

# Chapter 4 - Methods of Analysis of Resistive Circuits

## Lecture 11 Section 4.4

### MEMS 0031 Electrical Circuits

Mechanical Engineering and Materials Science Department  
University of Pittsburgh



# Student Learning Objectives

Chapter 4 -  
Methods of Analysis  
of Resistive Circuits

MEMS 0031

Learning Objectives

4.4 Node Voltage  
Analysis with  
Independent  
Voltage Sources

Summary

At the end of the lecture, students should be able to:

- ▶ Apply Node Voltage Analysis (NVA) to circuits with dependent sources



# NVA with Independent VS

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4.4 Node Voltage  
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Summary

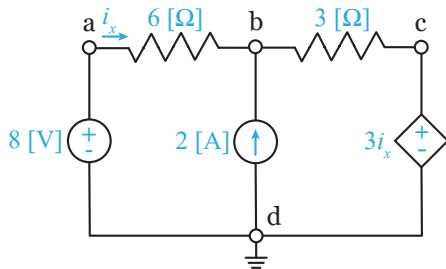
- ▶ By adding an dependent source, we must express behavior (voltage) in terms of node voltages.
- ▶ The number of KCL equations still holds as:

$$\# \text{ KCL Eqns.} = N - \# \text{ VS} - 1$$

- ▶ “Supernode” formulation is still valid



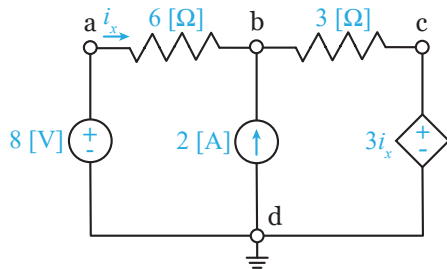
# Example #1



► Use NVA to determine the node voltages:



# Example #1



► Solution:

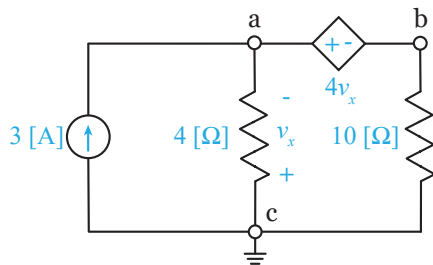
Learning Objectives

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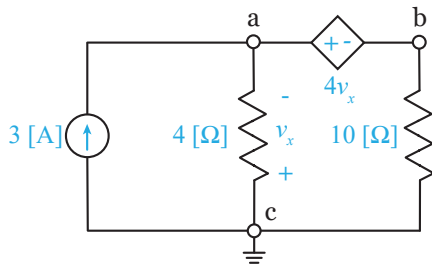
## Example #2



► Determine the voltage at  $a$  and  $b$ :



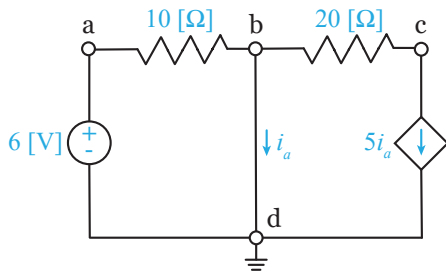
## Example #2



► Solution:



## Example #3

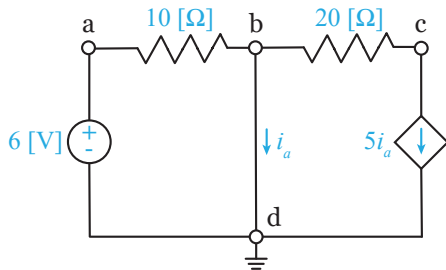


► Determine all unknowns:





## Example #3



► Solution:



# Student Learning Objectives

At the end of the lecture, students should be able to:

- ▶ Apply Node Voltage Analysis (NVA) to circuits with independent current sources
  - ▶ NVA requires the sole use of KCL. We construct  $N - 1 - \#VS$  KCL equations, applied at non-zero and non-specified, and relate the currents to voltages using Ohm's law.
  - ▶ A voltage source (independent and dependent) between two non-zero nodes creates a supernode, i.e. an equation that relates two node voltages - apply KCL here!
  - ▶ A voltage source between a non-zero and zero-voltage nodes specifies the non-zero node voltage.



# Suggested Problems

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4.4 Node Voltage  
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Voltage Sources

Summary

At the end of the lecture, students should be able to:

- ▶ 4.4-1, 4.4-2, 4.4-3, 4.4-4, 4.4-5, 4.4-6, 4.4-7, 4.4-13, 4.4-14

