

# Chapter 7 - Energy Storage Elements

## Lecture 25

### Section 7.9

## MEMS 0031 Electrical Circuits

Mechanical Engineering and Materials Science Department  
University of Pittsburgh



# Student Learning Objectives

Chapter 7 - Energy  
Storage Elements

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Learning Objectives

7.9 Op-Amp and  
Linear Differential  
Equations

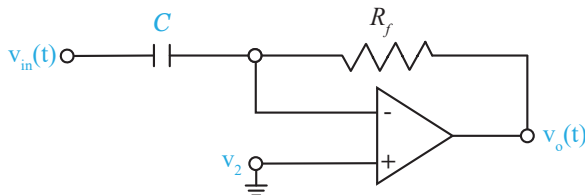
Summary

At the end of the lecture, students should be able to:

- ▶ Construct an integrator and differentiator circuit using op-amps and capacitors



- Recall the expression for the output of a differentiator op-amp:



$$V_o(t) = -R_f C \frac{dV_{in}(t)}{dt}$$

Learning Objectives

7.9 Op-Amp and  
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Summary

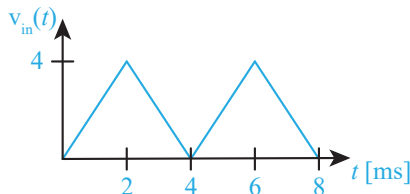


# Example #1

- Given a differentiator op-amp with  $C=0.2\text{ }[\mu\text{F}]$  and  $R_f=5\text{ }[\text{k}\Omega]$ , and the following input voltage

$$V_{\text{in}}(t) = \begin{cases} 2,000t & 0 < t < 2\text{ [ms]} \\ 8 - 2,000t & 2 < t < 4\text{ [ms]} \end{cases}$$

determine  $V_o(t)$  given  $V_o(0) = 0$



# Example #1

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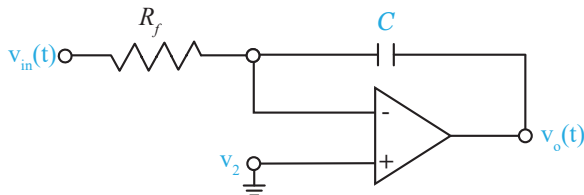
Learning Objectives

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Summary



- Recall the expression for the output of an integrator op-amp:



$$V_o(t) = \frac{-1}{R_f C} \int_{t=0}^t V_{in}(\tau) d\tau$$

Learning Objectives

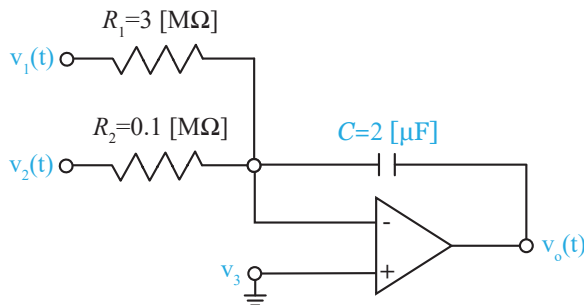
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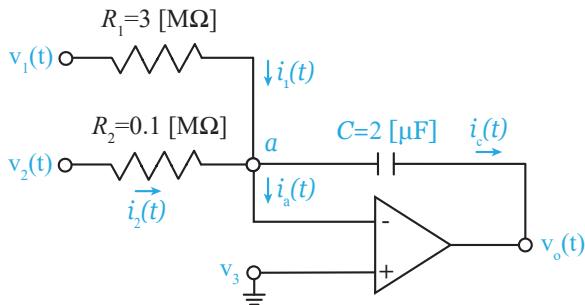


## Example #2

- Consider the following summing integrator with  $V_1(t)=10\cos(2t)$  [mV] and  $V_2(t)=0.5t$  [mV]. Determine  $V_o(t)$ , assuming the the system is initially at 0 voltage potential.



## Example #2





# Example #2

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Summary



At the end of the lecture, students should be able to:

- ▶ Construct an integrator and differentiator circuit using op-amps and capacitors
- ▶ A differentiating op-amp has the same construction as an inverting op-amp, but the input resistance is replaced with a capacitor. An integrating op-amp has the same construction as an inverting op-amp, but the follower resistance is replaced with a capacitor.



# Suggested Problems

- ▶ Ex. 7.12, for the text does not have unique homework problems associated with solely integrators and differentiators.

