

Imbalanced Data

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Outline

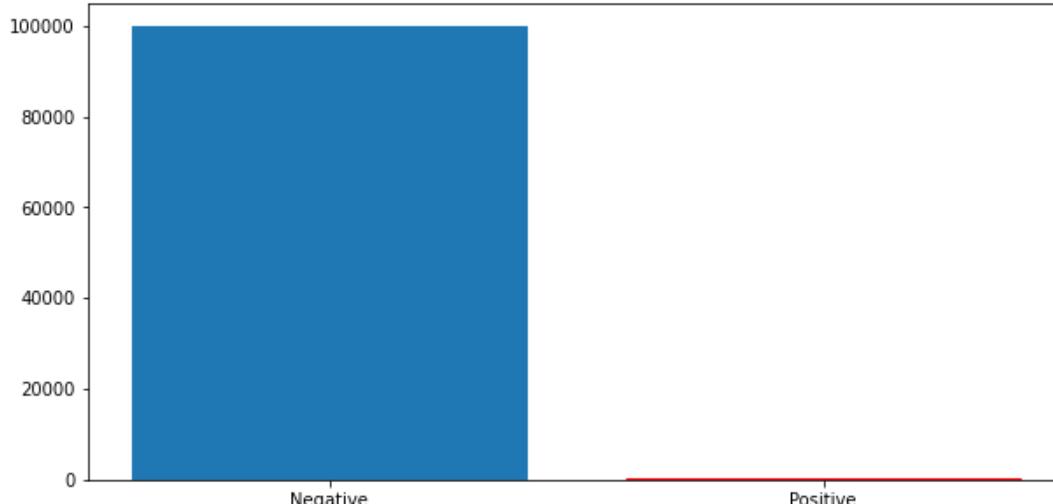
- Introduction
- Focal Loss
- Metrics
- Data Augmentation
- Experiments

Classification on Imbalanced Data

❖ Imbalanced Data vs. Balanced Data

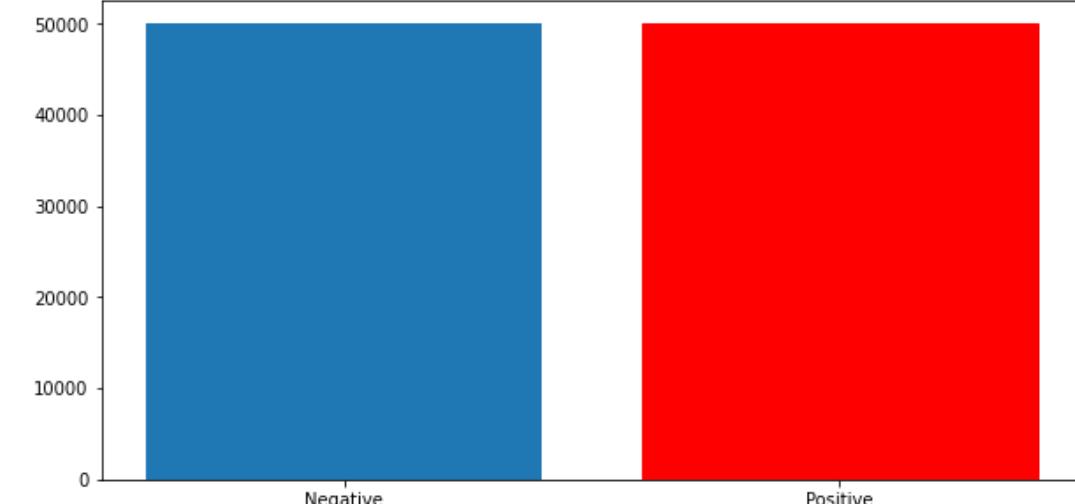
Imbalanced Data

| | |
|----------|--------|
| Negative | 100000 |
| Positive | 200 |



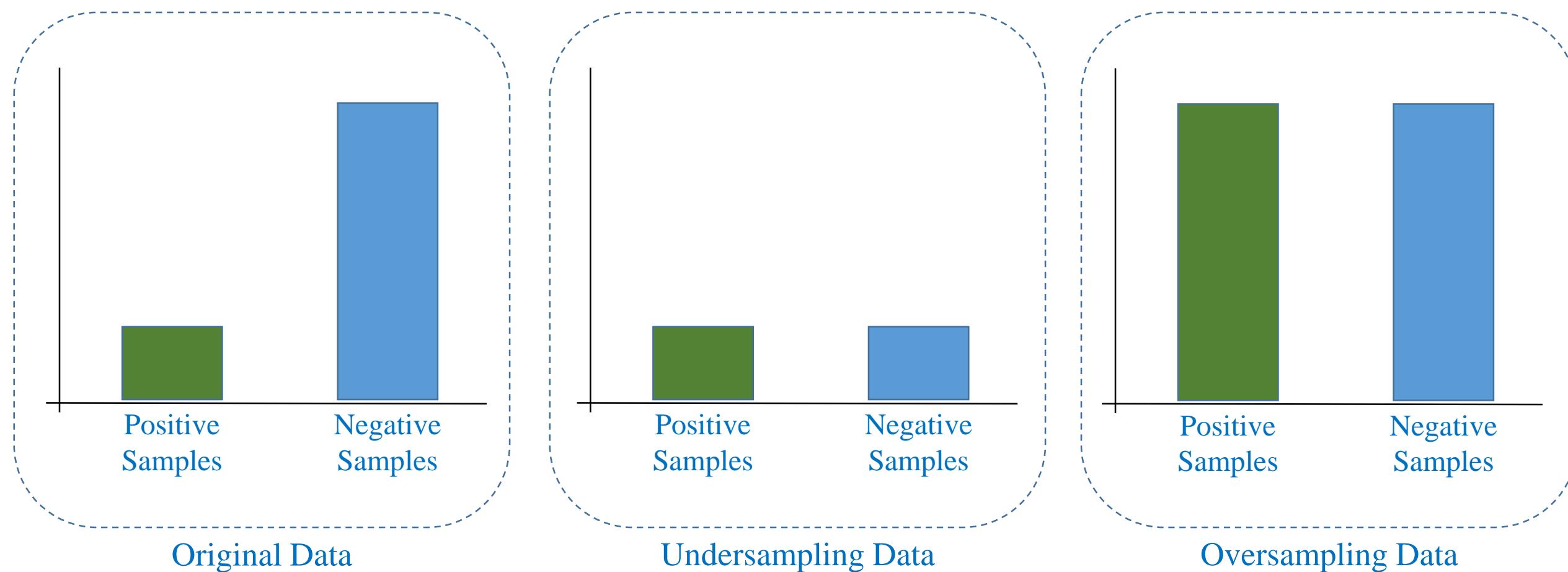
Balanced Data

| | |
|----------|-------|
| Negative | 50100 |
| Positive | 50100 |



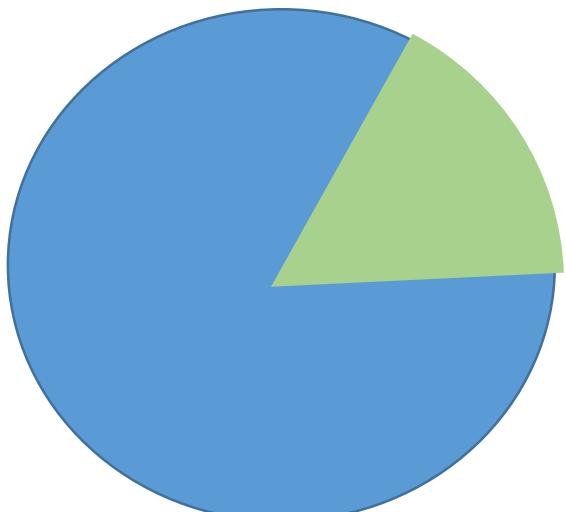
Imbalanced Data

❖ Approach 1: Data manipulation



Imbalanced Data

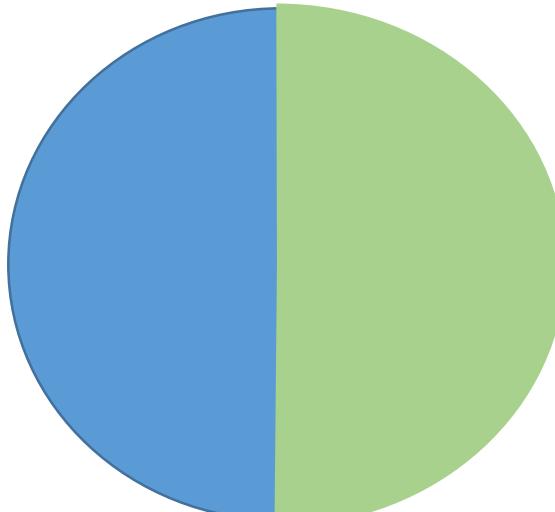
❖ Approach 2: Loss Functions



Total loss

Negative loss

Positive loss



Total loss

Class weight

$$w_p = \frac{N}{2N_p}$$

Tell the model to "pay more attention" to samples from an under-represented class

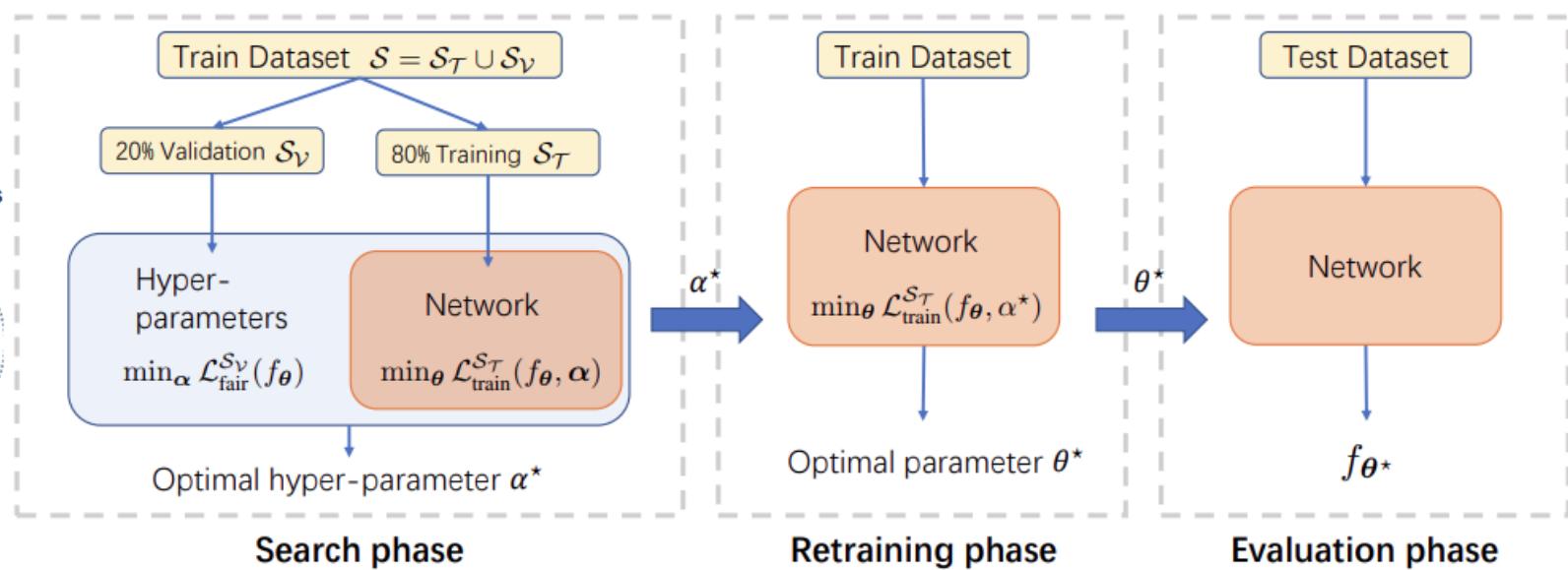
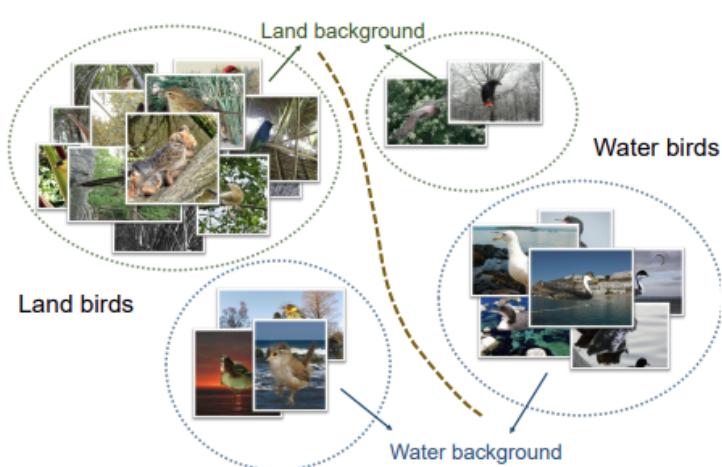
A higher loss means higher optimization which results in efficient classification

Focal loss

$$FL(p_t) = -(1 - p_t)^\gamma \log(p_t)$$

Imbalanced Data

❖ Approach 3: Optimization



<https://arxiv.org/pdf/2201.01212.pdf>

AutoBalance: Optimized Loss Functions for Imbalanced Data, 2022

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- Metrics
- Data Augmentation
- Experiments

Binary Crossentropy

❖ Linear regression

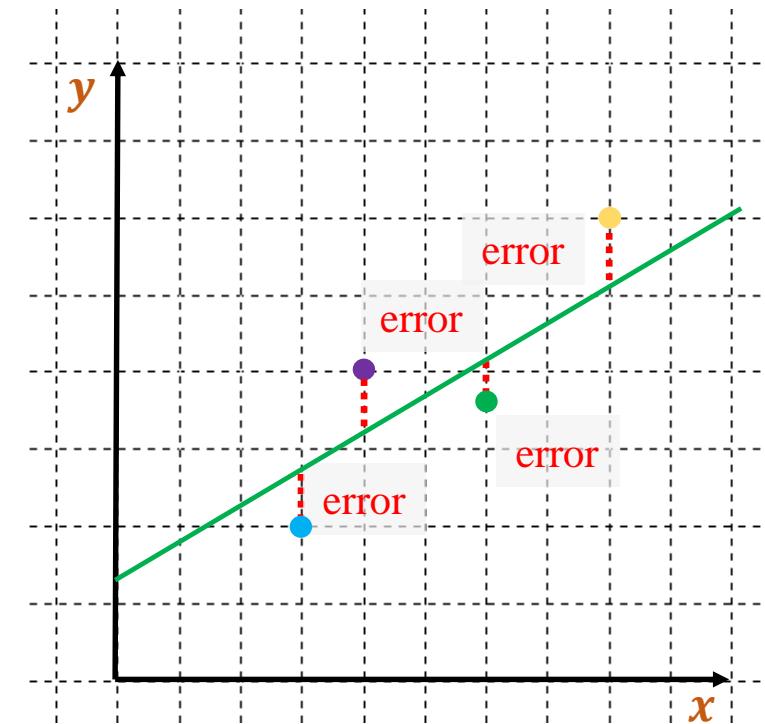
| Area-based House Price Data | |
|-----------------------------|-------|
| Feature | Label |
| area | price |
| 6.7 | 9.1 |
| 4.6 | 5.9 |
| 3.5 | 4.6 |
| 5.5 | 6.7 |

Training data

construct

$$\hat{y} = \theta^T x = ax + b$$
$$\hat{y} \in (-\infty, +\infty)$$

Model



Find the line $\hat{y} = \theta^T x$ that is best fit given data,
then use y to predict for new data

Binary Crossentropy

❖ Given a new kind of data

| Feature | Label |
|--------------|----------|
| Petal_Length | Category |
| 1.4 | Flower A |
| 1 | Flower A |
| 1.5 | Flower A |
| 3 | Flower B |
| 3.8 | Flower B |
| 4.1 | Flower B |

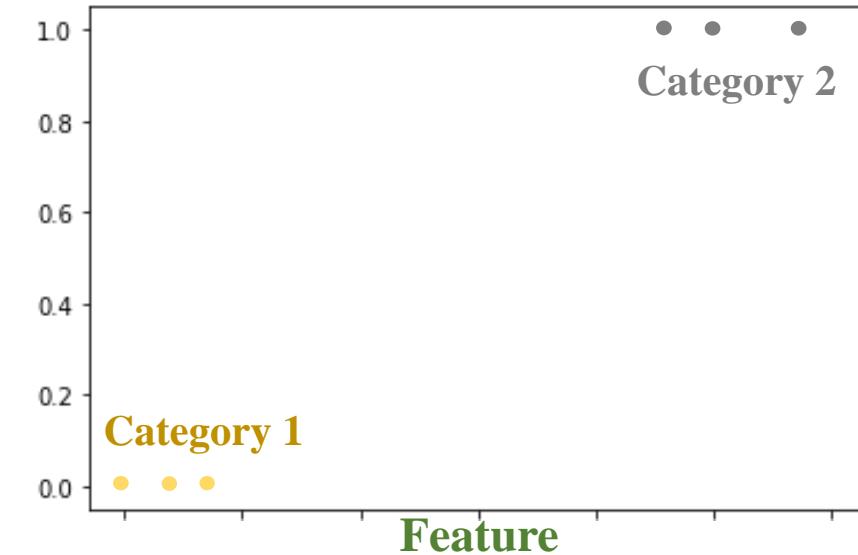
Category 1
Category 2

Assign numbers
to categories

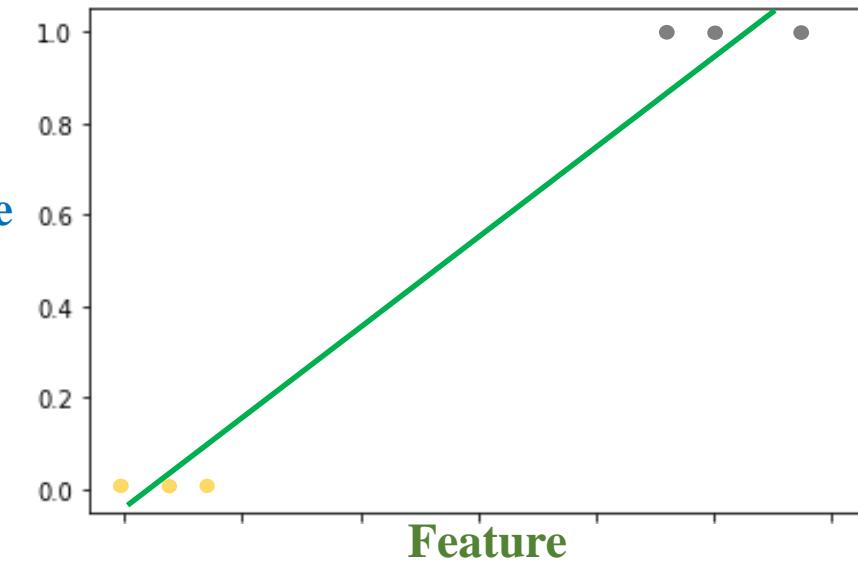
| Feature | Label |
|--------------|----------|
| Petal_Length | Category |
| 1.4 | 0 |
| 1 | 0 |
| 1.5 | 0 |
| 3 | 1 |
| 3.8 | 1 |
| 4.1 | 1 |

Category 1
Category 2

Plot data



A line is not suitable
for this data



Binary Crossentropy

❖ Given a new kind of data

| Feature | Label |
|--------------|----------|
| Petal_Length | Category |
| 1.4 | Flower A |
| 1 | Flower A |
| 1.5 | Flower A |
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Category 1
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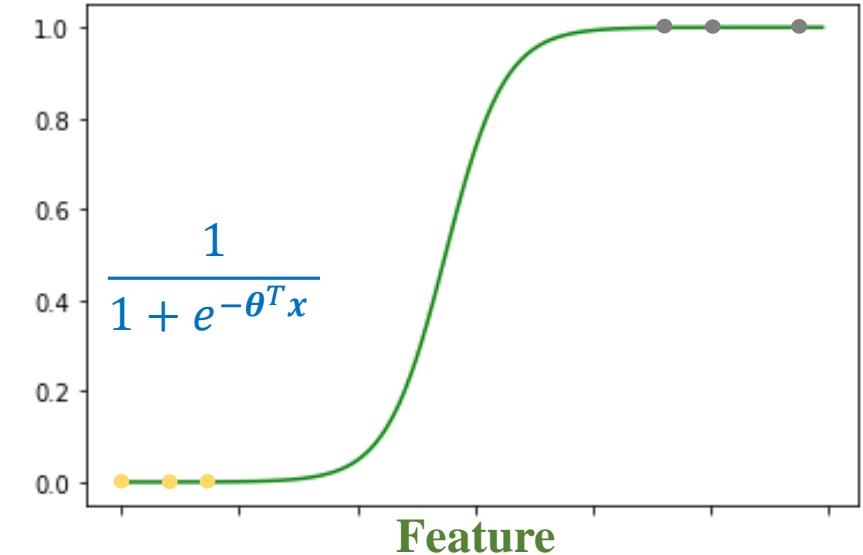
Category 1
Category 2

Sigmoid function
could fit the data

$$z = \theta^T x = x^T \theta$$

$$\hat{y} = \sigma(z) = \frac{1}{1 + e^{-z}}$$

$$\hat{y} \in (0 \quad 1)$$



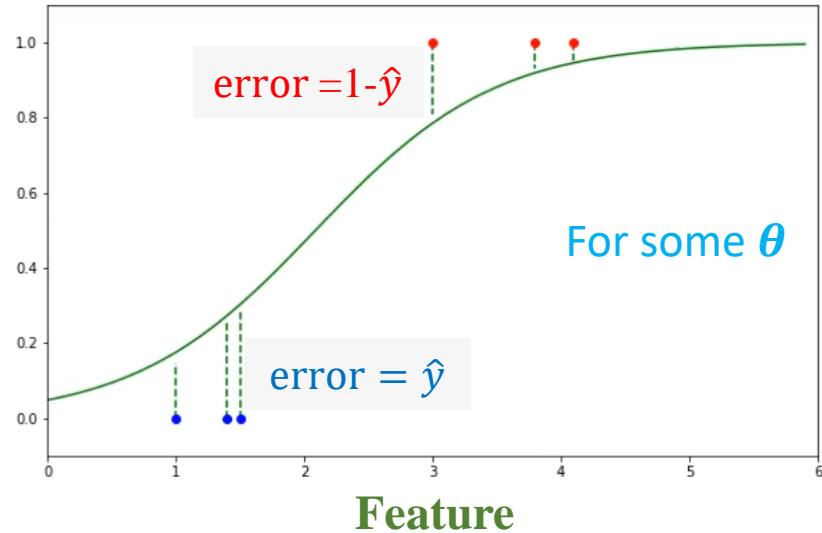
Error

if $y = 1$

$$\text{error} = 1 - \hat{y}$$

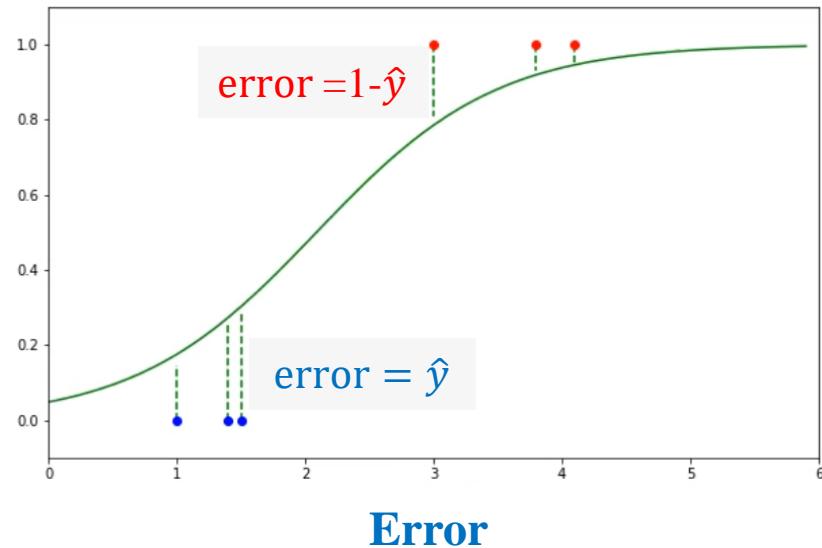
if $y = 0$

$$\text{error} = \hat{y}$$

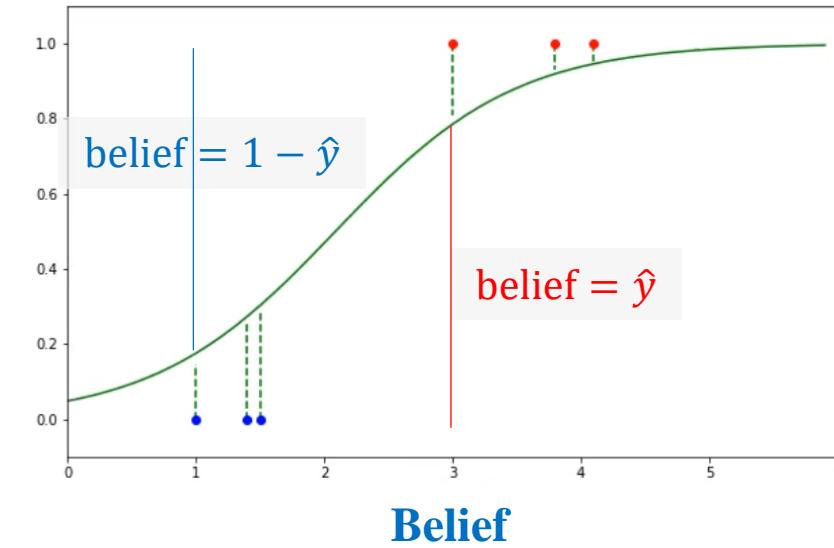


Binary Crossentropy

❖ Construct loss



if $y = 1$
 $\text{error} = 1 - \hat{y}$
if $y = 0$
 $\text{error} = \hat{y}$



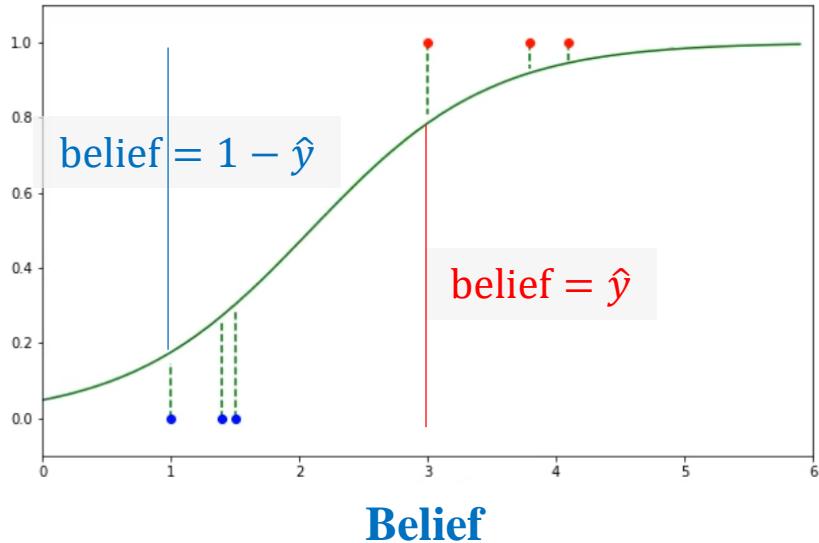
if $y = 1$
 $\text{belief} = \hat{y}$
if $y = 0$
 $\text{belief} = 1 - \hat{y}$

$$P = \hat{y}^y (1 - \hat{y})^{1-y}$$

Minimize error ~ maximize belief ~ Minimize (-belief)

Binary Crossentropy

❖ Construct loss



$$\text{belief} = P$$

$$\log_{\text{belief}} = \log P$$

$$\log_{\text{belief}} = y \log \hat{y} + (1 - y) \log(1 - \hat{y})$$

$$\text{loss} = -\log_{\text{belief}}$$

$$= -[y \log \hat{y} + (1 - y) \log(1 - \hat{y})]$$

$$\text{if } y = 1$$

$$\text{belief} = \hat{y}$$

$$\text{if } y = 0$$

$$\text{belief} = 1 - \hat{y}$$

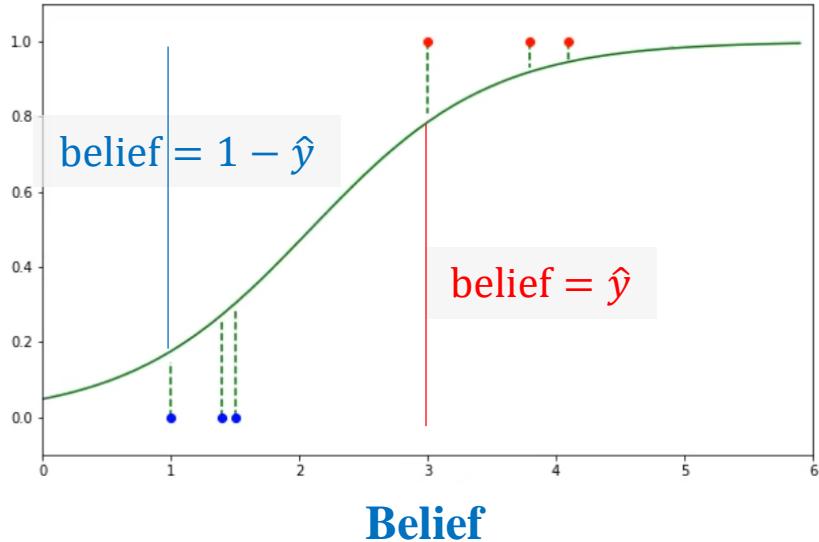
$$P = \hat{y}^y (1 - \hat{y})^{1-y}$$

$$L = -y \log \hat{y} - (1 - y) \log(1 - \hat{y})$$

Binary cross-entropy

Binary Crossentropy

❖ Construct loss



if $y_i = 1$

$$\text{belief} = \hat{y}_i$$

if $y_i = 0$

$$\text{belief} = 1 - \hat{y}_i$$

$$P_i = \hat{y}_i^{y_i} (1 - \hat{y}_i)^{1-y_i}$$

$$\text{belief} = \prod_{i=1}^n P_i \quad \text{since iid}$$

$$\text{log_belief} = \sum_{i=1}^n \log P_i$$

$$\text{log_belief} = \sum_{i=1}^n [y_i \log \hat{y}_i + (1 - y_i) \log (1 - \hat{y}_i)]$$

$$\text{loss} = -\text{log_belief}$$

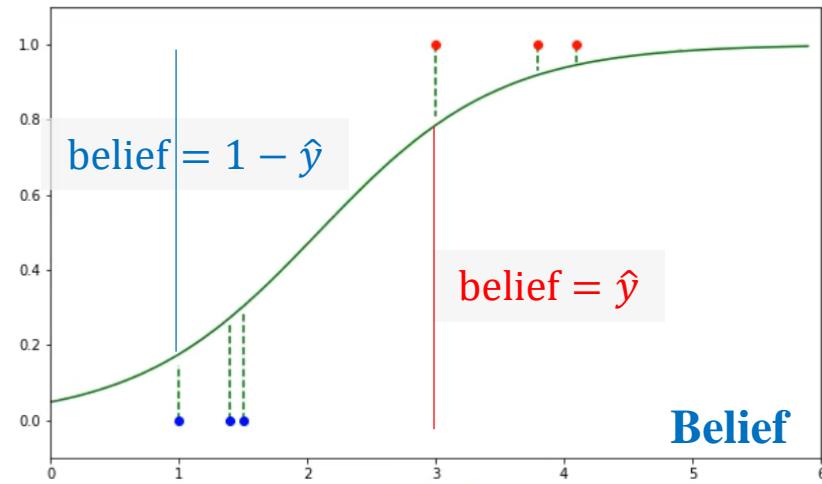
$$= - \sum_{i=1}^n [y_i \log \hat{y}_i + (1 - y_i) \log (1 - \hat{y}_i)]$$

$$L = \frac{1}{N} (-\mathbf{y}^T \log(\hat{\mathbf{y}}) - (1 - \mathbf{y}^T) \log(1 - \hat{\mathbf{y}}))$$

Binary cross-entropy

Binary Crossentropy

❖ Construct loss



$$L = \frac{1}{N} (-\mathbf{y}^T \log(\hat{\mathbf{y}}) - (1 - \mathbf{y}^T) \log(1 - \hat{\mathbf{y}}))$$

Binary cross-entropy

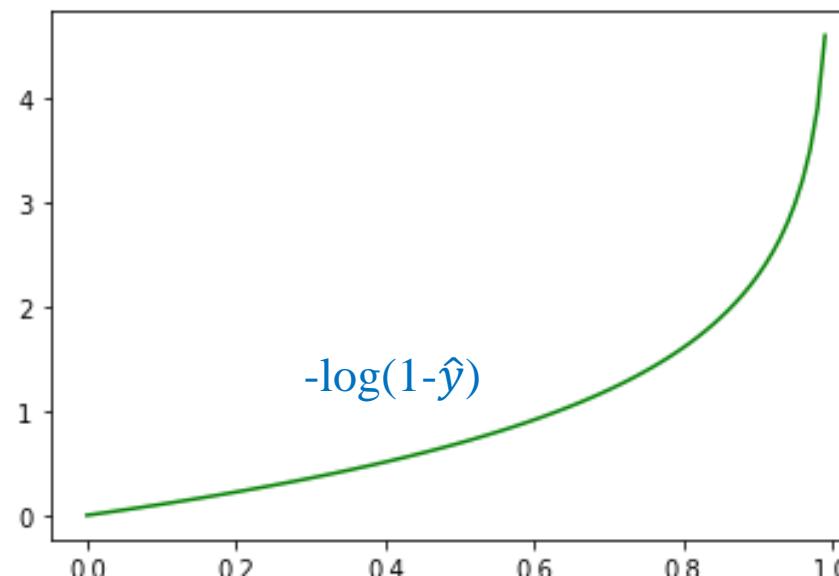
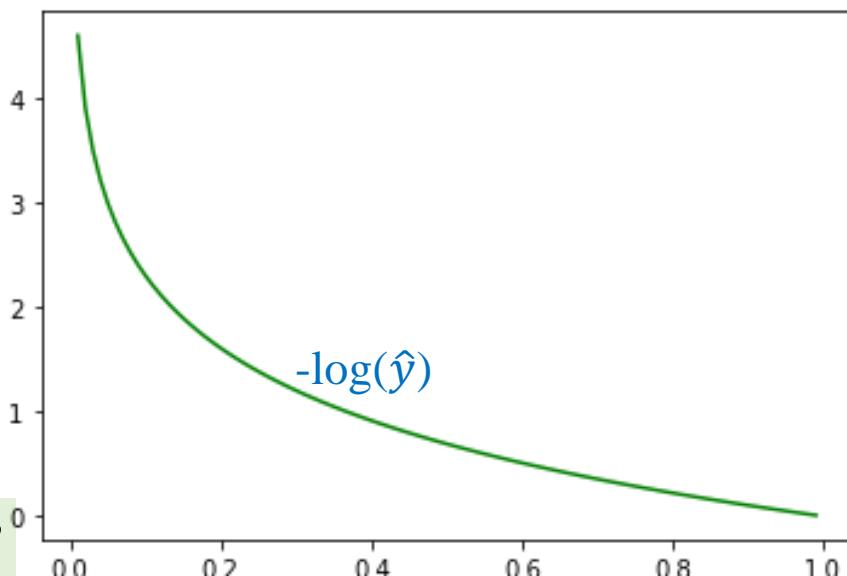
if $y_i = 1$

belief = \hat{y}_i

if $y_i = 0$

belief = $1 - \hat{y}_i$

$$P_i = \hat{y}_i^{y_i} (1 - \hat{y}_i)^{1-y_i}$$



Binary Crossentropy

❖ Construct loss

$$z = \theta^T x$$

$$\hat{y} = \sigma(z) = \frac{1}{1 + e^{-z}}$$

$$L = -y \log(\hat{y}) - (1 - y) \log(1 - \hat{y})$$

Model and Loss

$$\frac{\partial L}{\partial \theta} = \frac{\partial L}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial z} \frac{\partial z}{\partial \theta}$$

$$\frac{\partial L}{\partial \hat{y}} = -\frac{y}{\hat{y}} + \frac{1 - y}{1 - \hat{y}} = \frac{\hat{y} - y}{\hat{y}(1 - \hat{y})}$$

$$\frac{\partial \hat{y}}{\partial z} = \hat{y}(1 - \hat{y})$$

$$\frac{\partial z}{\partial \theta} = x$$

Derivative

$$\frac{\partial L}{\partial \theta} = x(\hat{y} - y)$$

Focal Loss

❖ Binary Cross Entropy Loss

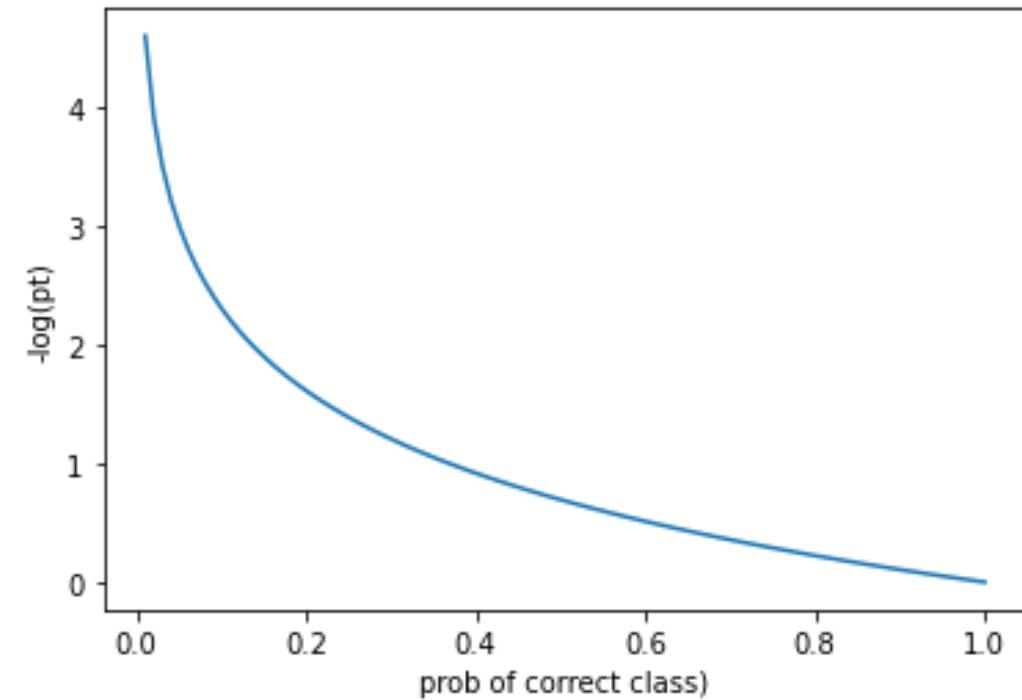
$$\text{BCE}(p, y) = \begin{cases} -\log(p) & \text{if } y = 1 \\ -\log(1 - p) & \text{otherwise} \end{cases}$$

$y \in \{0,1\}$ label cho negative và positive class
 $p \in [0,1]$ xác suất model predict cho một class

Rewrite

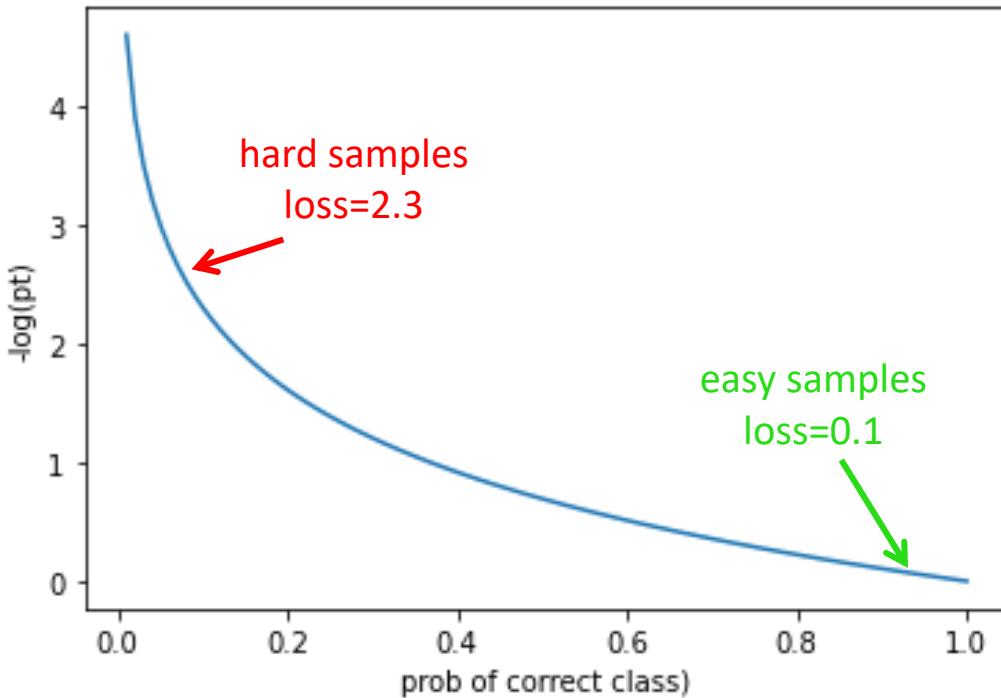
$$p_t = \begin{cases} p & \text{if } y = 1 \\ 1 - p & \text{otherwise} \end{cases}$$

$$\text{BCE}(p, y) = \text{BCE}(p_t) = -\log(p_t)$$



Focal Loss

❖ Binary Cross Entropy Loss



Easy samples loss = $100000 * 0.1 = 10000$

Hard samples loss = $100 * 2.3 = 230$

Loss = Easy samples loss + Hard samples loss

Easy samples loss : Hard samples loss = $10000 : 230 \approx 43$

=> Loss phần lớn bị ảnh hưởng của Easy samples và model có thể bỏ qua hard samples.

=> BCE không tốt cho trường hợp data bị imbalance nặng

Imbalanced Case:

- 100000 easy samples vs 100 hard samples

Focal Loss

❖ Balanced Binary Cross Entropy Loss

$$\text{BCE}(p, y) = \text{BCE}(p_t) = -\log(p_t)$$



weighting
factor

$$\text{Balanced BCE}(p_t) = -\alpha_t \log(p_t)$$

class 1: $\alpha_t \in [0,1]$

class 0 : $1-\alpha_t$

Thêm weighting factor: thông thường là tần suất xuất hiện của class

Số lượng sample >> thì weighting factor <<

Số lượng sample << thì weighting factor >>

=> Giúp cân bằng lại đóng góp vào loss của các class

=> Điều này chỉ giúp cho thay đổi trọng số trên loss của từng class. **Chưa giải quyết vấn đề tập trung vào học các class khó học**

Focal Loss

❖ Focal Loss

$$\text{BCE}(p, y) = \begin{cases} -\log(p) & \text{if } y = 1 \\ -\log(1 - p) & \text{otherwise} \end{cases}$$

Rewrite

$$p_t = \begin{cases} p & \text{if } y = 1 \\ 1 - p & \text{otherwise} \end{cases}$$

$$\text{BCE}(p, y) = \text{BCE}(p_t) = -\log(p_t)$$

modulating factor

$$\text{Focal Loss } (p_t) = -(1 - p_t)^\gamma \log(p_t)$$

γ theo paper test [0, 5]

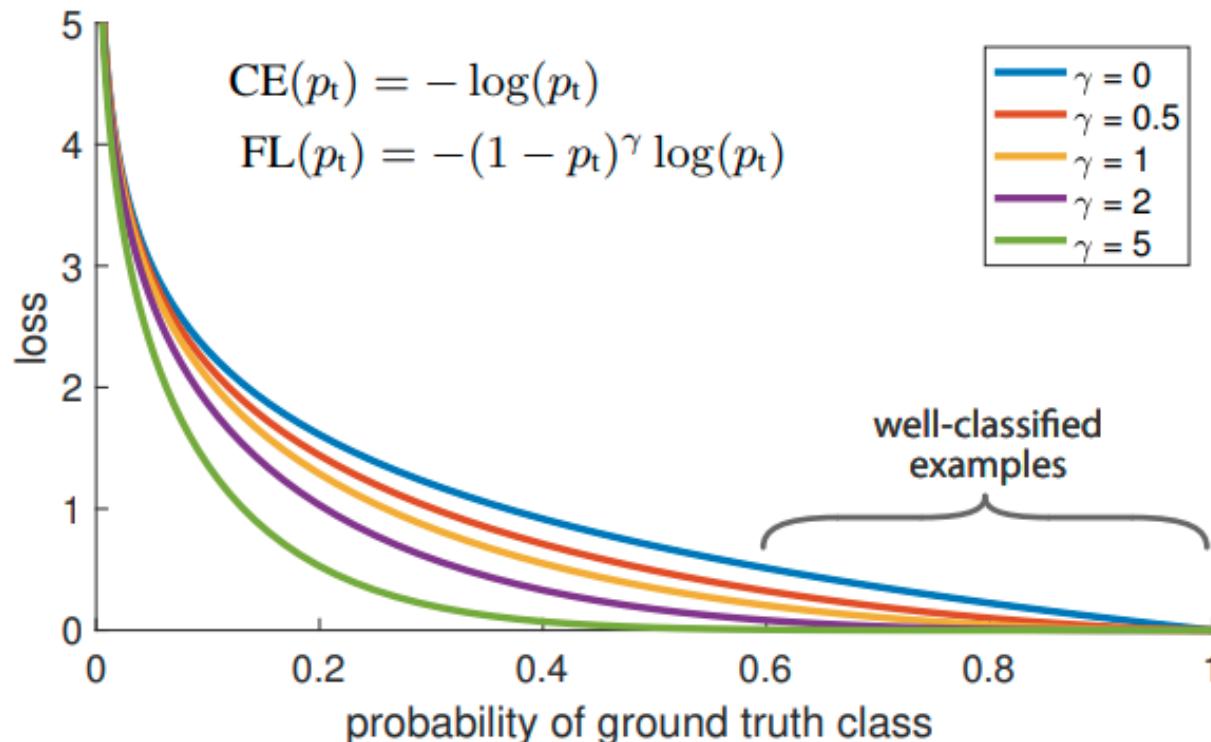
$$\text{BCE}(p, y) = \text{BCE}(p_t) = -\log(p_t)$$

- Khi model predict **xác suất càng gần với label**, p_t sẽ **tiến về 1** thể hiện model đã **học tốt** cho class này và **modulating factor tiến về 0**, đóng góp vào loss giảm (easy samples)

- Khi model predict **xác suất càng xa với label** p_t sẽ **tiến về 0** thể hiện model đã **học không tốt** cho class này và **modulating factor tiến về 1**, đóng góp vào loss tăng (hard samples)

Focal Loss

❖ Focal Loss



– $\gamma = 0$ chính là cross entropy loss

Focal Loss

❖ α -balanced Variant of The Focal Loss

$$\text{Focal Loss } (p_t) = -(1 - p_t)^\gamma \log(p_t)$$

γ theo paper test [0, 5]

weighting
factor

$$\text{Focal Loss } (p_t) = -\alpha_t(1 - p_t)^\gamma \log(p_t)$$

Thực nghiệm khi thêm α_t performance
có cải thiện

Khi sử dụng sigmoid activation để tính
 p_t thì kết quả stable hơn

γ giúp loss tập trung vào hard samples

α_t trọng số giúp cân bằng loss theo số
lượng samples

Focal Loss

❖ α -balanced Variant of The Focal Loss

| α | AP | AP ₅₀ | AP ₇₅ |
|----------|------|------------------|------------------|
| .10 | 0.0 | 0.0 | 0.0 |
| .25 | 10.8 | 16.0 | 11.7 |
| .50 | 30.2 | 46.7 | 32.8 |
| .75 | 31.1 | 49.4 | 33.0 |
| .90 | 30.8 | 49.7 | 32.3 |
| .99 | 28.7 | 47.4 | 29.9 |
| .999 | 25.1 | 41.7 | 26.1 |

(a) Varying α for CE loss ($\gamma = 0$)

| γ | α | AP | AP ₅₀ | AP ₇₅ |
|----------|----------|-------------|------------------|------------------|
| 0 | .75 | 31.1 | 49.4 | 33.0 |
| 0.1 | .75 | 31.4 | 49.9 | 33.1 |
| 0.2 | .75 | 31.9 | 50.7 | 33.4 |
| 0.5 | .50 | 32.9 | 51.7 | 35.2 |
| 1.0 | .25 | 33.7 | 52.0 | 36.2 |
| 2.0 | .25 | 34.0 | 52.5 | 36.5 |
| 5.0 | .25 | 32.2 | 49.6 | 34.8 |

(b) Varying γ for FL (w. optimal α)

Kết quả thực nghiệm so sánh giữa Cross Entropy và Focal Loss
trên cùng một network cho task Object Detection

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- Introduction
- Focal Loss
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- Data Augmentation
- Experiments

Metrics

Confusion Matrix

| | | Actual Value | |
|-----------------|----------|------------------------|------------------------|
| | | Positive | Negative |
| Predicted Value | Positive | TP (True Positive) | FP (False Positive) |
| | Negative | FN (False Negative) | TN (True Negative) |

- True Positive (TP) : Observation is positive, and is predicted to be positive.
- False Negative (FN) : Observation is positive, but is predicted negative.
- True Negative (TN) : Observation is negative, and is predicted to be negative
- False Positive (FP) : Observation is negative, but is predicted positive.

Result

Prediction

True Positive (TP): A correct detection.

False Positive (FP): A wrong detection.

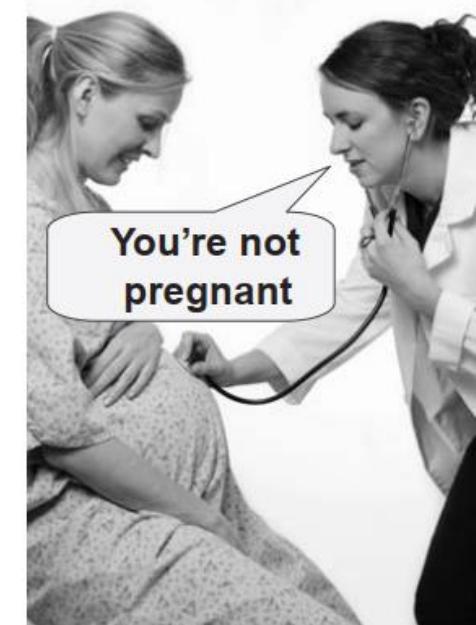
False Negative (FN): A ground truth not detected

True Negative (TN): Does not apply.

Type I error
(false positive)



Type II error
(false negative)



The Essential Guide to Effect Sizes

<https://www.kdnuggets.com/2020/04/performanc-evaluation-metrics-classification.html>

Metrics

❖ Precision

- ❖ Ability of a model to identify only the relevant objects

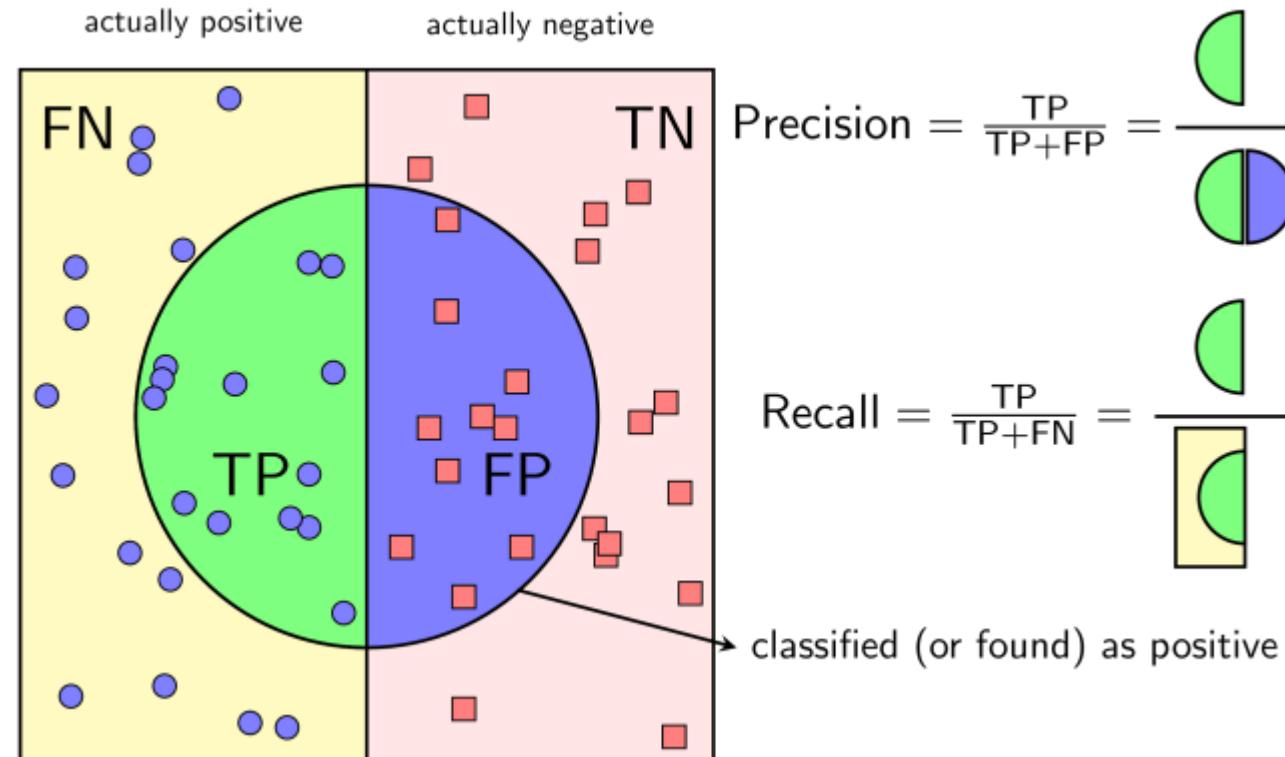
$$Precision = \frac{TP}{TP + FP} = \frac{TP}{\text{all detections}}$$

❖ Recall

- ❖ Ability of a model to find all the relevant cases (all ground truth bounding boxes)

$$Recall = \frac{TP}{TP + FN} = \frac{TP}{\text{all ground truths}}$$

| Result | Prediction |
|---|--|
| True Positive (TP): A correct detection. | |
| | False Positive (FP): A wrong detection. |
| False Negative (FN): A ground truth not detected | |
| | True Negative (TN): Does not apply. |



Metrics

❖ Precision

- ❖ Ability of a model to identify only the relevant objects

$$Precision = \frac{TP}{TP + FP} = \frac{TP}{all\ detections}$$

❖ Recall

- ❖ Ability of a model to find all the relevant cases (all ground truth bounding boxes)

$$Recall = \frac{TP}{TP + FN} = \frac{TP}{all\ ground\ truths}$$

| n=165 | Predicted: NO | Predicted: YES | |
|----------------|------------------|-------------------|-----|
| Actual: NO | TN = 50 | FP = 10 | 60 |
| Actual: YES | FN = 5 | TP = 100 | 105 |
| 55 | 110 | | |

Recall: When it's actually yes, how often does it predict yes?

$$TP/\text{actual yes} = 100/105 = 0.95$$

Precision: When it predicts yes, how often is it correct?

$$TP/\text{predicted yes} = 100/110 = 0.91$$

Classification on Imbalanced Data

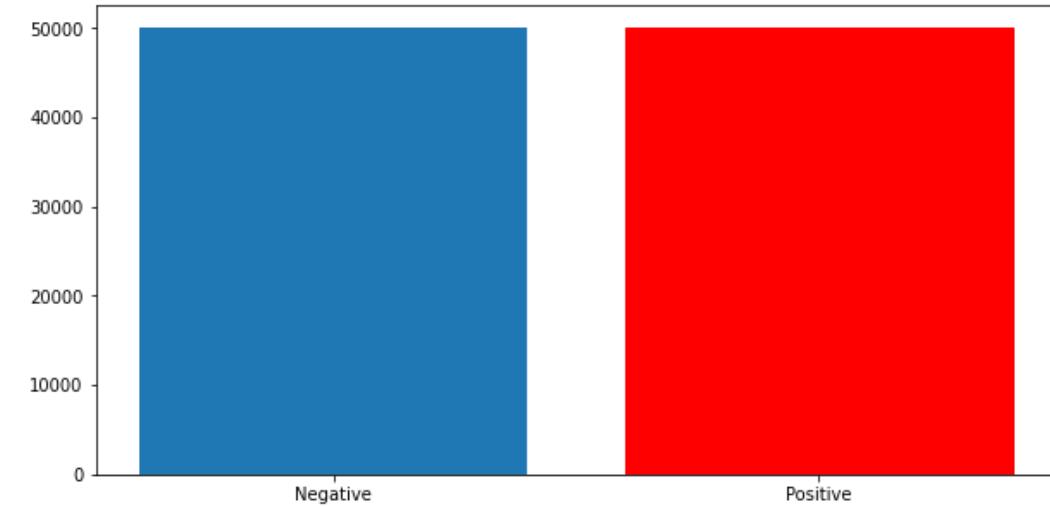
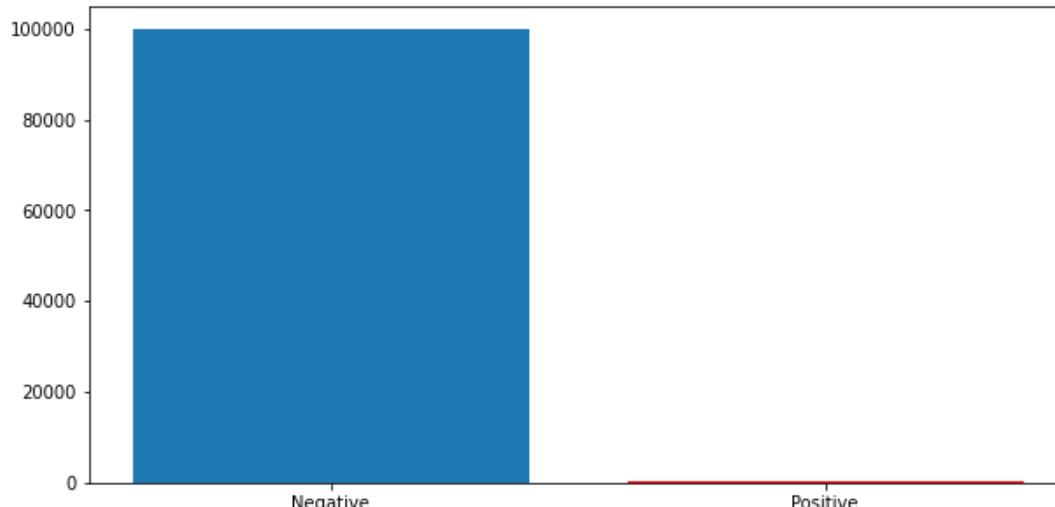
❖ Imbalanced Data vs Balanced Data

Imbalanced Data

| | Labels | Model Predict Negative | Model Predict Positive |
|----------|--------|------------------------|------------------------|
| Negative | 100000 | 99900 | 100 |
| Positive | 200 | 100 | 100 |

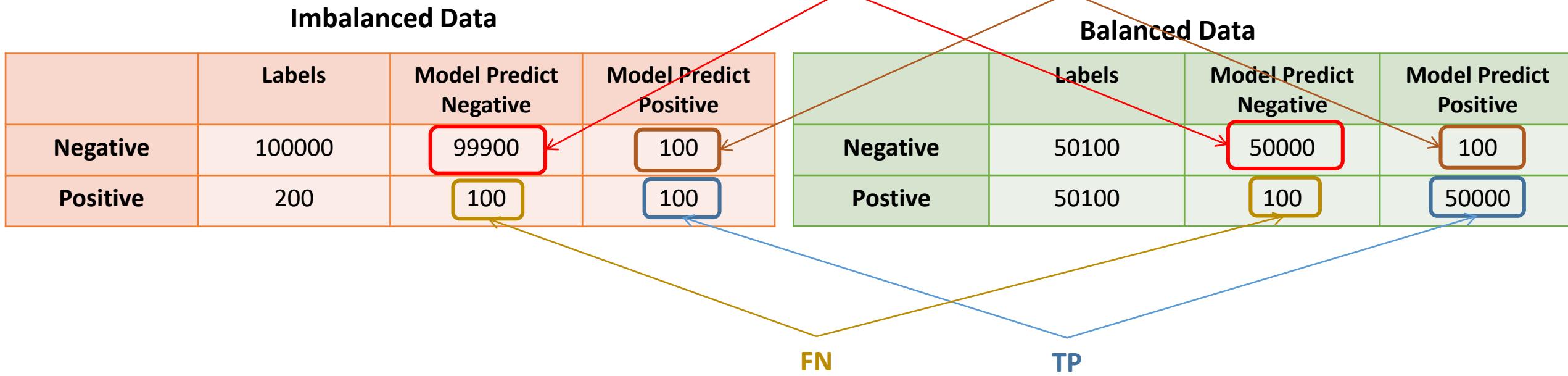
Balanced Data

| | Labels | Model Predict Negative | Model Predict Positive |
|----------|--------|------------------------|------------------------|
| Negative | 50100 | 50000 | 100 |
| Positive | 50100 | 100 | 50000 |



Classification on Imbalanced Data

❖ Imbalanced Data vs Balanced Data



True positive (TP): sample có **label** là **positive** và **model** phân loại là **positive**

True negative (TN): sample có **label** là **negative** và **model** phân loại là **negative**

False positive (FP): sample có **label** là **negative** và **model** phân loại là **positive**

False negative (FN): sample có **label** là **positive** và **model** phân loại là **negative**

Classification on Imbalanced Data

❖ Precision

- ❖ Ability of a model to identify only the relevant objects

$$Precision = \frac{TP}{TP + FP} = \frac{TP}{all\ detections}$$

❖ Recall

- ❖ Ability of a model to find all the relevant cases (all ground truth bounding boxes)

$$Recall = \frac{TP}{TP + FN} = \frac{TP}{all\ ground\ truths}$$

❖ Metric for Imbalanced Class

$$\text{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN}$$

$$\text{Recall} = \frac{TP}{TP + FN}$$

$$\text{Precision} = \frac{TP}{TP + FP}$$

$$F1 = \frac{2 * \text{Precision} * \text{Recall}}{\text{Precision} + \text{Recall}}$$

Precision: tỉ lệ model predict các positive sample đúng là positive

Recall: tỉ lệ model có thể nhận dạng được các positive sample

F1-score: Trung bình điều hòa giữa accuracy và precision

Outline

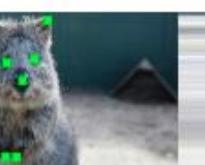
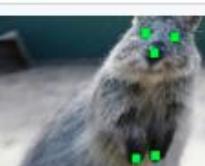
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Augmentation Library

❖ Imgaug Library

Có thể làm việc được với nhiều loại image data và groundtruth:

- Keypoints/Landmarks
- Bounding Boxes, Polygons
- Line Strings
- Heatmaps, Segmentation Maps

| | Image | Heatmaps | Seg. Maps | Keypoints | Bounding Boxes, Polygons |
|-----------------------------------|---|---|---|---|---|
| <i>Original Input</i> |  |  |  |  |  |
| Gauss. Noise + Contrast + Sharpen |  |  |  |  |  |
| Affine |  |  |  |  |  |
| Crop + Pad |  |  |  |  |  |
| Flplr + Perspective |  |  |  |  |  |

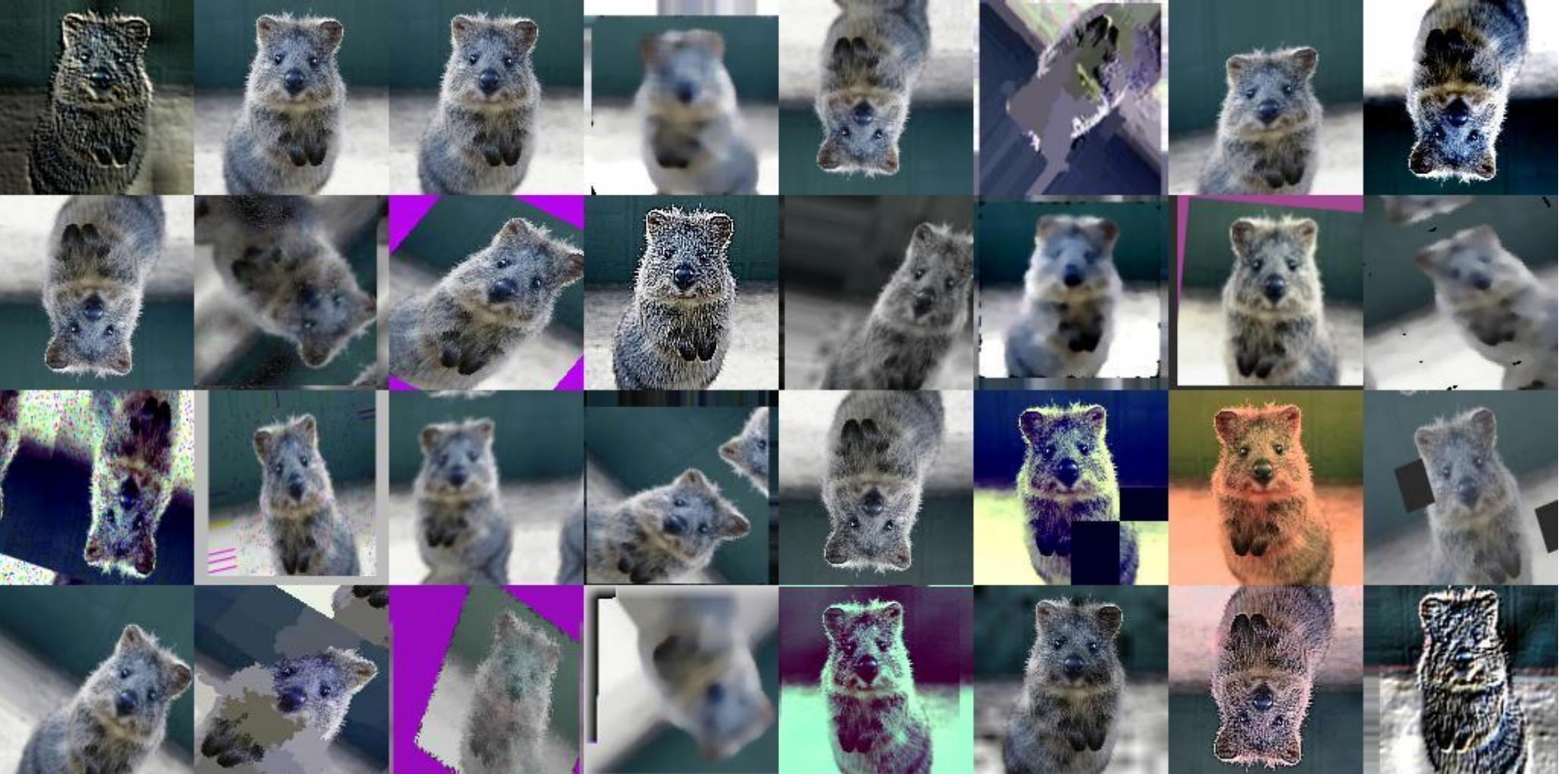
<https://github.com/aleju/imgaug#documentation>

Augmentation Library

❖ Image Augmentation



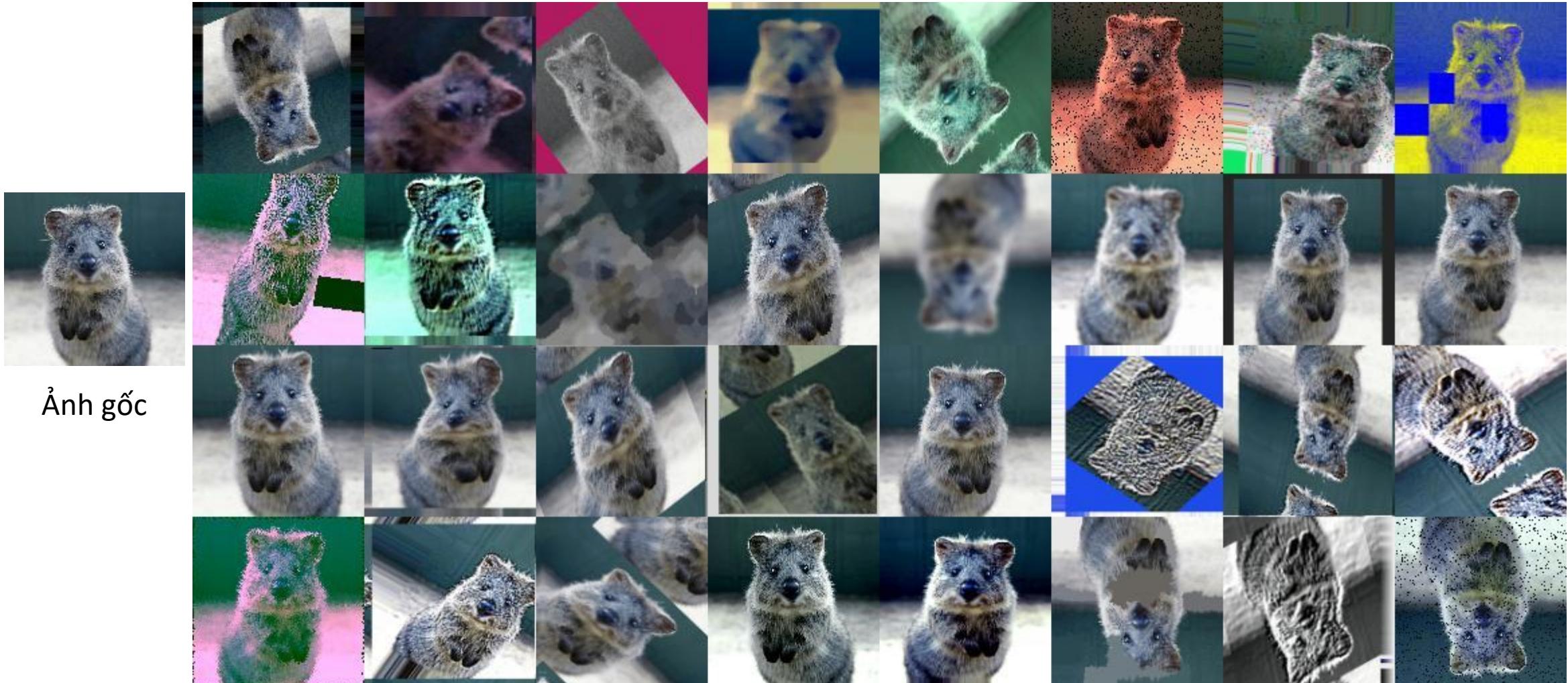
Ảnh gốc



Sau Augmentation

Augmentation Library

❖ Image Augmentation



Ảnh gốc

Sau Augmentation

Augmentation Library

❖ Image Augmentation

- Có chức năng augmentation 1 batch ảnh (batch, height, width, channel)
- Cho phép sử dụng một chuỗi các kỹ thuật augmentation và khai báo như Sequential mode của Tensorflow

```
import imgaug.augmenters as iaa
```

import thư viện

```
# Pipeline:  
# (1) Crop images from each side by 1-16px, do not resize the results  
#     images back to the input size. Keep them at the cropped size.  
# (2) Horizontally flip 50% of the images.  
# (3) Blur images using a gaussian kernel with sigma between 0.0 and 3.0.  
seq = iaa.Sequential([  
    iaa.Crop(px=(1, 16), keep_size=False),  
    iaa.FlipLR(0.5),  
    iaa.GaussianBlur(sigma=(0, 3.0))  
])
```

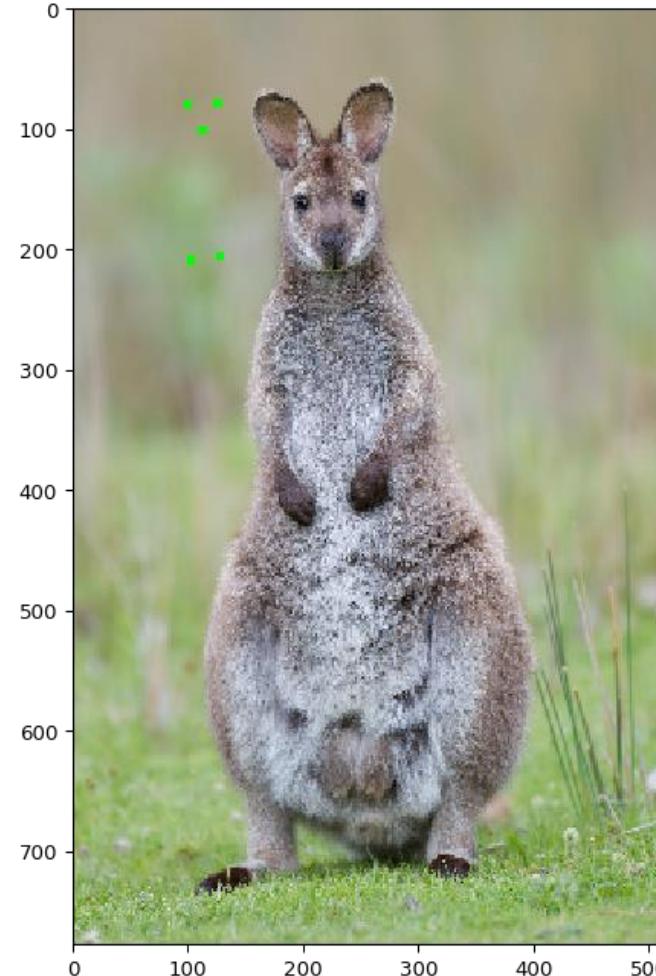
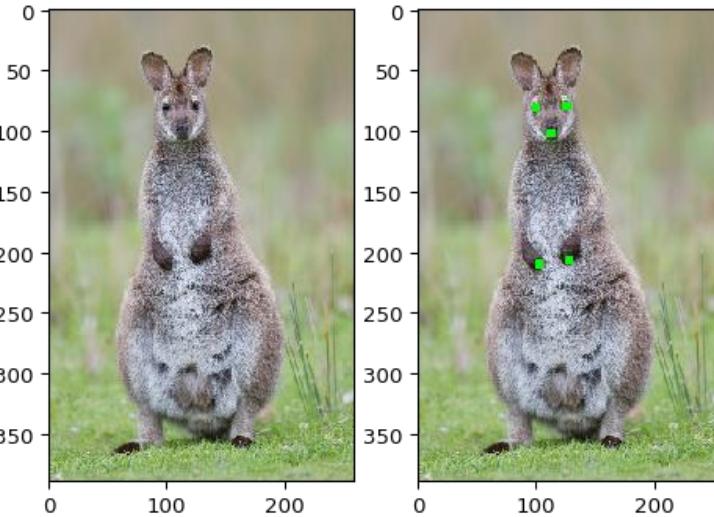
Khai báo các chuỗi kỹ thuật augmentations sẽ được sử dụng

```
images_aug = seq(images=images) # done by the library
```

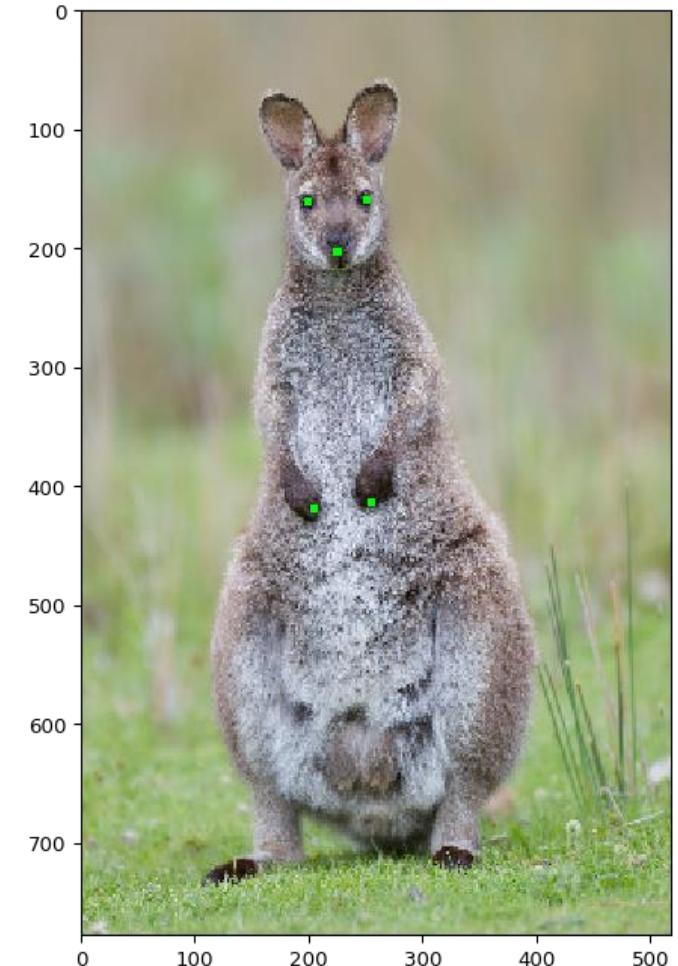
Áp dụng chuỗi các kỹ thuật augmentation cho 1 batch ảnh

Augmentation Library

❖ Augment Keypoints/Landmarks



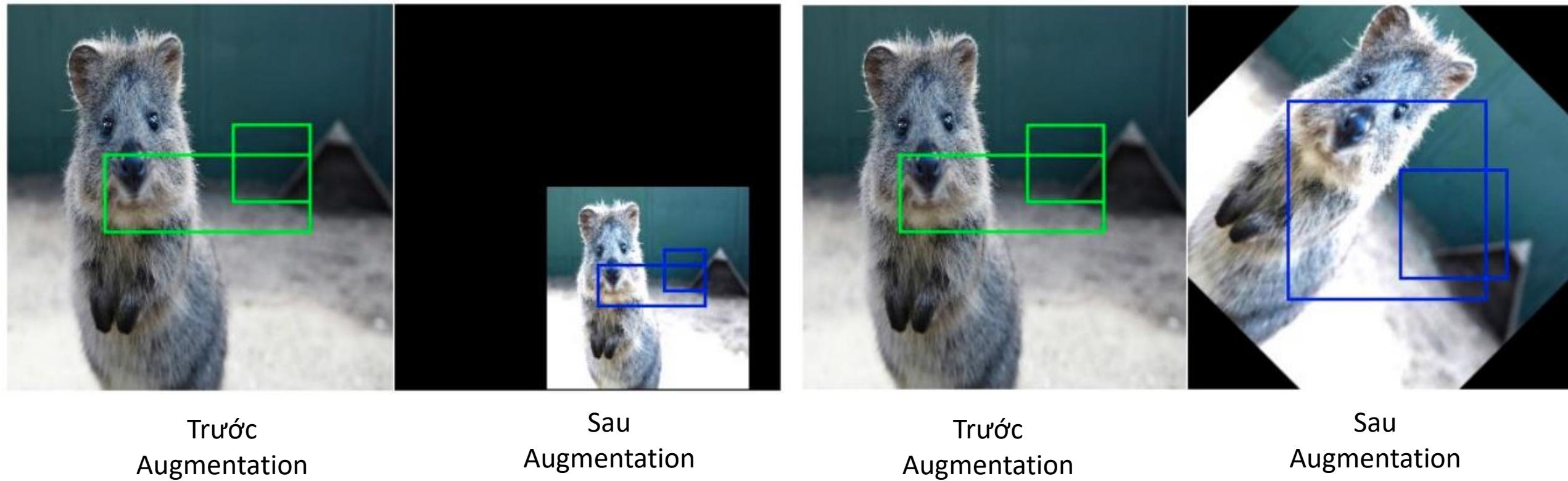
Resize ảnh lõi



Resize ảnh đúng

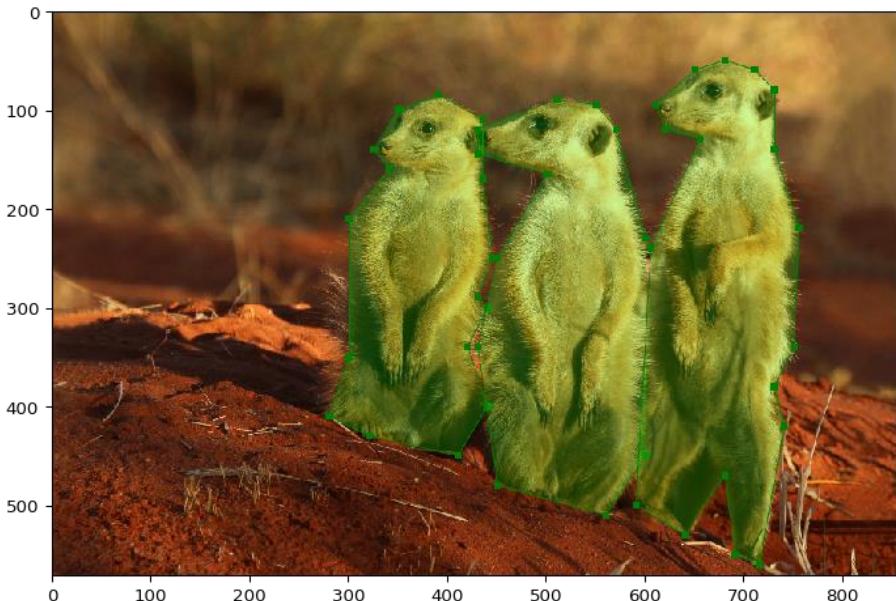
Augmentation Library

❖ Bounding Boxes

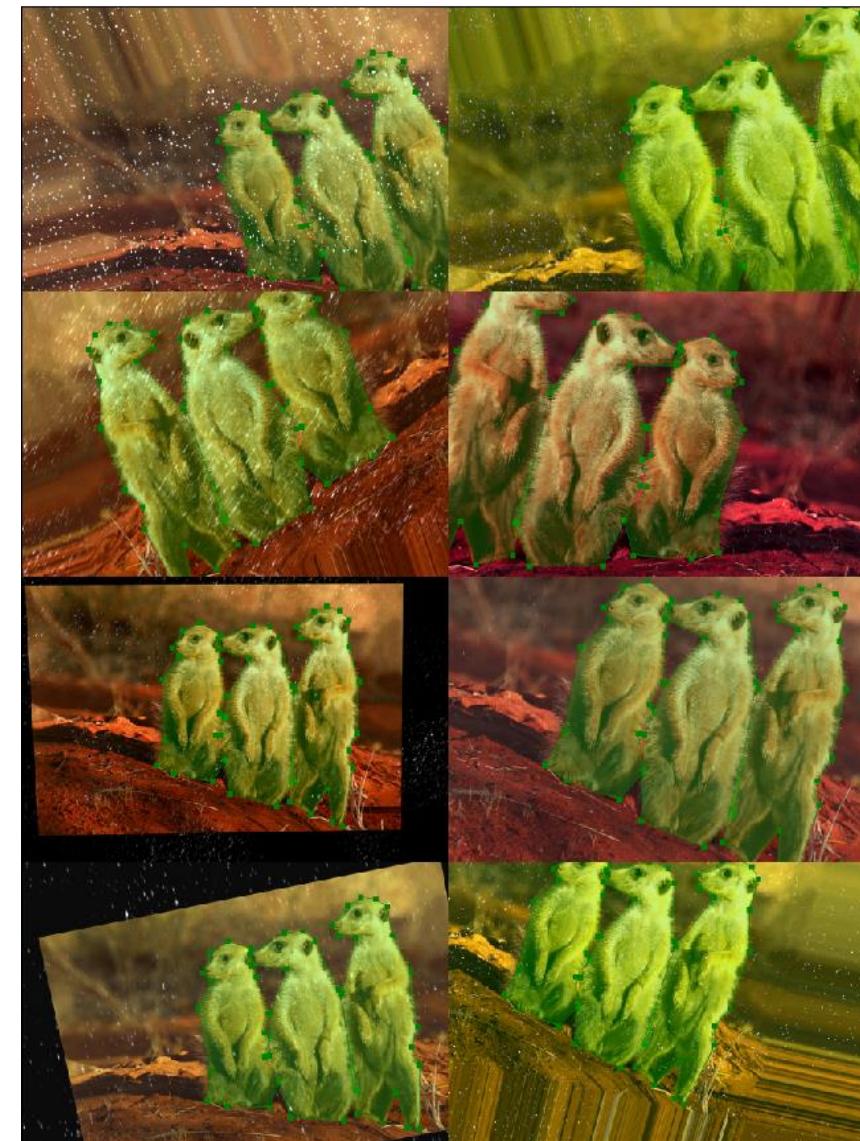


Augmentation Library

❖ Polygon



Trước
Augmentation



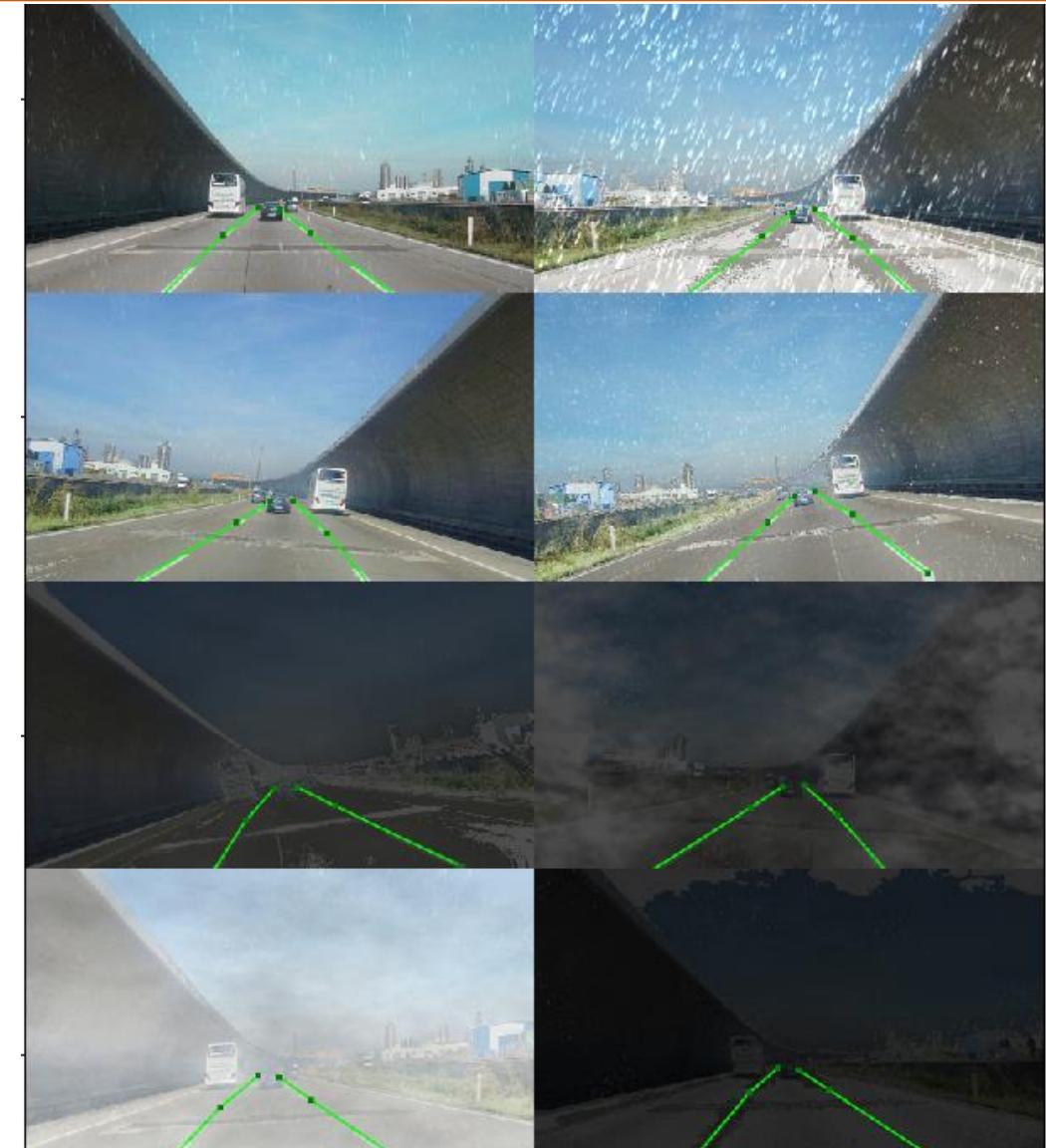
Sau Augmentation

Augmentation Library

❖ Line Strings



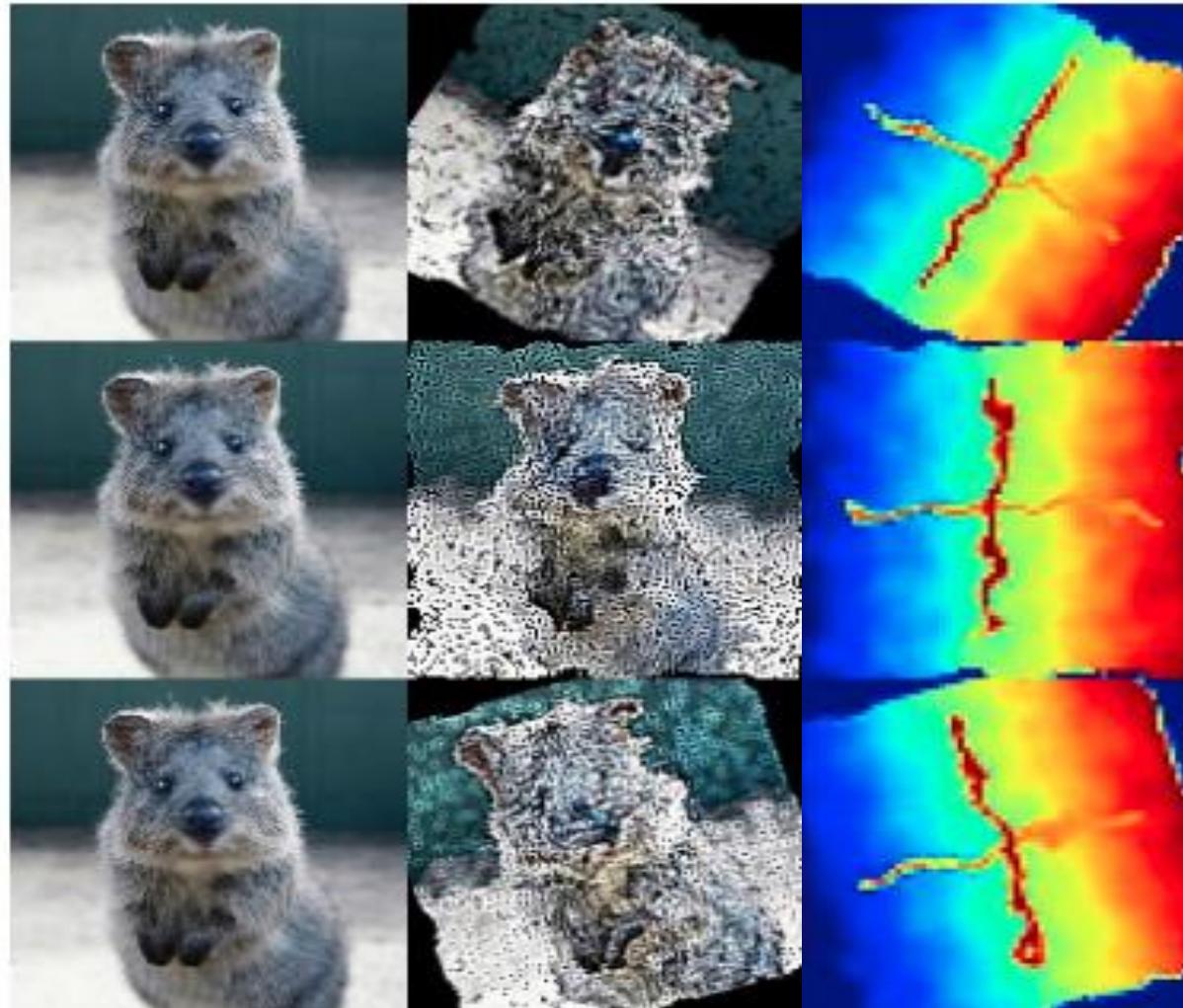
Trước
Augmentation



Sau Augmentation

Augmentation Library

❖ Heat Map



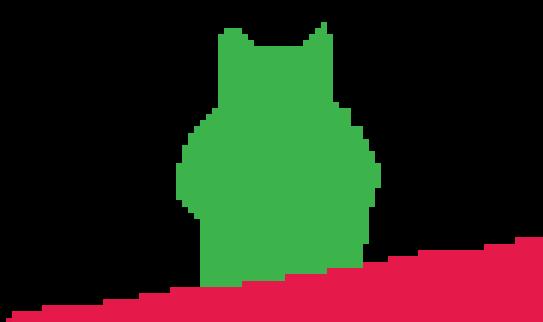
ảnh gốc

ảnh
augmentation

heat map
augmentation

Augmentation Library

❖ Segmentation



Trước Augmentation



Sau Augmentation

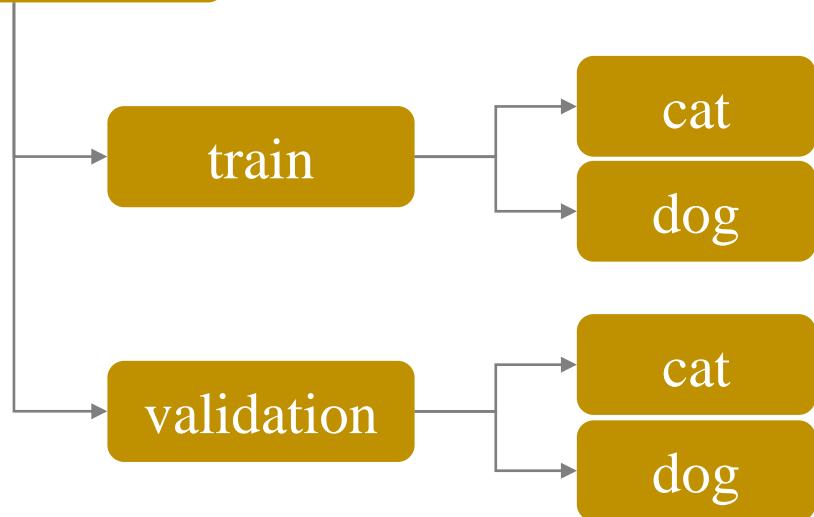
Outline

- Introduction
- Focal Loss
- Metrics
- Data Augmentation
- Experiments

Experiments

❖ Cat-Dog dataset

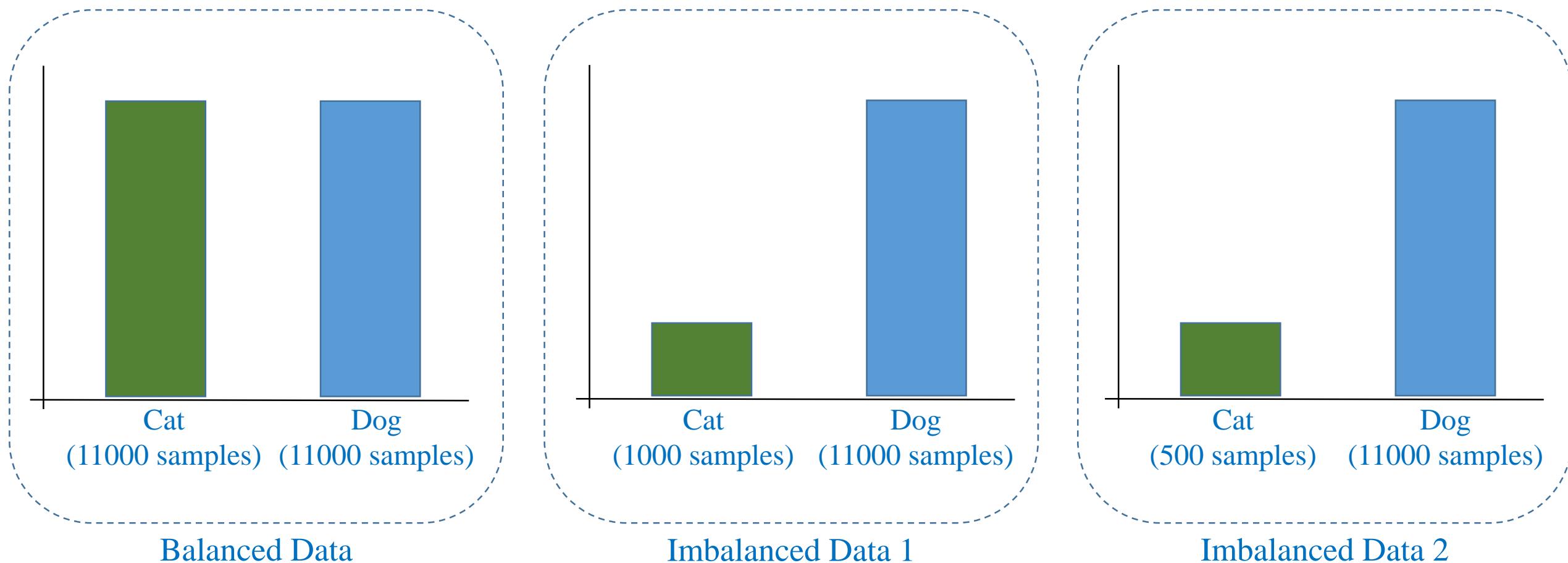
cats_and_dogs



Experiments

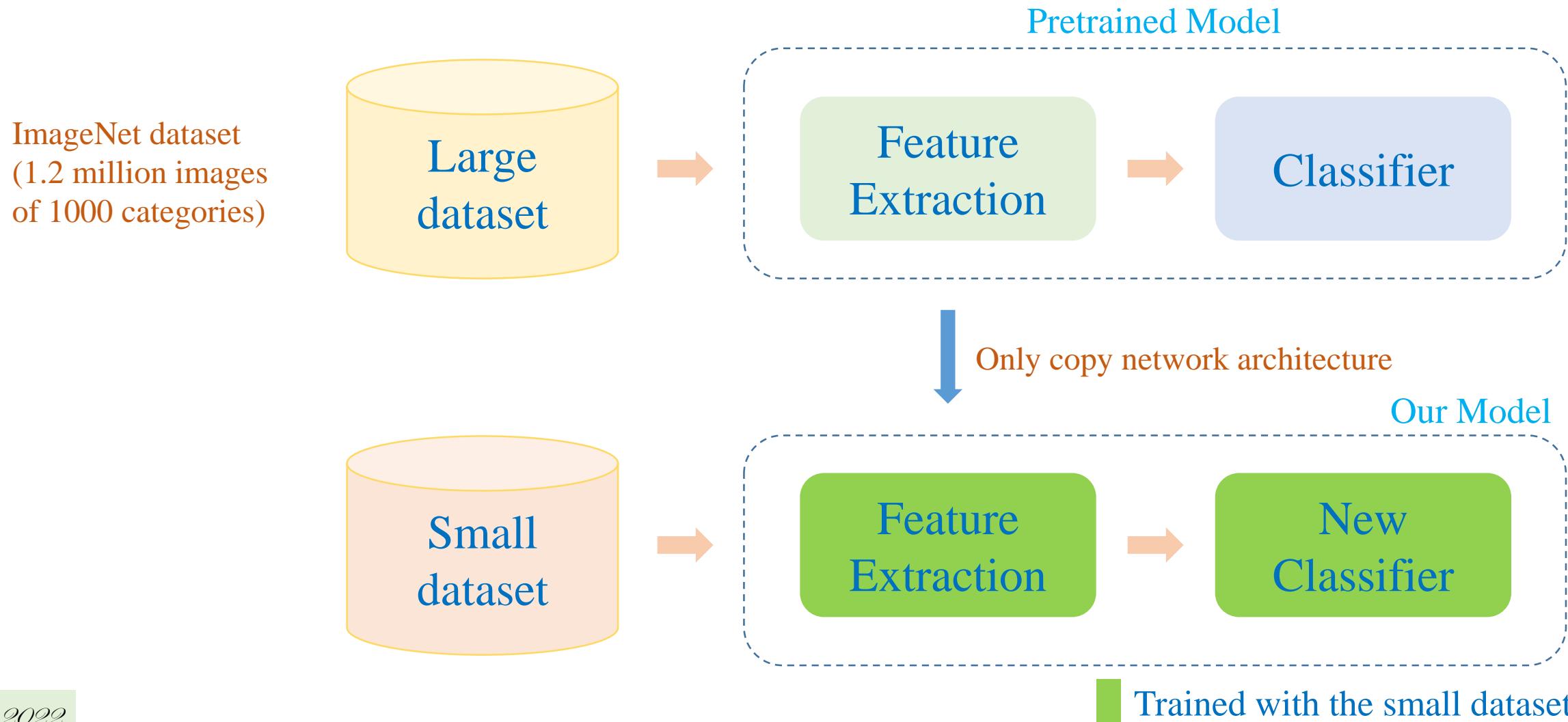
❖ Cat-Dog dataset

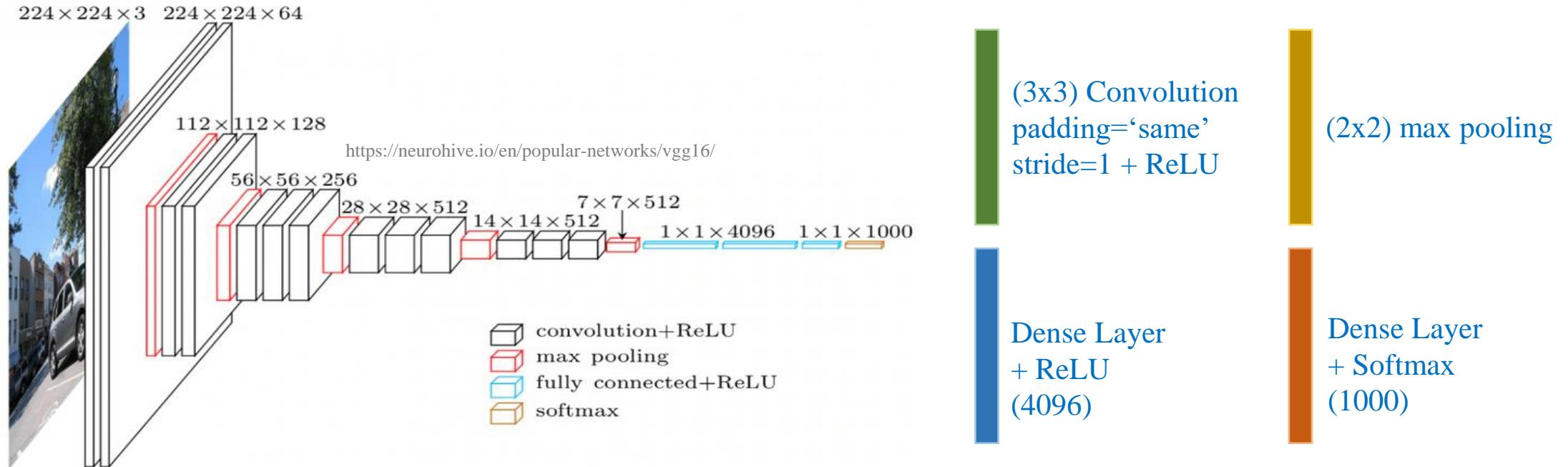
Validation data (3000 samples)



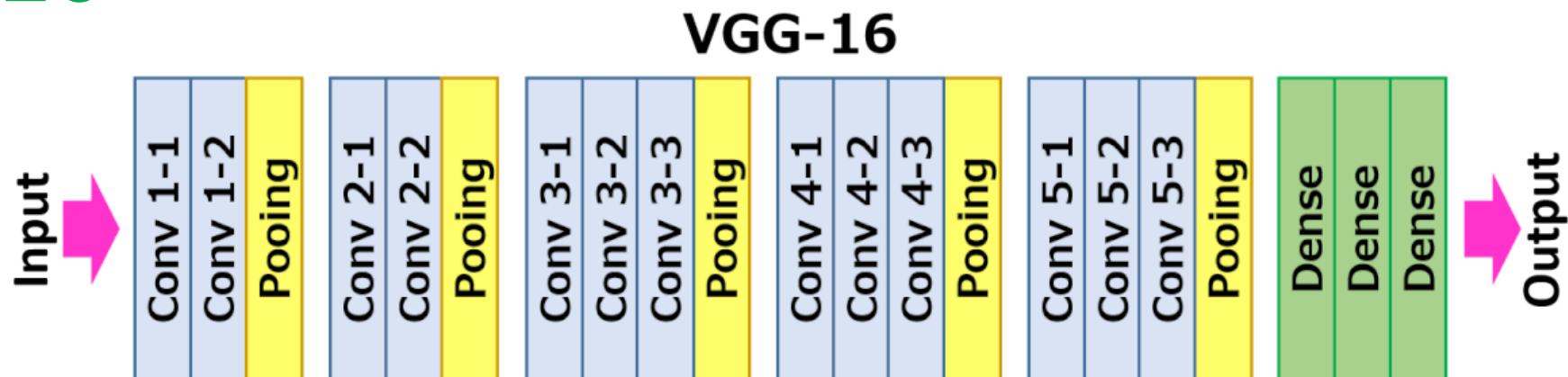
Experiments

❖ Train from scratch





VGG16



Experiments

❖ Cat-Dog dataset

❖ Train from scratch

```
1 PATH = 'cats_and_dogs_small/'  
2  
3 train_dir = os.path.join(PATH, 'train')  
validation_dir = os.path.join(PATH, 'validation')  
4  
5 BATCH_SIZE = 256  
6 IMG_SIZE = (160, 160)  
7 BUFFER_SIZE = BATCH_SIZE*5  
8  
9 train_dataset = image_dataset_from_directory(train_dir,  
10                                         shuffle=True,  
11                                         batch_size=BATCH_SIZE,  
12                                         image_size=IMG_SIZE)  
13
```

Found 2000 files belonging to 2 classes.

```
1 validation_dataset = image_dataset_from_directory(validation_dir,  
2                                         shuffle=True,  
3                                         batch_size=BATCH_SIZE,  
4                                         image_size=IMG_SIZE)
```

Found 1000 files belonging to 2 classes.

Experiments

❖ Cat-Dog dataset

❖ Train from scratch

Model: "vgg16"

| Layer (type) | Output Shape | Param # |
|----------------------------|-------------------------|---------|
| <hr/> | | |
| input_1 (InputLayer) | [(None, 160, 160, 3)] | 0 |
| block1_conv1 (Conv2D) | (None, 160, 160, 64) | 1792 |
| block1_conv2 (Conv2D) | (None, 160, 160, 64) | 36928 |
| block1_pool (MaxPooling2D) | (None, 80, 80, 64) | 0 |
| block2_conv1 (Conv2D) | (None, 80, 80, 128) | 73856 |
| block2_conv2 (Conv2D) | (None, 80, 80, 128) | 147584 |
| block2_pool (MaxPooling2D) | (None, 40, 40, 128) | 0 |
| block3_conv1 (Conv2D) | (None, 40, 40, 256) | 295168 |
| block3_conv2 (Conv2D) | (None, 40, 40, 256) | 590080 |
| block3_conv3 (Conv2D) | (None, 40, 40, 256) | 590080 |
| block3_pool (MaxPooling2D) | (None, 20, 20, 256) | 0 |

```
1 # top=False
2 model = tf.keras.applications.VGG16(input_shape=(160,160,3),
3                                     include_top=False,
4                                     weights=None)
5 model.summary()
```

| | | |
|------------------------------|---------------------|---------|
| block4_conv1 (Conv2D) | (None, 20, 20, 512) | 1180160 |
| block4_conv2 (Conv2D) | (None, 20, 20, 512) | 2359808 |
| block4_conv3 (Conv2D) | (None, 20, 20, 512) | 2359808 |
| block4_pool (MaxPooling2D) | (None, 10, 10, 512) | 0 |
| block5_conv1 (Conv2D) | (None, 10, 10, 512) | 2359808 |
| block5_conv2 (Conv2D) | (None, 10, 10, 512) | 2359808 |
| block5_conv3 (Conv2D) | (None, 10, 10, 512) | 2359808 |
| block5_pool (MaxPooling2D) | (None, 5, 5, 512) | 0 |
| <hr/> | | |
| Total params: 14,714,688 | | |
| Trainable params: 14,714,688 | | |
| Non-trainable params: 0 | | |

Experiments

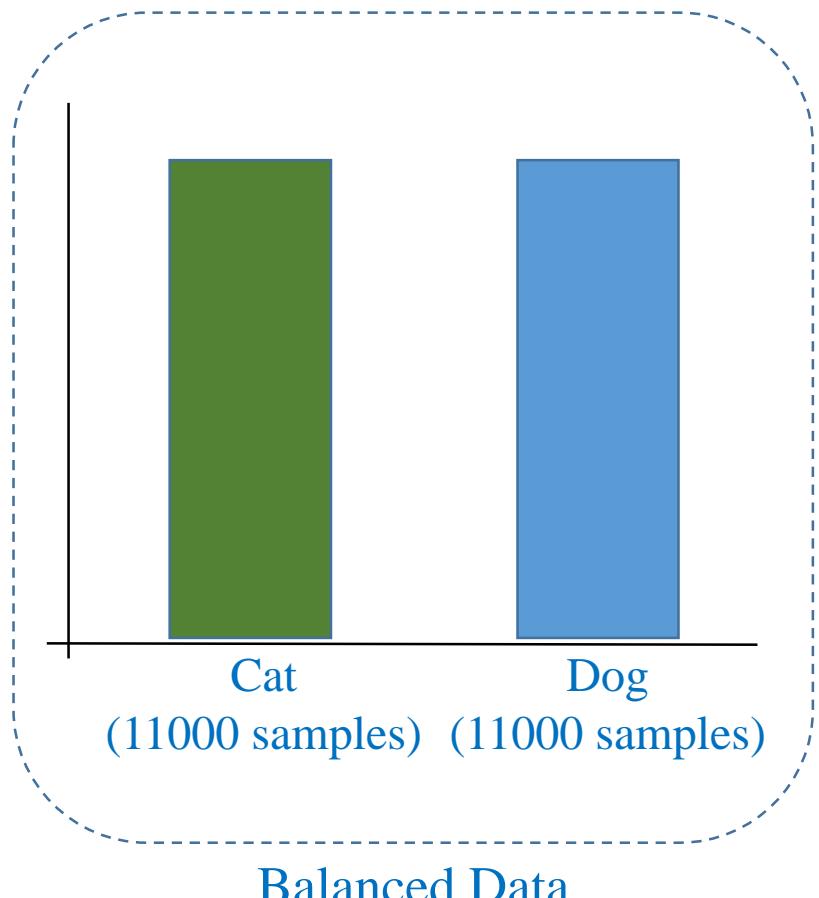
❖ Cat-Dog dataset

❖ Train from scratch

```
1 # process data
2 data_augmentation = tf.keras.Sequential([
3     tf.keras.layers.experimental.preprocessing.RandomFlip('horizontal'),
4     tf.keras.layers.experimental.preprocessing.RandomRotation(0.2),
5     tf.keras.layers.experimental.preprocessing.Rescaling(1./127.5, offset=-1)
6 ])
7
8 # flattening
9 flatten = tf.keras.layers.Flatten()
10
11 # final layer
12 prediction_layer = tf.keras.layers.Dense(1)
13
14 # construct a new network
15 inputs = tf.keras.Input(shape=(160, 160, 3))
16 x = data_augmentation(inputs)
17 x = base_model(x)
18 x = flatten(x)
19 outputs = prediction_layer(x)
20 model = tf.keras.Model(inputs, outputs)
```

Experiments

❖ Cat-Dog dataset



Balanced Loss

$$L_b = L_c + L_d$$

Validation data (3000 samples)

Correct prediction

$$\begin{aligned} \#_{cat} &= 1445 \\ \#_{dog} &= 1436 \\ F_1 &= 0.96 \end{aligned}$$

Imbalanced Loss 1

$$L_b = L_c + 100 \times L_d$$

Correct prediction

$$\begin{aligned} \#_{cat} &= 1076 \\ \#_{dog} &= 1499 \\ F_1 &= 0.835 \end{aligned}$$

Imbalanced Loss 2

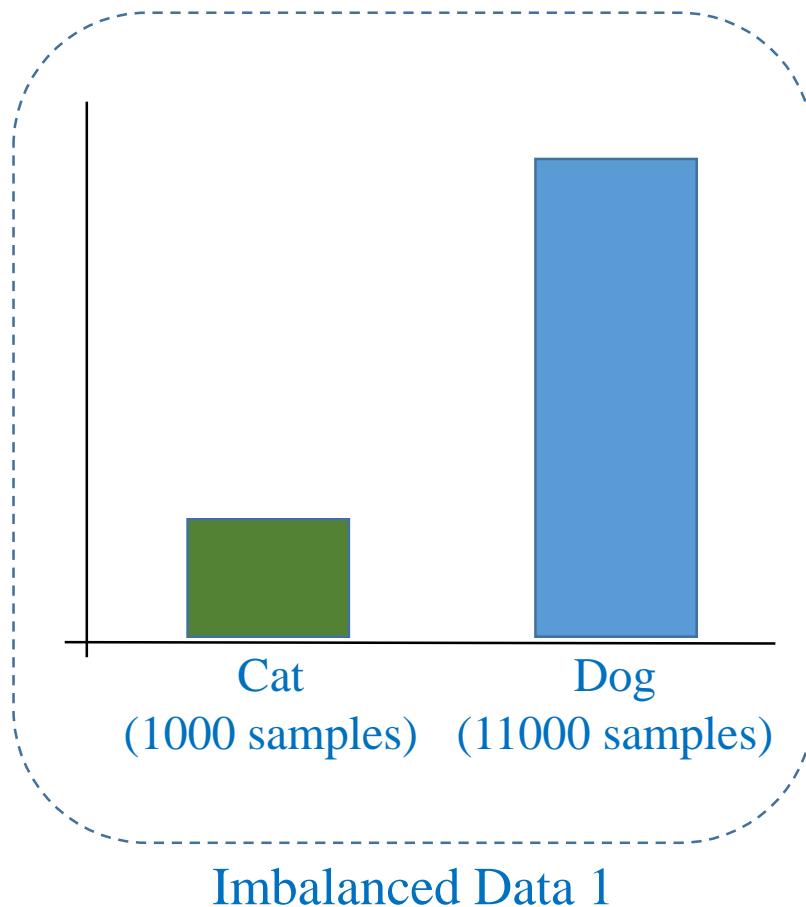
$$L_b = L_c + 1000 \times L_d$$

Correct prediction

$$\begin{aligned} \#_{cat} &= 670 \\ \#_{dog} &= 1498 \\ F_1 &= 0.617 \end{aligned}$$

Experiments

❖ Cat-Dog dataset



Validation data (3000 samples)

Balanced Loss

$$L_b = L_c + L_d$$

Correct prediction

$$\begin{aligned} \#_{cat} &= 1082 \\ \#_{dog} &= 1483 \\ F_1 &= 0.833 \end{aligned}$$

Imbalanced Loss

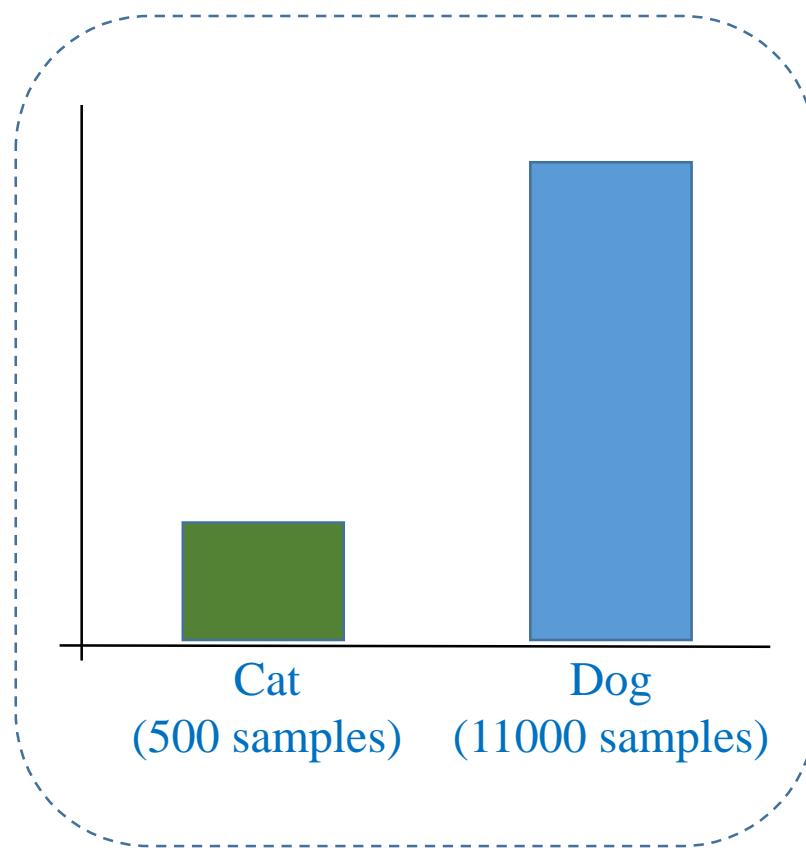
$$L_b = 6 \times L_c + 0.55 \times L_d$$

Correct prediction

$$\begin{aligned} \#_{cat} &= 1163 \\ \#_{dog} &= 1379 \\ F_1 &= 0.835 \end{aligned}$$

Experiments

❖ Cat-Dog dataset



Correct prediction
 $\#_{cat} = 821$
 $\#_{dog} = 1489$

| n=3000 | Predicted: NEGATIVE | Predicted: POSITIVE | |
|------------------|---------------------|---------------------|------|
| Actual: NEGATIVE | TN=1489 | FP=11 | 1500 |
| Actual: POSITIVE | FN=679 | TP=821 | 1500 |
| 2168 | 832 | | |

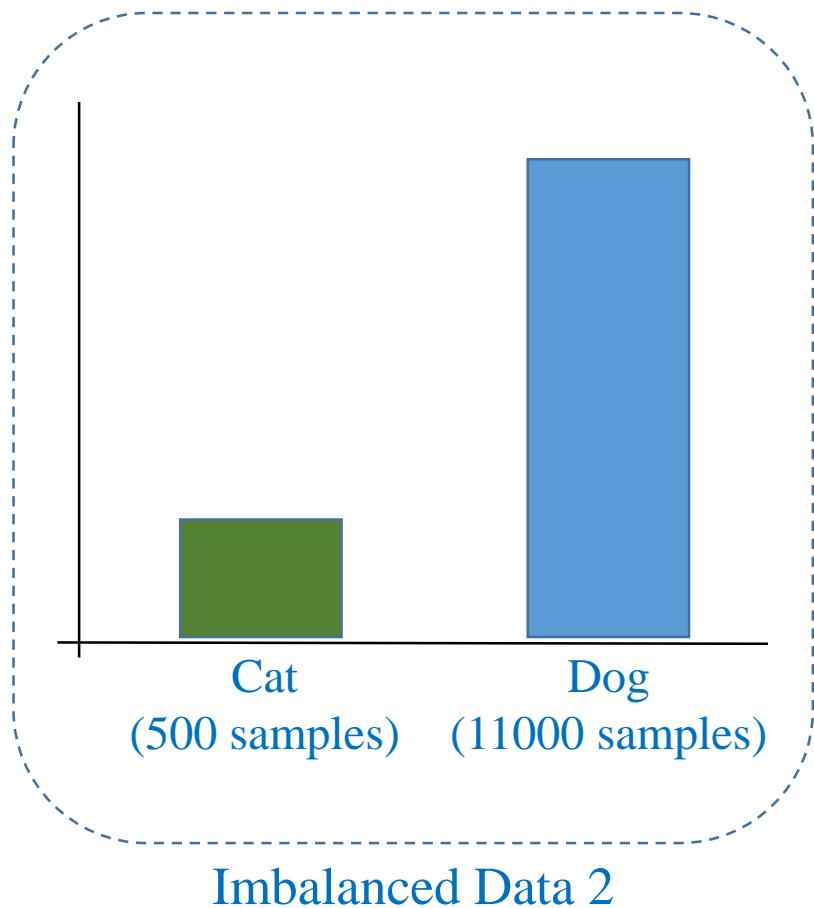
$$\text{Recal} = \frac{\text{TP}}{\text{TP} + \text{FN}} = \frac{821}{821 + 679} \approx 0.547$$

$$\text{Precision} = \frac{\text{TP}}{\text{TP} + \text{FP}} = \frac{821}{821 + 11} \approx 0.987$$

$$\text{F1} = \frac{2 * \text{Recal} * \text{Precision}}{\text{Recal} + \text{Precision}} = \frac{2 * 0.547 * 0.987}{0.547 * 0.987} \approx 0.704$$

Experiments

❖ Cat-Dog dataset



Validation data (3000 samples)

Balanced Loss

$$L_b = L_c + L_d$$

Correct prediction

$$\begin{aligned} \#_{cat} &= 821 \\ \#_{dog} &= 1489 \\ F_1 &= 0.704 \end{aligned}$$

Imbalanced Loss

$$L_b = 11.5 \times L_c + 0.52 \times L_d$$

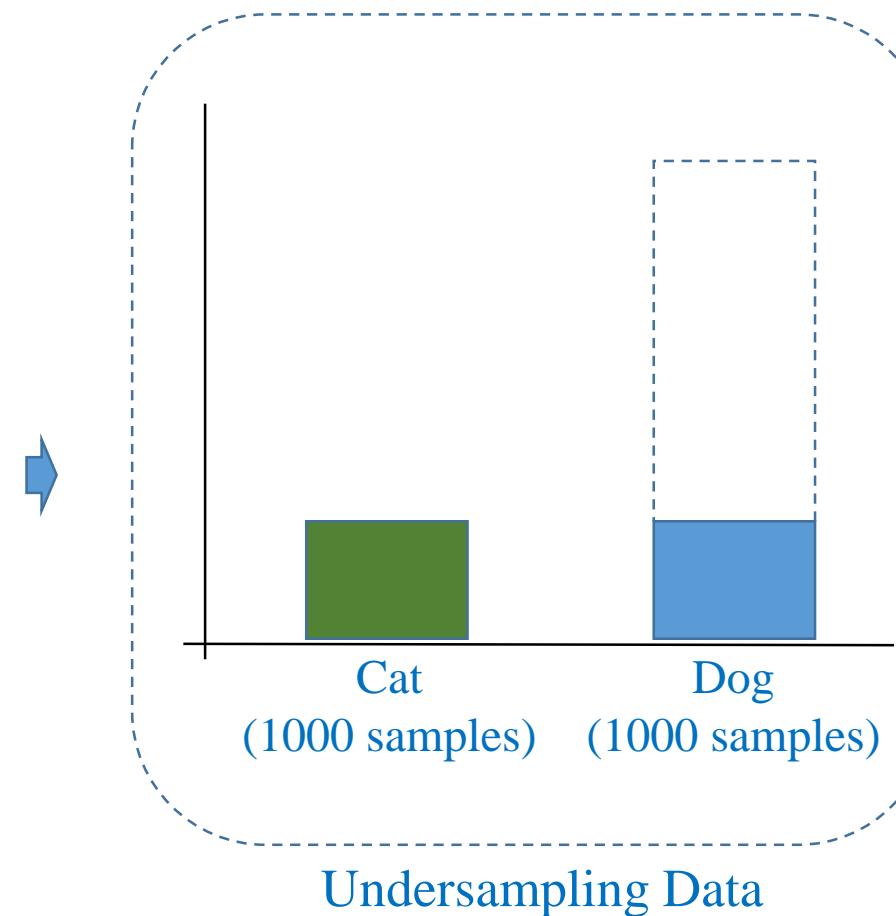
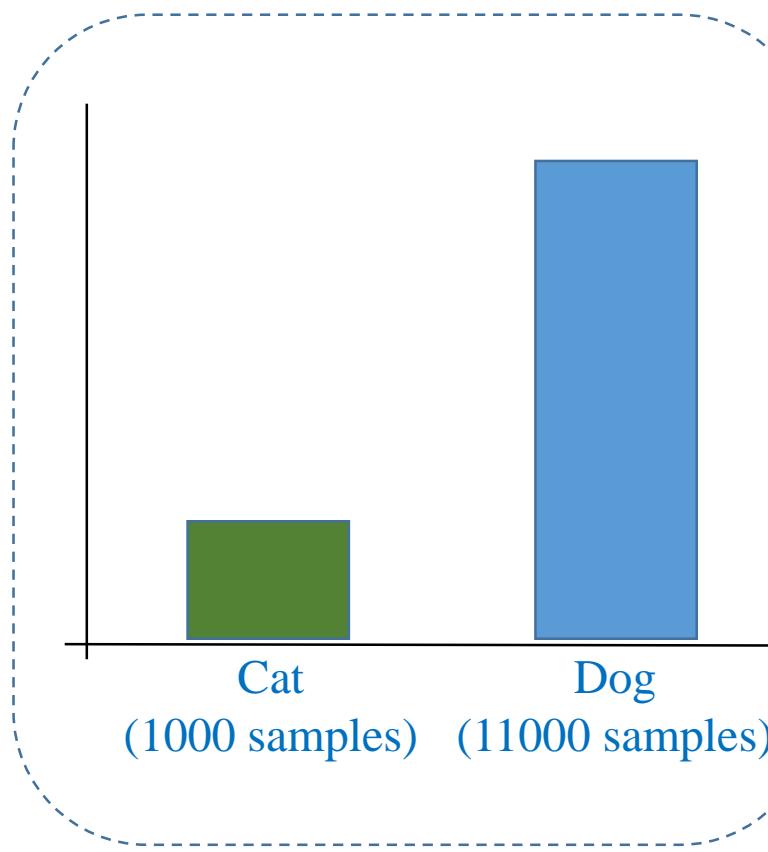
Correct prediction

$$\begin{aligned} \#_{cat} &= 1123 \\ \#_{dog} &= 1309 \\ F_1 &= 0.798 \end{aligned}$$

Experiments

❖ Cat-Dog dataset: Undersampling

Validation data (3000 samples)



Imbalanced Data 1

$\#_{cat} = 1082$
 $\#_{dog} = 1483$
 $F_1 = 0.833$

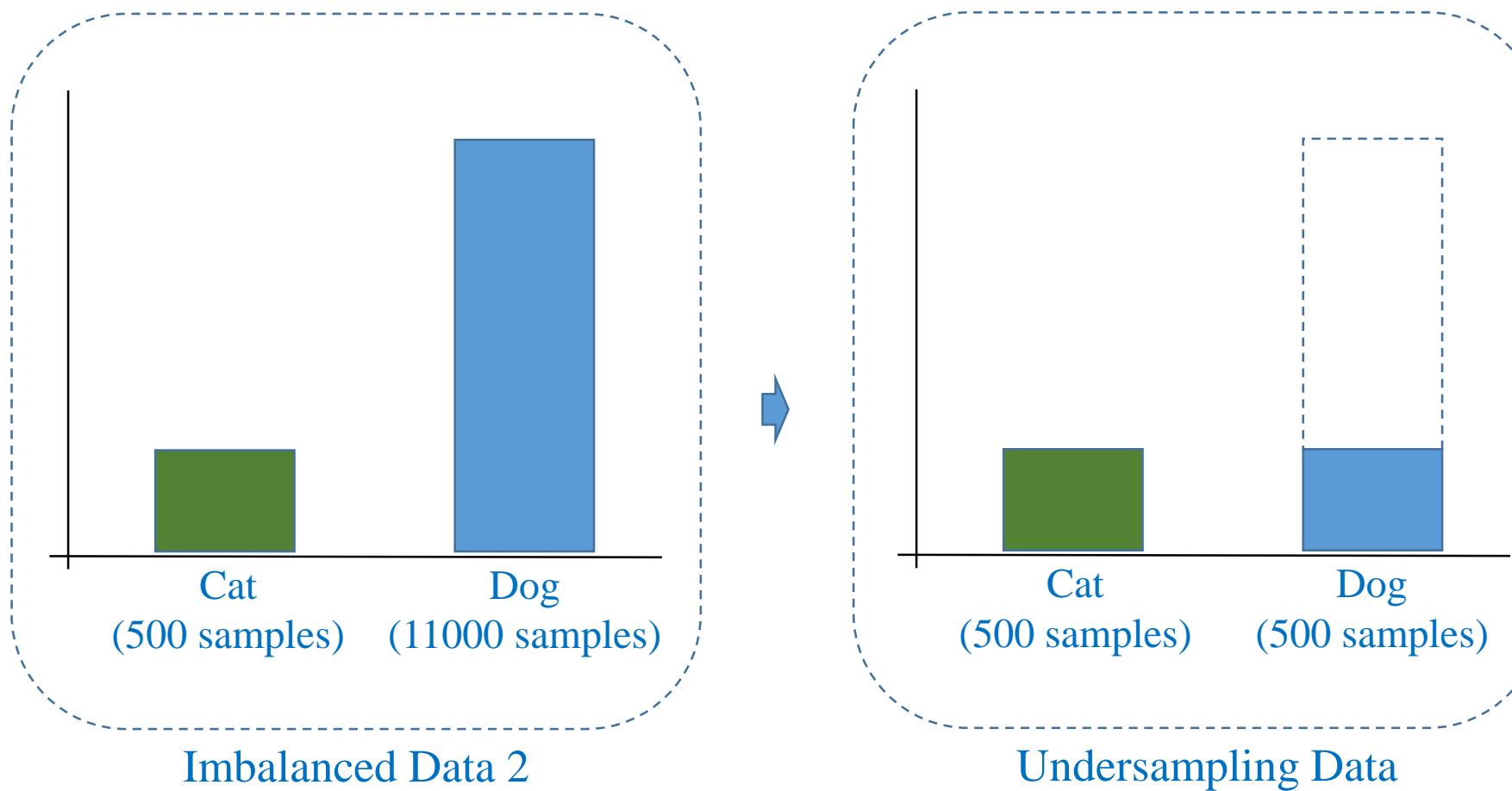
Undersampling Data

$\#_{cat} = 1282$
 $\#_{dog} = 1017$
 $F_1 = 0.785$!

Experiments

❖ Cat-Dog dataset: Undersampling

Validation data (3000 samples)



Imbalanced Data 2

$\#_{cat} = 821$
 $\#_{dog} = 1489$
 $F_1 = 0.704$

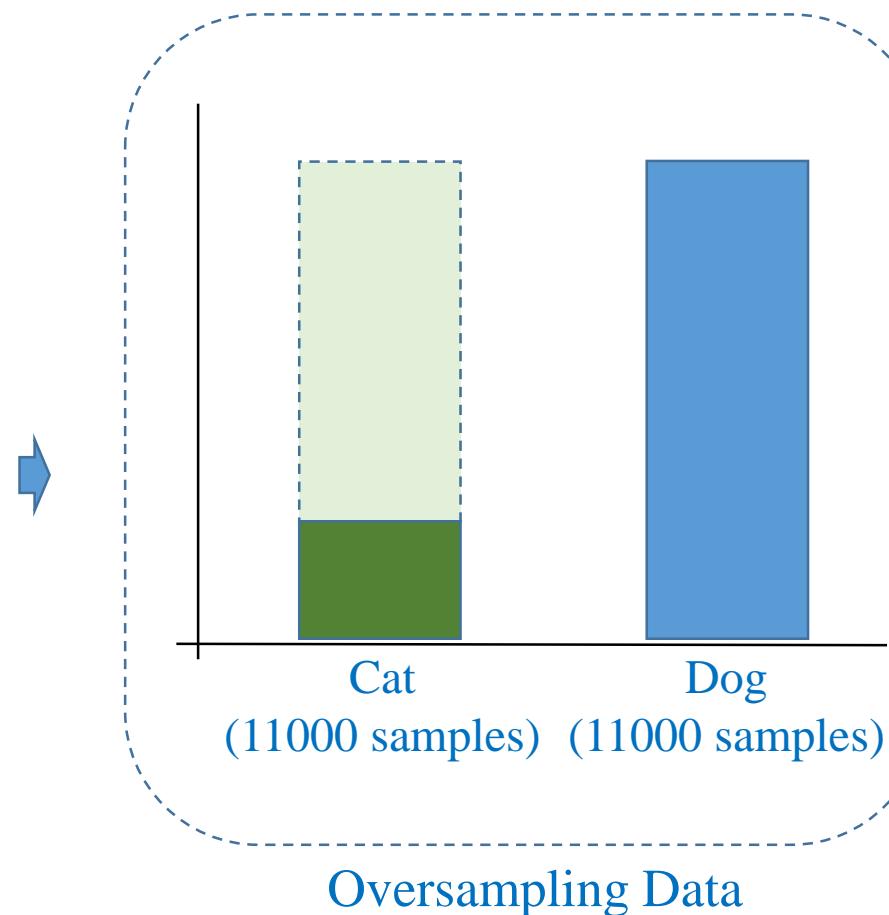
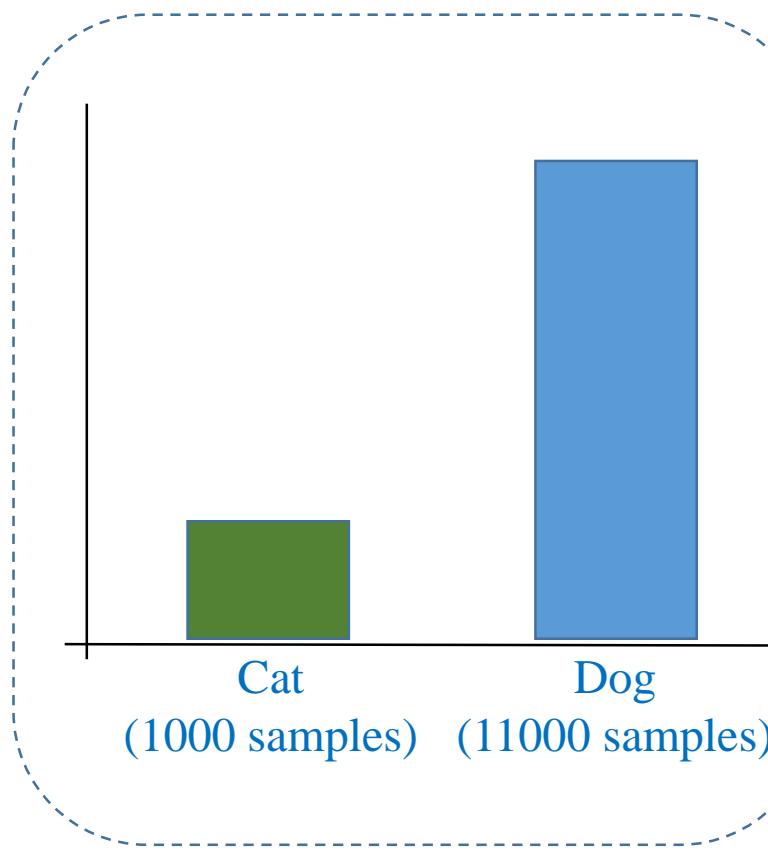
Undersampling Data

$\#_{cat} = 1335$
 $\#_{dog} = 734$
 $F_1 = 0.741$

Experiments

❖ Cat-Dog dataset: Oversampling

Validation data (3000 samples)



Imbalanced Data 1

$$\#_{cat} = 1082$$
$$\#_{dog} = 1483$$
$$F_1 = 0.833$$

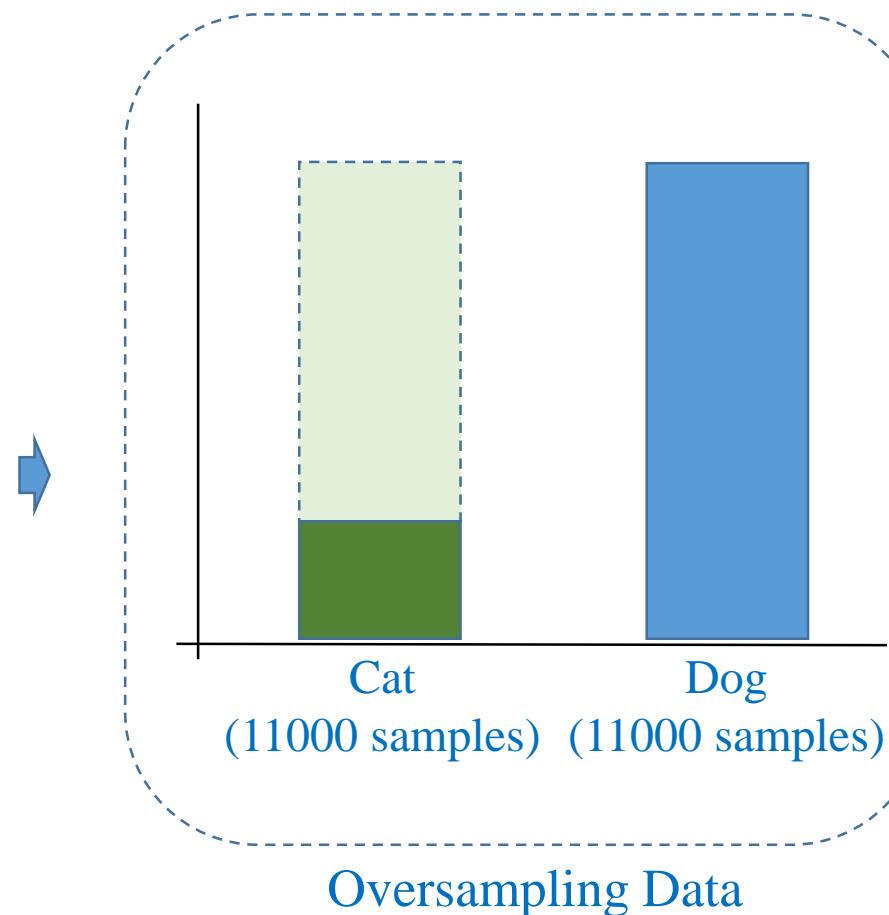
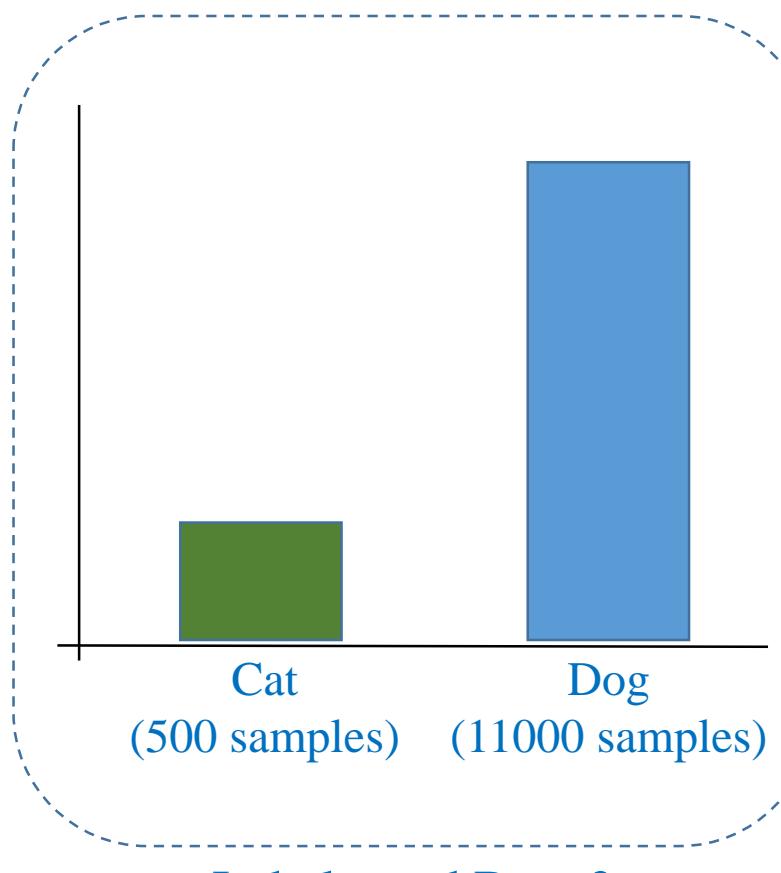
Oversampling Data

$$\#_{cat} = 1167$$
$$\#_{dog} = 1438$$
$$F_1 = 0.855$$

Experiments

❖ Cat-Dog dataset: Oversampling

Validation data (3000 samples)



Imbalanced Data 2

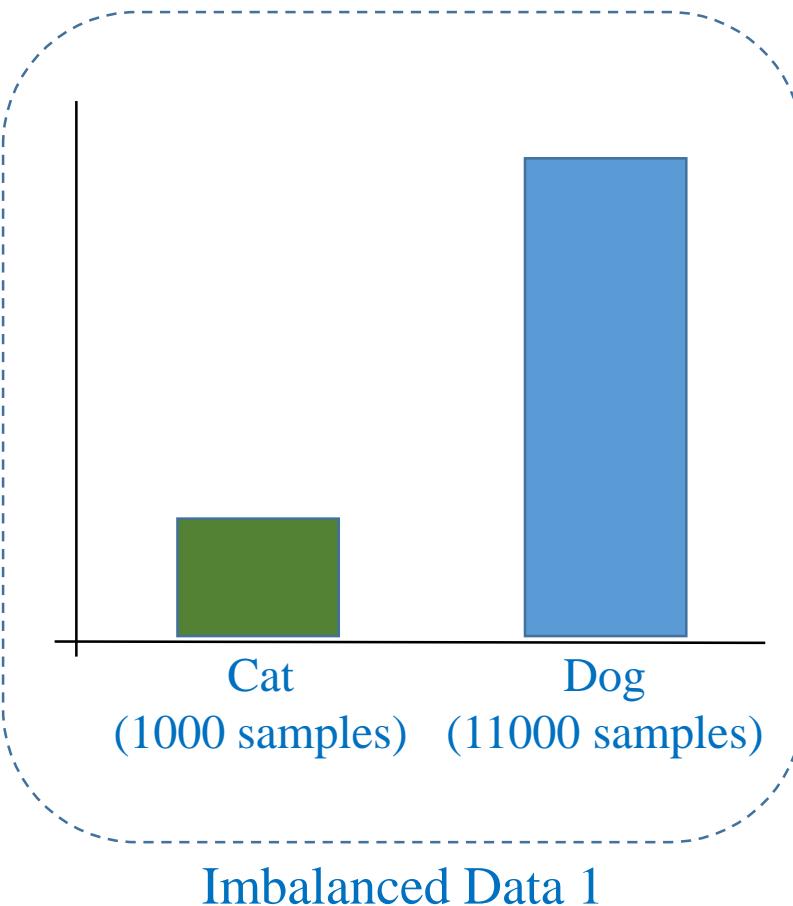
$$\begin{aligned} \#_{cat} &= 821 \\ \#_{dog} &= 1489 \\ F_1 &= 0.704 \end{aligned}$$

Oversampling Data

$$\begin{aligned} \#_{cat} &= 1159 \\ \#_{dog} &= 1386 \\ F_1 &= 0.836 \end{aligned}$$

Experiments

❖ Cat-Dog dataset: Focal loss



Normal crossentropy

$\#_{cat} = 1082$
 $\#_{dog} = 1483$
 $F_1 = 0.833$

Focal loss

$\#_{cat} = 1210$
 $\#_{dog} = 1447$
 $F_1 = 0.876$

