

# Chapter 4 - Methods of Analysis of Resistive Circuits

## Lecture 10 Section 4.3

### MEMS 0031 Electrical Circuits

Mechanical Engineering and Materials Science Department  
University of Pittsburgh



# Student Learning Objectives

Chapter 4 -  
Methods of Analysis  
of Resistive Circuits

MEMS 0031

Learning Objectives

4.3 Node Voltage  
Analysis with  
Independent  
Voltage Sources

Summary

At the end of the lecture, students should be able to:

- ▶ Apply Node Voltage Analysis (NVA) to circuits with independent current and voltage sources



# NVA with Independent VS

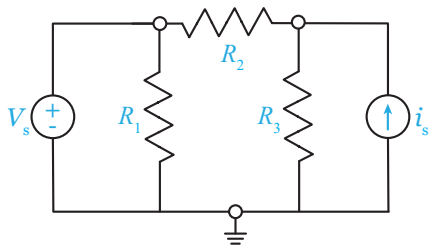
- ▶ By adding an independent VS, we remove a degree of freedom, for we are prescribing a node voltage
- ▶ Thus the number of KCL equations is as follows:

$$\# \text{ KCL Eqns.} = N - \# \text{ VS} - 1$$

- ▶ Additionally, we will introduce the concept of a “supernode” - two nodes connected by a VS



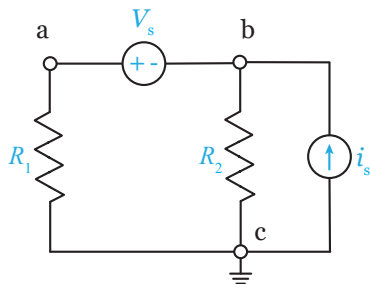
# Example #1



- Use NVA to determine the node voltages, symbolically:



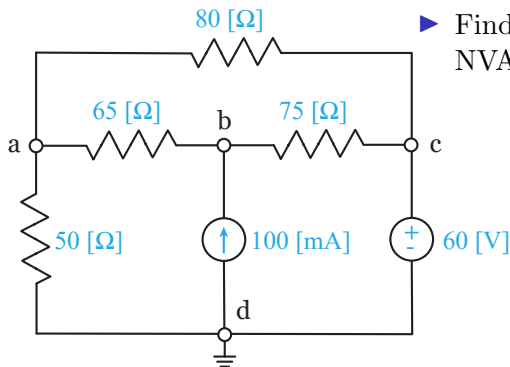
## Example #2 - Supernode



► Determine the voltage at node  $b$ :



## Example #3

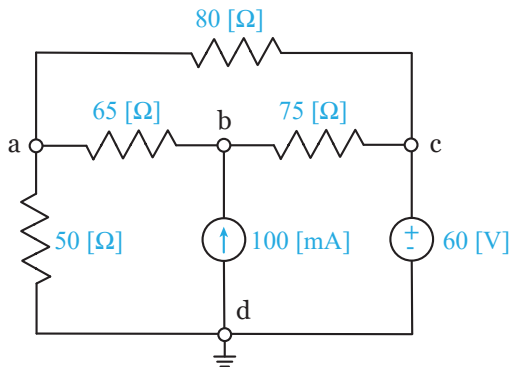


## Example #3

### Learning Objectives

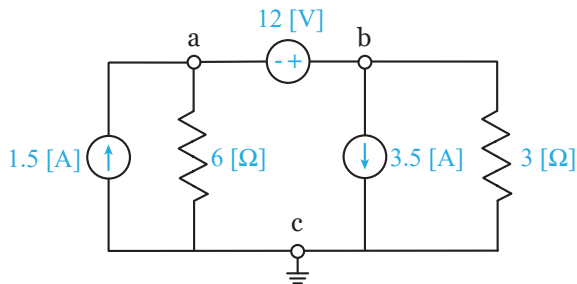
#### 4.3 Node Voltage Analysis with Independent Voltage Sources

#### Summary



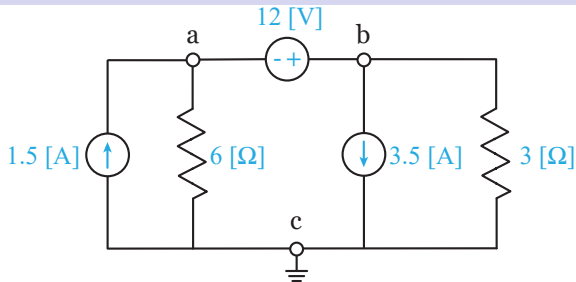
# Example #4

- Find node voltages via NVA:

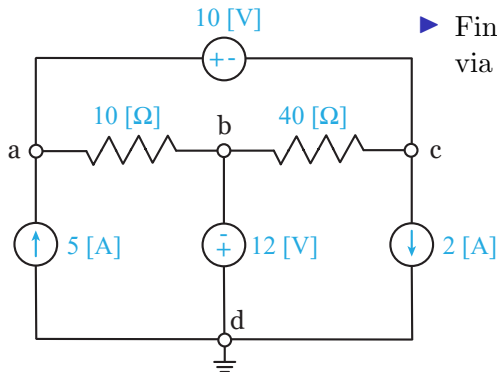




## Example #4



## Example #5



► Find node voltages  
via NVA:

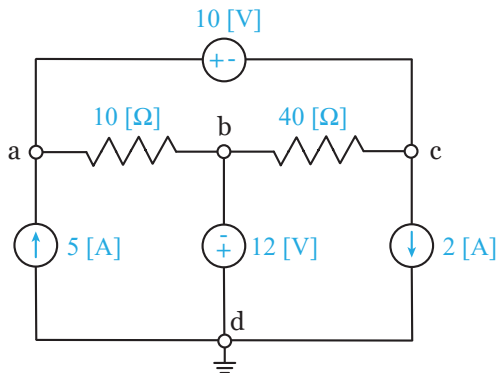
### Learning Objectives

#### 4.3 Node Voltage Analysis with Independent Voltage Sources

### Summary



## Example #5



# Student Learning Objectives

At the end of the lecture, students should be able to:

- ▶ Apply Node Voltage Analysis (NVA) to circuits with independent current sources
  - ▶ NVA requires the sole use of KCL. We construct  $N - 1 - \#VS$  KCL equations, applied at non-zero and non-specified, and relate the currents to voltages using Ohm's law.
  - ▶ A voltage source between two non-zero nodes creates a supernode, i.e. an equation that relates two node voltages - apply KCL here!
  - ▶ A voltage source between a non-zero and zero-voltage nodes specifies the non-zero node voltage.



# Suggested Problems

At the end of the lecture, students should be able to:

- ▶ 4.3-1, 4.3-2, 4.3-3, 4.3-4, 4.3-5, 4.3-6, 4.3-7, 4.3-10, 4.3-12

