

# Robust Camera Calibration for Sport Videos using Court Models

Dirk Farin, Susanne Krabbe,  
Peter H. N. de With, Wolfgang Effelsberg

Contact address:

Dirk Farin

Eindhoven University of Technology (TU/e)

Embedded Systems Institute

5600 MB, Eindhoven, The Netherlands

**d.s.farin@tue.nl**

# Introduction

Semantic analysis of sport videos depends on

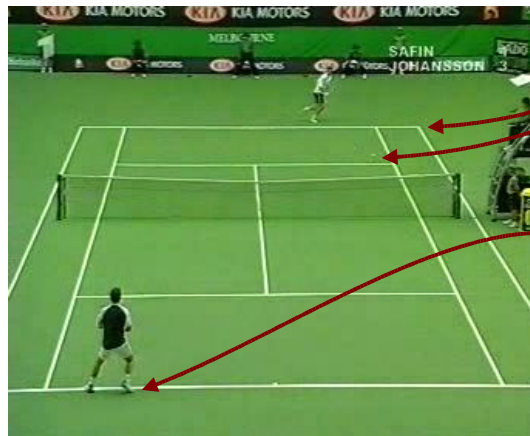
- information about player and ball position,
- position in real-world coordinates, not screen coordinates.

Geometric mapping between screen coordinates and real-world required.

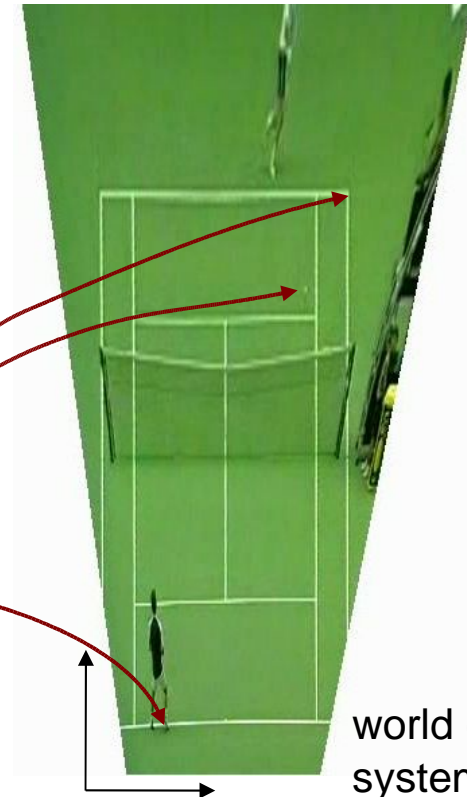
Algorithm design goals:

- robust to occlusion, partial court views,
- generic algorithm, applicable to all court sports,
- support arbitrary camera placement and motion.

image coordinate  
system



world coordinate  
system



# Camera Model

- 3D camera set-up and image formation (in homogeneous coordinates):

$$\mathbf{p}_i = \mathbf{H}\mathbf{p}'_i = \underbrace{\begin{pmatrix} f & 0 & o_x \\ 0 & f & o_y \\ 0 & 0 & 1 \end{pmatrix}}_{\text{camera projection}} \underbrace{\begin{pmatrix} r_{00} & r_{01} & r_{02} & t_x \\ r_{10} & r_{11} & r_{12} & t_y \\ r_{20} & r_{21} & r_{22} & t_z \end{pmatrix}}_{\text{camera rotation and placement}} \underbrace{\begin{pmatrix} x' \\ y' \\ z' = 0 \\ 1 \end{pmatrix}}_{\text{world coordinate}}$$

assume that court ground is at  $z=0$

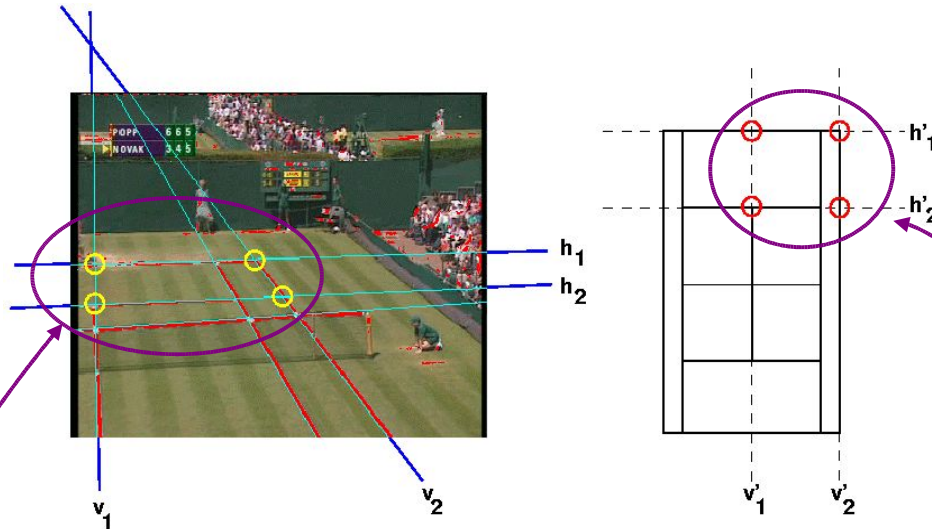
- multiplying this out leads to 8-parameter perspective motion model:

$$x' = \frac{h_{00}x + h_{01}y + h_{02}}{h_{20}x + h_{21}y + h_{22}}, \quad y' = \frac{h_{10}x + h_{11}y + h_{12}}{h_{20}x + h_{21}y + h_{22}}$$

- 8 parameters  $\rightarrow$  8 equations required to solve for parameters
- $\rightarrow$  4 point correspondences required (each gives 2 equations)

# Principle of Calibration Algorithm

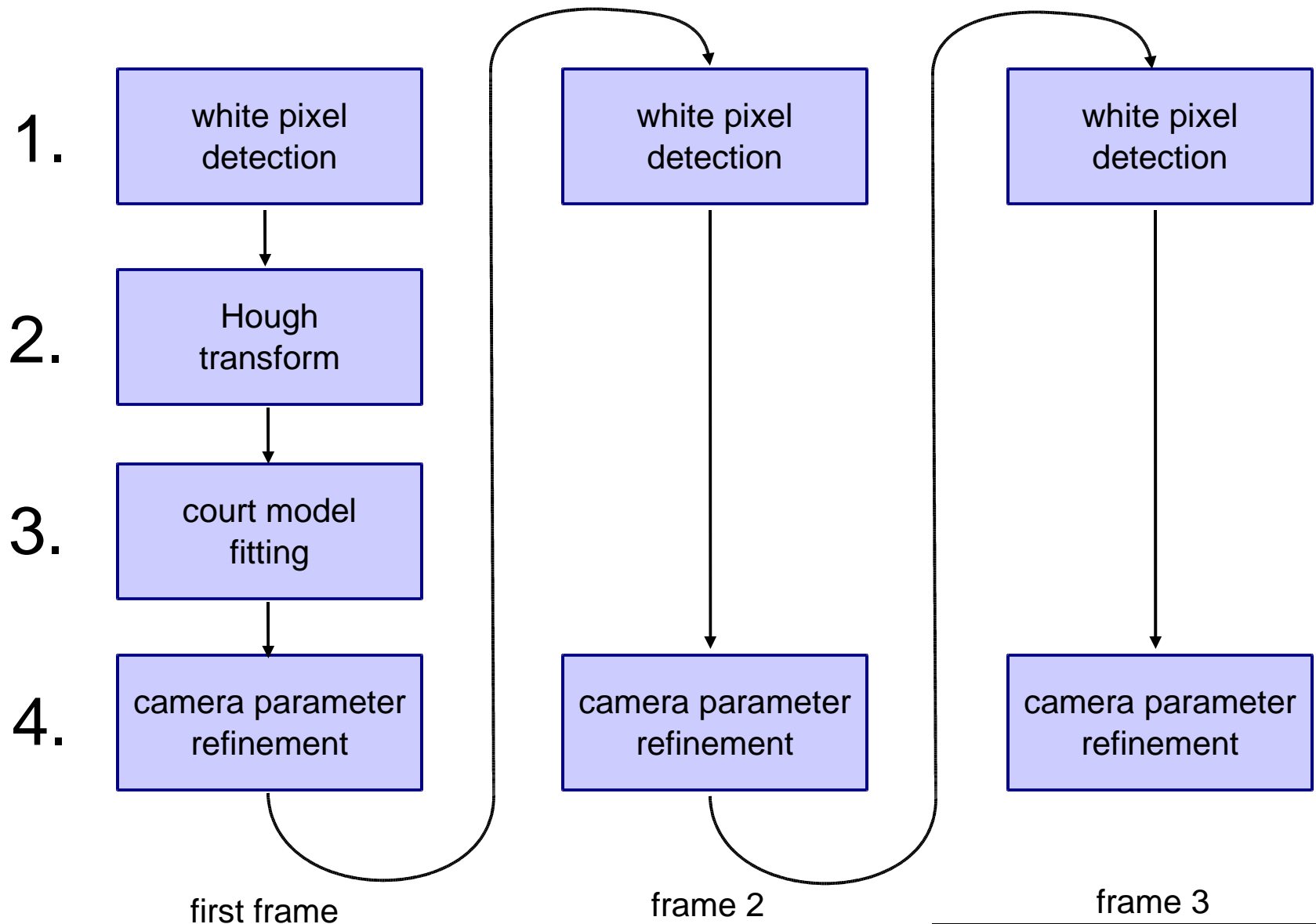
- Select (arbitrarily) two horizontal and two vertical court lines.
- Determine corresponding court lines / points in court model.
- Intersection gives four intersection points.



- Use point correspondences to solve for camera parameters:

$$\begin{pmatrix} x_1 & y_1 & 1 & 0 & 0 & 0 & x_1x'_1 & y_1x'_1 \\ 0 & 0 & 0 & x_1 & y_1 & 1 & x_1y'_1 & y_1y'_1 \\ x_2 & y_2 & 1 & 0 & 0 & 0 & x_2x'_2 & y_2x'_2 \\ 0 & 0 & 0 & x_2 & y_2 & 1 & x_2y'_2 & y_2y'_2 \\ x_3 & y_3 & 1 & 0 & 0 & 0 & x_3x'_3 & y_3x'_3 \\ 0 & 0 & 0 & x_3 & y_3 & 1 & x_3y'_3 & y_3y'_3 \\ x_4 & y_4 & 1 & 0 & 0 & 0 & x_4x'_4 & y_4x'_4 \\ 0 & 0 & 0 & x_4 & y_4 & 1 & x_4y'_4 & y_4y'_4 \end{pmatrix} \begin{pmatrix} h_{00} \\ h_{01} \\ h_{02} \\ h_{10} \\ h_{11} \\ h_{12} \\ h_{20} \\ h_{21} \end{pmatrix} = \begin{pmatrix} x'_1 \\ y'_1 \\ x'_2 \\ y'_2 \\ x'_3 \\ y'_3 \\ x'_4 \\ y'_4 \end{pmatrix}$$

# Flowgraph of Camera Calibration Algorithm

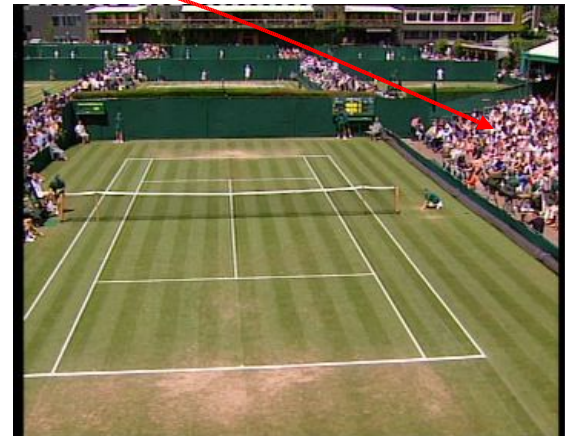
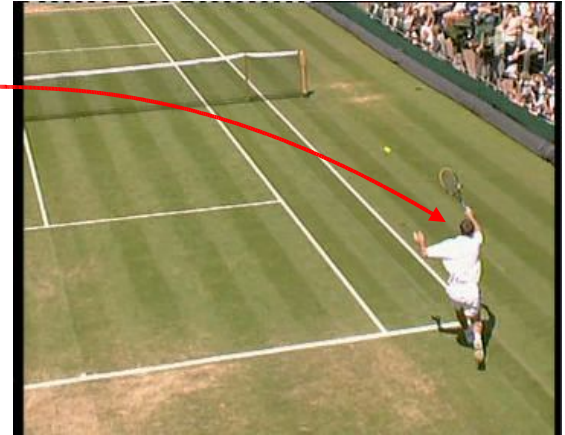


# White (Court-Line) Pixel Detection (1/3)

Detect white pixels belonging to court-lines.

Challenges:

- Players often dressed in white  
(large white regions)
- White colors in the audience, stadium  
(fine textured areas)



Each pixel must pass several tests:

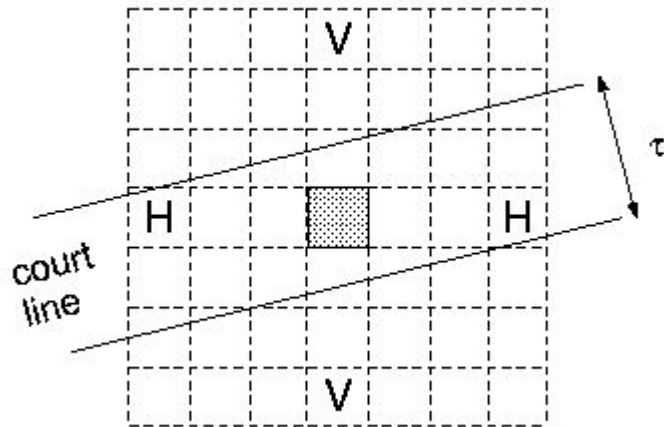
- ♦ above fixed brightness threshold ?
  - exclude dark regions
- ♦ brighter than neighborhood ?
  - exclude homogeneous areas
- ♦ linear structure in neighborhood ?
  - exclude textured areas

Tests have increasing complexity.

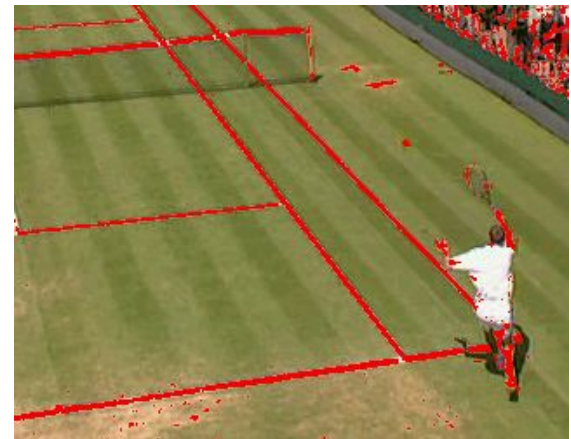
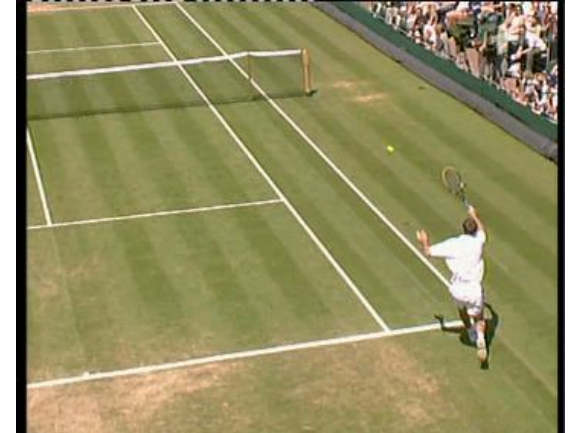
# White (Court-Line) Pixel Detection (2/3)

Flat area exclusion rule (test 2):

- pixel candidate must be brighter than both pixels marked 'H', or both pixels marked 'V'.



- Exclusion of homogeneous white areas with very low computational cost.





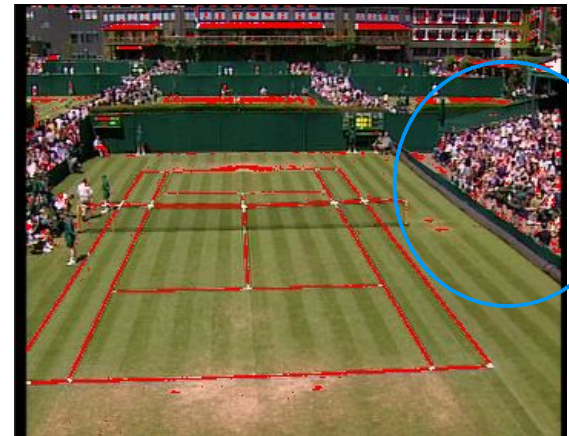
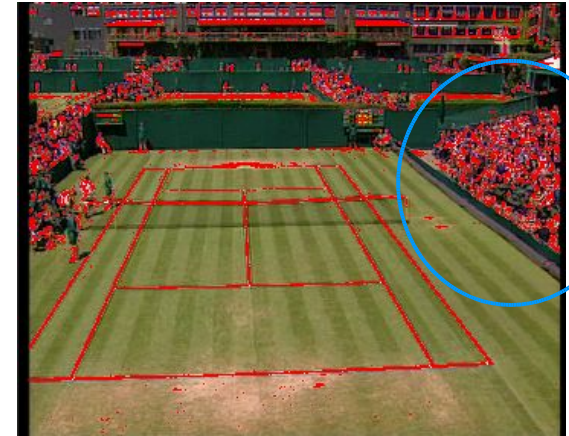
# White (Court-Line) Pixel Detection (3/3)

Textured area exclusion rule (test 3):

- compute structure matrix within the pixel neighborhood:

$$S = \begin{pmatrix} J_{xx} & J_{xy} \\ J_{xy} & J_{yy} \end{pmatrix} = \sum_{x=p_x-b}^{p_x+b} \sum_{y=p_y-b}^{p_y+b} \nabla g(x, y) \cdot (\nabla g(x, y))^T$$

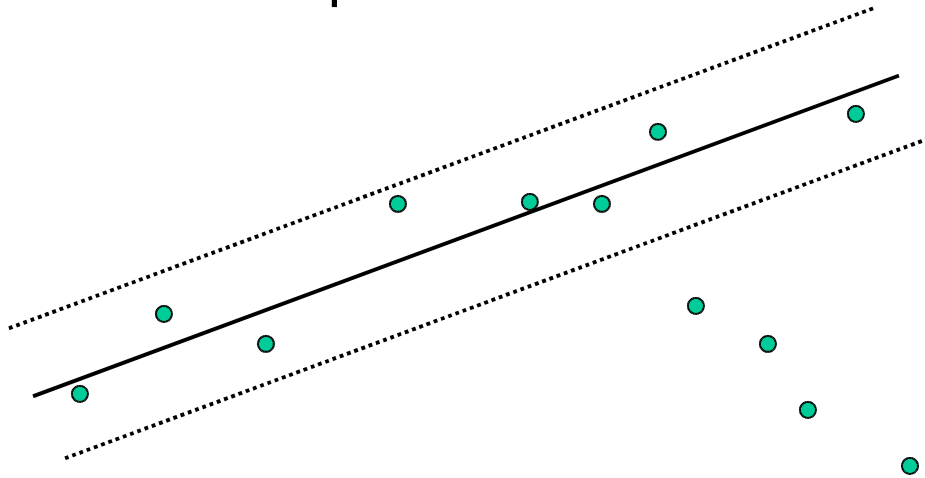
- structure can be classified by evaluating the magnitude of the two eigenvalues.
  - $\lambda_1 \gg \lambda_2 \rightarrow$  linear structure
- complex test, but has to be applied only to remaining candidate pixels



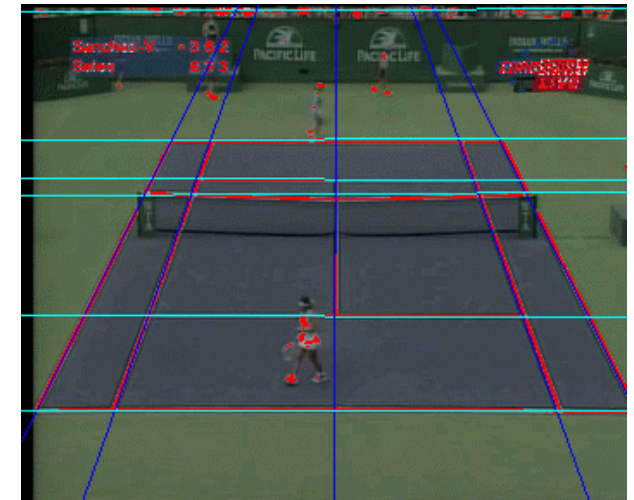
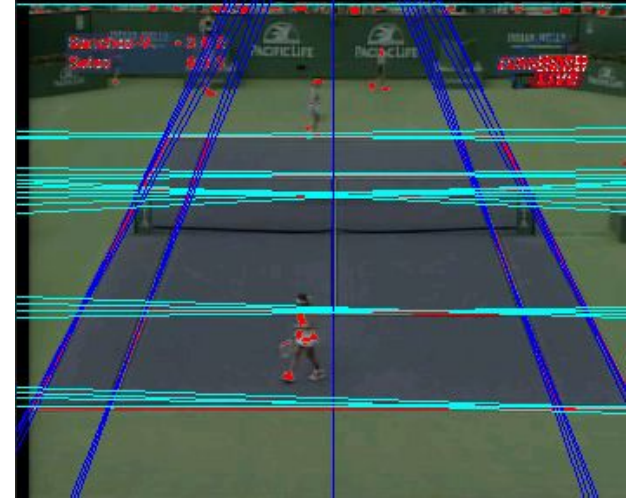


# Court-Line Detection

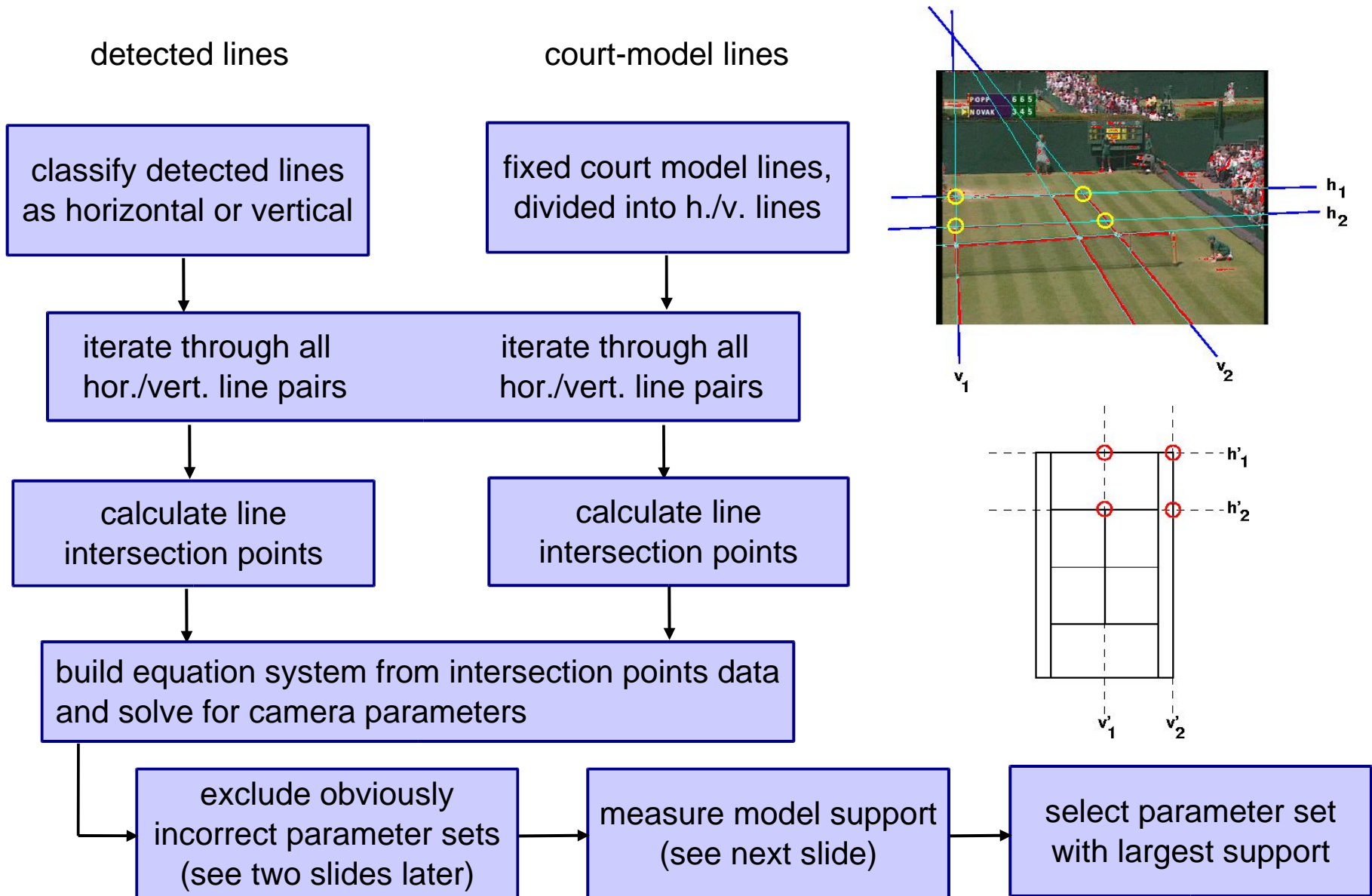
- Apply Hough-transform on *white* pixels to find line candidates.
  - Usually, too many line candidates are found.
- Apply robust regression algorithm (*LTS*) to refine line parameters.



- Remove duplicate lines if their parameters are (almost) equal.

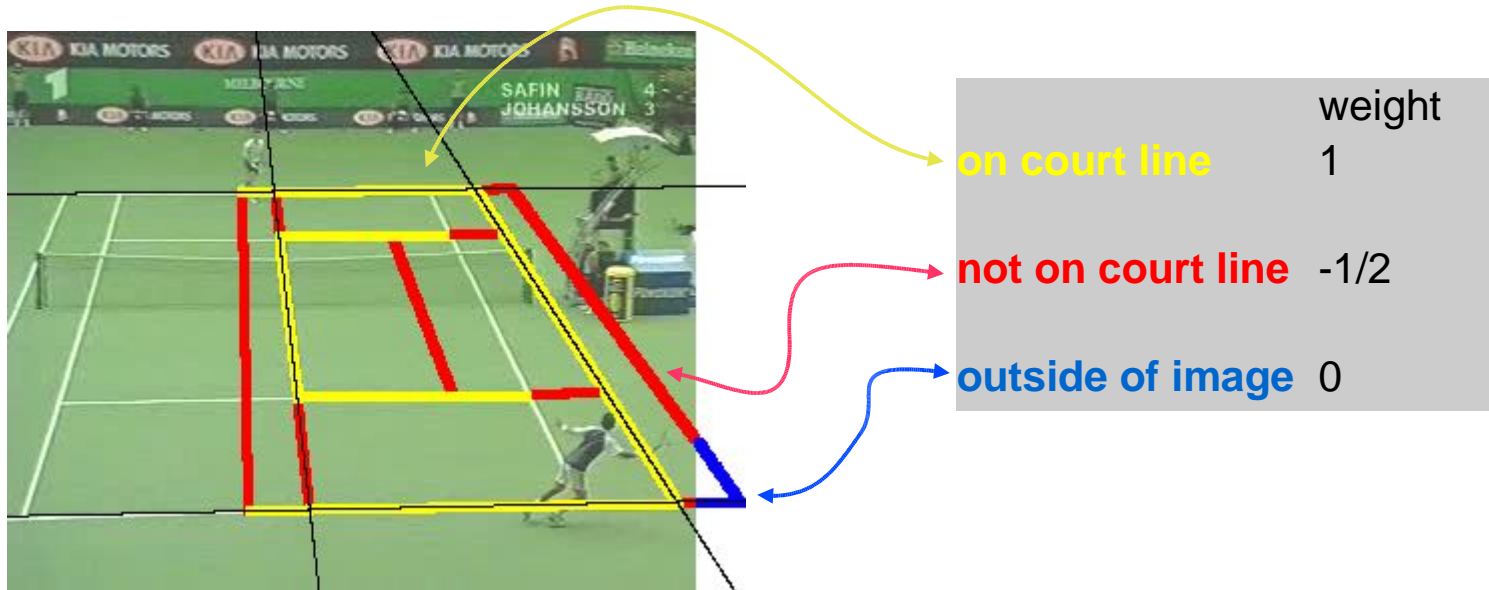


# Determining Court-Line Correspondences



# Selecting the Best Parameter Set

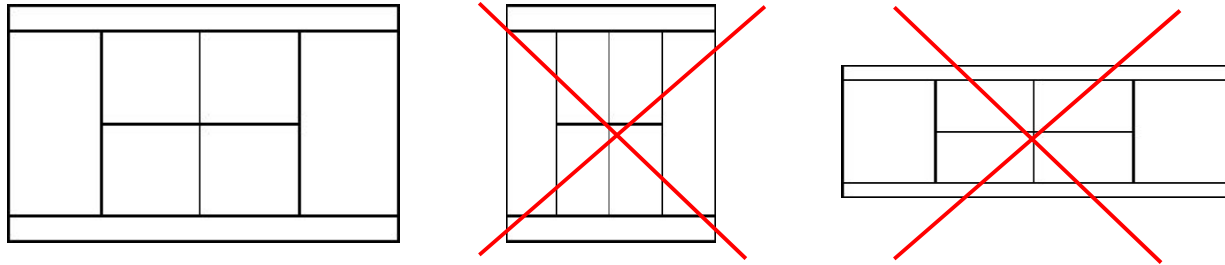
- Use obtained camera parameters to project model back onto image.
- Count court-line pixels that are covered by the model:



- The parameter set which gives the highest score is selected.
- But: before measuring score, perform parameter sanity check:
  - avoids computation of score if parameters are obviously wrong,
  - increases robustness by excluding impossible parameter values.

# Fast Parameter Set Exclusion Rule (1/2)

- Camera model allows non-isotropic scaling, which is impossible in the real world.



- Non-isotropic scaling in our camera model:

$$\mathbf{p}_i = \mathbf{H}\mathbf{p}'_i = \underbrace{\begin{pmatrix} f & 0 & o_x \\ 0 & f & o_y \\ 0 & 0 & 1 \end{pmatrix}}_{\text{internal camera parameters}} \underbrace{\begin{pmatrix} r_{00} & r_{01} & r_{02} & t_x \\ r_{10} & r_{11} & r_{12} & t_y \\ r_{20} & r_{21} & r_{22} & t_z \end{pmatrix}}_{\text{camera rotation, translation}} \underbrace{\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \beta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}}_{\text{non-isotropic scaling}} \begin{pmatrix} x' \\ y' \\ z' = 0 \\ 1 \end{pmatrix}$$

$\beta$  should always be equal to 1

# Fast Parameter Set Exclusion Rule (2/2)

- Decompose transformation matrix  $\mathbf{H}$  to obtain  $\beta$ .
- Assume that principal point is known.

$$\begin{pmatrix} 1 & 0 & -o_x \\ 0 & 1 & -o_y \\ 0 & 0 & 1 \end{pmatrix} \mathbf{H} = \mathbf{H}' = \begin{pmatrix} f & 0 & 0 \\ 0 & f & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} r_{00} & r_{01} & t_x \\ r_{10} & r_{11} & t_y \\ r_{20} & r_{21} & t_z \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & \beta & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} fr_{00} & \beta fr_{01} & ft_x \\ fr_{10} & \beta fr_{11} & ft_y \\ r_{20} & \beta r_{21} & t_z \end{pmatrix}$$

- We know that  $\{ r_i \}$  is orthonormal (rotation matrix).

$$\frac{h'_{00}{}^2}{f^2} + \frac{h'_{10}{}^2}{f^2} + h'_{20}{}^2 = \frac{h'_{01}{}^2}{\beta^2 f^2} + \frac{h'_{11}{}^2}{\beta^2 f^2} + \frac{h'_{21}{}^2}{\beta^2}$$

$$\frac{h'_{00}h'_{01}}{\beta f^2} + \frac{h'_{10}h'_{11}}{\beta f^2} + \frac{h'_{20}h'_{21}}{\beta} = 0$$

↑  
these are our camera  
parameters  
(except a scaling factor)

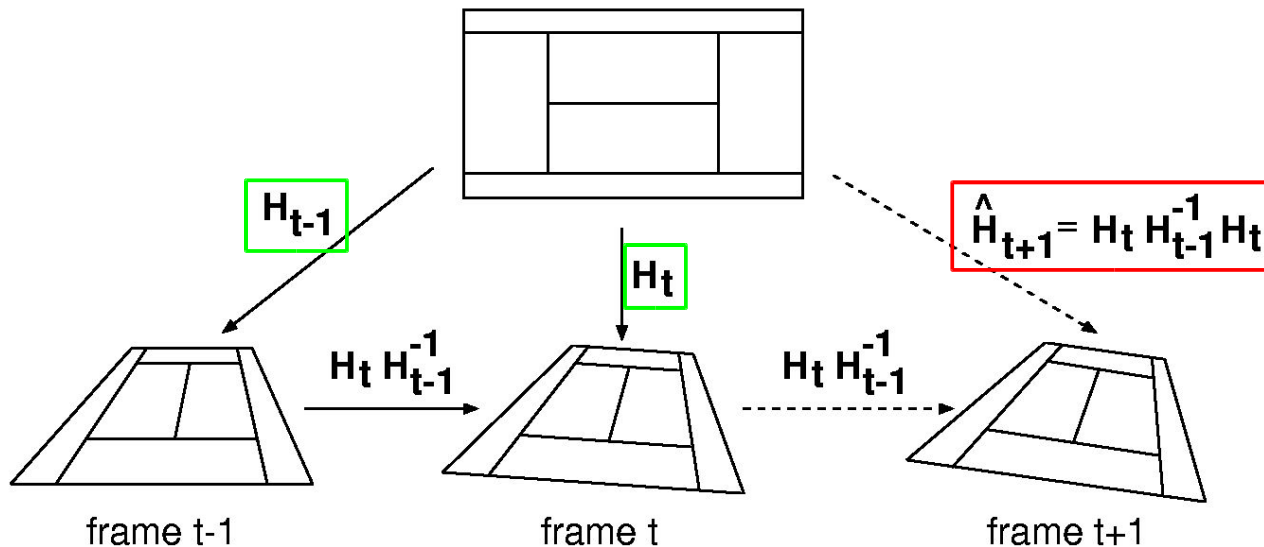
- Hence, we obtain as:

$$\beta^2 = \frac{h'_{01}{}^2 + h'_{11}{}^2 + f^2 h'_{21}{}^2}{h'_{00}{}^2 + h'_{10}{}^2 + f^2 h'_{20}{}^2} \quad ; \quad f^2 = -\frac{h'_{00}h'_{01} + h'_{10}h'_{11}}{h'_{20}h'_{21}}$$

- Consider a parameter set as invalid if  $\beta < 0.5$  or  $\beta > 2.0$

# Model Tracking

- Algorithm so far operated on single frames.
- When applied on a video-sequence, previous parameters sets can be used to compute an initial estimate.

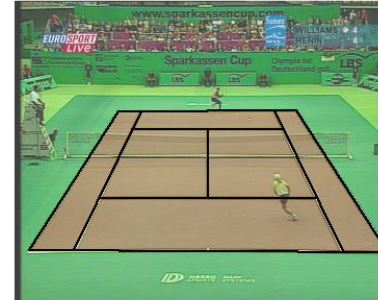
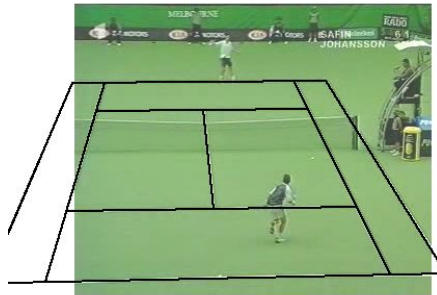
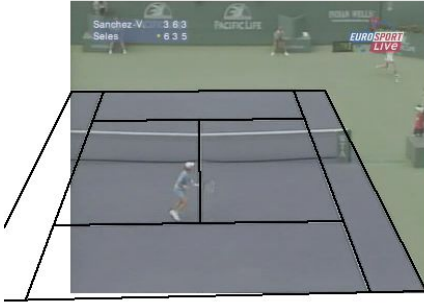


- Optimize camera parameters by minimizing distance between model lines and court-line pixels.
- Non-linear optimization problem  $\rightarrow$  use gradient-descent algorithm.

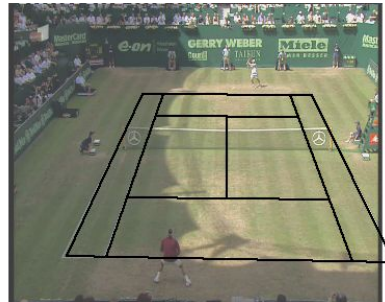


# Results (*Tennis*; 1/2)

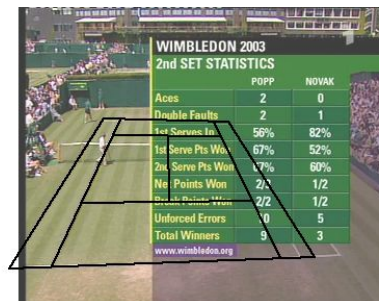
- different court types:



- strong shadow:

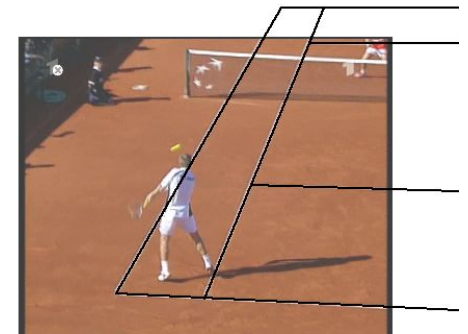
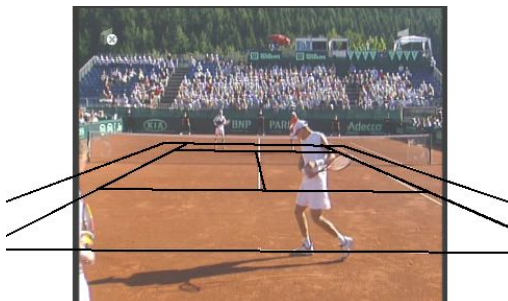
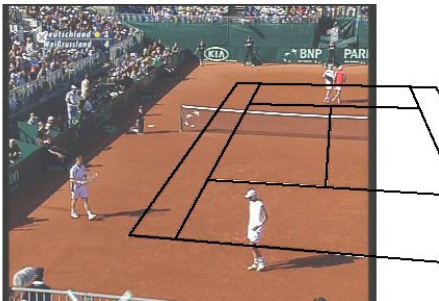
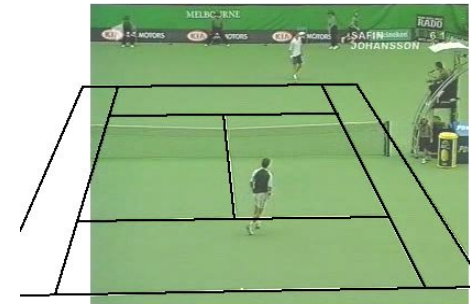
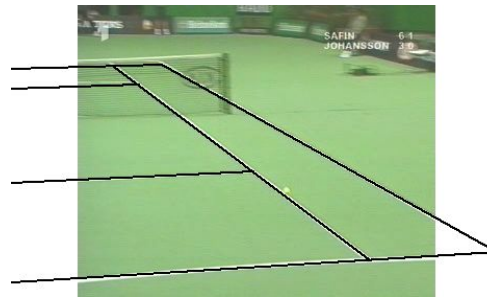
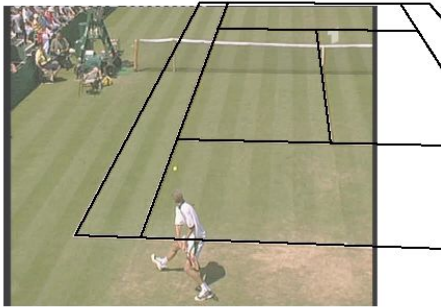
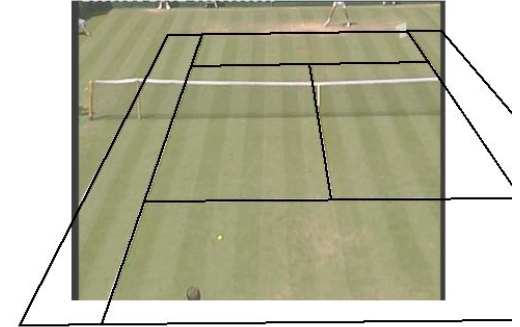
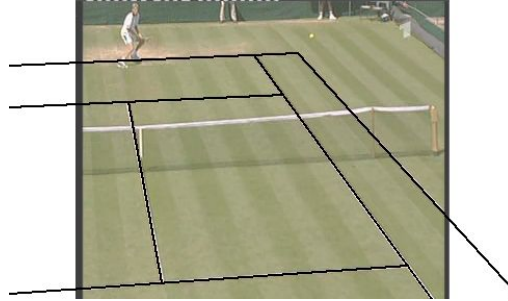
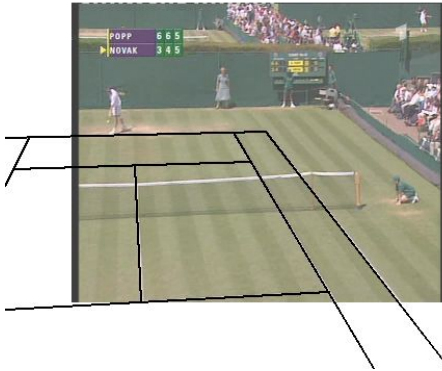


- very large occlusion:

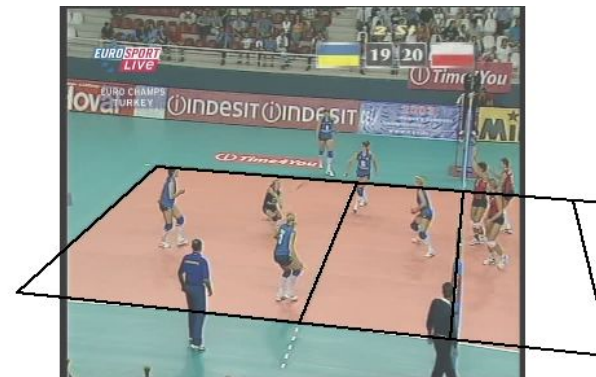
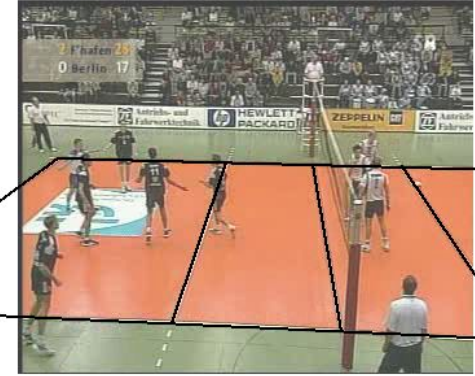
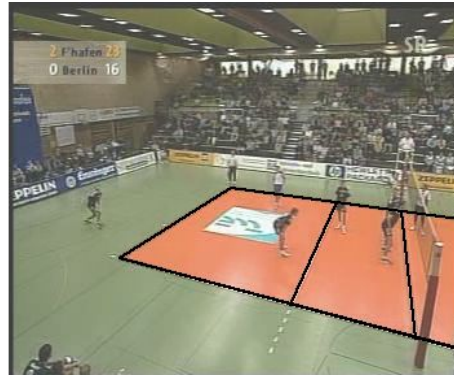
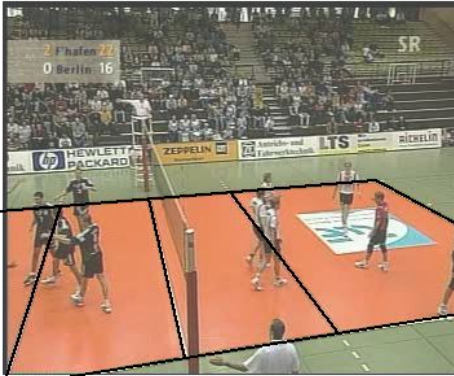


All results were obtained without any parameter adjustment.

# Results (*Tennis*; 2/2)

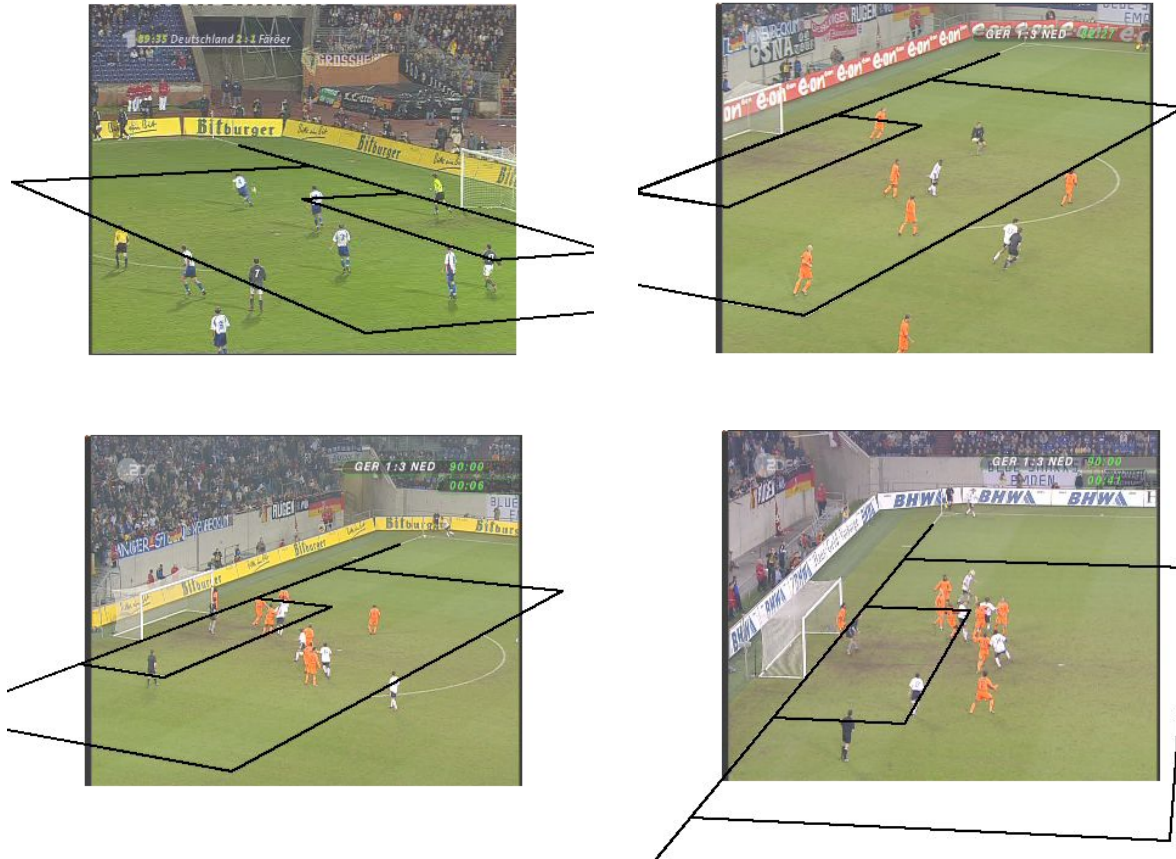


# Results (*Volleyball*)





# Results (Soccer)



- Only goal-area scenes can be processed.
  - 2 vertical & 2 horizontal lines required,
  - for remaining scenes, more restricted camera model is required, or some parameters must be known.

# Conclusions

- Camera calibration required to convert between screen coordinates and real-world coordinates.
- Generic algorithm, applicable to any court sport:
  - extract line segments of the input image,
  - use model of court-line arrangement,
  - establish correspondences between input lines and model lines.
- Very robust calibration results
  - insensitive to large occlusions,
  - no need for parameter adaptation.
- Possible extensions
  - include curved model primitives (e.g., circle in center of soccer field).