

HW8 KEY

1.

Source	DF	SS	MS	F	P-Value
C	1	8.161	8.161	3.64	0.074
D	1	13.082	13.082	5.84	0.028

a. Significant at the $\alpha=0.10$ level:

- Main effect of Factor C.
- Main effect of Factor D.

b. $R^2 = 100\% \times \left(1 - \frac{35.851}{75.264}\right) \approx 52.4\%$ of total variation in the response is explained by the full model involving factors A, B, C and D.

c. $R^2_{adj} = 100\% \times \left(1 - \frac{31}{16} \times \frac{35.851}{75.264}\right) \approx 7.71\%$

d. ANOVA table for interactive model involving factors C and D:

Source	DF	SS	MS	F	P-Val
C	1	8.161	8.161	4.84	0.036
D	1	13.082	13.082	7.75	0.010
C*D	1	6.771	6.771	4.01	0.055
Error	28	47.250	1.688		
Total	31	75.264			

e. $R^2_{adj} = 100\% \times \left(1 - \frac{31}{28} \times \frac{47.250}{75.264}\right) \approx 30.49\%$.

f. $R^2_{adj} = 100\% \times \left(1 - \frac{31}{29} \times \frac{54.0215}{75.2638}\right) \approx 23.27\%$.

g. Strictly based on R^2_{adj} values, the best model is the interactive model involving C and D, the model in part (e). Of the three, it has the highest R^2_{adj} which means that it is able to explain much of the variation in responses better than the other 2 models.

2. A.

A	B	D	C=ABD	E=AD	treatment
-	-	-	-	+	e
+	-	-	+	-	ac
-	+	-	+	+	bc e
-	-	+	+	-	cd
+	+	-	-	-	ab
+	-	+	-	+	ade
-	+	+	-	-	bd
+	+	+	+	+	abcde

B. treatment e ac

C. The defining relation is $I=ABCD=ADE=BCE$. Thus $A=BCD=DE=ABCE$, and α_2 is aliased with γ^{BCD}_{222} , γ^{DE}_{22} , and γ^{ABCE}_{222} .