OFDM mmWave Channel Estimation with OMP

Wuqiong Zhao

This is a simple simulation of millimeter wave (mmWave) channel estimation in wideband assisted by OFDM with orthogonal matching pursuit (OMP) algorithm. The main idea of OFDM mmWave channel estimation is the shared angle of arrival (AoA) and angle of departure (AoD). However, in wideband mmWave MIMO systems, the beam squint effect cannot be neglected. For simplicity, this effect is not considered in this simulation. The number in the bracket after OMP is the number of carriers used to estimate the AoA and AoD (i.e. non-zero elements in the beam domain). The R suffix means re-estimating the carriers used to estimate the AoA and AoD using least square (LS) after the support is calculated.

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1 System Settings

The simulation adopts the geometric channel model for millimeter wave (mmWave).

Name	Antenna Number	Beam Number	Grid Number
Transmitter	8×1	2×1	8 × 1
Receiver	16×1	4×1	16×1

• Channel Sparsity: 6;

• Off Grid Effect: false;

• Bandwidth: Wideband;

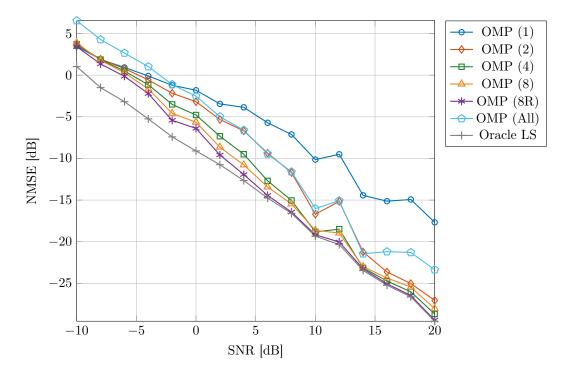
• Carriers: 64.



2 Simulation Results

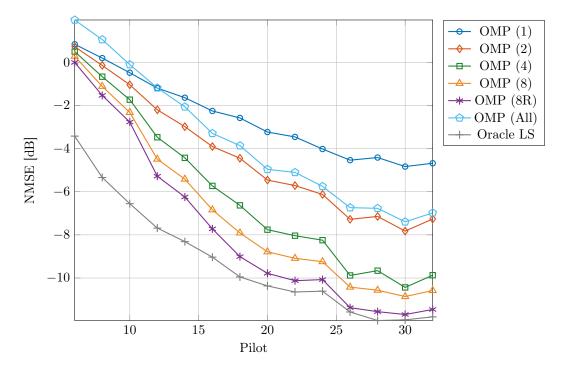
2.1 NMSE v.s. SNR (Pilot: 16)

SNR [dB]	OMP (1)	OMP (2)	OMP (4)	OMP (8)	OMP (8R)	OMP (All)	Oracle LS
-10	3.47	3.63	3.72	3.87	3.42	6.55	1.03
-8	1.88	1.92	1.87	1.77	1.34	4.27	-1.50
-6	0.93	0.79	0.50	0.29	-0.14	2.66	-3.18
-4	-0.10	-0.57	-1.15	-1.66	-2.22	1.02	-5.25
-2	-1.22	-2.17	-3.51	-4.59	-5.43	-1.13	-7.41
0	-1.81	-3.18	-4.78	-5.65	-6.39	-2.53	-9.10
2	-3.45	-5.32	-7.33	-8.65	-9.58	-4.99	-10.75
4	-3.86	-6.69	-9.50	-10.78	-11.94	-6.61	-12.65
6	-5.72	-9.37	-12.69	-13.43	-14.44	-9.48	-14.75
8	-7.12	-11.70	-15.05	-15.46	-16.44	-11.60	-16.59
10	-10.14	-16.70	-18.82	-18.63	-19.16	-16.02	-19.34
12	-9.50	-15.16	-18.50	-18.96	-20.03	-15.08	-20.34
14	-14.43	-21.23	-23.15	-23.00	-23.26	-21.45	-23.45
16	-15.13	-23.63	-24.71	-24.35	-25.05	-21.19	-25.22
18	-14.93	-25.03	-26.02	-25.45	-26.46	-21.29	-26.62
20	-17.67	-27.05	-28.68	-28.03	-29.41	-23.36	-29.54



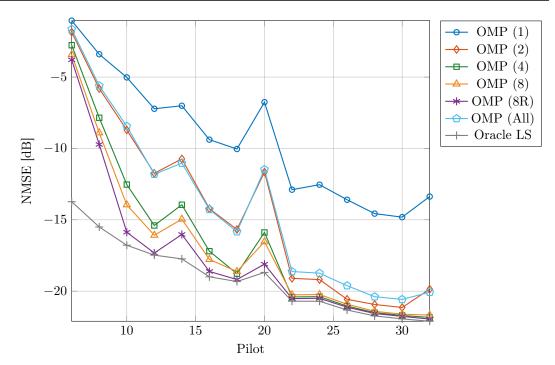
2.2 NMSE v.s. Pilot (SNR: 0 dB)

Pilot	OMP (1)	OMP (2)	OMP (4)	OMP (8)	OMP (8R)	OMP (All)	Oracle LS
6	0.84	0.72	0.50	0.28	0.00	1.96	-3.42
8	0.20	-0.14	-0.67	-1.11	-1.53	1.06	-5.34
10	-0.48	-1.04	-1.73	-2.32	-2.77	-0.10	-6.55
12	-1.19	-2.20	-3.47	-4.49	-5.28	-1.18	-7.68
14	-1.64	-2.98	-4.43	-5.42	-6.24	-2.06	-8.31
16	-2.26	-3.91	-5.73	-6.84	-7.72	-3.29	-9.03
18	-2.58	-4.45	-6.63	-7.91	-9.01	-3.86	-9.95
20	-3.23	-5.46	-7.76	-8.79	-9.78	-4.96	-10.37
22	-3.46	-5.71	-8.04	-9.09	-10.12	-5.10	-10.65
24	-4.02	-6.12	-8.25	-9.24	-10.07	-5.75	-10.61
26	-4.54	-7.28	-9.88	-10.42	-11.38	-6.74	-11.57
28	-4.41	-7.15	-9.66	-10.57	-11.56	-6.77	-11.97
30	-4.83	-7.82	-10.44	-10.86	-11.69	-7.39	-11.94
32	-4.68	-7.26	-9.87	-10.58	-11.46	-6.98	-11.80



2.3 NMSE v.s. Pilot (SNR: 10 dB)

Pilot	OMP (1)	OMP (2)	OMP (4)	OMP (8)	OMP(8R)	OMP (All)	Oracle LS
6	-1.05	-1.85	-2.77	-3.43	-3.79	-1.65	-13.73
8	-3.40	-5.81	-7.85	-8.91	-9.72	-5.61	-15.50
10	-5.02	-8.71	-12.53	-13.95	-15.87	-8.44	-16.78
12	-7.22	-11.74	-15.40	-16.08	-17.33	-11.81	-17.48
14	-7.01	-10.73	-13.95	-14.96	-16.03	-11.03	-17.74
16	-9.38	-14.22	-17.20	-17.78	-18.62	-14.27	-19.00
18	-10.04	-15.68	-18.78	-18.62	-19.19	-15.83	-19.33
20	-6.76	-11.65	-15.89	-16.54	-18.11	-11.47	-18.69
22	-12.89	-19.10	-20.41	-20.26	-20.52	-18.62	-20.70
24	-12.54	-19.19	-20.38	-20.24	-20.50	-18.74	-20.71
26	-13.59	-20.57	-21.04	-20.91	-21.13	-19.62	-21.32
28	-14.57	-20.93	-21.51	-21.41	-21.56	-20.39	-21.73
30	-14.81	-21.14	-21.70	-21.61	-21.77	-20.58	-21.94
32	-13.37	-19.86	-21.84	-21.68	-21.95	-20.08	-22.11



3 Simulation Configuration

3.1 Configuration File

Listing 1: MIMO_wideband.sim

```
# MIMO_wideband.sim
   # Wideband (OFDM) mmWave Channel Estimation with OMP
   # Author: Wuqiong Zhao
   # Date: 2022-09-26
4
6
   version: 0.1.0 # the targeted mmCEsim version
   meta: # document meta data
7
     title: OFDM mmWave Channel Estimation with OMP
9
     description:
10
       This is a simple simulation of millimeter wave (mmWave)
11
       channel estimation in wideband assisted by OFDM
12
       with orthogonal matching pursuit (OMP) algorithm.
       The main idea of OFDM mmWave channel estimation
13
       is the shared angle of arrival (AoA) and angle of departure
14
       (AoD). However, in wideband mmWave MIMO systems,
15
       the beam squint effect cannot be neglected. For simplicity,
16
17
       this effect is not considered in this simulation.
18
       The number in the bracket after OMP is the number of
19
       carriers used to estimate the AoA and AoD (i.e. non-zero
20
       elements in the beam domain). The R suffix means
21
       re-estimating the carriers used to estimate the AoA
22
       and AoD using least square (LS)
       after the support is calculated.
23
     author: Wuqiong Zhao
24
25
     email: contact@mmcesim.org
26
     website: https://mmcesim.org
27
     license: MIT
     date: "2022-09-16"
28
     comments: This is an uplink channel.
30
     frequency: wide # assume narrow band
31
32
     carriers: 64
33
     off_grid: false # do not consider off-grid problem
34
   nodes:
     - id: BS # this should be unique
35
       role: receiver
36
       num: 1 # this is the default value
37
38
       size: [16, 1] # ULA with size 16*1
39
       beam: [4, 1]
40
       grid: same # the same as physics size
41
       beamforming:
         variable: "W"
42
43
         scheme: random
     - id: UE # user
44
45
       role: transmitter
       num: 1 # a single-user model
46
       size: 8 # ULA with size 8
47
       beam: 2
48
49
       grid: 8
50
       beamforming:
         variable: "F"
51
         scheme: random
53
   channels:
54
     - id: H
       from: BS
       to: UE # 'from -> to' specifies the channel direction
56
57
       sparsity: 6
58
       gains:
```

```
mode: normal
          mean: 0
60
61
          variance: 1
62
    sounding:
63
      variables:
        received: "Y" # received signal vector
64
        noise: "noise" # received noise vector
65
        channel: "H_cascaded" # the cascaded channel (actually the same as 'H' for
66
         → simple MIMO)
67
    macro:
68
      - name: OFDM_ANGLE_EST_NUM
69
        value: 4
70
        in_alg: true
71
      - name: OFDM_RE_ESTIMATE
72
        value: false
73
        in_alg: true
74
      - name: SPARSITY_EST
75
        value: 6
76
        in_alg: true
77
    preamble: |
      COMMENT Here starts the preamble.
78
79
    estimation: |
      VNt::m = NEW `DICTIONARY.T`
80
81
      VNr::m = NEW `DICTIONARY.R`
82
      lambda_hat = INIT `GRID.*`
83
      H_hat = INIT `SIZE.R` `SIZE.T` `CARRIERS_NUM`
      Q = INIT `MEASUREMENT` `GRID.*`
84
      i::u0 = LOOP 0 `PILOT`/`BEAM.T`
85
        F_t::m = NEW F_{:,:,i}
86
        W_t::m = NEW W_{{:,:,i}}
87
        Q_{i*`BEAM.*`:(i+1)*`BEAM.*`-1,:} = \kron(F_t^T, W_t^H) @ \kron(VNt^*, VNr) #
88
          \rightarrow the sensing matrix
      END
89
90
      BRANCH
      angle_est = INIT `GRID.R`*`GRID.T` dtype=f
91
      k::u0 = LOOP 0 `OFDM_ANGLE_EST_NUM`
92
        none_zero::u1 = NEW \find(\abs(VNr^H@H_cascaded_{{:,:,k}@VNt)>0.1)
93
94
        lambda_hat = ESTIMATE Q Y_{:,k} none_zero
        angle_est = angle_est + \pow(\abs(lambda_hat), 2)
95
        IF ! OFDM_RE_ESTIMATE
96
97
          H_hat_{:,:,k} = VNr @ \reshape(lambda_hat, `GRID.R`, `GRID.T`) @ VNt^H
98
99
      ranking::u1 = NEW \sort_index(-angle_est)
100
101
      support::u1 = NEW ranking_{0:`SPARSITY_EST`-1}
102
      index_start::u0 = NEW 0
103
      IF ! OFDM_RE_ESTIMATE`
        index_start = `OFDM_ANGLE_EST_NUM`
104
      END
105
106
      k::u0 = LOOP index_start `CARRIERS_NUM`
107
        lambda_hat = CALL LS_support Q Y_{:,k} support
108
        H_hat_{:,:,k} = VNr @ \reshape(lambda_hat, `GRID.R`, `GRID.T`) @ VNt^H
      END
109
      RECOVER H_hat
110
111
      MERGE
112
    conclusion: |
      PRINT "">>\t"" `JOB_CNT`+1 '/' `JOB_NUM` '\n'
113
114
    simulation:
      backend: cpp # cpp (default) | matlab | octave | py
115
      metric: [NMSE] # used for compare
116
117
      jobs:
        - name: "NMSE v.s. SNR (Pilot: 16)"
118
119
          test_num: 500
120
       SNR: [-10:2:20]
```

```
121
    SNR_mode: dB # dB (default) | linear
122
          pilot: 16
          # pilot_mode: percent # num (default) | percent
123
          algorithms: # compare different languages
124
            - alg: OMP
125
126
              max_iter: 6
127
              macro:
128
                 - name: OFDM_ANGLE_EST_NUM
129
                   value: 1
130
              label: OMP (1) # used in report
131
            - alg: OMP
132
              max_iter: 6
133
               macro:
                 - name: OFDM_ANGLE_EST_NUM
134
135
                   value: 2
              label: OMP (2) # used in report
136
            - alg: OMP
137
              max_iter: 6
138
              macro:
139
140
                 - name: OFDM_ANGLE_EST_NUM
141
                   value: 4
              label: OMP (4) # used in report
142
143
            - alg: OMP
144
              max_iter: 6
145
              macro:
146
                 - name: OFDM_ANGLE_EST_NUM
147
                   value: 8
              label: OMP (8) # used in report
148
149
            - alg: OMP
150
              max_iter: 6
151
              macro:
                 - name: OFDM_ANGLE_EST_NUM
152
153
                   value: 8
                 - name: OFDM_RE_ESTIMATE
154
155
                   value: true
              label: OMP (8R) # used in report
156
157
            - alg: OMP
              max_iter: 6
158
159
              macro:
                 - name: OFDM_ANGLE_EST_NUM
160
161
                   value: 64
              label: OMP (All) # used in report
            - alg: Oracle_LS
164
              label: Oracle LS
165
               macro:
                 - name: OFDM_ANGLE_EST_NUM
166
167
                  value: 64
        - name: "NMSE v.s. Pilot (SNR: 0 dB)"
168
169
          test_num: 500
170
          SNR: 0
171
          pilot: [6:2:32]
          # pilot_mode: percent # num (default) | percent
172
          algorithms: # compare different languages
173
174
             - alg: OMP
175
              max_iter: 6
176
               macro:
                 - name: OFDM_ANGLE_EST_NUM
177
178
                   value: 1
              label: OMP (1) # used in report
179
            - alg: OMP
180
              max_iter: 6
181
182
              macro:
183
                 - name: OFDM_ANGLE_EST_NUM
184
                value: 2
```

```
185
              label: OMP (2) # used in report
186
             - alg: OMP
187
              max_iter: 6
188
               macro:
                 - name: OFDM_ANGLE_EST_NUM
189
190
                   value: 4
              label: OMP (4) # used in report
191
192
            - alg: OMP
193
               max_iter: 6
194
               macro:
195
                 - name: OFDM_ANGLE_EST_NUM
196
                   value: 8
               label: OMP (8) # used in report
197
198
            - alg: OMP
               max_iter: 6
199
200
               macro:
                 - name: OFDM_ANGLE_EST_NUM
201
202
                   value: 8
                 - name: OFDM_RE_ESTIMATE
203
204
                   value: true
205
              label: OMP (8R) # used in report
206
            - alg: OMP
207
              max_iter: 6
208
               macro:
209
                 - name: OFDM_ANGLE_EST_NUM
210
                   value: 64
              label: OMP (All) # used in report
211
212
            - alg: Oracle_LS
213
              label: Oracle LS
214
               macro:
                 - name: OFDM_ANGLE_EST_NUM
215
216
                   value: 64
217
        - name: "NMSE v.s. Pilot (SNR: 10 dB)"
218
          test_num: 500
          SNR: 10
219
          pilot: [6:2:32]
220
          # pilot_mode: percent # num (default) | percent
221
          algorithms: # compare different languages
222
            - alg: OMP
223
224
              max_iter: 6
225
              macro:
226
                 - name: OFDM_ANGLE_EST_NUM
227
                   value: 1
228
              label: OMP (1) # used in report
229
            - alg: OMP
230
              max_iter: 6
231
              macro:
                 - name: OFDM_ANGLE_EST_NUM
232
233
                   value: 2
234
              label: OMP (2) # used in report
235
            - alg: OMP
236
               max_iter: 6
237
               macro:
238
                 - name: OFDM_ANGLE_EST_NUM
239
                   value: 4
              label: OMP (4) # used in report
240
            - alg: OMP
241
               max_iter: 6
242
243
               macro:
244
                 - name: OFDM_ANGLE_EST_NUM
245
                   value: 8
246
              label: OMP (8) # used in report
247
            - alg: OMP
248
             max_iter: 6
```

```
249
               macro:
250
                 - name: OFDM_ANGLE_EST_NUM
251
                   value: 8
252
                 - name: OFDM_RE_ESTIMATE
253
                   value: true
254
              label: OMP (8R) # used in report
            - alg: OMP
255
256
               max_iter: 6
257
               macro:
258
                 - name: OFDM_ANGLE_EST_NUM
259
                   value: 64
260
               label: OMP (All) # used in report
261
             - alg: Oracle_LS
262
               label: Oracle LS
263
               macro:
                 - name: OFDM_ANGLE_EST_NUM
264
265
                   value: 64
266
      report:
        name: OFDM_mmWave_CE_OMP_Simulation
267
268
        format: [pdf, latex] # both compiled PDF and tex files
269
        plot: true # plot data
270
        table: false # do not print table
271
        latex:
272
           command: pdflatex # command to compile the report
273
          UTF8: false # no need for UTF8 support with this setting
```

3.2 Algorithms

Listing 2: OMP.alg

```
1 #! Function: OMP
2 #! Description: Orthogonal matching pursuit compressed sensing.
3 #! Author: Wuqiong Zhao
4 #! Date: 2022-09-16
   #! Version: 0.1.0
5
6
7
   # Input:
      - Q: Sensing matrix
8
   #
9
   #
      - y: Received signal
10
   #
       - L: Sparsity
11
   # Output:
12
   # - h: The estimated sparse signal
   h::v = FUNCTION OMP Q::m y::v L::u0
     COMMENT Start of OMP algorithm!
14
     h = \langle zeros(size(Q, 1)) # initialize as zeros
15
     Q_H:= m = NEW Q^H # the conjugate transpose of Q
16
     r = NEW y # residual
17
     r_{last:v} = NEW r * 2 # the residual in last iteration
18
     support = INIT \length(y) dtype=u # over-length support array
19
20
     term = INIT $\size(Q_H, 0)$ dtype=f # float number array
     j::u0 = NEW 0
21
     a::v = INIT
22
     FOR "" j != \left(y\right) = j + 1
23
24
       term = \abs(Q_H @ r)
25
       index::u0 = NEW \index_max(term)
26
       IF j && \ismember(index, support_{0:j-1})
2.7
         BREAK # end of the LOOP
28
       END
       support_{j} = index
29
       columns::m = NEW Q_{{:, support_{0:j}}}
30
       a = \solve(columns, y)
31
32
       r = y - columns @ a
     IF \sum_{sum(abs(r-r_last))} / \sum_{abs(r_last)} < 0.0001 || j + 1 >= L
```

```
j = j + 1
34
35
         BREAK # accurate enough to end iteration
36
       ELSE
37
         r_{last} = r
38
       END
     END
39
     # prepare for the final return
40
     h_{support_{0:j-1}} = a
41
42
   END
```

Listing 3: Oracle_LS.alg

```
#! Function: Oracle_LS
   #! Description: Oracle LS compressed sensing.
2
   #! Author: Wuqiong Zhao
3
   #! Date: 2022-09-18
4
   #! Version: 0.1.0
5
6
7
   # Input:
8
   #
      - Q: Sensing matrix
       - y: Received signal
9
     - indices: Indices of non-zero elements
10
   #
   # Output:
11
   # - h: The estimated sparse signal
12
   h::v = FUNCTION Oracle_LS Q::m y::v indices::u1
13
   h = \langle zeros(\langle size(Q,1) \rangle)
14
   h_{indices} = \min(Q_{indices}) Q y
15
  END
```

4 mmCEsim Information

This report is auto generated by mmCEsim. The application **mmCEsim** is a powerful tool to simulate millimeter wave (mmWave) channel estimation (CE) for both experts and learners.

mmCEsim is open source! The software can be freely used and distributed under the MIT license.

- Official Website: https://mmcesim.org
- Documentation: https://mmcesim.org/doc
- Tutorial: https://mmcesim.org/tutorial
- Examples: https://mmcesim.org/example
- Web Application: https://app.mmcesim.org
- Blog: https://blog.mmcesim.org
- Publications: https://pub.mmcesim.org
- GitHub Organization: https://github.com/mmcesim
- Twitter: https://twitter.com/mmcesim
- VS Code Extension: https://marketplace.visualstudio.com/items?itemName=mmcesim.mmcesim