

# Chapter 4 - Methods of Analysis of Resistive Circuits

## Lecture 9 Section 4.2

MEMS 0031

Learning Objectives

4.2 Node Voltage  
Analysis with  
Independent  
Current Sources

Summary

MEMS 0031 Electrical Circuits

Mechanical Engineering and Materials Science Department  
University of Pittsburgh



# Student Learning Objectives

At the end of the lecture, students should be able to:

- ▶ Apply Node Voltage Analysis (NVA) to circuits with independent current sources

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- ▶ So far, we've used KCL, KVL and Ohm's law to solve for the behavior of a circuit
- ▶ We want a formal, automated way to analyze circuits
- ▶ NVA uses strictly KCL and Ohm's law
- ▶ We will construct “node voltages” - based upon  $N$  nodes we will have  $N-1$  KCL equations

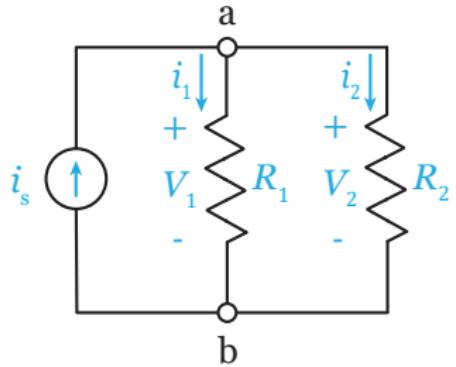
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4.2 Node Voltage Analysis with Independent Current Sources

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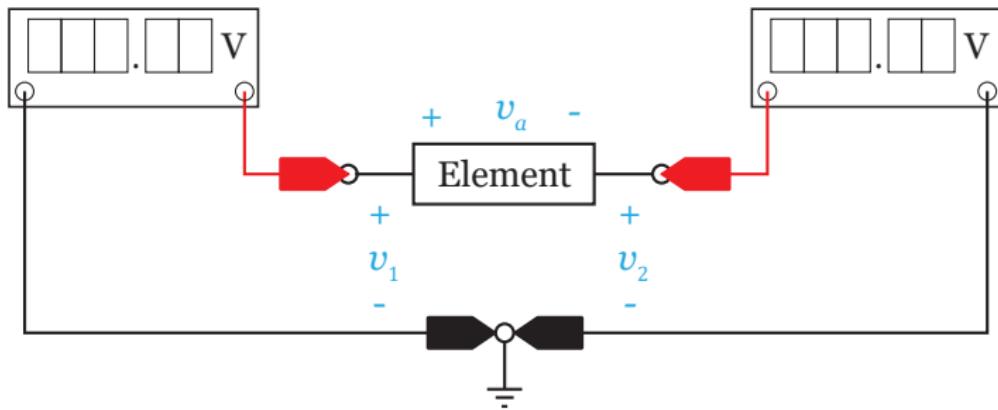
# NVA



- ▶ Consider the following circuit: How many nodes do we have?



- ▶ Finding the voltage across an element:



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- ▶ Finding the current through a resistive element:



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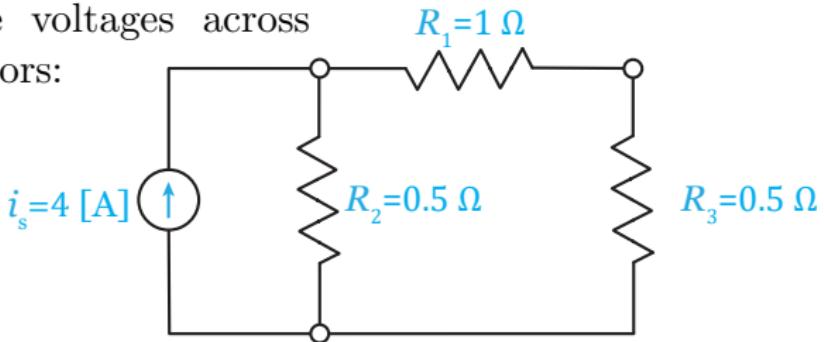
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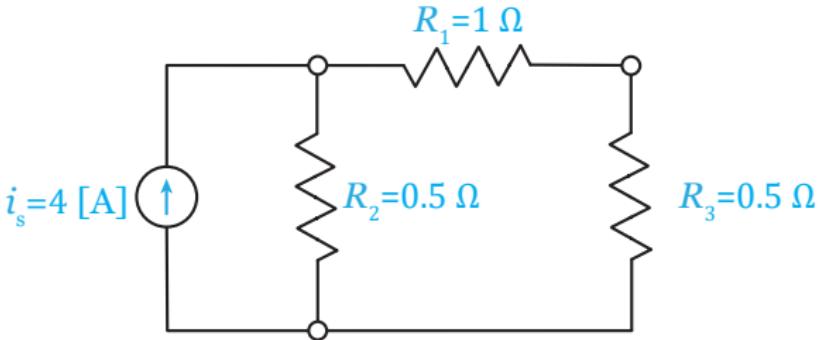
# Example #1

Find the voltages across the resistors:



# Example #1

Solution:



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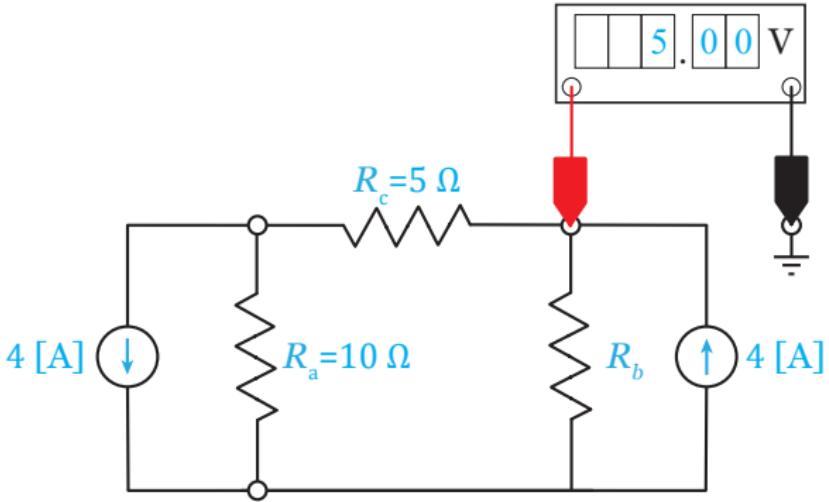
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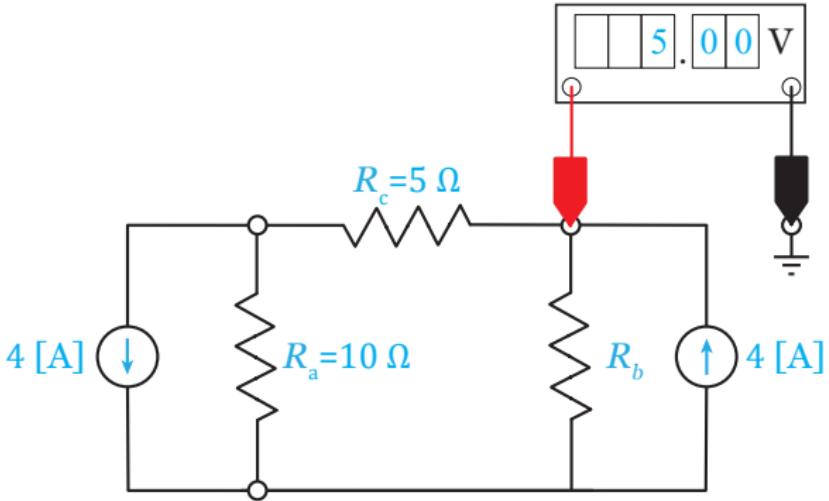
# Example #2

Find  $R_b$ :



# Example #2

Solution:



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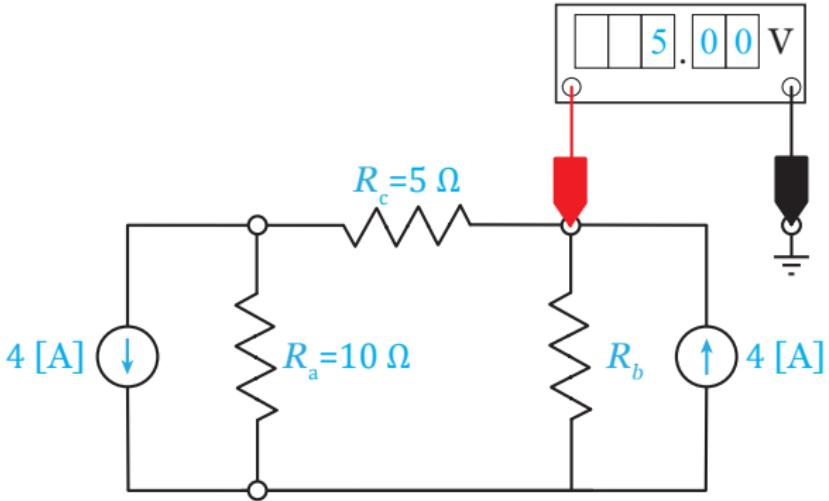
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# Example #2

Solution:



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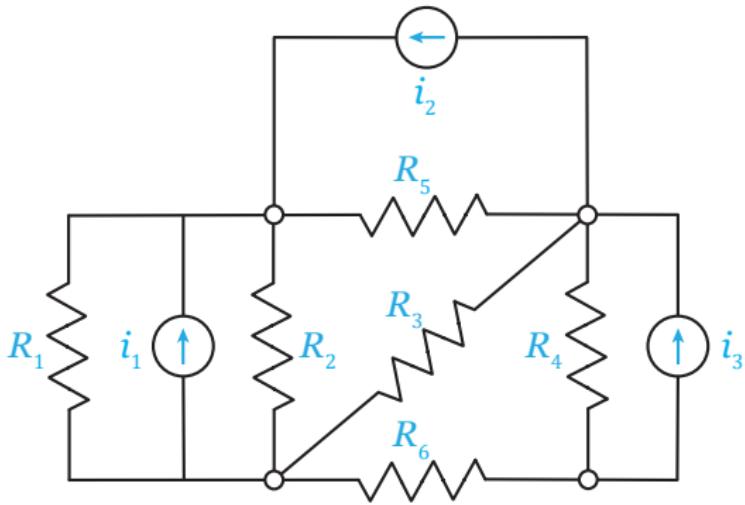
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# Example #3

- Solve for the node voltages of the given circuit given  $i_1=1$  [A],  $i_2=2$  [A],  $i_3=3$  [A],  $R_1=5$  [ $\Omega$ ],  $R_2=2$  [ $\Omega$ ],  $R_3=10$  [ $\Omega$ ],  $R_4=4$  [ $\Omega$ ],  $R_5=5$  [ $\Omega$ ] and  $R_6=2$  [ $\Omega$ ]



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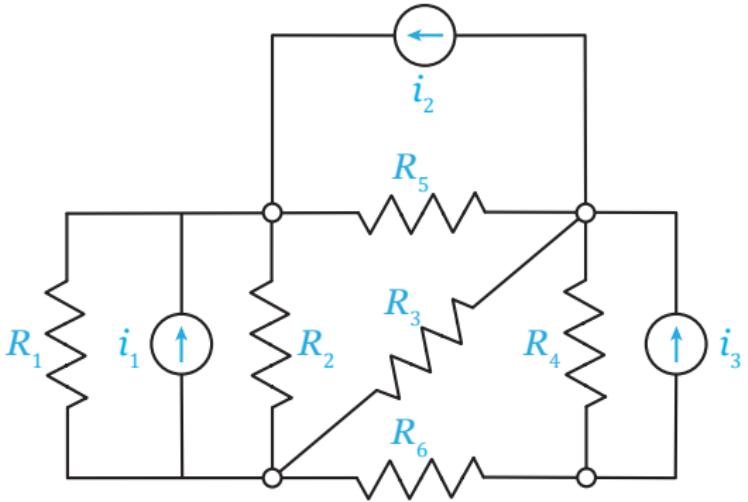
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# Example #3

Solution:



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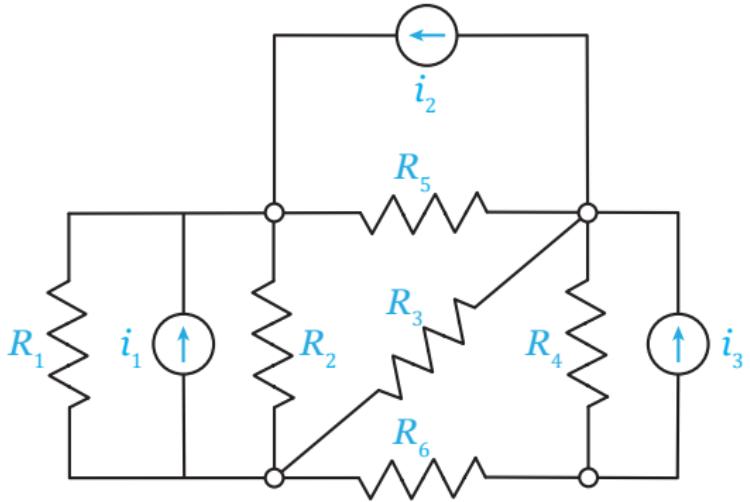
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# Example #3

Solution:



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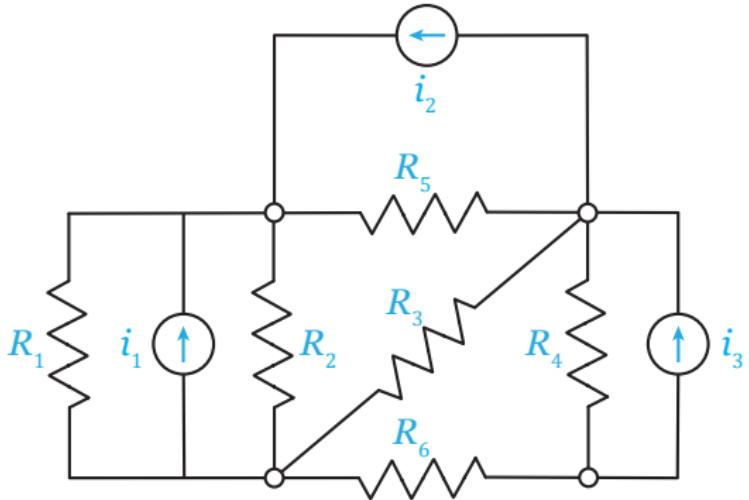
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# Example #3

Solution:



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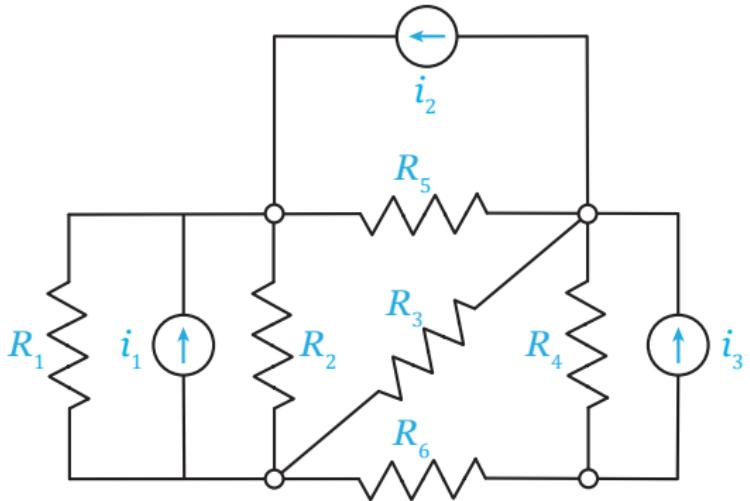
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# Example #3

Solution:



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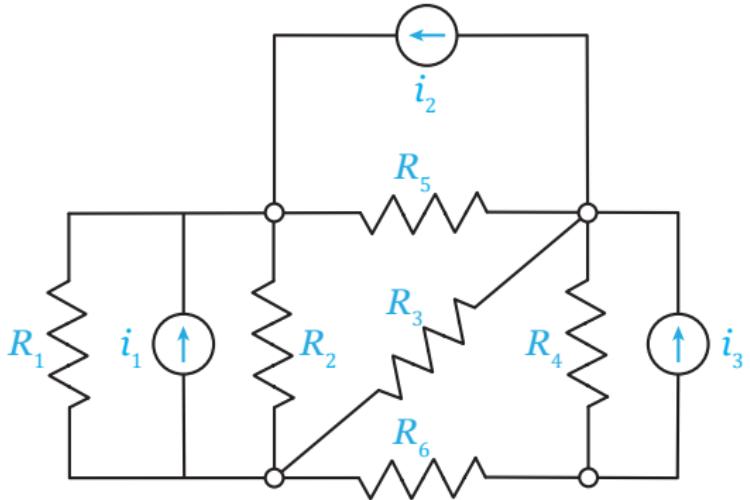
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# Example #3

Solution:



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# Student Learning Objectives

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At the end of the lecture, students should be able to:

- ▶ Apply Node Voltage Analysis (NVA) to circuits with independent current sources
  - ▶ NVA requires the sole use of KCL. We construct  $N - 1$  KCL equations, applied at non-zero, and relate the currents to voltages using Ohm's law.

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# Suggested Problems

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At the end of the lecture, students should be able to:

- ▶ 4.2-1, 4.2-2, 4.2-3, 4.2-4, 4.2-5, 4.2-6, 4.2-7

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