## **PHY 316M**

Marc Matvienko

October 24, 2017

# 1 Capacitors

$$C = |\frac{Q}{V}|$$

## 2 Current

Is the flow of charge in on direction. Current:

$$I = \frac{\Delta Q}{\Delta t} = \frac{\delta Q}{\delta t}$$

Current Density (current per unit area):  $J = \frac{I}{A}$  $n = \text{charge carriere density}, q = \text{charge per carrier}, v_d = \text{drift velocity This can give us}, \boxed{J = nqv_d}$ 

#### 2.1 Ohm's Law

Usually we see Ohm's law in different forms, i.e. for a particular chunk. Consinder some block with volume  $A \cdot l$ , some source of energy(battery) forces current thorugh by applying an electric field.

For a uniform electric field:  $V = E \cdot l$ 

$$J = \frac{I}{A}$$
$$= \sigma E$$
$$= \sigma \frac{V}{I}$$

$$\frac{V}{I} = \frac{1}{\sigma} \frac{l}{A} = \rho \frac{l}{A} = R = \text{resistance}$$

 $\left[ \begin{array}{c} V \\ \overline{I} \end{array} = R \right]$  Resistance is not resistivity (opisiton of current flow of a particular material  $[\rho]$ ) Ohmic material is a material that has a constant slope on Voltage to Current graph. Most common materials like copper behave like this.

**Example** The resistivity of nichrome wire (heaters, toasters) is  $1.5 \times 10^{-6} \Omega m$ . If a household voltage of 115V is applied acros a 0.2mm radius write, 1.0m long, what current flows?

$$R=\rho\frac{l}{A}=\rho\frac{l}{\pi r^2}=\frac{1.5\times 10^{-6}\Omega m\cdot 1.0m}{(\pi(2\times 10^{-4}m)^2))}=11.9\Omega$$

### 2.2 Model for electric conduction

- electron unergo many rapid ocllision when E=0
- when  $E \neq 0$ , the electrons accelrate between collisions
- $F = ma = qE \Longrightarrow a = \frac{qE}{m}$
- $v = v_0 + at = v_0 + \frac{qE}{m}t$

Let  $\tau =$  average collision time =  $R \cdot C$ the  $v_d = v_{avg} = < v_0 > + \frac{qE}{m} \tau$ so,  $J = nqv_d = nq = \frac{qE}{m} \tau = \sigma E$ so conductivity  $\sigma = \frac{nq^2\tau}{m}$ 

Called the Drude model or free electron mode

$$\sigma = \frac{nq^2\tau}{m}$$

$$\frac{1}{\sigma} = \rho$$

**Example** Assume for copper that each atom donates one free electron. What is the average time between collision for electrons in copper.? Given:

- Density=  $8.98 \frac{g}{cm^3}$
- Atomic Weight =  $63.54 \frac{g}{mole}$
- $\rho = 1.7 \times 10^{-8} \Omega \cdot m$

$$\tau = \frac{m}{nq^2\rho} = \frac{9.14 \times 10^{-31} kg}{(8.5 \times 10^2 2)(1.6 \times 10^{-19})^2 1.7 \times 10^{-8} \Omega m} = 2.5 \times 10^{-14} s$$

# 2.3 Temerature Dependence of resistivity

- resistivities tabulated for 20 °celsius
- for metals,  $\rho$  is higher and T is higher
- $\alpha = \text{linear temprature coefficient}$
- over some range,  $\rho = \rho_0(1 + \alpha(T T_0))$

As T increases, the scattering time decreases due to collisions with vibrating atoms

At higher temperatures the  $\rho$  to temperature graph is linear. But at the beginning there is residual resistivity due to impurities.

**Semiconductors** The number of carriers decreases as the temperature decreases, this means that all the electrons are sticking to their atoms.

### 3 Resistors in Series and Parallel

Circuit symbol: 
$$---$$

#### 3.1 Resistors in series

For resistors in series the resistivities add

$$R_{tot} = R_1 + R_2 + \dots$$
 
$$R_{tot} = \frac{V}{I} = \frac{V_1}{I_1} + \frac{V_2}{I_2} = R_1 + R_2$$

The current (I) is the same everywhere too. Resistors don't add in parallel. Capacitors do.

$$V = V_1 + V_2$$

The voltage divider

$$V_1 = I \cdot R_1 = \frac{V}{R_1 + R_2} \cdot R_1$$

#### 3.2 Resistors in parallel

For resisitors in parallel halve the resistance if two exact resistors are put in parallel

- In parallel have the same voltage across each element
- In parallel also the current divides among branches

$$I = I_1 + I_2 = \frac{V}{R_1} + \frac{V}{R_2} \Longrightarrow R_{tot} = \frac{V}{I} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$

**Superconductors** Electrons pair up and when electron jumps to the lattice another electrons pulls it right back.

### 3.3 Resistors Disipate Energy

Electrons undergo collisions, and give up energy as heat. A steady release of current (I) causes a steady realease of energy.

$$\Delta U = \Delta Q V$$

Better to discess the rate, which is really known as:

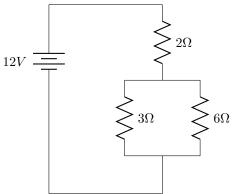
Power = 
$$P = \frac{\Delta U}{\Delta t} = \frac{\Delta U}{\Delta t}V = IV$$

$$P = IV = I^2 R = \frac{V^2}{R}$$

This power is also known as Joule heating.

**Putting this into practice:** many circuits can be analyzed with just Ohm's Law and Resistance.

- What is the total power delivered?
- What is the power dissipated in each R?



$$P_{\text{dissapated in } 3\Omega} = \frac{V_3^2}{R} = \frac{(6V)^2}{3\Omega} = 12W$$

### 3.4 Direct Current Circuits

Real battery is an ideal  $\mathscr{E}\mathrm{MF}$  plus intended resistance

Batteries are a source of voltage ———

Source of voltage = "electromotive force" =  $\mathscr{E}MF = \mathscr{E}$ 

$$V = \mathcal{E} - Ir$$

<sup>&</sup>quot;Open-circuit voltage", where I=0

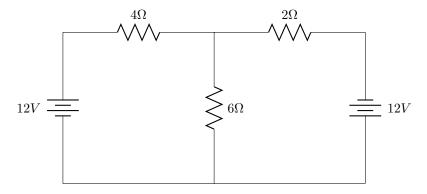
Analysis of circuits Any circuit can be analyzed with Kirchhoffs Rules:

- Junction Rule, algebraic sum of currents into a junction = sum of currents  $\Sigma i_{in} = \Sigma i_{out}$
- Loop Rule, algebraic sum of voltages around any closed loop is zero. Where voltage rises are positive (- to +) and votlage drops are negative (+ to -)

For resistors the current directino determines voltage drop(negative)

#### Example

- What is the current in the  $6\Omega$  resisitor?
- Is it flowing up or down?



- (I) Junction at A:  $i_1 = i_2 + i_3$
- (II) Loop A:  $12V i_1(4\Omega) i_3(6\Omega) = 0$
- (III) Loop B:  $I_3(6\Omega) i_2(2\Omega) + 12V = 0$  $i_3 = \frac{-12V}{22\Omega} = -\frac{6}{11}A$

### 2 other techniques:

- i) same, except use ficticious "loop currents"
- ii) Source suppressing can look at effects of sources seperately

**Next: Circuits with Capacitors** will see time-depedent behavior Before "transient phenomena", look at *Steady-state*: "after a long time". The capacitor starts acting like the current is 0.

# 4 Magnetism

We saw:

$$F = qv \frac{\mu_0 I}{2\pi r} = 0$$

for  $\vec{v}$  tangent to circle. where  $\mu_0 = 4\pi \times 10^{-7} \frac{Ns^2}{C^2}$ Rewrite this as

$$\boxed{\vec{F} = q\vec{v} \times \vec{B}}$$

where  $B = \frac{\mu_0 I}{2\pi r}$  magentic field due to a long wire where direction of  $\vec{B}$  is tangent to circle.

If also electric force, combination of electric and magnetic force is called "Lorentz Force"  $\,$ 

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

 $\vec{F} = q\vec{v} \times \vec{B}$ 

- Like  $\vec{E}, \vec{F}$  opposite for +q, -q
- Depends on  $\vec{v}: \vec{F} = 0$  for  $\vec{v} = 0$
- Direction  $\vec{F} = q\vec{v} \times \vec{B}$  given by right hand rule

Magnetic field does no work because the magnetic force is perpendualar to displacement.

So  $\vec{B}$  changes direction of  $\vec{v}$  but not its magnitude  $(KE = \frac{1}{2}mv^2)$ Unit of B =  $\frac{Ns}{Cm}$  = tesla = T also gauss =  $G = 10^{-4}T$ 

# 4.1 Evaluating Cross Products

- 1. Get general equation by expaning determinant  $\begin{vmatrix} i & j & k \\ v_x & v_y & v_z \\ B_x & B_y & B_z \end{vmatrix} = \vec{v} \times \vec{B} = i(v_y B_z v_z B_y) j(v_x B_z v_z B_x) + k(v_x B_y v_y B_x)$
- 2. Just multiply out. know that  $i \times j = k$  and that  $j \times i = -k$
- 5. Magnetic field does no work

## 5 Exam

Chapters 25-28