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DISTRIBUTED GPU- ACCELERATED RAY-TRACING FOR DETERMINATION OF RADIATION VIEW FACTORS USING CUDA

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Background: View factor

Radiation view factor (F_{ij}):

$$F_{ij} = \frac{1}{A_i} \int_{A_i} \int_{A_j} \frac{\cos(\theta_i) \cos(\theta_j)}{\pi \|\vec{R}_{ij}\|^2} dA_i dA_j$$

A geometric property that quantifies the proportion of diffuse radiation emitted from one surface, A_i , and received by another surface, A_j

Radiation Heat Transfer Rate (Q_i):

$$Q_i = \varepsilon \sigma A_i F_{ij} (T_i^4 - T_j^4)$$

ε : material emissivity

σ : Stefan-Boltzmann constant

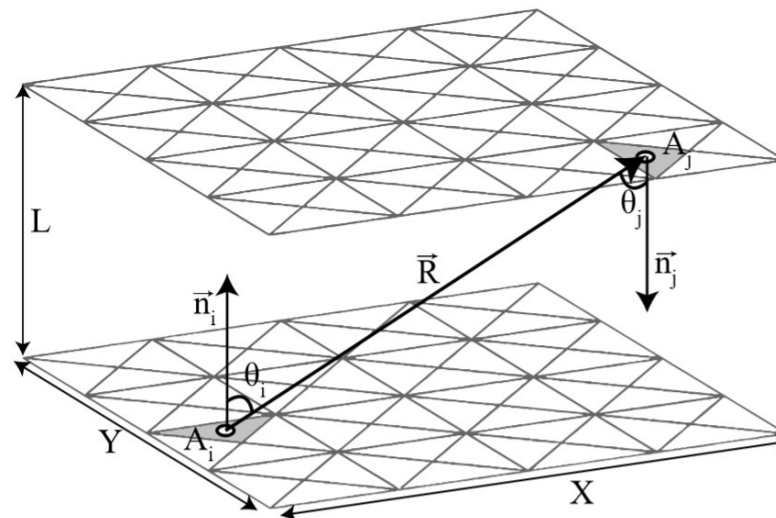
T_i : temperature of emitter

T_j : temperature of receiver

Why do we care?

Accurate heat transfer models

Parasitic radiative transfer that lowers temperature gradient



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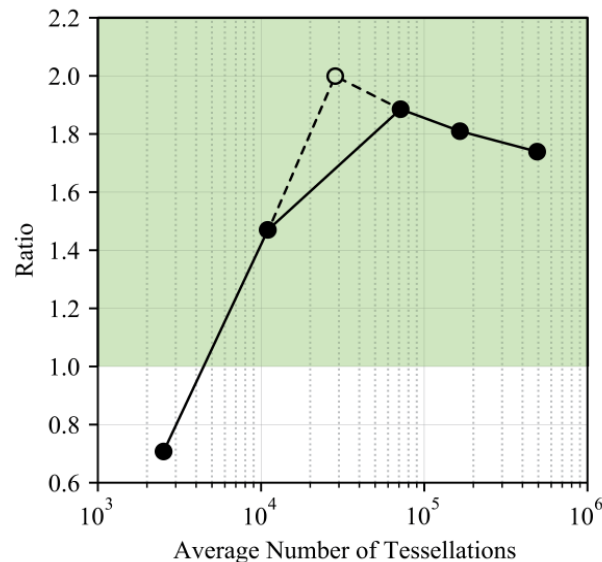
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Motivation: Previous Work

Hancock et. al. implemented a numeric view-factor solver using Aparapi, a library to convert JAVA bytecode to OpenCL GPU code

While the Aparapi code outperforms CPU and scales to multiple GPUs, the speedup factor decays when large numbers of tessellations are applied

The successes and drawbacks of the Aparapi code necessitates a new implementation



Avg. Tess.	F_{ij}	Time [s]		
		CPU	1 GPU	2 GPU
2,527	5.759450587e-4	5.505	0.955	1.350
11,015	5.751577438e-4	16.13	2.764	1.881
71,586	5.754201918e-4	113.5	62.69	33.25
165,291	5.754852079e-4	472.8	274.7	151.8
491,186	5.7545765976e-4	4,160	2,387	1,372

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Methodology: GPU-accelerated programming and geometry definition

Graphics Processing Unit (GPU) can achieve massive runtime gains

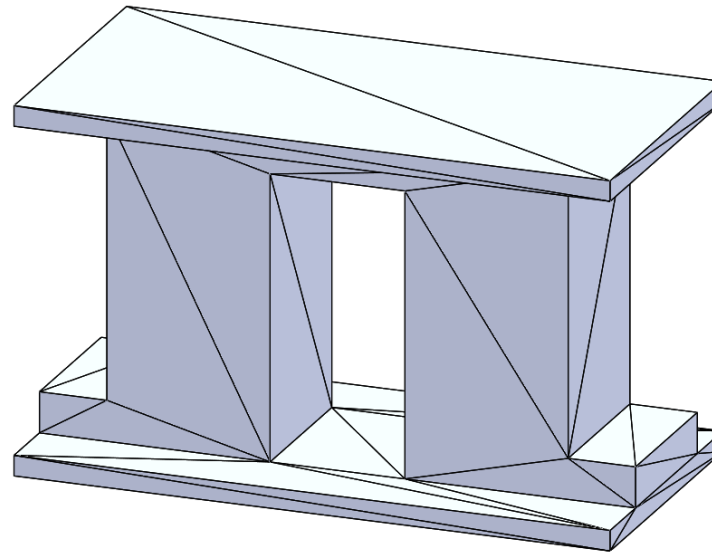
Thousands of cores that operate in parallel
Computational structure is ideal for repetitive, arithmetic tasks

Geometry Input: STL Files

Ubiquitous in CAD software
Robust geometry definition

```
solid ThermoelectricGenerator.STL
  facet normal 0.000000e+00 -1.000000e+00 0.000000e+00
    outer loop
      vertex -4.128709e-01 1.750000e+00 5.000000e-01
      vertex -4.128709e-01 1.750000e+00 -5.000000e-01
      vertex 4.128709e-01 1.750000e+00 5.000000e-01
    endloop
  endfacet
```

Example ASCII STL format



Example TEG unit-cell defined
in STL format

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Methodology: View factor computation

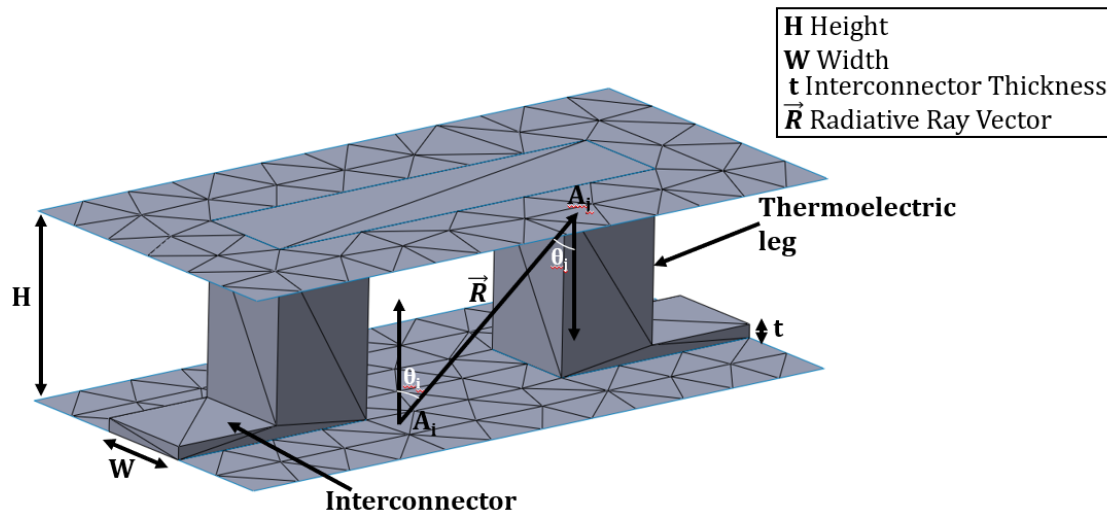
View factor:

$$F_{ij} = \frac{1}{A_i} \int_{A_i} \int_{A_j} \frac{\cos(\theta_i) \cos(\theta_j)}{\pi \|\vec{R}_{ij}\|^2} dA_i dA_j$$

View factor summation:

$$F_{ij} = \frac{1}{A_i} \sum_{i=1}^{N_i} \sum_{j=1}^{N_j} \frac{\cos(\theta_i) \cos(\theta_j)}{\pi \|\vec{R}_{ij}\|^2} dA_i dA_j$$

Every differential area of the emitter surface creates a corresponding ray for each receiver differential area, where the ray vectors are determined by the centroidal locations of each triangle, as determined from the STL file.



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Methodology: Shadow effect and Möller–Trumbore intersection algorithm

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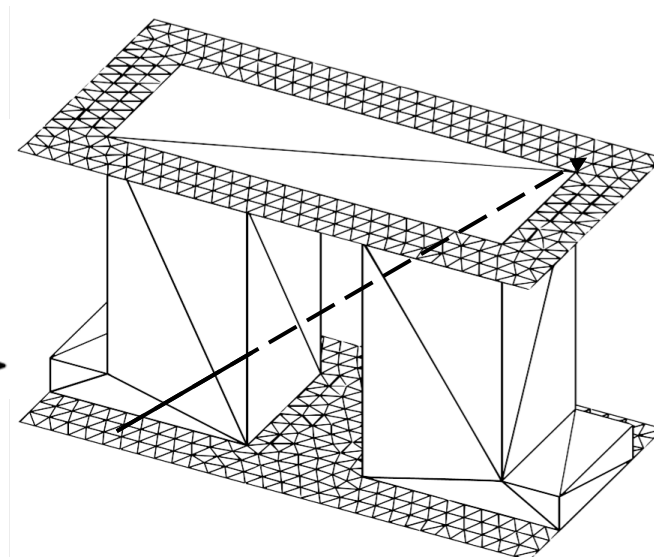
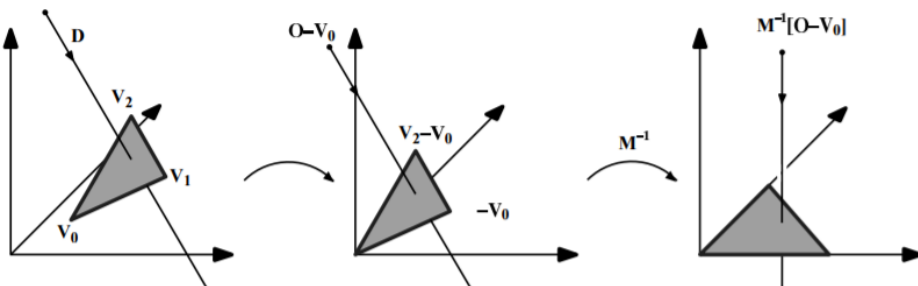
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Shadow effect: a phenomenon that represents any potential ray intersection with a non-participating surface

Reduces view factor magnitude

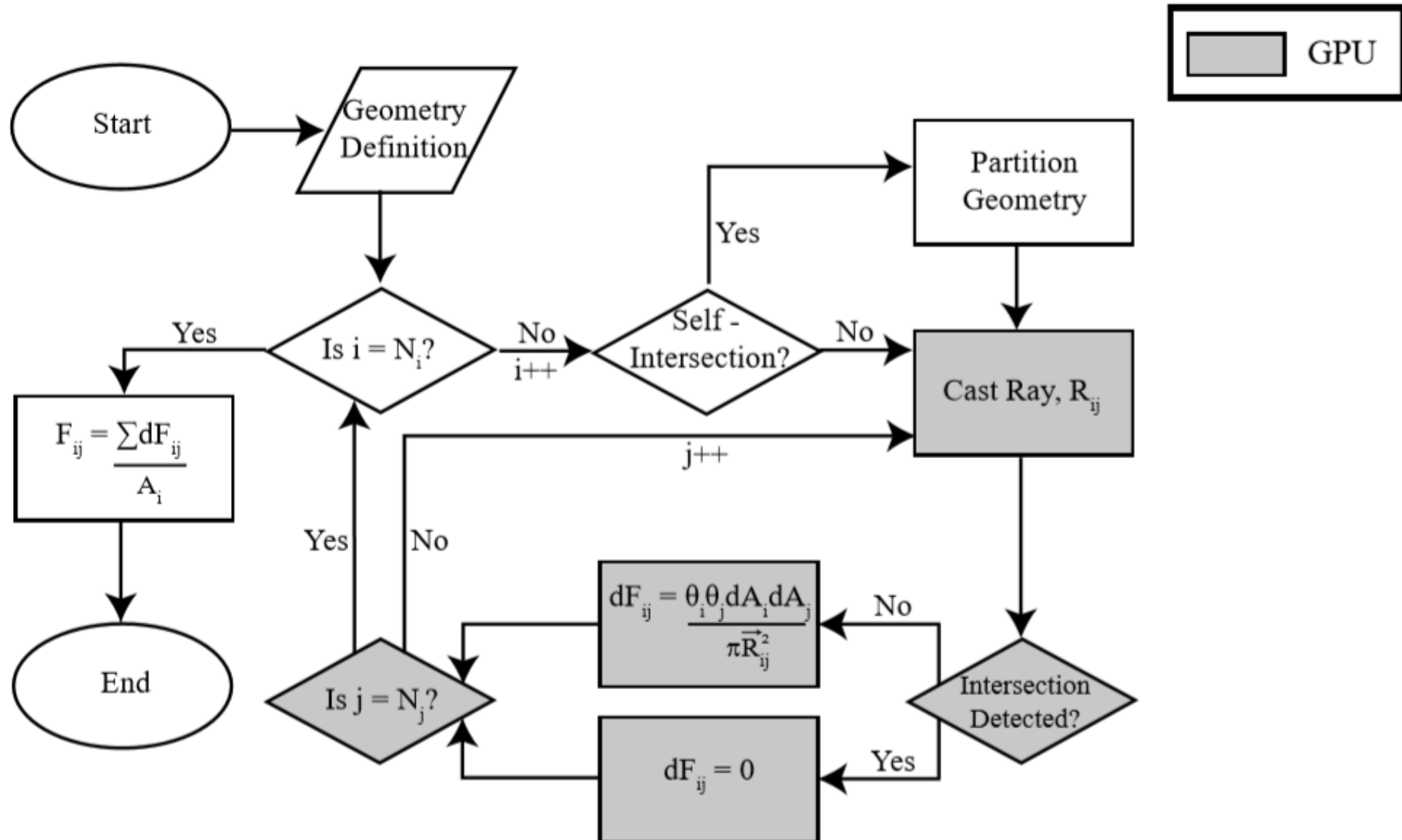
Möller–Trumbore ray-triangle intersection algorithm:



Example of shadow effect

“Fast, minimum storage ray-triangle intersection” (1997) in
Journal of graphics tools

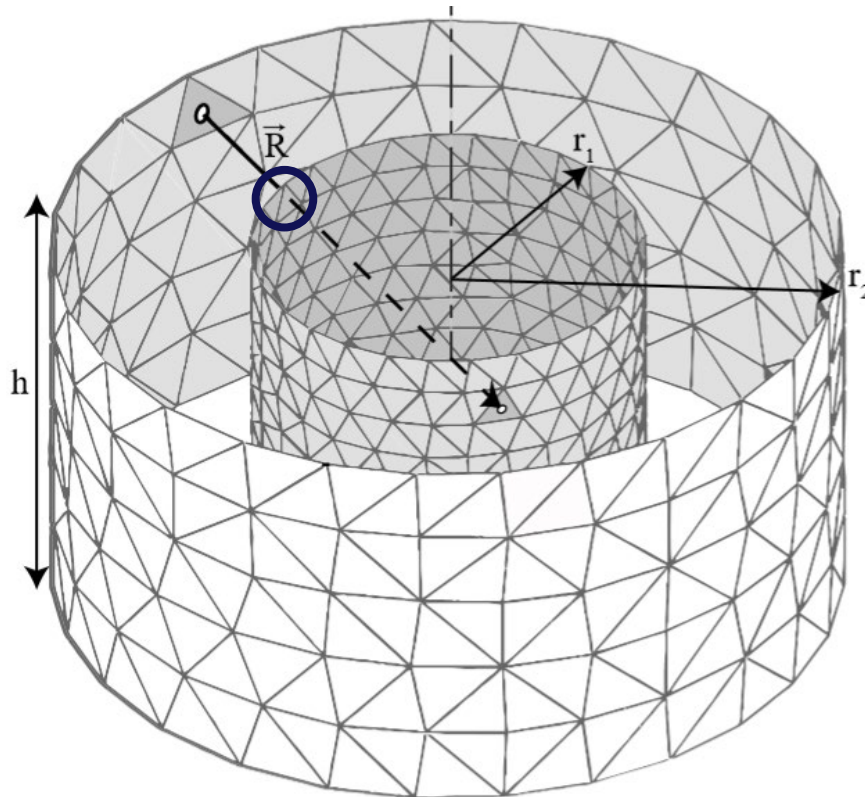
Methodology: Flow chart



Methodology: Self-intersection

Self-intersection : refers to any obstructive surface, intrinsic of either emitting or receiving surface, that need checked by the MT algorithm for possible ray-intersection to properly resolve the view factor

Normally exhibited in curved surfaces



Concentric cylinders that exhibit self-intersection

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Methodology: Self-intersection algorithm

Self-intersection algorithm: dynamics updates the emitting/receiving surfaces to consider only one tessellation at a time

All other surfaces are considered non-participatory (blocking)

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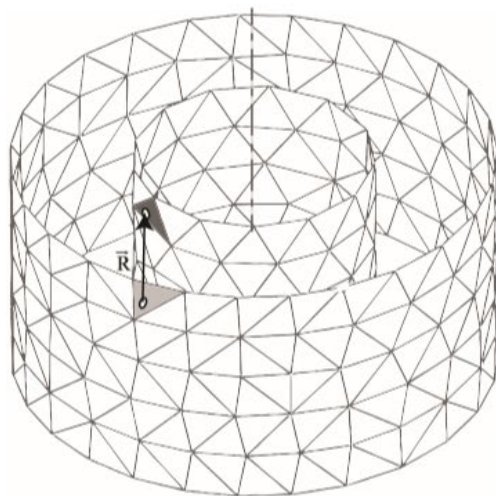
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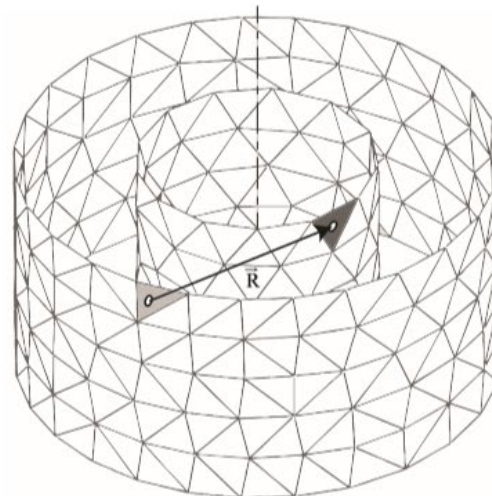
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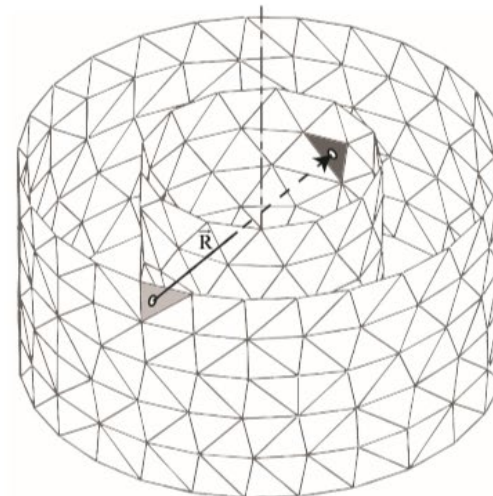
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Geometry Partitioning:
Iteration 1



Geometry Partitioning:
Iteration 2



Geometry Partitioning:
Iteration 3

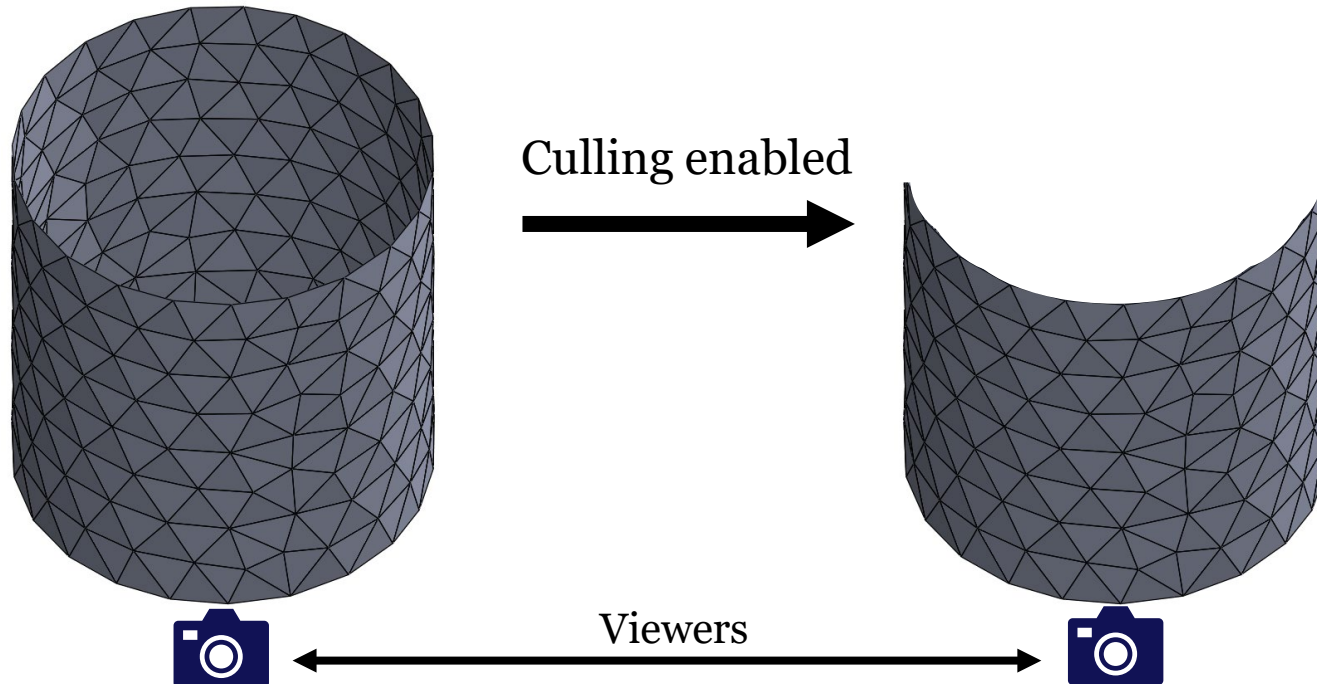
Dynamic geometry partitioning during
self-intersection algorithm

Methodology: Back-face culling

Back-face culling: a computer graphics technique that refers to the removal of primitive geometries that face away from the camera

In this context, tessellations that “face away” from the emitting tessellation appear clockwise oriented

Increases computational savings and it prevents intersection miscalculations.



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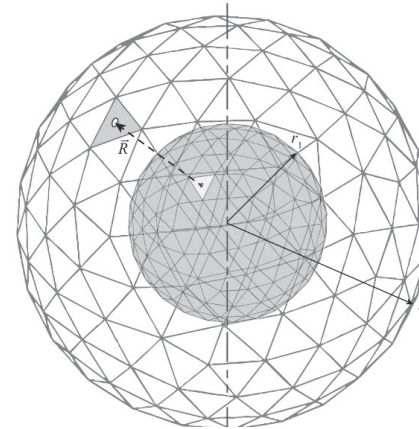
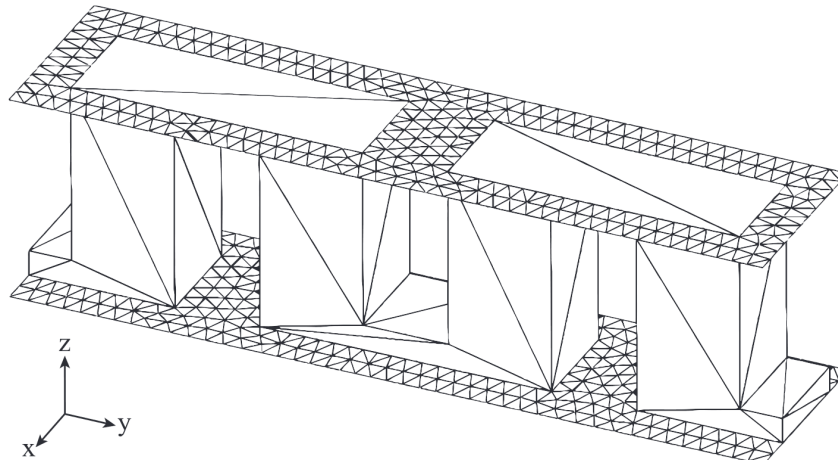
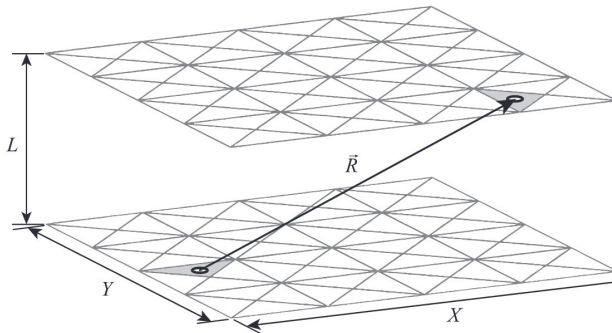
Validation:

Small Validation Set:

- Parallel Plates (5 tessellation counts, ASCII, RTX 2070)
- Spheres (4 tessellation counts, ASCII, RTX 2080ti)
- TEG Unicouple (5 tessellation counts, BINARY, RTX 2070)

Each case is run on 1 and 2 cards separately

Results compared with true values



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Results:

View factor approach true analytic values

Does not reach double-precision limit, even with very high runtime

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Case	CUDA VF	Analytic VF	Absolute Error	Relative Error
Parallel Plates	0.199824915	0.1998248957	1.93e-8	9.66e-8
TEG	0.000575456	N/A	N/A	N/A
Spheres	1.000063232	1.0000000000	6.32e-5	6.32e-5



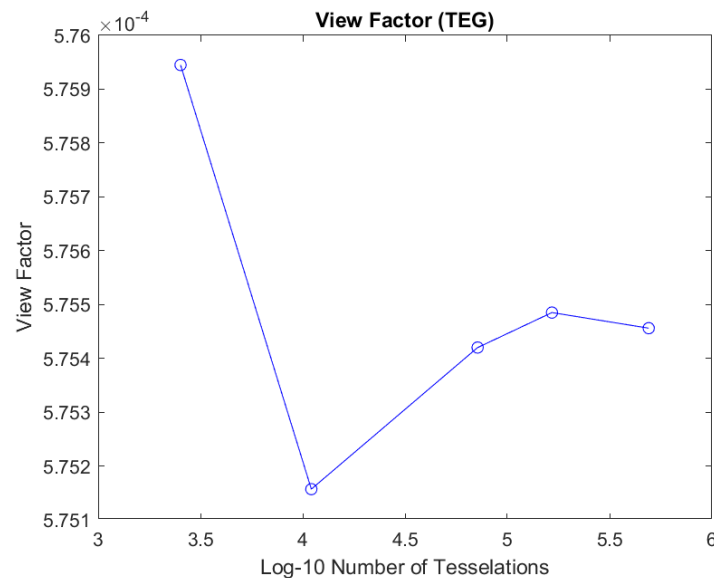
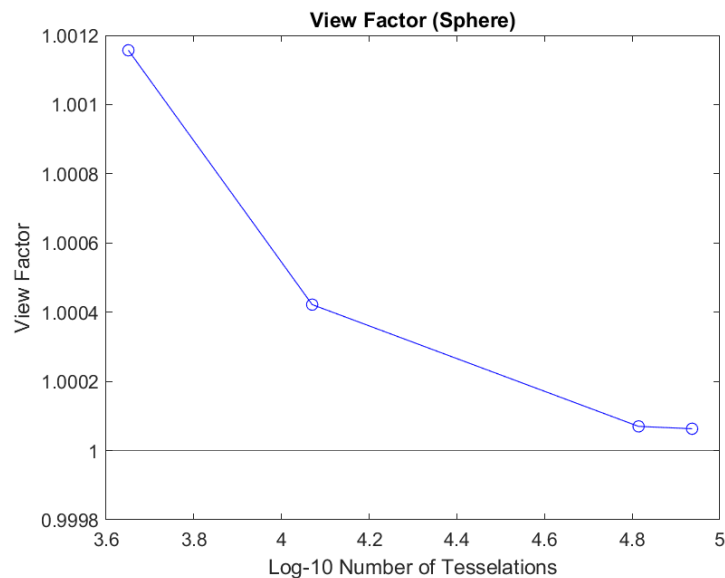
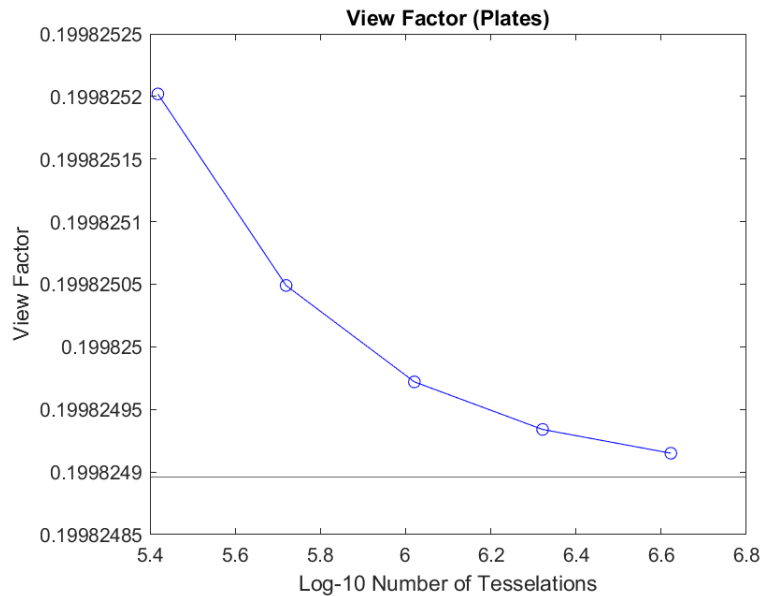
Discussion:

Result not dependent on number of GPU's

Black lines refer to analytical solution (not present for TEG)

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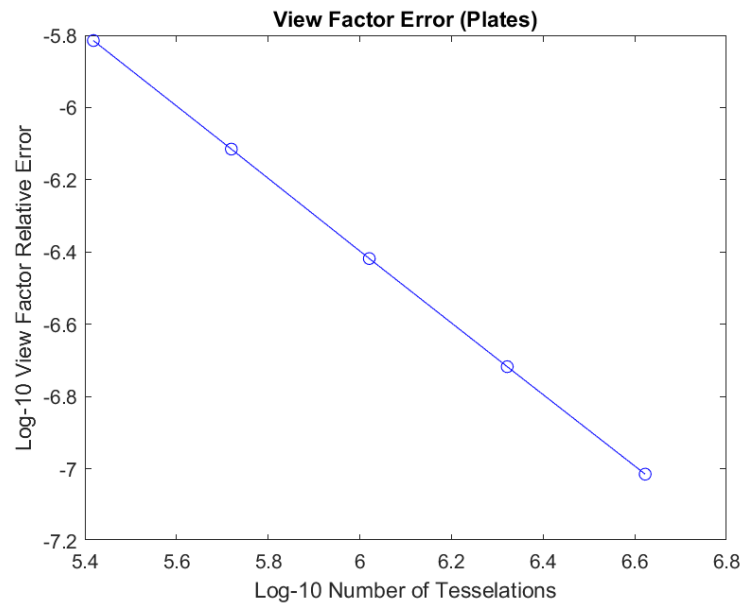
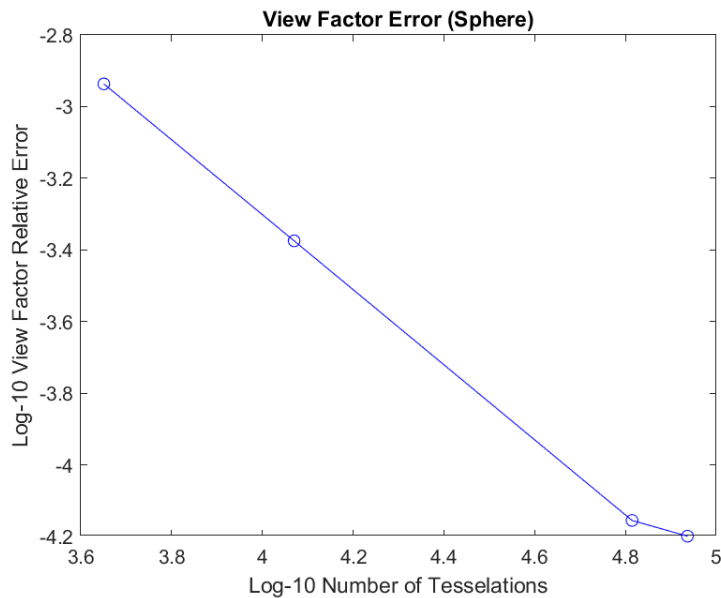
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Discussion:

Result not dependent on
number of GPU's



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Discussion:

Due to two-loop nature of non-self-intersecting code,
 $O(n^2)$ asymptotic runtime is expected

Binary STL's load much faster than ASCII

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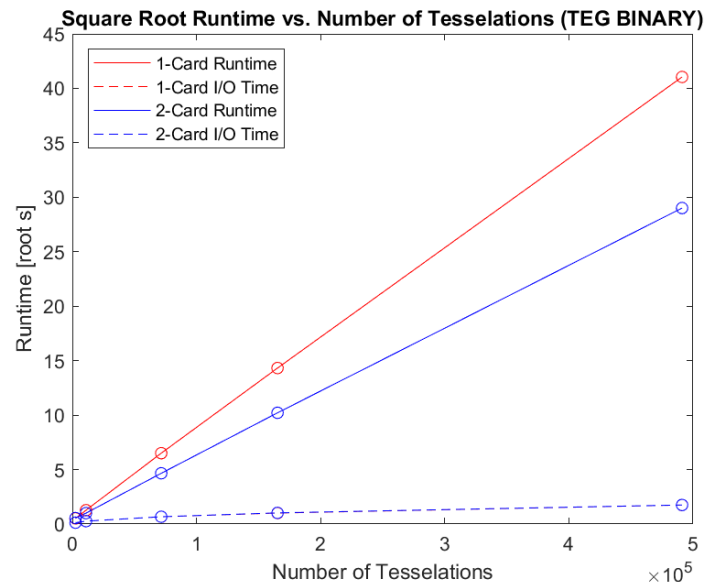
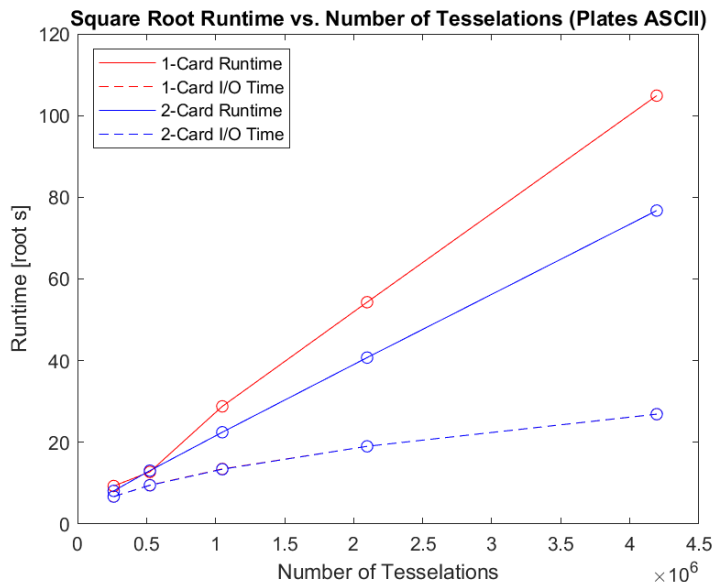
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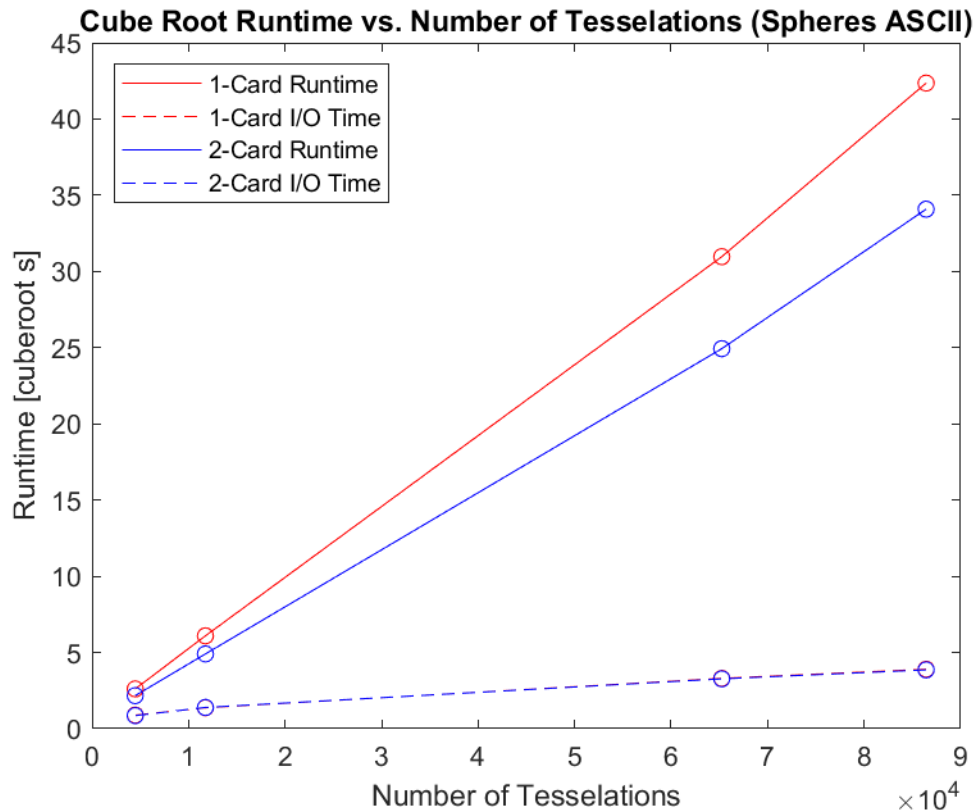
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Discussion:

Due to three-loop nature of self-intersecting code,
 $O(n^3)$ asymptotic runtime is expected



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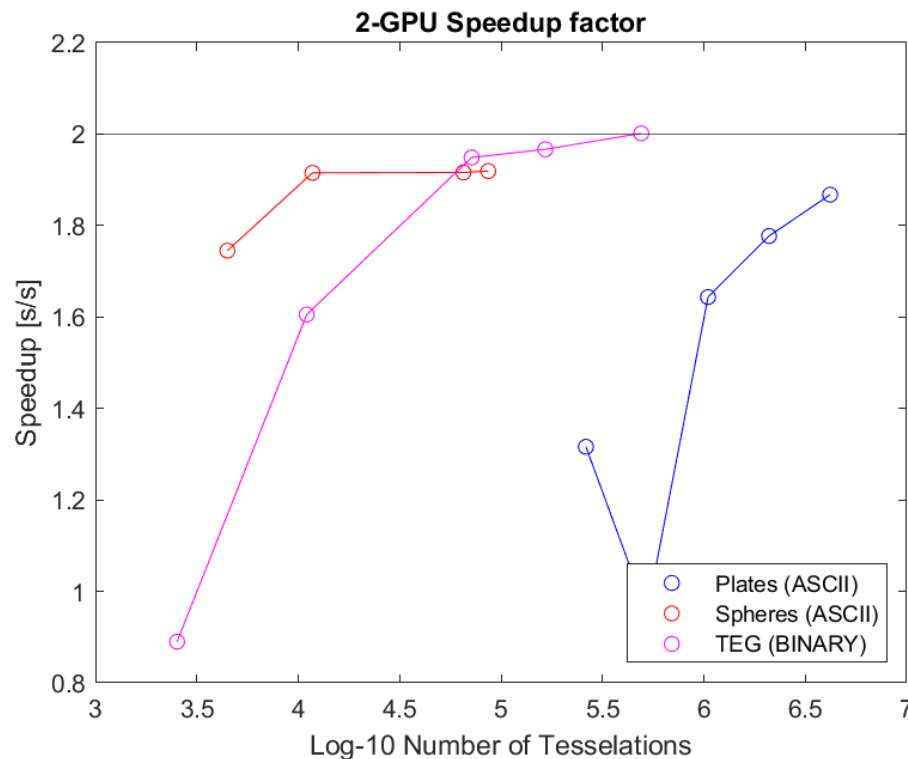
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Discussion:

Per case, the speedup factor approaches 2x

Speedup hampered by I/O time, which cannot be parallelized, and grows linearly with problem size

Using binary STL files greatly improves on I/O time, improving speedup



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Conclusion:

View factor computation lends well to parallelized computing on GPU

Given fast I/O, the speedup factor for 2 cards can approach 2x for large problems, without altering results

GPU vastly outperforms CPU in runtime, and the CUDA implementation is faster than a similar OpenCL implementation applied to the same problems
(Hancock et. al)

Given the need for fast and accurate view-factor calculations in heat transfer simulation, a need is presented for view-factor solvers that offer flexible options for backend computation
(e.g. multicore CPU or GPU)

Worth investigating single vs. double-precision GPU compute

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