0
        for row_idx in range(3):
            for col_idx in range(3):
                if self._board[row_idx][col_idx] and \
                    self._board[row_idx][col_idx] != self_goal_state[row_idx][col_idx]:
                    misplaced_tiles_count += 1

        print(misplaced_tiles_count)
        return misplaced_tiles_count

    # calculates the manhattan distance of the current state
    def _findManhattanDistance(self):
        manhattan_distance = 0
        for row_idx in range(3):
            for col_idx in range(3):
                if self._board[row_idx][col_idx] and \
                    self._board[row_idx][col_idx] != self_goal_state[row_idx][col_idx]:
                    goal_row_idx, goal_col_idx = \
                        self._goal_value_position_mapping[ self._board[row_idx][col_idx] ]
                    distance = abs(row_idx - goal_row_idx) + abs(col_idx - goal_col_idx)
                    manhattan_distance += distance

        print(manhattan_distance)
        return manhattan_distance

    # calculates the total cost according to the heuristic used for the search
    def _calculateTotalCost(self):
        if self.heuristic == UNIFORM_COST:
            self_total_cost = self_depth

        elif self.heuristic == MISPLACED_TILES:
            self_total_cost = self_depth + self._findMisplacedTilesCount()

        else:
            self_total_cost = self_depth + self._findManhattanDistance()

        # returns the total cost calculated
    def getTotalCost(self):
        return self._total_cost

    # returns the current cost and heuristic cost
    def getCurrentAndHeuristicCost(self):
        if self.heuristic == UNIFORM_COST:
            return self_depth, 0

        elif self.heuristic == MISPLACED_TILES:
            return self_depth, self._findMisplacedTilesCount()

        else:
            return self_depth, self._findManhattanDistance()

    # comparator function used for the priority queue
    def __lt__(self, nxt):
        if self.heuristic != UNIFORM_COST:
            if self.getTotalCost() == nxt.getTotalCost():
                return self.getDepth() < nxt.getDepth()

            return self.getTotalCost() < nxt.getTotalCost()

In [5]:
# gets selection of heuristic to be used from the user
def select_heuristic_search_approach():
    while True:
        heuristic_choice = input('Press 1 to select Uniform Cost Search\n' + \
                                'Press 2 to select Misplaced Tile Heuristic search\n' + \
                                'Press 3 to select Manhattan Distance Search\n').strip()

        if heuristic_choice not in heuristic_choices:
            print('Wrong selection')
            continue

        else:
            print(heuristic_choices[heuristic_choice], ' selected')
            return heuristic_choices[heuristic_choice]

# gets input of a new puzzle from the user
def get_new_puzzle():
    print('You will be prompted to enter each row of three rows of the puzzle\n' + \
          'You need to use a zero to represent the blank in your puzzle\n' + \
          'Each of the row can contain three digits delimited by spaces\n' + \
          'Please enter a valid puzzle')

    puzzle = []
    for row_index in range(3):
        row_values = input('Enter row ' + str(row_index + 1) + '\n')
        puzzle.append(list(map(int, row_values.split()))))

    return puzzle

# converts the board state to a string to maintain the repeated states of the solution
def getPuzzleString(board):
    puzzle_string = ''
    for row_idx in range(3):
        for col_idx in range(3):
            puzzle_string += str(board[row_idx][col_idx])

    return puzzle_string

# creates a priority queue
def makeQueue(nodes):
    nodes = [puzzle]
    heapq.heapify(nodes)

    return nodes

# finds the expanded nodes from the given node
def getNewNode(blank_row_idx, blank_col_idx, board, heuristic_choice, depth,
               new_blank_row_idx, new_blank_col_idx, repeated_states):
    if 0 <= new_blank_row_idx < 2 and 0 <= new_blank_col_idx < 2:
        new_board = copy.deepcopy(board)
        new_board[blank_row_idx][blank_col_idx], \
            new_board[new_blank_row_idx][new_blank_col_idx] = \
            board[new_blank_row_idx][new_blank_col_idx], \
            board[blank_row_idx][blank_col_idx]

        new_puzzle_string = getPuzzleString(new_board)
        if new_puzzle_string not in repeated_states:
            return EightPuzzleNode(new_board, heuristic_choice, depth)

    return None

# returns the expanded nodes from the given node
def getHeurNodes(puzzle_node, repeated_states):
    blank_row_idx, blank_col_idx = puzzle_node.getBlankCellIndex()
    board = puzzle_node.getBoard()
    heuristic_choice = puzzle_node.getHeuristic()
    depth = puzzle_node.getDepth()

    new_nodes = []

    # left
    new_node = getNewNode(blank_row_idx, blank_col_idx, board, heuristic_choice,
                          depth + 1, blank_row_idx, blank_col_idx - 1,
                          repeated_states)
    if not isinstance(new_node, type(None)):
        new_nodes.append(new_node)

    # right
    new_node = getNewNode(blank_row_idx, blank_col_idx, board, heuristic_choice,
                          depth + 1, blank_row_idx, blank_col_idx + 1,
                          repeated_states)
    if not isinstance(new_node, type(None)):
        new_nodes.append(new_node)

    # top
    new_node = getNewNode(blank_row_idx, blank_col_idx, board, heuristic_choice,
                          depth + 1, blank_row_idx - 1, blank_col_idx,
                          repeated_states)
    if not isinstance(new_node, type(None)):
        new_nodes.append(new_node)

    # bottom
    new_node = getNewNode(blank_row_idx, blank_col_idx, board, heuristic_choice,
                          depth + 1, blank_row_idx + 1, blank_col_idx,
                          repeated_states)
    if not isinstance(new_node, type(None)):
        new_nodes.append(new_node)

    return new_nodes

# returns the solution for the given puzzle node
def solvePuzzle(puzzle_node):
    max_queue_size = 0
    depth = -1
    expanded_node_count = 0
    start_time = time.time()

    repeated_states = {}
    nodes = makeQueue(puzzle_node)
    repeated_states[getPuzzleString(puzzle_node.getBoard())] = True

    while True:
        if len(nodes) > max_queue_size:
            max_queue_size = len(nodes)

        if len(nodes) == 0:
            is_solved = False
            break

        node = heapq.heappop(nodes)
        g_n, h_n = node.getCurrentAndHeuristicCost()
        print('The best state to expand with a g(n) = ' + g_n + ', g(n) = ' + h_n)
        node.printCurrentState()

        if node.isSolved():
            depth = node.getDepth()
            is_solved = True
            break

        else:
            new_nodes = getHeurNodes(node, repeated_states)
            if len(new_nodes) > 0:
                expanded_node_count += 1

                for new_node in new_nodes:
                    heapq.heappush(nodes, new_node)
                    print(new_node.printCurrentState())

    end_time = time.time()
    execution_time_in_seconds = end_time - start_time

    return (is_solved, max_queue_size, depth,
            expanded_node_count, "(%.1f)%" % format(execution_time_in_seconds))

In [6]:
# driver function
if __name__ == '__main__':
    while True:
        heuristic_choice = select_heuristic_search_approach()

        input_case = input('Press 1 to run eight puzzle simulation with default test cases\n' + \
                            'Press 2 to enter a new puzzle\n' + \
                            'Press any key to exit\n').strip()

        if input_case == '1':
            counter = 0
            for board in test_cases:
                puzzle = EightPuzzleNode(board, heuristic_choice, 0)

                print()
                print("Puzzle Test Case: ", counter + 1)
                puzzle.printCurrentState()
                print(heuristic_choice)

                is_solved, max_queue_size, depth, \
                    expanded_node_count, execution_time_in_seconds = \
                        solvePuzzle(puzzle)

                print('is_solved = ', is_solved, ' max_queue_size = ', max_queue_size,
                      ' depth = ', depth, ' expanded_node_count = ', expanded_node_count,
                      ' execution_time_in_seconds = ', execution_time_in_seconds)

                counter += 1

            elif input_case == '2':
                board = get_new_puzzle()
                puzzle = EightPuzzleNode(board, heuristic_choice, 0)

                print("Puzzle Test Case: ", counter + 1)
                puzzle.printCurrentState()
                print(heuristic_choice)

                is_solved, max_queue_size, depth, \
                    expanded_node_count, execution_time_in_seconds = \
                        solvePuzzle(puzzle)

                print('is_solved = ', is_solved, ' max_queue_size = ', max_queue_size,
                      ' depth = ', depth, ' expanded_node_count = ', expanded_node_count,
                      ' execution_time_in_seconds = ', execution_time_in_seconds)

                break

            print('Thank you')
            break

Press 1 to select Uniform Cost Search
Press 2 to select Misplaced Tile Heuristic search
Press 3 to select Manhattan Distance Search
3
Manhattan distance heuristic selected
Press 1 to run eight puzzle simulation with default test cases
Press 2 to enter a new puzzle
Press any key to exit
1

Puzzle Test Case: 1
[[1, 2, 3],
 [4, 5, 6],
 [7, 8, 0]]
Manhattan distance heuristic
The best state to expand with a g(n) = 0 and h(n) = 0
[[1, 2, 3],
 [4, 5, 6],
 [0, 7, 8]]
is_solved = True max_queue_size = 1 depth = 0 expanded_node_count = 0 execution_time_in_seconds = 0.0s

Puzzle Test Case: 2
[[1, 2, 3],
 [4, 5, 6],
 [0, 7, 8]]
Manhattan distance heuristic
The best state to expand with a g(n) = 0 and h(n) = 2
[[1, 2, 3],
 [4, 5, 6],
 [0, 7, 8]]
The best state to expand with a g(n) = 1 and h(n) = 1
[[1, 2, 3],
 [7, 0, 8],
 [4, 5, 6]]
The best state to expand with a g(n) = 2 and h(n) = 0
[[1, 2, 3],
 [4, 5, 6],
 [0, 7, 8]]
is_solved = True max_queue_size = 3 depth = 2 expanded_node_count = 2 execution_time_in_seconds = 0.0s

Puzzle Test Case: 3
[[1, 2, 3],
 [5, 0, 6],
 [4, 7, 8]]
Manhattan distance heuristic
The best state to expand with a g(n) = 0 and h(n) = 4
[[1, 2, 3],
 [5, 0, 6],
 [4, 7, 8]]
The best state to expand with a g(n) = 1 and h(n) = 3
[[1, 2, 3],
 [4, 7, 8],
 [0, 5, 6]]
The best state to expand with a g(n) = 2 and h(n) = 2
[[1, 2, 3],
 [4, 5, 6],
 [0, 7, 8]]
The best state to expand with a g(n) = 3 and h(n) = 1
[[1, 2, 3],
 [7, 0, 8],
 [4, 5, 6]]
The best state to expand with a g(n) = 4 and h(n) = 0
[[1, 2, 3],
 [4, 5, 6],
 [0, 7, 8]]
is_solved = True max_queue_size = 8 depth = 4 expanded_node_count = 4 execution_time_in_seconds = 0.0s
Press 1 to select Uniform Cost Search
Press 2 to select Misplaced Tile Heuristic search
Press 3 to select Manhattan Distance Search
2
Misplaced tiles heuristic selected
Press 1 to run eight puzzle simulation with default test cases
Press 2 to enter a new puzzle
Press any key to exit
k
Thank you

In [7]:
#

In [ ]:
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