A Hybrid Neuro-Fuzzy Model for Stock Market Time-Series Prediction

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Abstract— In this paper we propose a hybrid five-layer neuro-fuzzy model and a corresponding learning algorithm with application in stock market time-series prediction tasks. The key difference between classical ANFIS architecture and the proposed model is in the fourth layer – multidimensional Gaussian functions are used instead of polynomials in order to achieve better computational performance and representational abilities in processing highly nonlinear volatile data. The experimental results have shown the clear advantages of the described model and its learning.

Keywords— time series, neuro-fuzzy, membership function, Gaussian, prediction

I. INTRODUCTION

Time series prediction is the one of the most common complex practical problems which appears in various applied domains. Among different types of time series financial data (e.g. currency exchange, stock and derivatives market) could Olena Vynokurova

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be distinguished by their highly nonlinear, nonstationary, volatile and chaotic nature and high-frequency dynamics.

For decades' statistical models have dominated the field of quantitative time-series analysis. The most popular among them are Autoregressive Moving Average (ARMA), Autoregressive Integrated Moving Average (ARIMA) etc. However, such models require time-series to be stationary and this is achieved through different differencing techniques, effectiveness of which is disputed due to highly nonstationary nature of real life time-series [1].

Except classical statistical models different computational intelligence techniques have been applied to the time series forecasting problems. Among them neurofuzzy models have gained popularity due to their universal approximation abilities and robustness combined with good computational performance and inherited from ANNs learning capabilities. They have been successfully used in the many forecasting tasks in different domains e.g. electric networks loading [2, 3], finances [4, 5, 6, 7] and others.

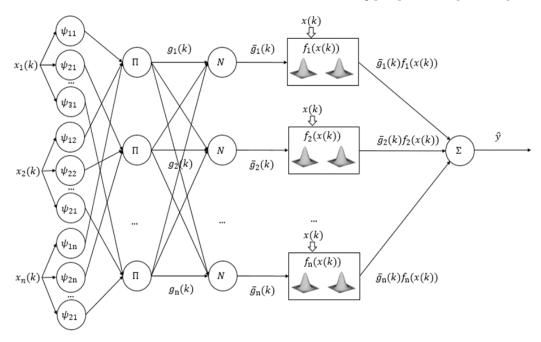


Fig. 1. The general architecture of the proposed model.

II. ARCHITECTURE AND INFERENCE

The proposed model is based on the classical ANFIS [8] model and comprises five layers. Fig.1 depicts a general architecture of the introduced model

The first layer is responsible for the fuzzification of the input variables represented by a n-dimensional vector $x(k) = (x_1(k), x_2(k), ..., x_n(k))^T$. For the prediction task the input vector means the historical gap of the observed variable. Each input parameter is processed by the h^{ν} membership functions, hence total amount of the first layer membership functions is $h^{\nu} \times n$. In current study we've used the Gaussian membership function, but in general case other common membership function types (e.g. triangular or generalized bell shaped) are acceptable. The Gaussian membership function has the following form:

$$\psi_{jl}\left(x_{i}\left(k\right)\right) = \exp\left(-\frac{\left(x_{i}\left(k\right) - c_{jl}^{\phi}\right)}{2\sigma_{ji}^{2}(k)}\right) \tag{1}$$

Where x(k) is an input vector, c_{jl}^{φ} – a centre of current Gaussian and σ_{jl} is a width parameter. The argument of the

exponential function
$$-\frac{\left(x_i\left(k\right)-c_{jl}^\phi\right)}{2\sigma_{ji}^2(k)}$$
 is a quadratic function

of x_i . The main advantages of this membership function is relatively small amount of parameters and proneness to outliers.

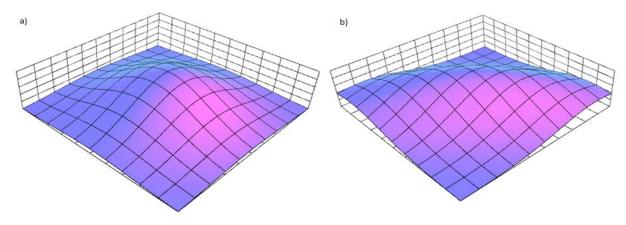


Fig. 2. The examples of multidimensional Gaussain with different covariance matrices: a) – with diagonal matrix; b – with matrix $\begin{bmatrix} 0.9 & 0.6 \\ 0.7 & 0.9 \end{bmatrix}$.

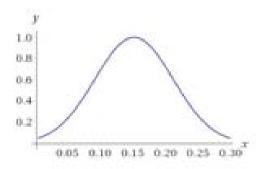


Fig. 3. The example of the first layer membership function with centre 0.15 and with width 0.06.

The second layer represents an aggregation of the antecedent premises values. It consists of h^{ψ} multiplier units which implement algebraic product fuzzy T-norm:

$$g_{j}(k) = \prod_{i=1}^{n} \psi_{jl}(x_{i}(k))$$
 (2)

The third layer is non-parametrised and responsible for normalization. It also has h^{ψ} units which output is computed by the following formula:

$$\frac{1}{g_{j}(k)} = \frac{g_{j}(k)}{\sum_{j=1}^{h^{\psi}} g_{j}(k)} = \frac{\prod_{i=1}^{n} \psi_{jl}(x_{i}(k))}{\sum_{i=1}^{h^{\psi}} \prod_{i=1}^{n} \psi_{jl}(x_{i}(k))}$$
(3)

This is necessary for satisfying the Ruspini partitioning condition:

$$\sum_{j=1}^{h^{\nu}} \overline{g}_{j}(k) = 1 \tag{4}$$

The forth layer is presented by multidimensional Gaussian consequent functions $\varphi_{je}(x(k))$ and their weights p. Multidimensional Gaussians are used instead of the standard TSK/ANFIS polynomials:

$$\varphi_{je}(x(k)) = \exp\left(-\frac{\left(x(k) - c\frac{\varphi}{je}\right)^T Q_{je}^{-1}\left(x(k) - c\frac{\varphi}{je}(k)\right)}{2}\right)$$
 (5)

where x(k) is an input vector, c_{je}^{φ} – a vector which represents the centre of the current Gaussian and Q_{je} – covariance (receptive field) matrix, $Q_{je} \in S_{++}^n$. In this case a quadratic function from (1) becomes a quadratic form of the whole input vector x(k).

Multidimensional Gaussian is a powerful tool to represent data which are not distributed evenly on the main axes. Hence the forth layer output is:

$$f_{j}(x(k)) = \sum_{i=1}^{h^{\varphi}} p_{je} \varphi_{je}(x(k))$$
 (6)

where h^{φ} is a number of multidimensional Gaussian functions for each unit f_i .

Fifth layer is non-parametrized and produces overall model output as a sum of its inputs:

$$\hat{y} = \sum_{j=1}^{h^{\varphi}} g_{j} f_{j}(x(k))$$
 (7)

In matrix form it could be rewritten as:

$$\hat{\mathbf{y}} = \mathbf{p}^T f(\mathbf{x}(k)) \tag{8}$$

where x(k) is an input vector, p -weights vector and f(x(k)) is a vector of normalised consequent functions values:

$$f(x(k)) = (\overline{g}_1 \varphi_{11}(x(k)) ... \overline{g}_{h^{\psi}} \varphi_{h^{\psi}h^{\sigma}}(x(k)))$$
(9)

where h^{ν} is a number of functions in the first layer and h^{φ} -number of multidimensional Gaussians in the fourth layer for each normalized output \overline{g}_1 .

III. LEARNING ALGORITHMS

Learning process in proposed model consists of adjusting weights vector p and tuning Multidimensional Gaussian functions parameters - both centres c_{jl}^{φ} and matrices Q_{jl} . First layer membership functions centres c_{jl}^{φ} are distributed equidistantly on initialization and they are not tuned during learning. Weights p are initialised randomly in range [-0.1;0.1] and their learning is achieved through the Kaczmarz iterative method:

$$p(k+1) = p(k) + \frac{y(k) - p^{T} f(x(k))}{f^{T}(x(k)) f(x(k))} f(x(k))$$
 (10)

where p(k) is a weights matrix represented as a vector, y(k) -reference signal, $p^T f(x(k))$ - overall model output according to (7).

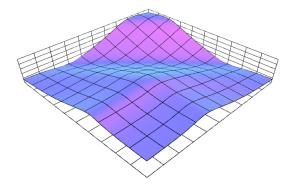


Fig. 4. The example of error surface in weights space.

Forth layer Gaussians learning performed by the firstorder gradient backpropagation procedure based on the standard mean square error criterion:

$$E = \frac{1}{N} \sum_{k=1}^{N} (y(k) - \hat{y}(k))^{2}$$
 (11)

where y(k) - reference signal value, $\hat{y}(k)$ - prognosis signal value and N is the training set length.

The Q_{jl}^{-1} matrices are initialized as identity matrices and their learning can be written in the following way:

$$\begin{cases} Q_{jl}^{-1}(k+1) = Q_{jl}^{-1}(k) + \lambda_{\mathcal{Q}} \frac{\tau_{jl}^{\mathcal{Q}}(k)e(k)}{\eta_{q}(k)} \\ \eta_{\mathcal{Q}}(k+1) = \beta_{\mathcal{Q}}\eta_{\mathcal{Q}}(k) + Tr\left(\tau_{jl}^{\mathcal{Q}^{T}}\tau_{jl}^{\mathcal{Q}}\right) \end{cases}$$
(12)

where λ_Q is a learning step and β_Q is a momentum hyperparameters, τ_{jl}^Q is a vector of values back propagated for each multidimensional Gaussian.

The centres c_{jl}^{φ} are placed equidistantly on initialization step and then tuned by the formula below.

$$\begin{cases}
c_{jl}^{\varphi}(k+1) = c_{jl}^{\varphi}(k) + \lambda_c \frac{\tau_{jl}^c(k)e(k)}{\eta_c(k)} \\
\eta_c(k+1) = \beta_c \eta_c(k) + \tau_{jl}^{cT} \tau_{jl}^c
\end{cases}$$
(13)

where λ_c is a learning step and β_c is a momentum hyperparameters, τ_{il}^c is a vector of back propagated values.

IV. EXPERIMENTAL RESULTS

Proper and unbiased comparison of the different forecasting models is a complex task [9]. The proposed

model and learning algorithm have shown good performance in real-life stock market datasets - daily log returns of IBM and Cisco. We have compared performance and prediction accuracy to ANN based on bipolar sigmoid activation functions and resilient backpropagation learning algorithm. RMSE and SMAPE criteria were used.

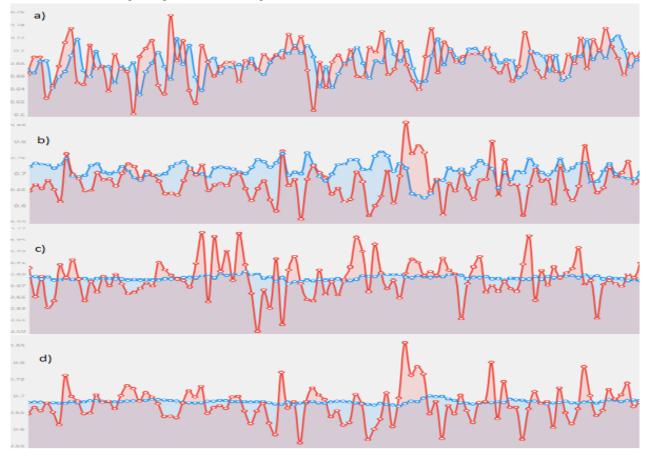


Fig. 5. Experiments on Cisco daily returns plots: a) proposed model – learning; b) proposed model – verification; c) bipolar sigmoid network – learning; d) bipolar sigmoid network – verification

The best results for the introduced model were achieved with $h^{\varphi}=2$, $\lambda_c=0.87$, $\beta_c=1.01$, $\lambda_Q=0.81$, $\beta_Q=1.02$. The bipolar sigmoid network was trained with alpha value 0.4, learning rate 0.67 and 100 epochs.

Model	Cisco daily log returns dataset results		
	Execution time, ms	RMSE, %	SMAPE, %
Proposed model	442	3.237	3.53
Bipolar Sigmoid Network	2668	3.31	3.6

V. CONCLUSION

In the paper a novel MIMO neuro-fuzzy model with multidimensional Gaussian functions in consequent layer is introduced. This solution allows to handle complex nonlinear data, which is demonstrated on the stock market time-series prediction tasks.

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