Homework #2 Solutions

MEMS 0051 - Introduction to Thermodynamics

Assigned January $19^{\rm th}$, 2018Due January $26^{\rm th}$, 2018

Problem #1

Consider a 2,000 [kg] car driving up a 10 [m] tall hill. The car is driving at a velocity of 10 [m/s] and has a total internal energy (U) of 600 [kJ] [1 kJ = 10^3 J]. Determine:

(a) Determine the kinetic energy (KE) of the car [kJ].

$$KE = \frac{mV^2}{2} = \frac{2,000 \,[\text{kg}](10 \,[\text{m/s}])^2}{2} = 100 \,[\text{kJ}]$$

(b) Determine the potential energy (PE) of the car based on the hill height [kJ].

$$PE = mgh = (2,000 \,[\text{kg}])(9.81 \,[\text{m/s}^2])(10 \,[\text{m}]) = 196 \,[\text{kJ}]$$

(c) Determine the total energy (E) of the car [kJ].

$$E = U + KE + PE = 600 + 100 + 196 = 896 [kJ]$$

(d) Determine the total specific energy (e) of the car [kJ/kg].

$$e = \frac{E}{m} = \frac{896\,[\mathrm{kJ}]}{2,000\,[\mathrm{kg}]} = 0.448\,[\mathrm{kJ/kg}]$$

(e) Determine the specific internal energy (u) of the car [kJ/kg].

$$u = \frac{U}{m} = \frac{600 \,[\text{kJ}]}{2,000 \,[\text{kg}]} = 0.3 \,[\text{kJ/kg}]$$

Problem #2

Answer the following questions based on the P-T diagram for CO2 given below. (Short answers are fine, no need to re-draw the diagram on your solution)

- 1. What phase is CO_2 in at the following temperature and pressure combinations?
 - (a) $250 \text{ K}, 10^4 \text{ [kPa] liquid}$
 - (b) 170 K, 10² [kPa] solid
 - (c) $270 \text{ K}, 10^1 \text{ [kPa] vapor}$
 - (d) 330 K, 10² [kPa] supercritical fluid
- 2. Consider a piece of dry ice that is dropped into a room at 20 °C and 1 atm (101.3 [kPa]). What phase change(s) will the dry ice undergo? sublimation (solid to gas)
- 3. Consider CO₂ gas enclosed in an isothermal chamber fixed at 250 K. More CO₂ is injected into the chamber, causing the internal pressure to rise from 100 [kPa] to 10⁴ [kPa]. What phase change(s) will the CO₂ undergo? condensation (vapor to liquid)

Problem #3

Answer the following questions based on the T-v diagram for H_2O given below. (Short answers are fine, no need to re-draw the diagram on your solution)

- 1. What phase(s) of H₂O are present at the following conditions?
 - (a) $200 \, ^{\circ}\text{C}$, $2 \, [\text{m}^3/\text{kg}] \, \text{vapor}$
 - (b) $200 \, ^{\circ}\text{C}$, $10^{-4} \, [\text{m}^3/\text{kg}] \, \text{liquid}$
 - (c) 0.1 [MPa], 0.1 [m³/kg] liquid+vapor
 - (d) 400 °C, 10⁻² [m³/kg] supercritical fluid
- 2. What phase change is occurring for a mass of H_2O going from $B\rightarrow C$ on the diagram? vaporization (liquid to gas)
- 3. Let's say that we know the temperature and pressure of a mass of H₂O are 1 [MPa] and 179.9 °C. Can we determine the specific volume of this sample? Why or why not? No, because those are the saturation temperature and pressure; a third property is needed to fix the state in the two-phase region.
- 4. Consider liquid water enclosed in a piston-cylinder. The water is heated, causing an isobaric expansion at 0.1 [MPa] until all of the water boils, making saturated vapor. What is the final specific volume of the sample? $2 \text{ [m}^3/\text{kg]}$

Problem #4

You will need the steam tables (Tables B.1.1-B.1.5) in order to complete these exercises.

- 1. Determine the phase(s) for each of the following water states:
 - (a) 70 °C, 50 [kPa] liquid
 - (b) $100 \, ^{\circ}\text{C}$, $0.1 \, [\text{m}^3/\text{kg}] \, \text{liquid+vapor}$
 - (c) 75 [kPa], 3.0 [m³/kg] vapor
 - (d) 10 [kPa], 50 °C vapor
 - (e) 125 °C, 250 [kPa] liquid
- 2. Look up the requested properties for H2O at the following states:
 - (a) Specific volume at 100 [kPa], 250 °C T $T_{\rm sat}$ for the given saturation pressure, meaning its a superheated vapor. Using Table B.1.3 on pg. 784, ν =2.40604 [m³/kg]
 - (b) Specific internal energy at 5,000 [kPa], 120 °C $PP_{\rm sat}$ for the given saturation temperature, meaning its a compressed liquid. Using Table B.1.4. on pg. 790, u=501.79 [kJ/kg], which is close to ν_f (120 °C)=503.48 [kJ/kg]
 - (c) Specific volume for saturated liquid at 40 °C Using Table B.1.1 on pg. 776, $\nu_f = 0.001008 \,[\text{m}^3/\text{kg}]$
- 3. Use linear interpolation (show your work) to calculate the following properties for H₂O at the given states:
 - (a) Specific internal energy at 10,000 [kPa], 75 °C Using Table B.1.4 on pg. 790:

$$\frac{75-60\,[^{\circ}\mathrm{C}]}{80-60\,[^{\circ}\mathrm{C}]} = \frac{u-249.34\,[\mathrm{kJ/kg}]}{332.56-249.34\,[\mathrm{kJ/kg}]} \implies u = 311.755\,[\mathrm{kJ/kg}]$$

(b) Specific volume of superheated steam existing at 250 °C and 1,700 [kPa] Using Table B.1.3 on pg. 786:

$$\frac{1,700-1,600\,[\text{kPa}]}{1,800-1,600\,[\text{kPa}]} = \frac{\nu - 0.14184\,[\text{m}^3/\text{kg}]}{0.12497-0.14184\,[\text{m}^3/\text{kg}]} \implies \nu = 0.133405\,[\text{m}^3/\text{kg}]$$

(c) Specific volume of water existing at 375 °C and 5,500 [kPa] Using Table B.1.3 on pg. 788, we first interpolate to get $\nu(350$ [°C]) at 5,500 [kPa]:

$$\frac{5,500-5,000\,[\text{kPa}]}{6,000-5,000\,[\text{kPa}]} = \frac{\nu - 0.05194\,[\text{m}^3/\text{kg}]}{0.04223 - 0.05194\,[\text{m}^3/\text{kg}]} \implies \nu = 0.047085\,[\text{m}^3/\text{kg}]$$

Next we interpolate to get $\nu(400 \ [^{\circ}C])$ at 5,500 [kPa]:

$$\frac{5,500-5,000\,[\text{kPa}]}{6,000-5,000\,[\text{kPa}]} = \frac{\nu - 0.05781\,[\text{m}^3/\text{kg}]}{0.04739 - 0.05781\,[\text{m}^3/\text{kg}]} \implies \nu = 0.0526\,[\text{m}^3/\text{kg}]$$

Lastly, we interpolate between 350 [°C] and 400 [°C] at 5,500 [kPa]:

$$\frac{375 - 350 \, [^{\circ}\text{C}]}{400 - 350 \, [^{\circ}\text{C}]} = \frac{\nu - 0.047085 \, [\text{m}^{3}/\text{kg}]}{0.0526 - 0.047085 \, [\text{m}^{3}/\text{kg}]} \implies \nu = 0.0498425 \, [\text{m}^{3}/\text{kg}]$$

This is seen graphically as:

$5,000 \; [kPa]$		5,500 [kPa]		$6,000 \; [kPa]$	
T [°C]	$\nu [\mathrm{m}^3/\mathrm{kg}]$	T [°C]	$\nu [\mathrm{m}^3/\mathrm{kg}]$	T [°C]	$\nu [\mathrm{m}^3/\mathrm{kg}]$
$\overline{350}$	0.05194	350	0.047085	$\overline{350}$	0.04223
375		375	0.0498425	375	
400	0.05781	400	0.0526	400	0.04739

(d) Specific volume of water at 75 °C and 500 [kPa] Using Table B.1.4 on pg. 790:

$$\frac{75 - 60 \, [^{\circ} \text{C}]}{80 - 60 \, [^{\circ} \text{C}]} = \frac{\nu - 0.001017 \, [\text{m}^{3}/\text{kg}]}{0.001029 - 0.001017 \, [\text{m}^{3}/\text{kg}]} \implies \nu = 0.001026 \, [\text{m}^{3}/\text{kg}]$$

(e) Specific volume of water at 100 °C and 1,500 [kPa] Using Table B.1.4 on pg. 790:

$$\frac{1,500-500\,[\text{kPa}]}{2,000-500\,[\text{kPa}]} = \frac{\nu - 0.001043\,[\text{m}^3/\text{kg}]}{0.001043-0.001043\,[\text{m}^3/\text{kg}]} \implies \nu = 0.001043\,[\text{m}^3/\text{kg}]$$

(f) Specific volume of water at 22.5 °C and 17,500 [kPa] Using Table B.1.4 on pg. 791, we first interpolate to get $\nu(20 \ [^{\circ}C])$ at 17,500 [kPa]:

$$\frac{17,500 - 15,000 \, [\text{kPa}]}{20,000 - 15,000 \, [\text{kPa}]} = \frac{\nu - 0.000995 \, [\text{m}^3/\text{kg}]}{0.000993 - 0.000995 \, [\text{m}^3/\text{kg}]} \implies \nu = 0.000994 \, [\text{m}^3/\text{kg}]$$

Next we interpolate to get $\nu(00 \ [^{\circ}C])$ at 17,500 [kPa]:

$$\frac{17,500-15,000\,[\text{kPa}]}{20,000-15,000\,[\text{kPa}]} = \frac{\nu-0.001001\,[\text{m}^3/\text{kg}]}{0.000999-0.001001\,[\text{m}^3/\text{kg}]} \implies \nu = 0.001\,[\text{m}^3/\text{kg}]$$

Lastly, we interpolate between 20 [°C] and 40 [°C] at 17,500 [kPa]:

$$\frac{22.5 - 20 \,[^{\circ}\text{C}]}{40 - 20 \,[^{\circ}\text{C}]} = \frac{\nu - 0.000994 \,[\text{m}^{3}/\text{kg}]}{0.001 - 0.000994 \,[\text{m}^{3}/\text{kg}]} \implies \nu = 0.00099475 \,[\text{m}^{3}/\text{kg}]$$

This is seen graphically as:

15,000 [kPa]		$17,500 \; [kPa]$		20,000 [kPa]	
$T [^{\circ}C]$	$\nu [\mathrm{m}^3/\mathrm{kg}]$	$T [^{\circ}C]$	$\nu [\mathrm{m}^3/\mathrm{kg}]$	$T [^{\circ}C]$	$\nu [\mathrm{m}^3/\mathrm{kg}]$
20	0.000995	20	0.000994	$\overline{20}$	0.000993
22.5		22.5	0.00099475	22.5	
40	0.001001	40	0.001	40	0.000999

- 4. Your friend asks you for the specific volume (ν) of liquid water at room conditions (25 °C, 100 [kPa]), but you can't find that low of a pressure in the compressed liquid water table. Is it okay to use the saturated liquid value (ν_f) at 25 °C as an approximation? Why or why not? Yes, it is okay to use the saturated liquid value as an approximation because liquid water is incompressible, so specific volume doesn't vary much with pressure ($\nu \approx \nu_f$).
- 5. Now your (pesky) friend asks you for the specific volume (ν) of water vapor at 200 °C, 50 [kPa]. Is it okay to use the saturated vapor value (ν_g) at 200 °C as an approximation? Why or why not? No, it is not okay to use the saturated vapor volume as an approximation because water vapor is a compressible gas, so specific volume varies significantly with pressure. In this case, ν =4.35595 [m³/kg], which is about 40x greater than the saturated value of ν_g =0.12736 [m³/kg].