

Q Given  $y' = \frac{y-x}{y+2}$  with  $y_0 = 1$  find  $y$  for  
 $x = 0.1$  in four steps Euler's Method.

Solution:

So let  $h = 0.1 = 0.025$  given  $y_0 = 1$   
where  $x = 0$

we know that,

$$y_{n+1} = y_n + h f(x_n, y_n)$$

By putting  $n = 0, 1, 2, 3$ , we obtain

$$y_1 = y_0 + h f(x_0, y_0) \\ = 1 + 0.025 \frac{(1-0)}{(1+0)} = 1.025$$

$$y_n = 1.025$$

$$\text{Again } y_2 = y_1 + h f(x_1, y_1) \\ = 1.025 + 0.025 \frac{(1.025 - 0.25)}{(1.025 + 0.025)}$$

$$(\text{where } x_1 = x_0 + h = 0 + 0.025 \\ \Rightarrow x_1 = 0.025)$$

$$= 1.0488$$

$$y_2 = 1.0488$$

$$\text{Now again, } y_3 = y_2 + h f(x_2, y_2)$$

$$(\text{where } x_2 = x_0 + 2h = 0 + 1 \times 0.025 = 0.05)$$

$$= 1.0488 + 0.025 \frac{(1.0488 - 0.05)}{(1.0488 + 0.05)}$$

$$= 1.0715$$

$$y_3 = 1.07152$$

$$y_4 = y_3 + h f(x_3, y_3) \text{ where } x_3 = x_0 + 3h = 0 + 3 \times 0.025 = 0.075$$

$$= 1.07152 + 0.025 \frac{(1.07152 - 0.075)}{(1.07152 + 0.075)}$$

$$y_4 = 1.09324 \text{ at } (x_4 = x_0 + 4h = 0 + 4 \times 0.025 = 0.1)$$

$$y_4 = 1.09324 \text{ Hence,}$$

$$\boxed{y(0.1) = 1.09324}$$