

→ largest SOT has then a complete graph  
→ find maximal by writing auxiliary to T  
Sque → find a dense subgraph instead and

2 → 2-coloring: disjoint covering bipartite components → DP3.

3 → Turking chromatic number of graph  
Coding → & not complete.

4 → Merge iteration: if it is max size, we can edge-color with 2+1.

5 → This allows an O(n!) algorithm  
Coding → for finding (n,n)-coloring of the graph

- Can it be local?
- Can I simplify? (Bussom-Wheeler)
- Does it have to be exhaustive?

6 → Mattheson colors it by tree search  
is not adaptive

Implementation → loop-invariant including LRU cache

→ build index as we go and reuse it when dequeued later

→ use a stack to store nodes that have been processed

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## Programming Pearls [2]<sup>n</sup>

• state for you  
• use a binary search on a set of numbers in a  $\Theta(n^2)$  structure

• how we can sort such a file with a very limited number of passes.

### Jon Bentley

• whenever possible, use a binary search of the problem space  
• doesn't have to be linear. Anding an item in a sorted list and then the missing item in the sorted list of items.

• Rotating vector:  $\{1, 2, 3, 4, 5\}$  or  $\{10, 15, 5, 10, 15\}$

• Use shifts, rotations, and other operations

• Use pointers to  $\{1, 2, 3, 4, 5\}$

• Use half jumps:  $\{1, 2, 3, 4, 5\}$

• See [dijkstra's algorithm](#) for tree search

• program using a for loop

• Research of [Knuth-Morris-Pratt](#)

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8 pages

2016,11,14-2016,11,16

- 1
- state the problem in clear terms
  - use a bit-vector to represent a set of numbers in a given range.  $\Rightarrow$  Bitmap Data Structure

$\hookrightarrow$  We can sort such a file with a very limited number of passes.

- 2
- Use binary search (one/two sided) whenever possible.
  - $\hookrightarrow$  binary search of the problem statement doesn't have to be about finding an item in a sorted list  $\Rightarrow$  find the missing item
  - rotating vector  $S_{i \dots n} \text{ arr } i \text{ to } S_{i \dots n}$

$\hookrightarrow$  ① Use shifts

② Use pointers

$S_i \Rightarrow S_0$

③ Use half jumps:

$S_{2i} \Rightarrow S_i$

④ See  $ab \Rightarrow ba$  as  $\{ab, br\}$  then

swap a for br  $\Rightarrow b_r b_r a$  and reverse

⑤ Reverse:

$ab \Rightarrow a^r b$

$a^r b \Rightarrow a^r b^r$

$a^r b^r \Rightarrow (a^r b^r)^r = ba$

-1-

→ Find anagrams → reduce words to their signature by lexicographically sorting each word (hello → elillo) and finding words with the same signature.

- Good programmers are a little bit lazy: they sit back and think before rushing to code.

→ Use templating and separate control from results. (3)

→ Extract switch parameters into a DB

→ In general think of extensibility.

- Use "Data Structures" to reduce big programs to small programs.

- Generalization helps form an objective view.

↳ Let the data, structure the program!

• Be liberal with assertions (4)

• Control bugs at all three stages: see CLRS (3)

• Clearly define the contract: ① pre-conditions  
② post-conditions

• Assertions provide insight into intentions

• Try to program units simple and small.

⑤

- Instead of directly incorporating the new code into the system build a scaffolding.
- Run the function in isolation against easily verifiable test cases.

- put meaningful assertions in the code that do not cause errors themselves

- write automated tests that exhaustively runs our code through possible valid AND invalid inputs.

- We can also test run time complexity by measuring actual runtime and check if it falls within E of expected time.

⑥

- Efficiency can be achieved at various levels.

- problem specification

- system structure & modularization

- algorithms & data structures

- code tuning

- system software

- hardware

- figure out which gives you the biggest boost with the least effort & possibly work on many levels

- ⑦
- Try back-of-the-envelope estimates
    - ↳ try your calculations from multiple points of view if possible
  - Check the units, check the obvious issues with your basic calculations.
  - 72 seconds is a nano century.
  - Try to estimate performance and space efficiency in this way.
  - Incorporate safety factors to compensate for mistakes & oversimplifications.
  - Little's Law: calculate entry rate based on exit rate and time spent in-the-process
- 
- ⑧
- Save the state to avoid recomputation
  - Preprocess data to help with the actual processing
  - Try to see if solving for  $\gamma_2$  helps solving for  $n \rightarrow$  divide & conquer
  - See if the solution for  $\pi_{[0..i-1]}$  can be extended for  $\pi_{[i..j]}$  → scanning technique
  - Use cumulative data when dealing with ranges.
  - Find out the lower bounds!

- ⑨
- Premature optimization is the root of all many:0 evil.
  - use measurement tools to zoom in on the culprit.
  - make sure your code optimizations at the small scale do not affect the overall speed
  - try to follow these rules in code optimization
    - exploit algebraic identities
    - collapse procedure hierarchies
    - unroll the loops
    - augment the data structures
- 
- ⑩
- Simplicity of data structures is usually the key to reducing data / memory usage
  - Be aware of the density / sparsity of data
    - reducing data space → recompute
      - use dynamic allocation
      - use pointers to shared space
    - exploit sparsity
      - use compression techniques
    - use interpreters
  - reducing code space → Factor into functions
    - write machine code
    - optimize the compiler

- ⑪
- Do not implement generic algorithms such as sorting unless you have reason to.
  - Sorting is a powerful tool that might be overused at times.

- ⑫
- An important part of a programmer's job is solving tomorrow's problems:
    - understand the perceived problem & do not take the implied solution as the way to go.
    - abstract the problem to see how it relates to other problems.
    - use an informal high-level language to design a solution then evaluate the merits of different algorithms/data structures before coding.
  - Implement a solution and optimize it
    - {-prototype many solutions & compare them
    - do retrospection after the solution to see how else/better you could've done

- ⑬
- Using interfaces to decouple the contract from implementation let's us improve existing code by dropping in better implementations.
  - consider using libraries in place of home made implementations unless absolutely necessary.
  - remember that not all space is equal. Know when your data is crossing from external storage to main memory, to CPU cache and within RAM fragments.
  - Use code tuning (see 9) to optimize

- ⑭
- always measure the efficiency of code
  - stating loop invariants helps with validity correctness
  - distinguish between "what" & "how"
  - use abstraction to allow for easy fixes and improvements
  - ↳ interface implementation ↳ decouple what & how
  - ↳ heap sort can make use of freed heap space to co-host both the sorted array & the heap

## Introduction to Information Retrieval

Christopher D. Manning

Prabhakar Raghavan

- Suffix arrays are arrays of proper suffixes of a given string:

SAMPLE :  
 $A_1$  SAMPLE  
 $A_2$  AMPLE  
 $A_3$  PLE  
 $A_4$  LE  
 $A_5$  E

} We can sort them lexicographically. After that comparing two adjacent entries' prefixes can yield the longest repeated substring of S.

- Generating random text & searching for phrases are among the uses of suffix arrays.