

Chapter 3 - First Law of Thermodynamics and Energy

Lecture 12 Section 3.11

MEMS 0051 Introduction to Thermodynamics

Mechanical Engineering and Materials Science Department
University of Pittsburgh



Student Learning Objectives

Chapter 3 - First
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Thermodynamics
and Energy

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Learning Objectives

3.11 - U, H and C
of Ideal Gases

Summary

At the end of the lecture, students should be able to:

- Understand the concept of internal energy, enthalpy and specific heat of Ideal Gases under the Ideal Gas law framework



Internal Energy and C_{V0}

- ▶ Recall u is determined from two independent properties such as T , P , ν , etc.
- ▶ For low to medium density gases, u depends primarily on T and less on P , that is $u=u(T)$
- ▶ Recalling the Ideal Gas law, if $u=u(T)$ implies u is independent of P and ν

$$P\nu = mRT \implies P\nu = RT$$

- ▶ Therefore, recalling constant-volume specific heat, the C_V is independent of ν (ν)

$$C_V = \left(\frac{\delta u}{\delta T} \right)_\nu \implies C_{V0} = \frac{du}{dT}$$

- ▶ C_{V0} is the **constant-volume specific heat of an Ideal Gas** (notice the 0)



- ▶ Recalling the definition of enthalpy in a constant-volume specific heat framework

$$h = u + P\nu$$

- ▶ From the Ideal Gas law, $P\nu=RT$

$$h = u + RT$$

- ▶ It is evident that $h=h(T)$
- ▶ Therefore, recalling constant-pressure specific heat, the C_P is independent of P

$$C_P = \left(\frac{\delta h}{\delta T} \right)_P \implies C_{P0} = \frac{dh}{dT}$$

- ▶ C_{P0} is the **constant-pressure specific heat of an Ideal Gas** (notice the 0)



- ▶ These two properties are given in Table A.5
- ▶ C_{V0} and C_{P0} are related through the definition of enthalpy of an Ideal Gas

$$h = u + P\nu = u + RT$$

- ▶ Differentiating this equation,

$$dh = du + d(RT) = du + RdT + TdR$$

- ▶ The gas constant R is constant, and dh and du can be expressed in terms of C_{P0} and C_{V0} , respectively

$$dh = du + RdT \implies C_{P0}dT = C_{V0}dT + RdT$$

- ▶ Rearranging, the gas constant R is the difference of C_{P0} and C_{V0}

$$R = C_{P0} - C_{V0}$$



- ▶ Note Table A.5 has C_{P0} and C_{V0} as constants taken at STSP
- ▶ Table A.6 Has C_{P0} as a function of temperature

$$C_{P0} = C_0 + C_1\theta + C_2\theta^2 + C_3\theta^3$$

- ▶ Note $\theta = (T \text{ [K]})/1,000$
- ▶ h is also tabulated as a function of temperature in Table A.8



- When evaluating the change of enthalpy between two states, there are multiple ways to evaluate C_{P0} (order of worst to best)
1. If dT is small and near 25 °C, use Table A.5
 2. If dT is small, and between 250 and 1,200 [K], use Table A.6
 3. If dT is large, use the integral of C_{P0} from Table A.6 (up to 1,200 [K])
 4. Use published values in Table A.8 (up to 3,000 [K])



Example #1

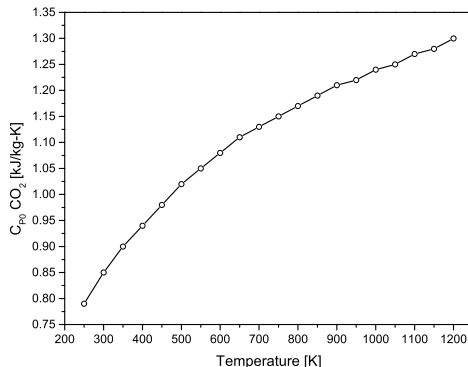
- Calculate the change of enthalpy of CO_2 from 250 to 1,200 [K], assuming Ideal Gas behavior using the following techniques:
1. Treat C_{P0} as a constant from Table A.5
 2. Treat C_{P0} as a constant, averaged between 250 and 1,200 [K], from Table A.6
 3. Evaluate the integral of C_{P0} between the temperature bounds from Table A.6
 4. Use the values published on Table A.8



Example #1

Solution:

We first look at the behavior of C_{P0} as a function of temperature: it increases by 64% over our range of interest



Example #1

Solution:

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Solution:



Example #2

- Determine the final temperature of 15 [kg] of carbon dioxide, that while undergoing a constant-pressure process which starts at a temperature of 25 °C, receives 10.2 [MJ] of heat, by treating the constant-pressure specific heat as:
- A constant taken from Table A.5;
 - A constant evaluated at the average temperature using the polynomial expression from Table A.6;
 - A constant evaluated at the average constant-pressure specific heat using the polynomial expression from Table A.6;
 - As the integral-average evaluated between the initial and final temperature using the polynomial expression from Table A.6.



Example #2

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Solution: (a)

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Example #2

Solution: (b)

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Example #2

Solution: (b)

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Example #2

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Solution: (c)

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Example #2

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Solution: (c)

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Example #2

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Solution: (d)

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Example #2

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Solution: (d)

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At the end of the lecture, students should be able to:

- ▶ Understand the concept of internal energy, enthalpy and specific heat of Ideal Gases under the Ideal Gas law framework
 - ▶ The change of internal energy for an Ideal Gas is merely the constant-volume specific heat times change of temperature.
 - ▶ The enthalpy of an Ideal Gas can be expressed as the internal energy plus pressure times specific volume, or internal energy plus the gas constant times temperature
 - ▶ The change of enthalpy for an Ideal Gas is merely the constant-pressure specific heat times change of temperature.
 - ▶ Table A.6 provides $C_P(T)$



Suggested Problems

- ▶ 3.127, 3.128, 3.130, 3.131, 3.139, 3.140, 3.143, 3.213, 3.214

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