

\*Please email your programming write-up (pdf) and source code in a single zip file to our TA by the due date.

Each student will turn in an individual assignment. You are allowed to use any high-level programming language of preference, however the use of Python is strongly encouraged (C++, Java, Matlab, etc., are also fine). You may use standard libraries (NumPy, math and plotting libraries, etc.) for this assignment, with the exception that the **main algorithm in each part** (as clearly identified in the instructions) **must be written explicitly** by you. In other words, for example, in Part 1 you can't simply invoke the function applying Sobel filters from the Opencv library, etc.

This assignment consists of (3) parts:

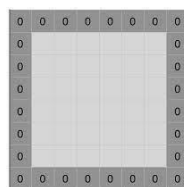
### Part 1

*Dataset:* Two test images are provided: filter1\_img.jpg and filter2\_img.jpg; the images are available on D2L.

(i) For the two test images provided, write a simple program to explicitly apply a *Gaussian filter*. Use the following standard 3x3 and 5x5 Gaussian filters, given by:

$$\frac{1}{16} \cdot \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix} \quad \frac{1}{273} \cdot \begin{bmatrix} 1 & 4 & 7 & 4 & 1 \\ 4 & 16 & 26 & 16 & 4 \\ 7 & 26 & 41 & 26 & 7 \\ 4 & 16 & 26 & 16 & 4 \\ 1 & 4 & 7 & 4 & 1 \end{bmatrix}$$

This means that you will need to convolve each filter with different patches in the test images; please use a stride=1 in your code and apply zero padding of width 1 when using the 3x3 filter and zero padding of width 2 for the 5x5 filter. For instance, zero padding of width 1 results in:



Zero-padding added to image

(ii) For the same test images, write a program to apply DoG (*derivative of Gaussian*)  $g_x$  and  $g_y$  filters (use stride=1 and padding=1):

$$g_x = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}, g_y = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

(iii) Finally, compute the result of the *Sobel filter* for the test images:

$$\mathbf{X} * \mathbf{G} = \sqrt{(\mathbf{X} * \mathbf{g}_x)^2 + (\mathbf{X} * \mathbf{g}_y)^2}$$

where  $\mathbf{X}$  represents the test image.

\*For part 1, in your write-up show the “before” and “after” of the original image(s) and the resultant image(s) after applying the stated convolutions.

## **Part 2**

*Dataset:* A 2D dataset generated by sampling 3 Gaussian distributions is provided. There are 500 points from each Gaussian, ordered together in the file. The dataset is posted on D2L with this assignment.

(i) Implement the standard version of the K-Means algorithm as described in lecture. The initial starting points for the K cluster means can be K randomly selected data points. You should have an option to run the algorithm  $r$  times from  $r$  different randomly chosen initializations (e.g.,  $r = 10$ ), where you then select the solution that gives the lowest sum of squares error over the  $r$  runs. Run the algorithm for K=2, K=3, and K=4 and report the sum of squares error for each of these models. Please include a 2-d plot of several different iterations of your algorithm with the data points and clusters.

(ii) For the two test images provided: Kmean\_img1.jpg and Kmean\_img2.jpg, execute your K-means algorithm from part 2(i) in the RGB color space (i.e. in 3D space) with K=5 and K=10, respectively.

\*For part 2(i), in your write-up include the visualizations of the execution of K-means for K=2, 3, and 4 on the Gaussian data; for part 2(ii), include a visualization of your K-means clustering in the color space of each image for K=5 and K=10.

## **Part 3**

*Dataset:* Two test images are provided: SIFT1\_img.jpg and SIFT2\_img.jpg.

(i) Using a built-in library (e.g., OpenCV), calculate the **SIFT features** for the test images. Visualize the SIFT features for each of the test images by superimposing the locations of these SIFT-based keypoints on each test image, respectively (if the library includes a visualization of the descriptor orientation, etc., you may also include this in the visualization).

From the generated set of SIFT keypoints for the first test image, determine the keypoint matches between the two images. To do this, calculate the nearest-neighbor (NN) for each keypoint detected in image 1 with respect to the set of keypoints detected for image 2. Here the nearest-neighbor criterion is the **minimum L2 distance** between the key point SIFT vectors. Next you will determine the “top 10%” of keypoint matches. Once you have determined the NN keypoint (in image 2) associated with each keypoint in image 1, determine the top 10% of the image 1 keypoints and their matches by retaining only the pairs of keypoints with that represent the top 10% per minimum L2 distance.

\*For part 3, in your write-up include visualizations of all of the SIFT keypoints detected for the test images. After pruning the bottom 90% of matches, include a visualization of the top 10% of keypoint matches that correlates each of the remaining keypoints in image 1 with its corresponding keypoint in image 2 (this

visualization can be done through a common color scheme so that matching keypoints have the same color, or by drawing lines between matching keypoints as shown below).

