

Equations of motion: (for Runge-Kutta)

$$\text{Let } \omega_1 \equiv \dot{\theta}_1 \Rightarrow \ddot{\theta}_1 = \dot{\omega}_1$$

$$\text{Let } \omega_2 \equiv \dot{\theta}_2 \Rightarrow \ddot{\theta}_2 = \dot{\omega}_2$$

$$\dot{\omega}_1 = \frac{-g(2m_1 + m_2) \sin \theta_1 - m_2 g \sin(\theta_1 - 2\theta_2) - 2 \sin(\theta_1 - \theta_2) m_2 (L_2 \omega_2^2 + L_1 \omega_1^2 \cos(\theta_1 - \theta_2))}{L_1 (2m_1 + m_2 (1 - \cos(2(\theta_1 - \theta_2))))}$$

Setting  $m_1 = m_2 = m$ ,  $L_1 = L_2 = L$ , we get

$$= \frac{-3gm \sin \theta_1 - mg \sin(\theta_1 - 2\theta_2) - 2m \sin(\theta_1 - \theta_2) (L \omega_2^2 + L \omega_1^2 \cos(\theta_1 - \theta_2))}{L (2m + m - m \cos(2(\theta_1 - \theta_2)))}$$

$$= \frac{-3mg \sin \theta_1 - mg \sin(\theta_1 - 2\theta_2) - 2mL \sin(\theta_1 - \theta_2) (\omega_2^2 + \omega_1^2 \cos(\theta_1 - \theta_2))}{mL (3 - \cos(2(\theta_1 - \theta_2)))}$$

$$\begin{aligned} \dot{\omega}_2 &= \frac{2 \sin(\theta_1 - \theta_2) (\omega_1^2 L_1 (m_1 + m_2) + g(m_1 + m_2) \cos \theta_1 + \omega_2^2 L_2 m_2 \cos(\theta_1 - \theta_2))}{L^2 (2m_1 + m_2 - m_2 \cos(2\theta_1 - 2\theta_2))} \\ &= \frac{2 \sin(\theta_1 - \theta_2) (2mL \omega_1^2 + 2mg \cos \theta_1 + \omega_2^2 mL \cos(\theta_1 - \theta_2))}{L (2m + m - m \cos(2\theta_1 - 2\theta_2))} \\ &= \frac{2 \sin(\theta_1 - \theta_2) [2(L \omega_1^2 + g \cos \theta_1) + \omega_2^2 mL \cos(\theta_1 - \theta_2)]}{mL (3 - \cos(2\theta_1 - 2\theta_2))} \end{aligned}$$

$$\dot{\theta}_1 = \omega_1$$

$$\dot{\theta}_2 = \omega_2$$