

# Outline

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- Evaluation

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- Metrics for Performance Evaluation
  - How to evaluate the performance of a model?
- Methods for Performance Evaluation
  - How to obtain reliable estimates?
- Methods for Model Comparison
  - How to compare the relative performance among competing models?

# Model Evaluation

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# Metrics for Performance Evaluation

- Focus on the predictive capability of a model
  - Rather than how fast it takes to classify or build models, scalability, etc.
- Confusion Matrix:

ACTUAL CLASS	PREDICTED CLASS		
		Class=Yes	Class=No
	Class=Yes	a	b
	Class=No	c	d

a: TP (true positive)  
b: FN (false negative)  
c: FP (false positive)  
d: TN (true negative)

# Confusion Matrix

ACTUAL CLASS	PREDICTED CLASS		
		Cat	Dog
	Cat	a	b
	Dog	c	d

**a: TP (true positive)**

**b: FN (false negative)**

**c: FP (false positive)**

**d: TN (true negative)**

# Measure

	PREDICTED CLASS		
ACTUAL CLASS		Class=Yes	Class=No
	Class=Yes	a	b
	Class=No	c	d

All samples of “yes”

$$\text{Recall (r)} = \frac{a}{a + b}$$

# Measure

		PREDICTED CLASS	
ACTUAL CLASS		Class=Yes	Class=No
	Class=Yes	a	b
	Class=No	c	d
	All samples predicted as yes"		

$$\text{Precision (p)} = \frac{a}{a + c}$$

# Measure

		PREDICTED CLASS		
ACTUAL CLASS		Class=Yes	Class=No	
	Class=Yes	a	b	All samples of "yes"
	Class=No	c	d	
		All samples predicted as "yes"		

$$F\text{-measure (F)} = \frac{2rp}{r + p} = ? \qquad \frac{2a}{2a + b + c}$$



# Accuracy

ACTUAL CLASS	PREDICTED CLASS	
	Class=Yes	Class=No
Class=Yes	a (TP)	b (FN)
	c (FP)	d (TN)

- Most widely-used metric:

$$\text{Accuracy} = \frac{a + d}{a + b + c + d} = \frac{TP + TN}{TP + TN + FP + FN}$$

# Limitation of Accuracy

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- Consider a 2-class problem
  - Number of Class 0 examples = 9990
  - Number of Class 1 examples = 10
- If model predicts everything to be class 0, accuracy is  $9990/10000 = 99.9\%$ 
  - Accuracy is misleading because model does not detect any class 1 example

# Cost Matrix

	PREDICTED CLASS		
	$C(i j)$	Class=Yes	Class=No
	Class=Yes	$C(\text{Yes} \text{Yes})$	$C(\text{No} \text{Yes})$
	Class=No	$C(\text{Yes} \text{No})$	$C(\text{No} \text{No})$

$C(i|j)$ : Cost of misclassifying class  $j$  example as class  $i$

# Computing Cost of Classification

Cost Matrix	PREDICTED CLASS		
ACTUAL CLASS	C(i j)	+	-
	+	-1	100
	-	1	0

Model $M_1$	PREDICTED CLASS		
ACTUAL CLASS		+	-
	+	150	40
	-	60	250

Accuracy = 80%

Cost = 3910

Model $M_2$	PREDICTED CLASS		
ACTUAL CLASS		+	-
	+	250	45
	-	5	200

Accuracy = 90%

Cost = 4255

# Weighted Accuracy

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$$\text{Weighted Accuracy} = \frac{w_1 a + w_4 d}{w_1 a + w_2 b + w_3 c + w_4 d}$$

# Quiz: evaluation

We developed a Random Decision algorithm to classify an email to be spam and non-spam.

Data: 100 spam emails, 200 nonspam emails.

With the following results, please calculate: i) recall; ii) precision; iii) F- measure; and iv) accuracy

Ground-truth label	Prediction		
		Spam	Non-spam
	spam	70	30
	Non-spam	20	180

# Quiz: accuracy

Animal classification problem. Given the following confusion matrix, can you calculate the accuracy?

	Dog	Cat	monkey
Dog	80	10	5
Cat	30	60	10
monkey	10	8	82

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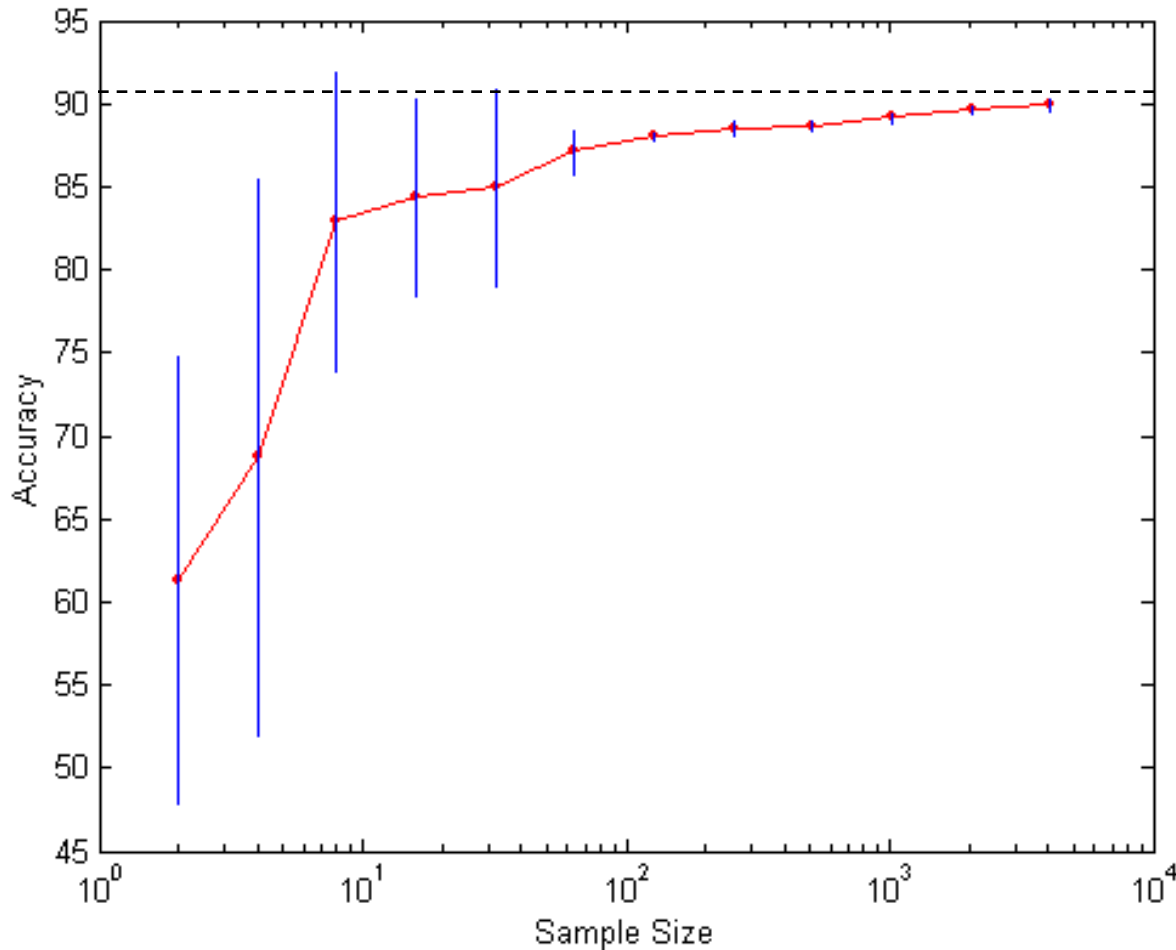


# Methods for Performance Evaluation

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- How to obtain a reliable estimate of performance?
- Performance of a model may depend on other factors besides the learning algorithm:
  - Class distribution
  - Cost of misclassification
  - Size of training and test sets

# 1. Learning Curve



- Learning curve shows how accuracy changes with varying sample size
- Requires a sampling schedule for creating learning curve:
  - Arithmetic sampling (Langley, et al)
  - Geometric sampling (Provost et al)

Effect of small sample size:

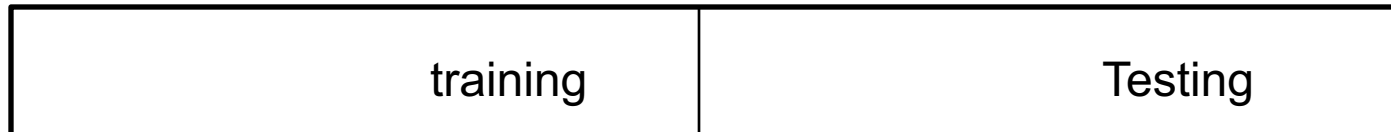
- Bias in the estimate
- Variance of estimate

## 2. Holdout

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Reserve  $2/3$  for training and  $1/3$  for testing



Reserve  $1/2$  for training and  $1/2$  for testing

# 3. Cross validation

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**Partition data into  $k$  disjoint subsets**

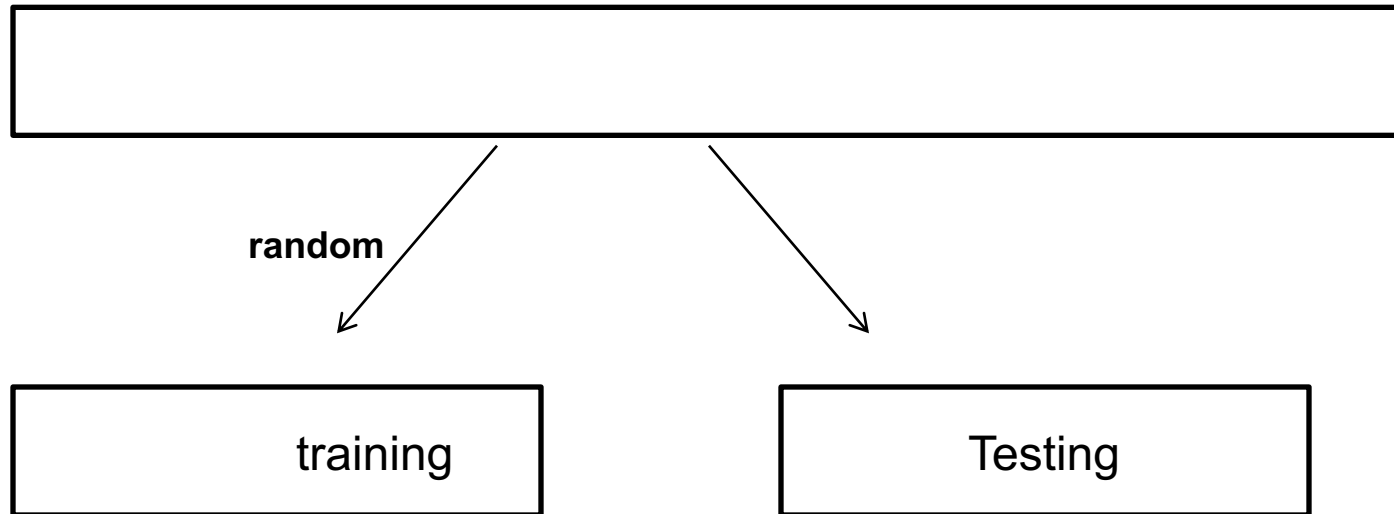
**k-fold: train on  $k-1$  partitions, test on the remaining one;**

**Leave-one-out**

# 4. Sampling: bootstrap

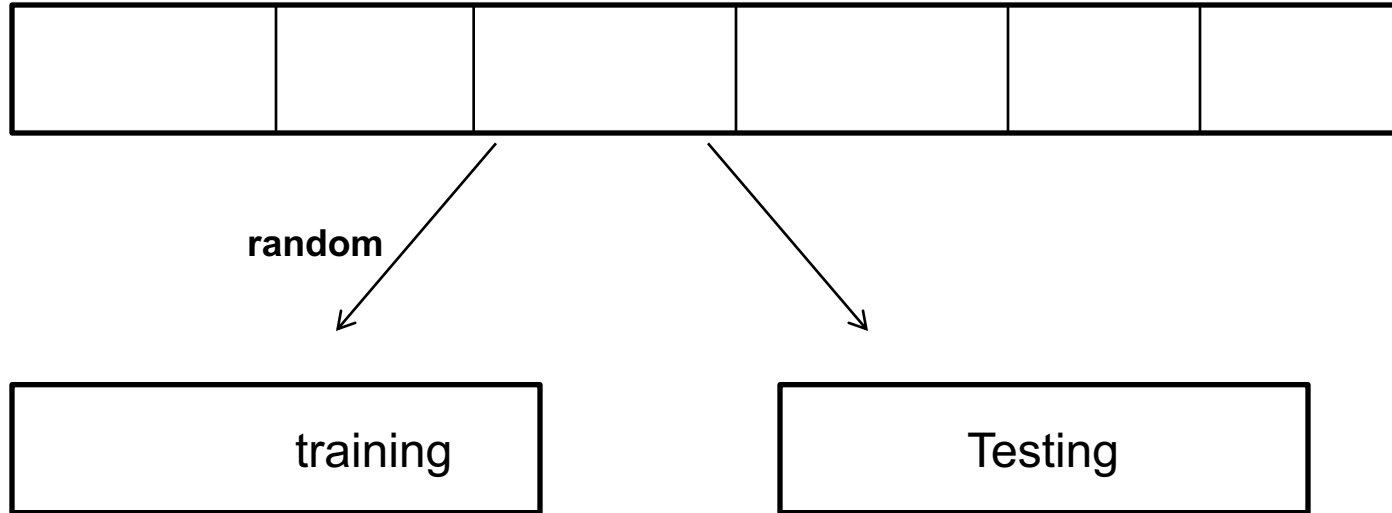
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## Sampling with replacement



# 5. Stratified sampling

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**oversampling vs undersampling**

# Recap: evaluation methods

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1. Learning curve
2. Hold-out
3. Cross-validation
4. Bootstrap
5. Stratified sampling

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- **Methods for Model Comparison**
  - How to compare the relative performance among competing models?



# ROC (Receiver Operating Characteristic)

- Developed in 1950s for signal detection theory to analyze noisy signals
  - Characterize the trade-off between positive hits and false alarms
- ROC curve plots TP (on the y-axis) against FP (on the x-axis)

ACTUAL CLASS	PREDICTED CLASS	
	Class=Yes	Class=No
Class=Yes	a (TP)	b (FN)
	c (FP)	d (TN)

# ROC: basic idea

Instance	$P(+ A)$	True Class
1	0.95	+
2	0.93	+
3	0.87	-
4	0.85	-
5	0.85	-
6	0.85	+
7	0.76	-
8	0.53	+
9	0.43	-
10	0.25	+

- Use classifier that produces posterior probability for each test instance  $P(+|A)$
- Sort the instances according to  $P(+|A)$  in decreasing order
- What's the appropriate threshold to pick up the positive samples?

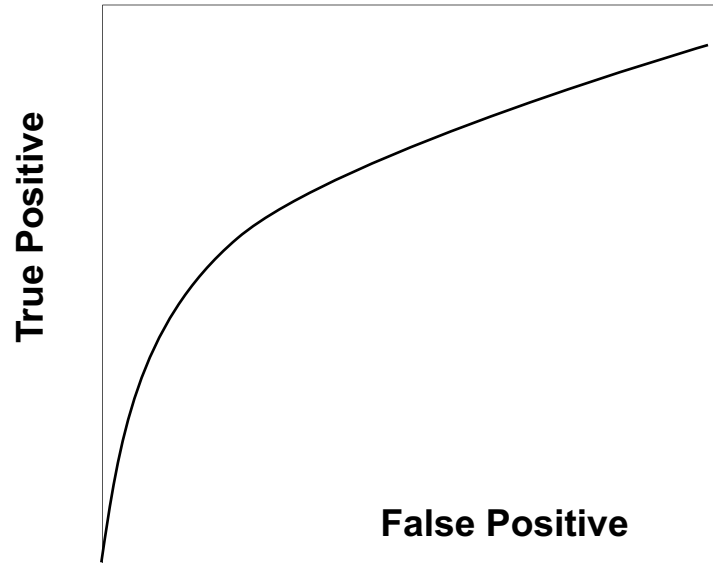
# Conti.

Instance	$P(+ A)$	True Class
1	0.95	+
2	0.93	+
3	0.87	-
4	0.85	-
5	0.85	-
6	0.85	+
7	0.76	-
8	0.53	+
9	0.43	-
10	0.25	+

• For each unique value, consider it as a threshold

- Count the number of TP, FP, TN, FN.
- TP rate, TPR =  $TP / (TP + FN)$
- FP rate, FPR =  $FP / (FP + TN)$

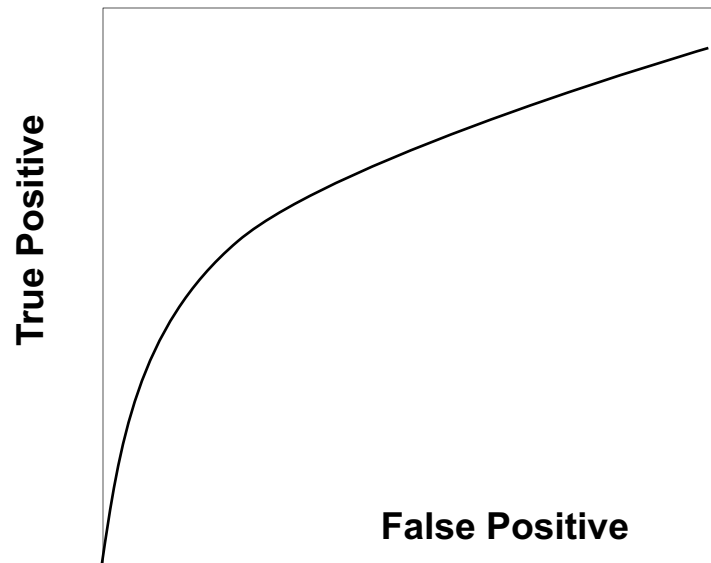
	Class=Yes	Class=No
Class=Yes	a (TP)	b (FN)
Class=No	c (FP)	d (TN)



**ROC (Receiver Operating Characteristic)**

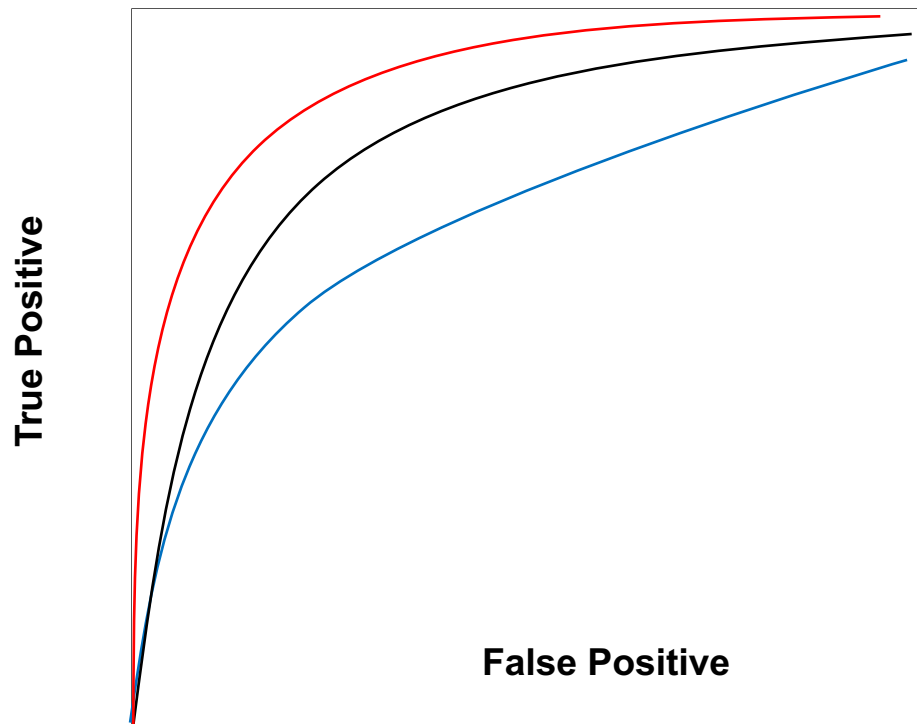
# ROC

- Performance of each classifier represented as a point on the ROC curve
  - changing the threshold of algorithm, sample distribution or cost matrix changes the location of the point



# Quiz

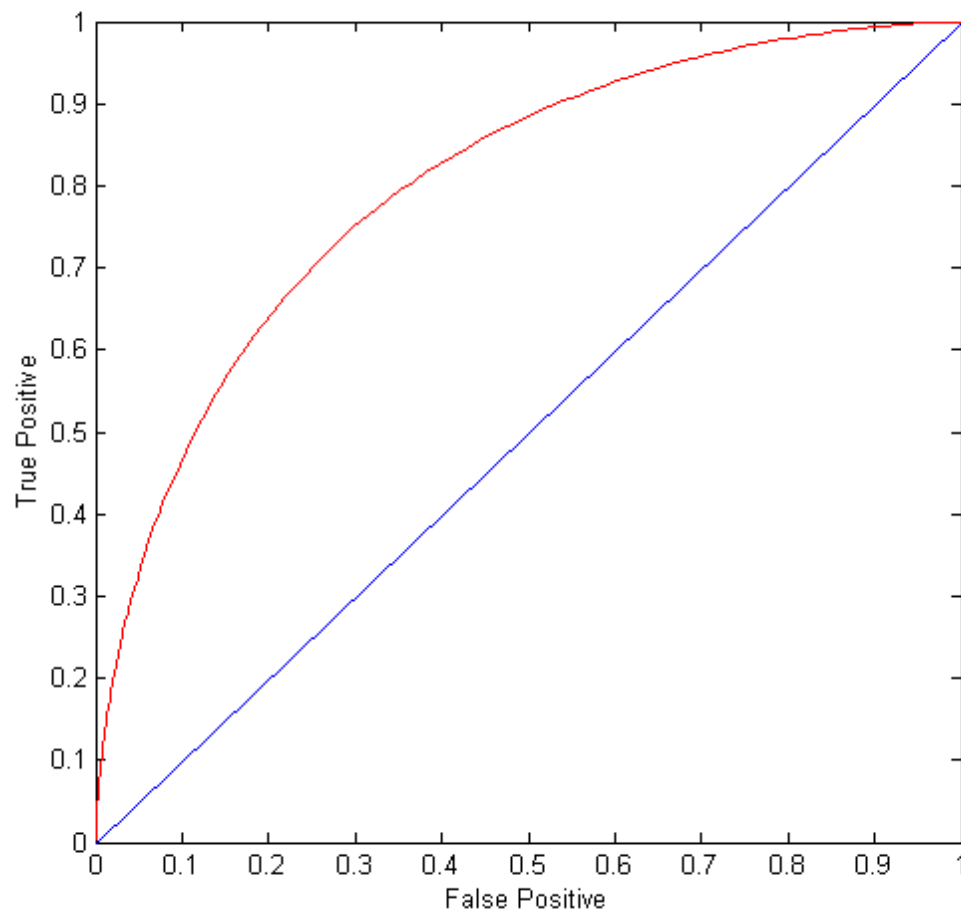
For spam email classification problem, suppose you have three different models with the following ROCs. Which algorithm is the best?



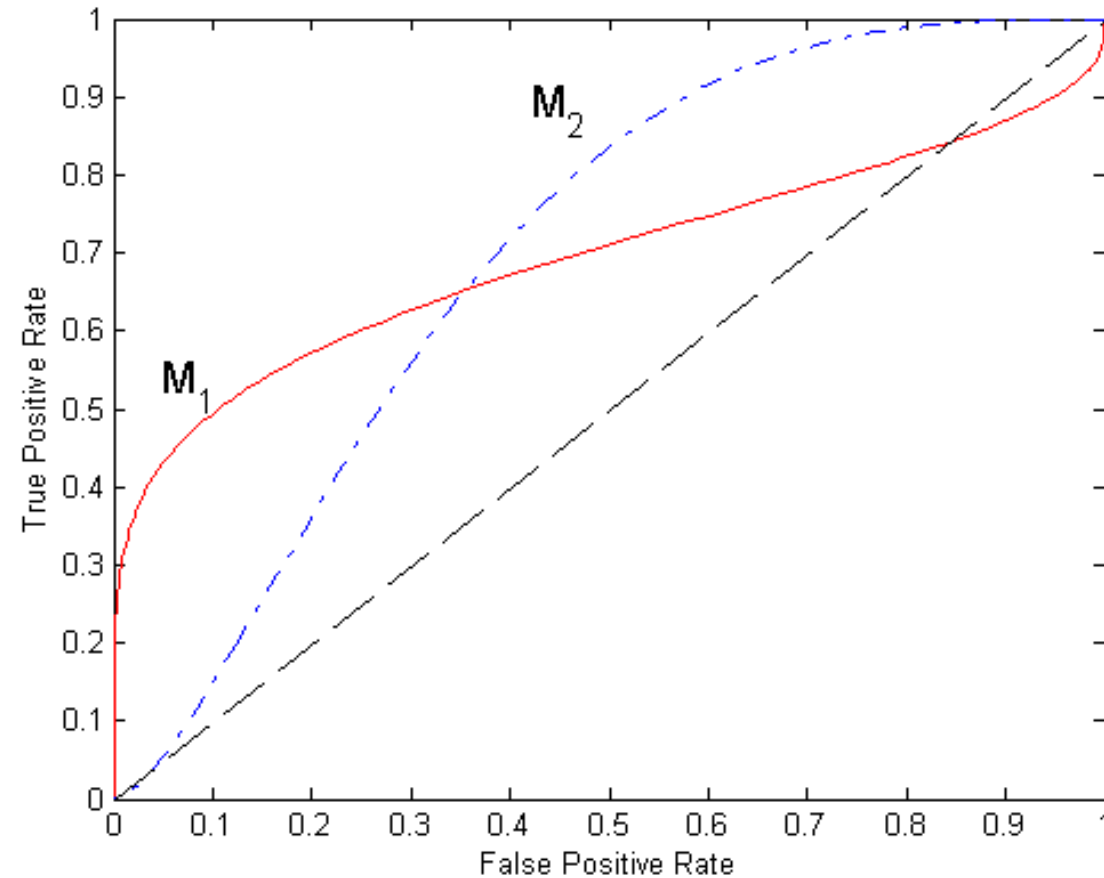
# Understanding ROC Curve

(True Positive, False Positive)

- (0,0): declare everything to be negative class
- (1,1): declare everything to be positive class
- (1,0): ideal
- Diagonal line:
  - Random guessing
  - Below diagonal line:
    - ◆ prediction is opposite of the true class



# Using ROC for Model Comparison



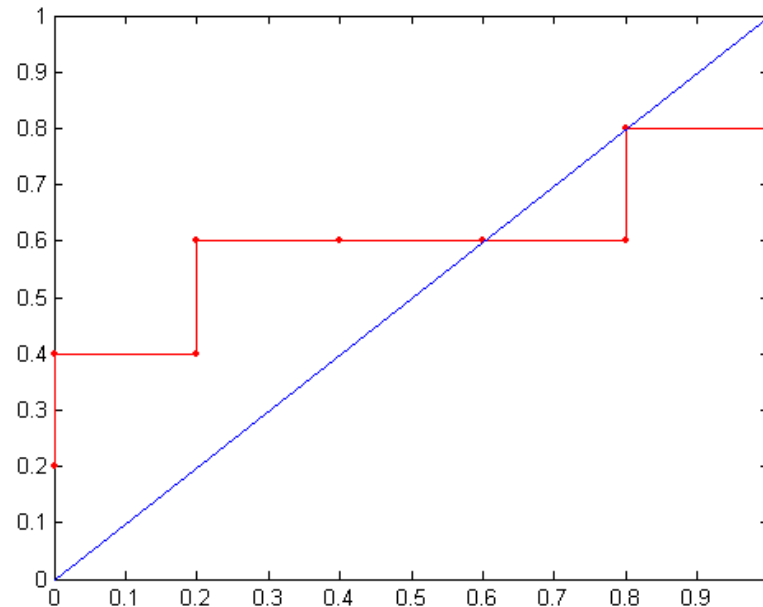
- No model consistently outperform the other
  - $M_1$  is better for small FPR
  - $M_2$  is better for large FPR
- Area Under the ROC curve
  - Ideal:
    - Area = 1
  - Random guess:
    - Area = 0.5



# How to construct an ROC curve

Class	+	-	+	-	-	-	+	-	+	+	
Threshold $\geq$	0.25	0.43	0.53	0.76	0.85	0.85	0.85	0.87	0.93	0.95	1.00
TP	5	4	4	3	3	3	3	2	2	1	0
FP	5	5	4	4	3	2	1	1	0	0	0
TN	0	0	1	1	2	3	4	4	5	5	5
FN	0	1	1	2	2	2	2	3	3	4	5
TPR	1	0.8	0.8	0.6	0.6	0.6	0.6	0.4	0.4	0.2	0
FPR	1	1	0.8	0.8	0.6	0.4	0.2	0.2	0	0	0

ROC Curve:



# Summery of today

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- Metrics for Performance Evaluation
  - Confusion Matrix; recall; precision; F-measure; accuracy
- Methods for Performance Evaluation
  - Learning curve; Hold-out; Cross-validation; Bootstrap; Stratified sampling
- Methods for Model Comparison
  - ROC curves