

# Genetic Mapping in Polyploids: from genotyping to haplotype reconstruction

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# North Carolina State University



- Some Numbers (fall 2020)
  - 36,762 students enrolled (48.7% female, 51.3% male)
    - (71% undergrads, 29% grads)
  - 2,457 professors (40.6% female, 59.4% male)
  - 7,239 staff (47.9% female, 52.1% male)
- Motto: Think and do!
- Public, land-grant and research university
- Raleigh, NC
- 3 campuses: Main, centennial, biomedical centennial.
- Nickname: Wolfpack (Go pack!)



# Main campus



# Talley Students Union



# NCSU – Carter-Finley Stadium



aaphc.com



# NCSU - PNC Arena



# Centennial Campus



# Centennial Campus – J. B. Hunt Library



# Plant Sciences Initiative



# Outline

- Introduction to linkage
- Genotype calling in polyploids
- Modeling gamete formation, linkage and phasing
- Genetic mapping in hexaploid sweetpotato
- Assessing meiotic configurations and preferential chromosome pairing
- Multi-parental analysis in complex polyploids



# Genomic Tools for Sweetpotato Improvement – GT4SP

- Bill & Melinda Gates Foundation has a large portfolio and 10% is dedicated to agriculture development in Sub-Saharan Africa and South Asia for food supply purposes.
- Key Crops: Cassavas, Yams, Bananas and **Sweetpotatoes**
- Phase I: GT4SP (PI: Dr. G. Craig Yencho – NCSU)
- Phase II: SweetGAINS (PI: Dr. Hugo Campos - International Potato Center)



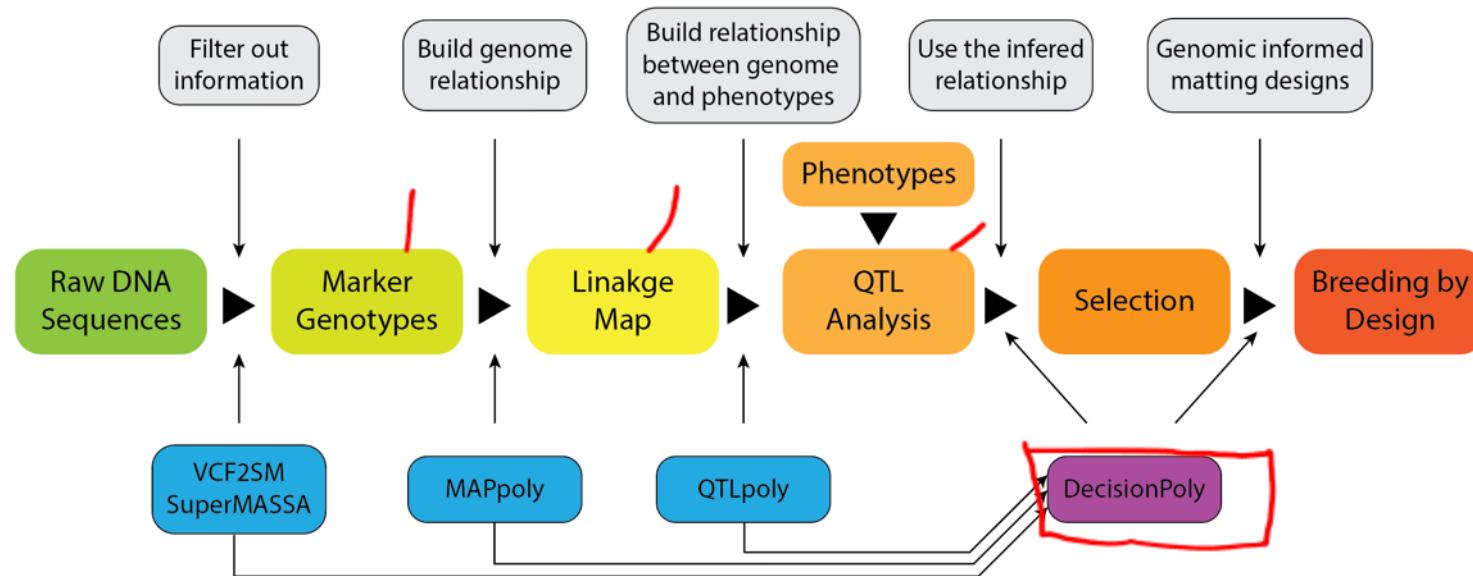
# Sweetpotato for profit and health initiative

Food security for Sub-Saharan Africa



# GT4SP & SweetGAINS

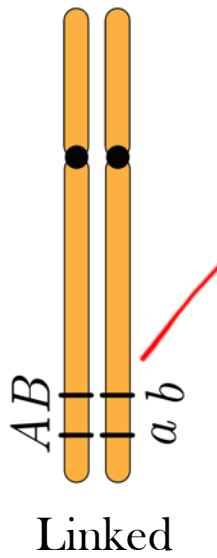
- Develop computational tools for the whole pipeline data analysis



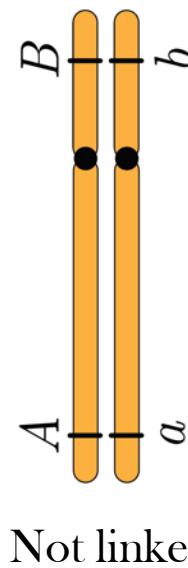
- VCF2SM:** Python scripts processing DNA calls (VCF files) for SuperMASSA
- SuperMASSA:** Call SNP dosage marker genotype probability distribution.
- MAPpoly:** An R package for constructing a complete linkage map for 2X, 4X, 6X, 8X
- QTLpoly:** An R package for QTL mapping in full-sib families for 2X, 4X, 6X, 8X
- DecisionPoly:** user-friendly **computational tool** to assist breeders in making long and short-term **breeding decisions** based on collected and learned **information** about their breeding populations.

# Introduction

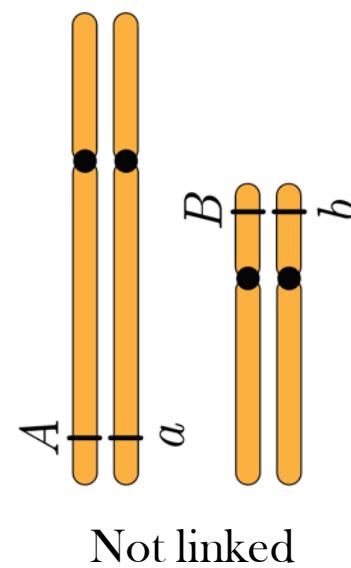
- Genetic linkage is the phenomenon where markers are likely to be inherited together.
- The closer the markers are, the lower the probability of crossing over events occur between them; consequently, the more likely they will be co-inherited.



Linked



Not linked



Not linked

- How can we measure how likely A and B are co-inherited?

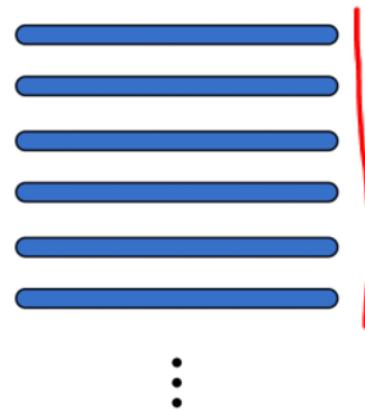
# Linkage analysis

- We measure linkage using the *recombination frequency* (or fraction) in a segregation population.
- Genetic linkage is a concept applied to *at least two loci*.
- Recombination fraction is the *probability* that an odd number of crossovers occurs between the markers. Ranges from 0.0 to 0.5 (considering double reduction this number can be higher)
- We can transform these probabilistic values into distances using *mapping functions*. (Morgan, Haldane, Kosambi, etc.)
- By computing the recombination frequencies between pairs of markers and using mapping functions, we can construct *linkage maps* which show the linear order and relative distance between adjacent markers.
- First, let us address the *behavior of a single loci* when transited across generations.

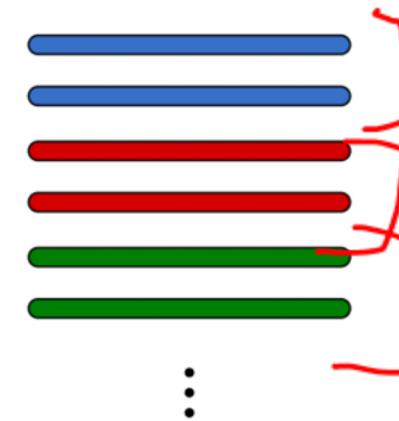
# Polyplloid Species

- Organisms with more than 2 complete sets of chromosomes

Autohexaploid

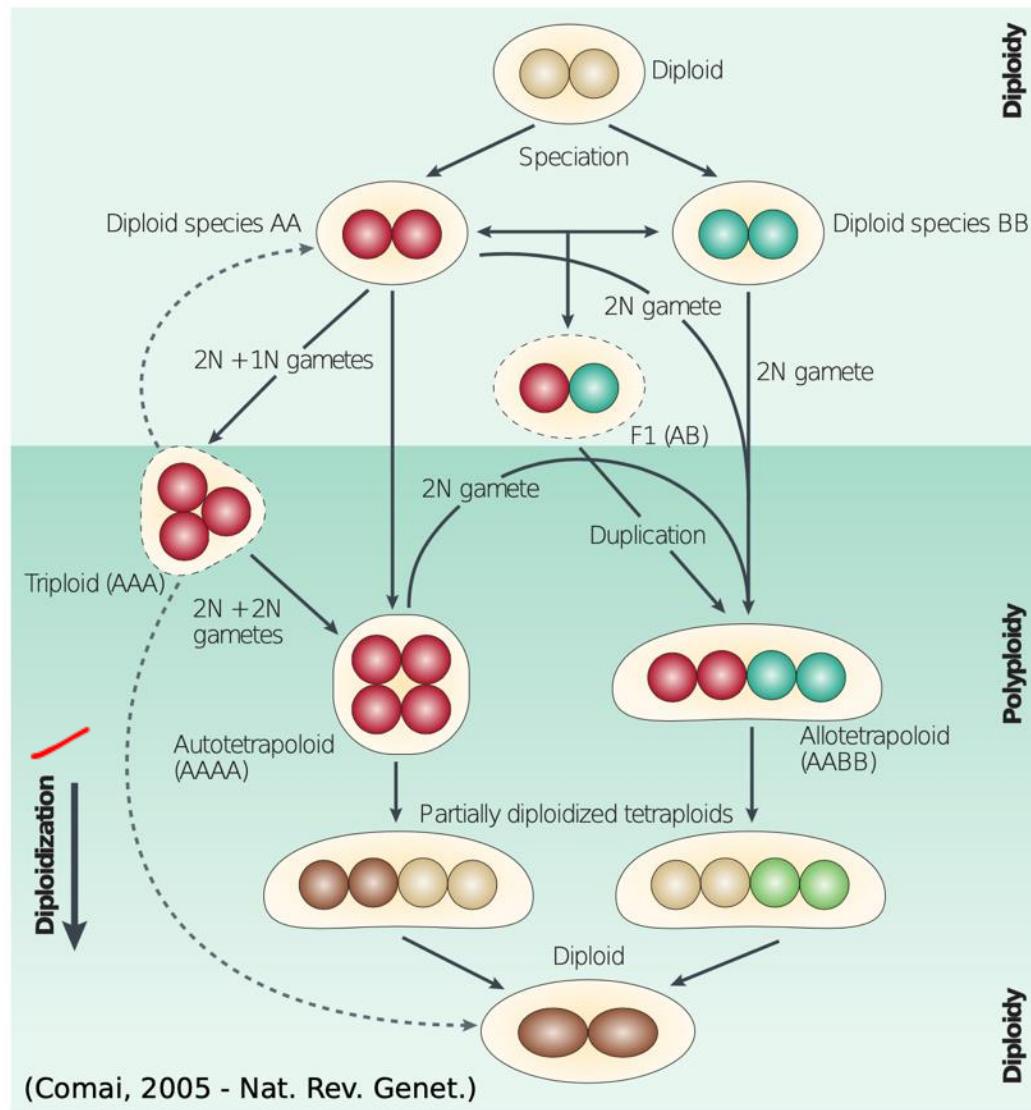


Allohexaploid

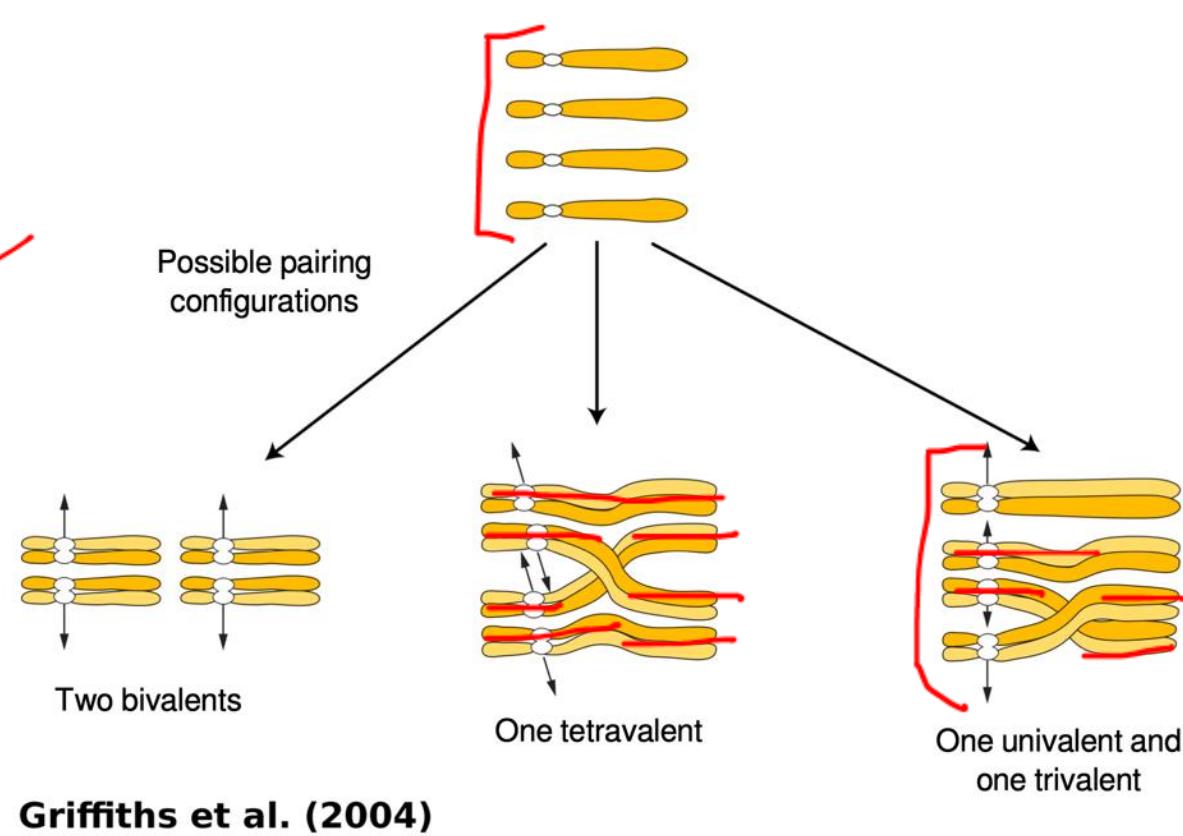
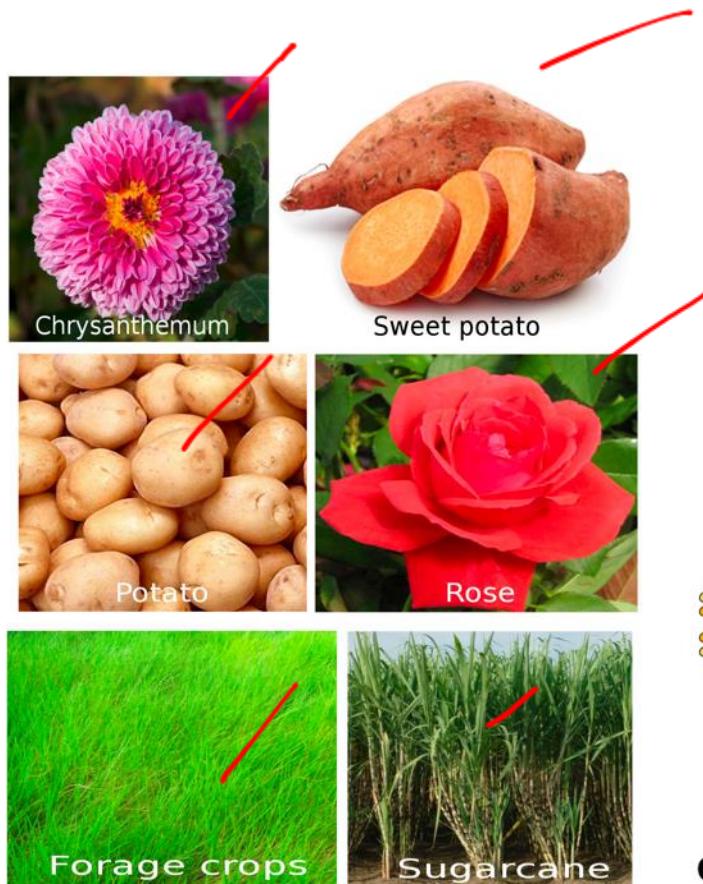


- Multiple sets have the **same** origin
- Multiple sets have **different** origins

# How are polyploids formed

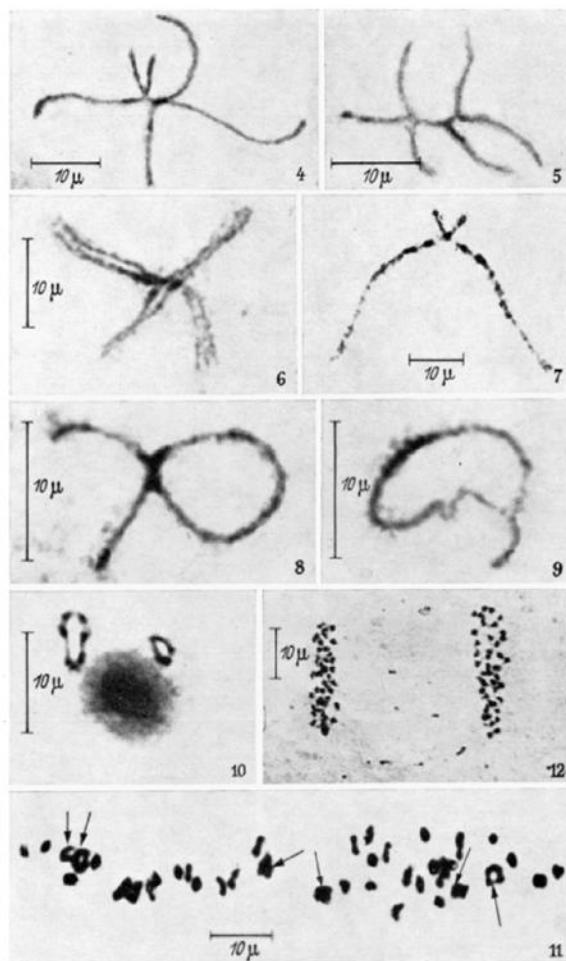


# Autopolyploids and meiotic pairing



# Meiotic Pairing in polyploids

Sweetpotato



Hexavalents, quadrivalents and bivalents  
in sweetpotato (Magoon *et al.* 1970)

Sugarcane

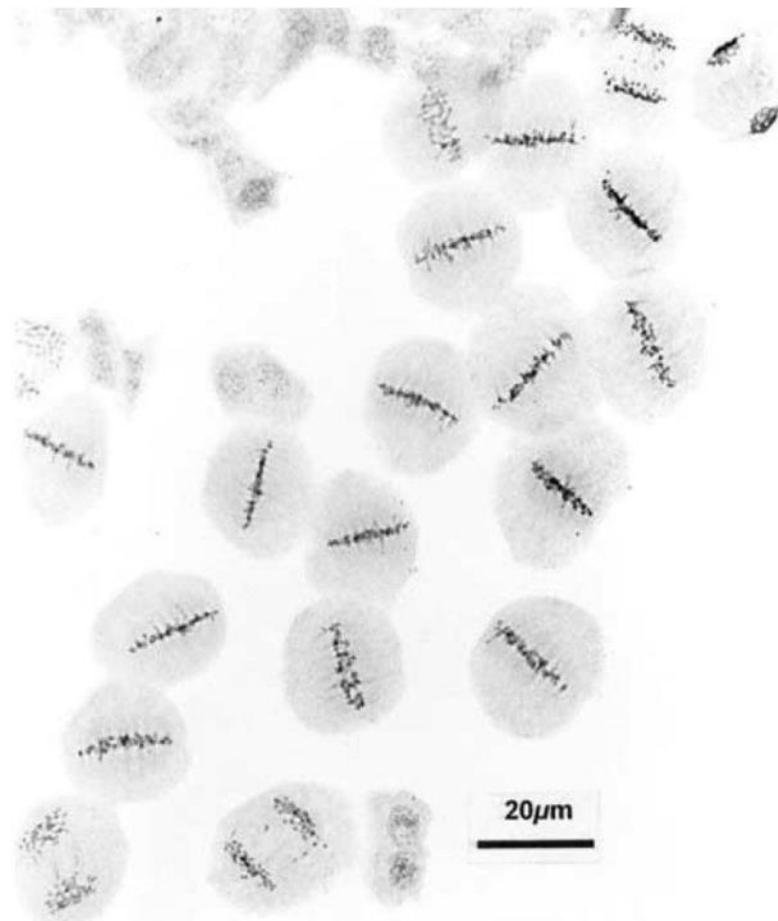


Figure 1. PMCs of *Saccharum* spp. hybrid clone 79N9059 at meiosis. As was the case in other clones, pairing was regular, bivalents generally formed. (Bielig *et al.* 2003)

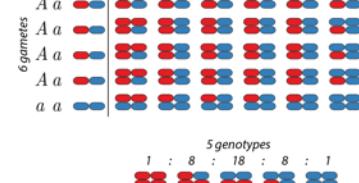
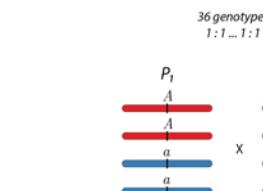
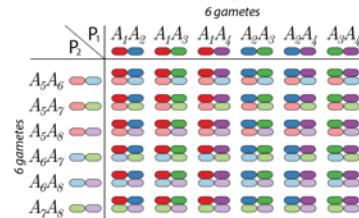
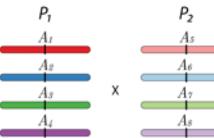
# Segregation in polyploids\*

Multiallelic

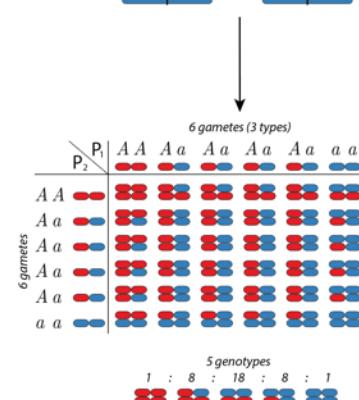
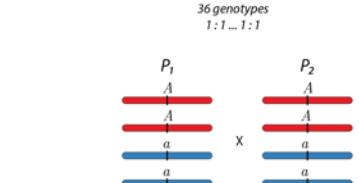
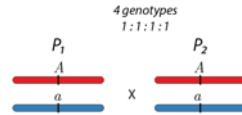
Diploid



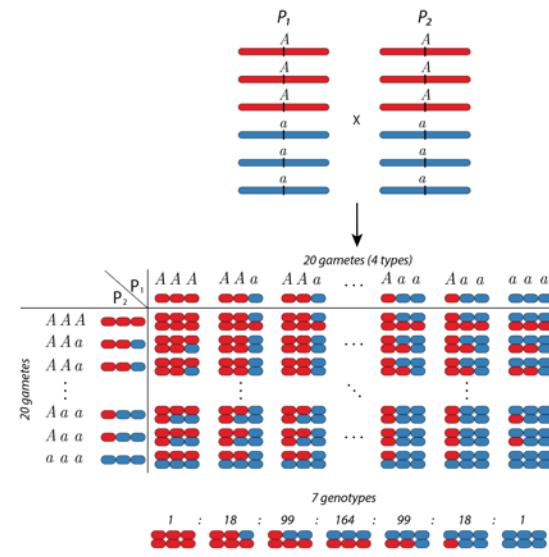
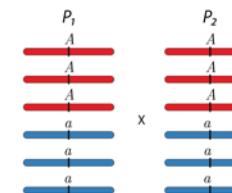
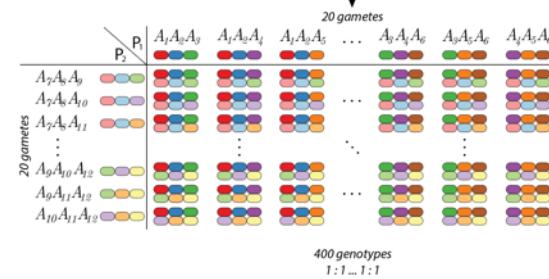
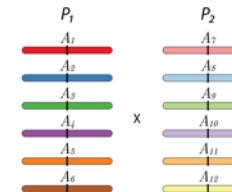
Tetraploid



Biallelic



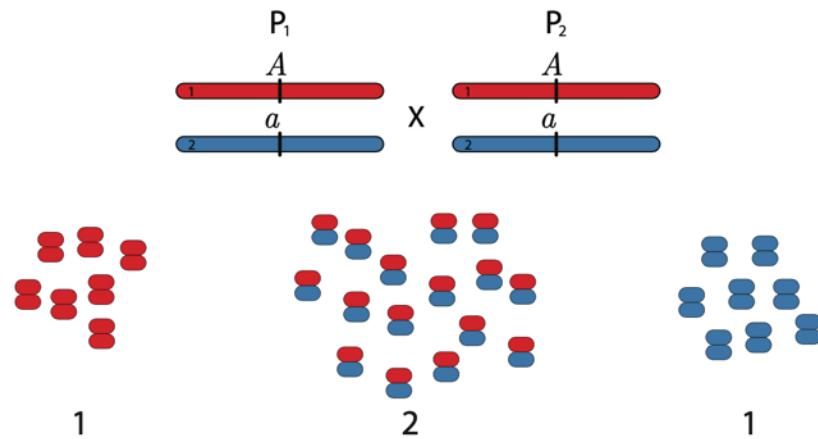
Hexaploid



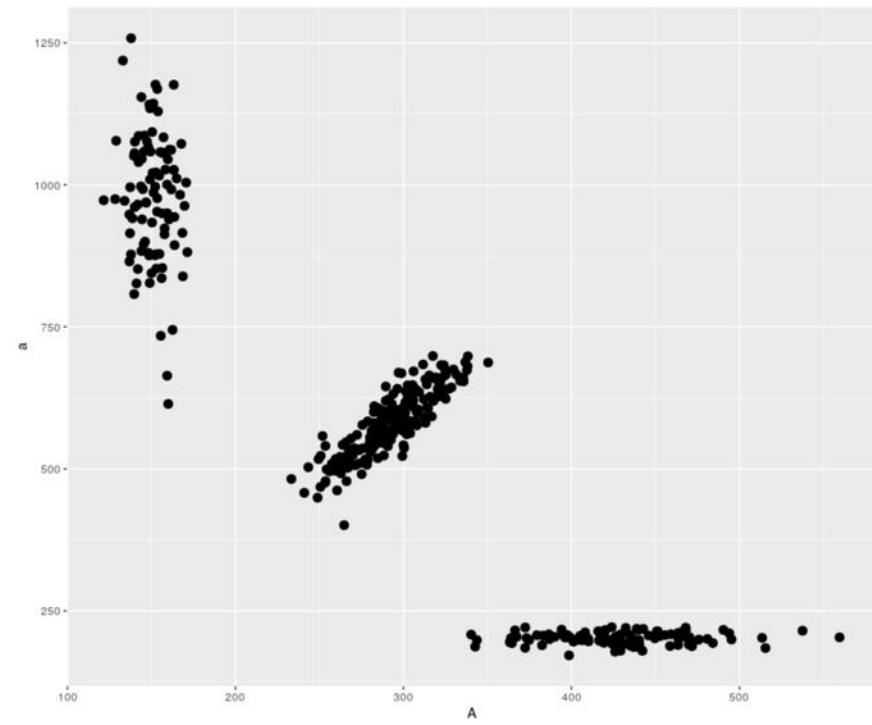
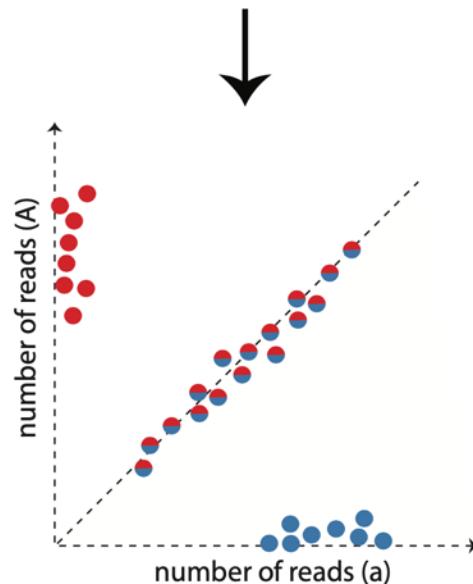
\*random pairing and no double reduction



# Genotype calling in diploids

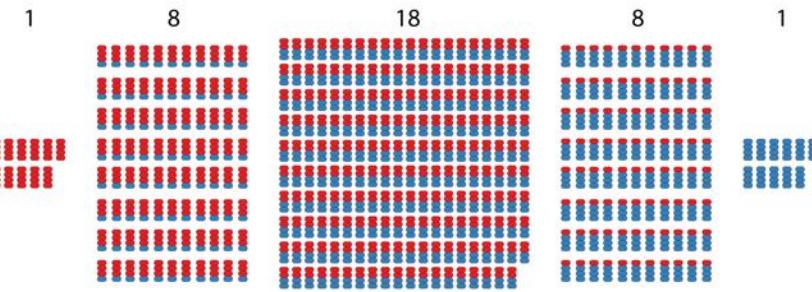
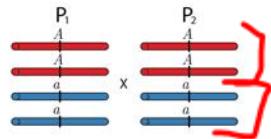


**GBS**  
Read counts for each one of the allelic variants

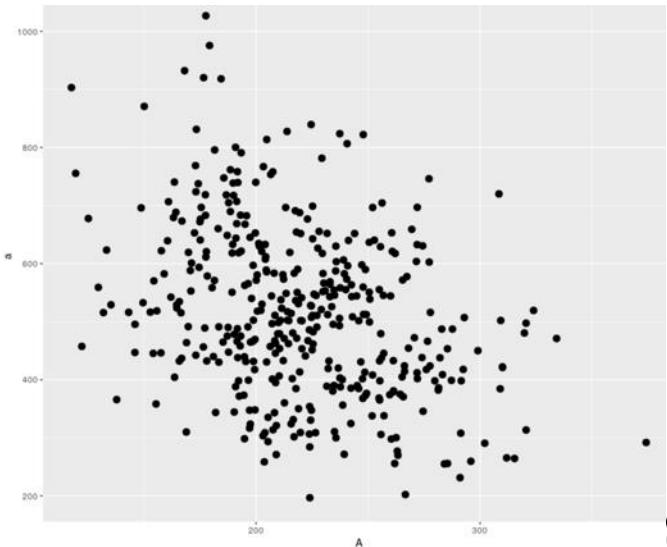
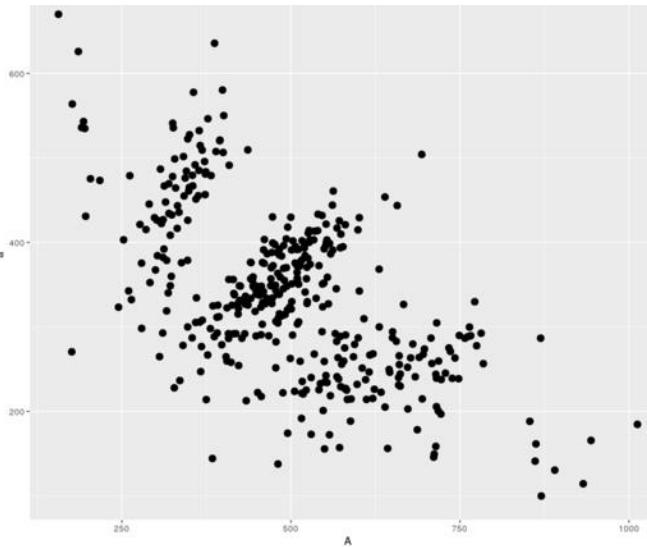
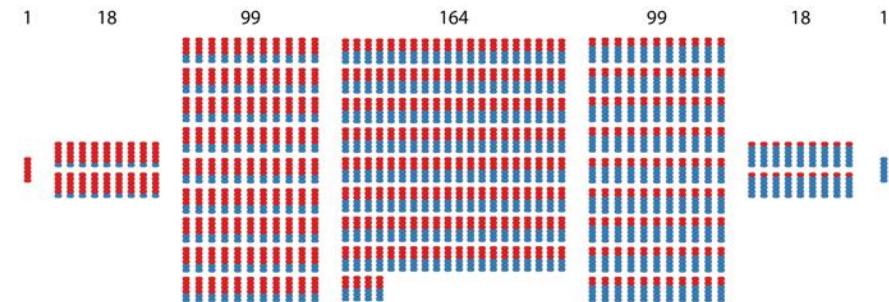
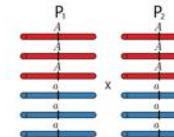


# Genotype calling in polyploids

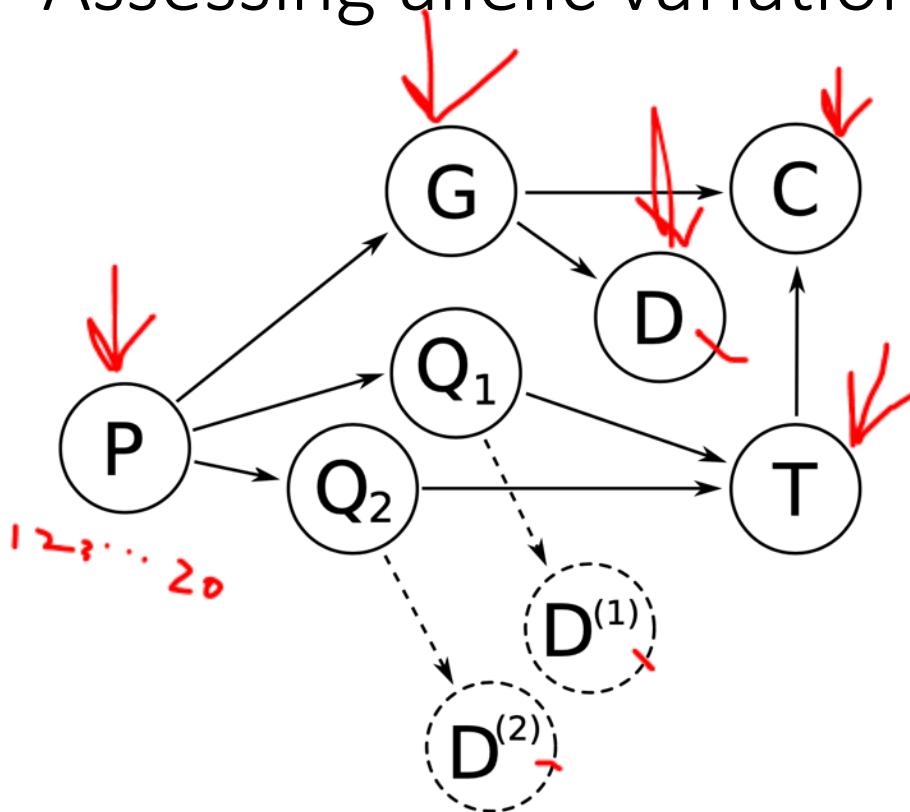
Tetraploid



Hexaploid



# Assessing allelic variation in polyploids



Serang et al. (2012)

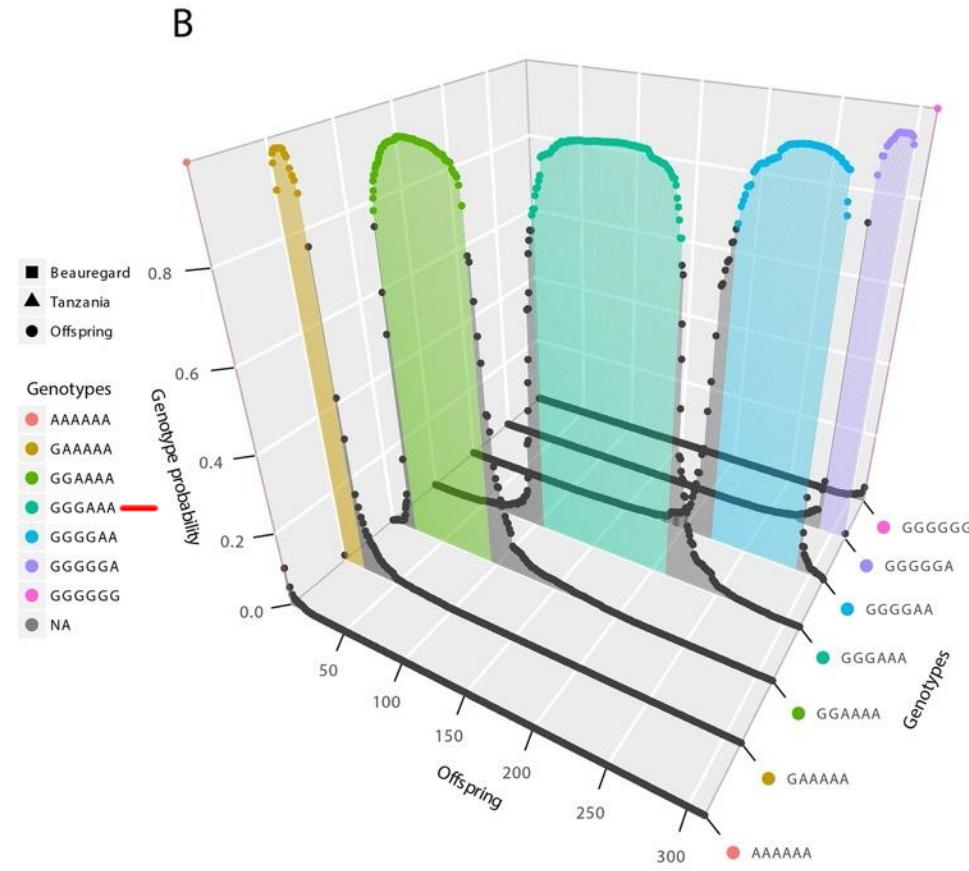
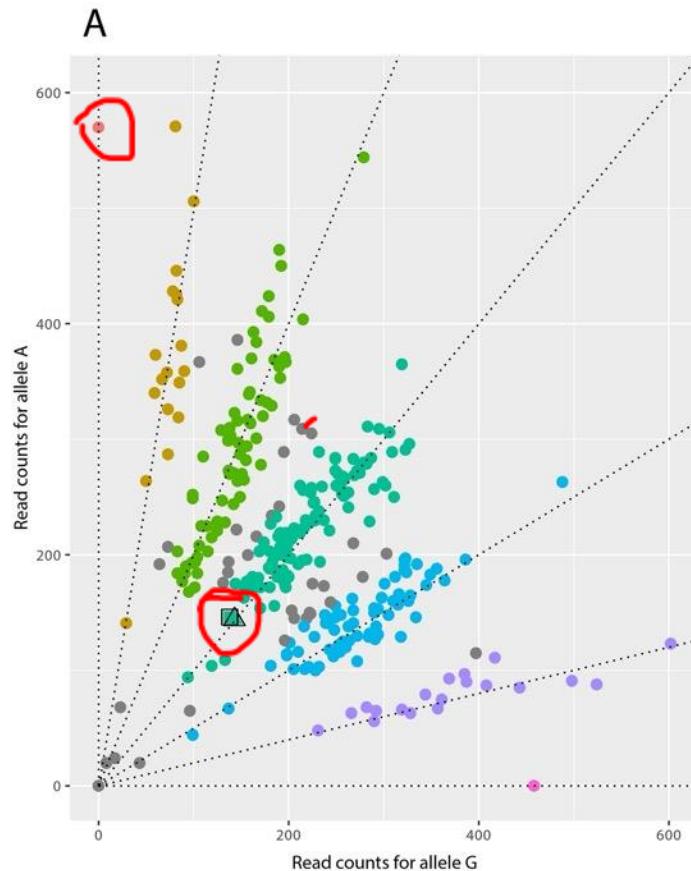
Molinari and Serang (2015)

$$\Pr(P, G, D, T, C, Q_1, Q_2, D_1, D_2)$$

- ▶  $P$ : ploidy
- ▶  $G$ : genotype of all individuals
- ▶  $D$ : observed data
- ▶  $T$ : theoretical distribution of genotypes
- ▶  $C$ : histogram of genotypes
- ▶  $Q_1$  and  $Q_2$ : parent genotypes, with data  $D_1$  and  $D_2$  (if available)

# Genotyping Calling using SuperMASSA

Dosage calling Including the probability distribution of the genotypes



Beauregard: 3 doses

Tanzania: 3 doses

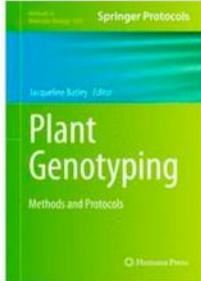
# Genotype calling

OPEN  ACCESS Freely available online PLoS one

## Efficient Exact Maximum a Posteriori Computation for Bayesian SNP Genotyping in Polyploids

Oliver Serang<sup>1,2\*</sup>, Marcelo Mollinari<sup>3</sup>, Antonio Augusto Franco Garcia<sup>3</sup>

**1** Department of Neurobiology, Harvard Medical School, Boston, Massachusetts, United States of America, **2** Department of Pathology, Children's Hospital Boston, Boston, Massachusetts, United States of America, **3** Department of Genetics, University of São Paulo/ESALQ, Piracicaba, São Paulo, Brazil

 [Plant Genotyping pp 215-241](#) | [Cite as](#)

## Quantitative SNP Genotyping of Polyploids with MassARRAY and Other Platforms

Authors

[Authors and affiliations](#)

Marcelo Mollinari, Oliver Serang 

# Genotype calling in polyploids

- fitTetra (tetraploids – array data):

<https://www.wur.nl/en/show/Software-fitTetra.htm>

- ClusterCall (tetraploids):

<https://potatobreeding.cals.wisc.edu/software/>

- SuperMASSA (any ploidy level):

<https://bitbucket.org/orserang/supermassa>

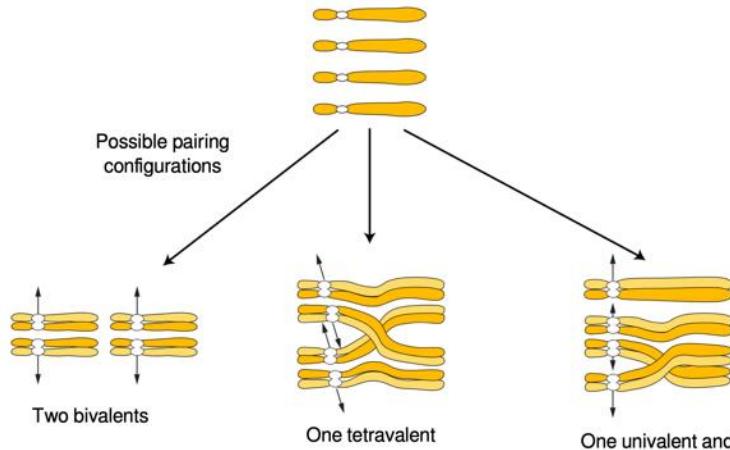
- Updog (any ploidy level, allows preferential pairing):

<https://github.com/dcgerard/updog>

- polyRAD (any ploidy level, reads VCF, BAM, etc):

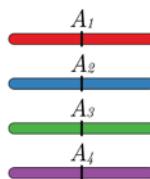
<https://github.com/lvclark/polyRAD>

# Gamete formation in polyploids\*

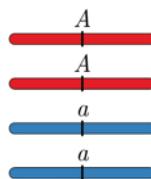


Griffiths et al. (2004)

Multiallelic



Biallelic



Number of possible gamtes considering  
one locus with no double-reduction in  
one and two parents

Ploidy	$\binom{p}{2}$	$\binom{p}{2}^2$
4	6	36
6	20	400
8	70	4900
10	252	63504
12	924	853776
14	3432	11778624
16	12870	165636900

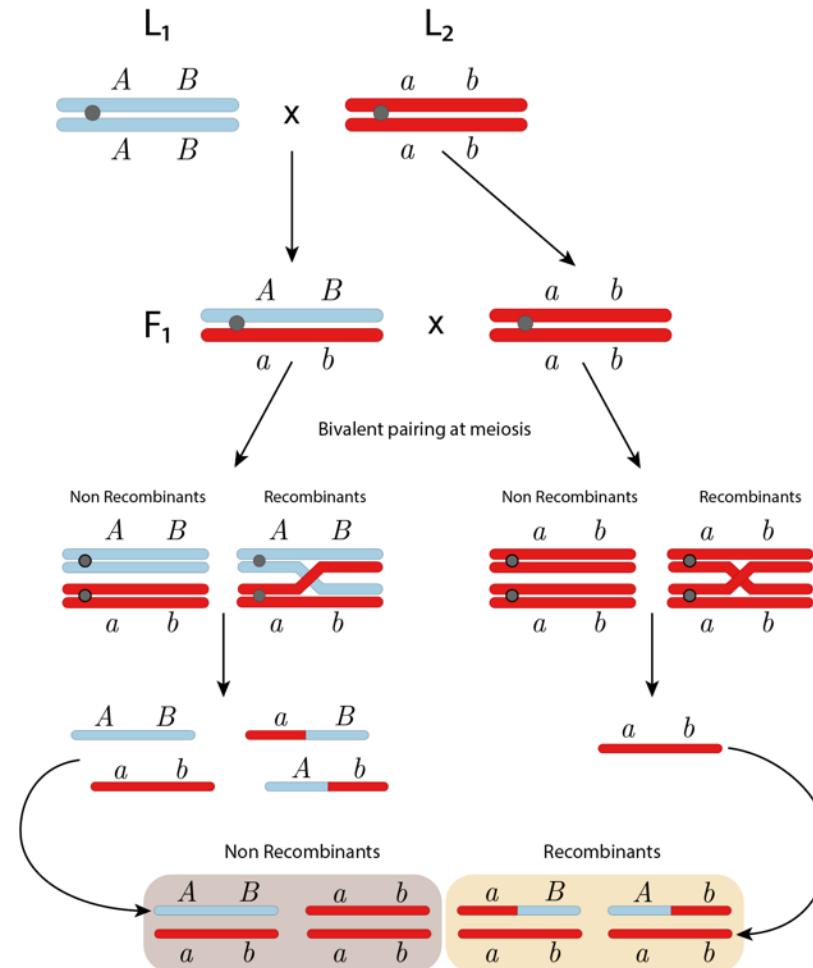
- $A_1A_2$
- $A_1A_3$
- $A_1A_4$
- $A_2A_3$
- $A_2A_4$
- $A_3A_4$

- $A A$

\*random pairing and no double reduction

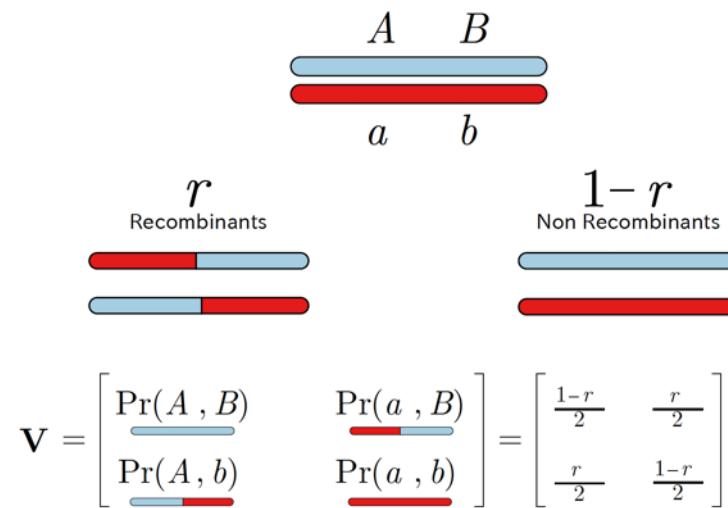


# Recombination fraction in diploids



$$\hat{r} = \frac{\#\text{recombinants}}{\#\text{total}}$$

# Recombination fraction in diploids - Likelihood



$$L(r) = \prod_n \Pr(G_A, G_B \mid r)$$

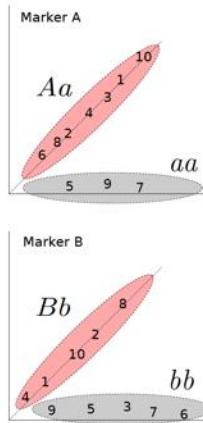
where n is the number of individuals. The maximum likelihood estimator of r is

$$\hat{r} = \operatorname{argmax}_r L(r)$$

# Recombination fraction in diploids

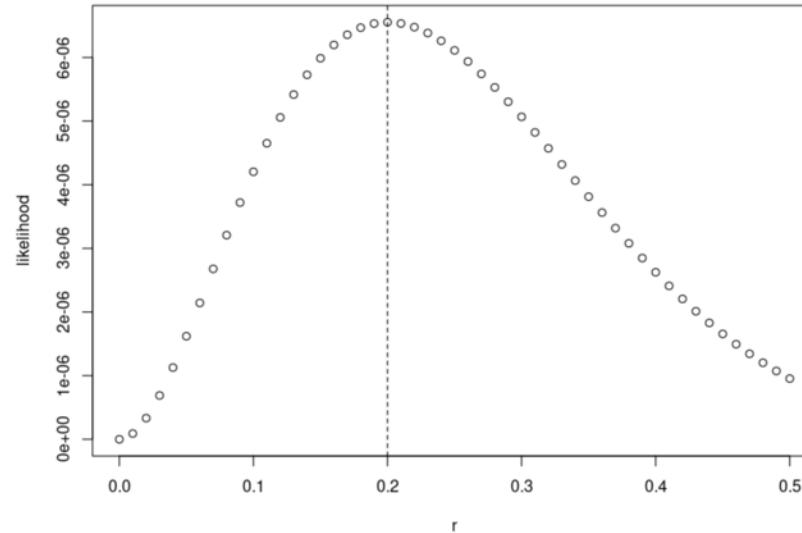


Toy example



Marker A	Individual	Obs. Gen.
	1	(A ,B)
	2	(A ,B)
	3	(A ,b )
	4	(A ,B)
	5	(a ,b )
	6	(A ,b )
	7	(a ,b )
	8	(A ,B)
	9	(a ,b )
	10	(A ,B)

$\hat{r} = 2/10 = 0.2$



$$L = \prod_n \Pr(\text{loc}_B, \text{loc}_A \mid \text{Data})$$

Individual	Obs. Gen.	$\Pr(\text{loc}_B, \text{loc}_A)$
1	(A ,B)	$\frac{1}{2}(1-r)$
2	(A ,B)	$\frac{1}{2}(1-r)$
3	(A ,b )	$\frac{1}{2}(r)$
4	(A ,B)	$\frac{1}{2}(1-r)$
5	(a ,b )	$\frac{1}{2}(1-r)$
6	(A ,b )	$\frac{1}{2}(r)$
7	(a ,b )	$\frac{1}{2}(1-r)$
8	(A ,B)	$\frac{1}{2}(1-r)$
9	(a ,b )	$\frac{1}{2}(1-r)$
10	(A ,B)	$\frac{1}{2}(1-r)$

$$L = \left(\frac{r}{2}\right)^2 \left(\frac{1-r}{2}\right)^8$$

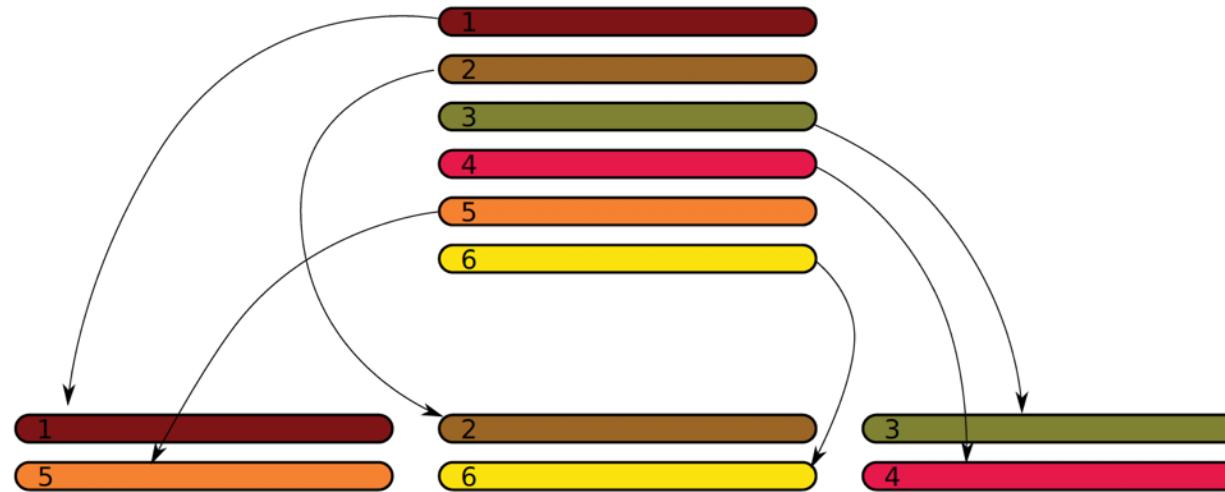
$$L = \prod_n \Pr(G_A, G_B) = \left(\frac{r}{2}\right)^2 \left(\frac{1-r}{2}\right)^8$$

The MLE (maximum likelihood estimate) of  $r$  is  $\hat{r} = 0.2$

Computing recombination frequencies in diploids using R and C++  
[https://github.com/mmollina/Cpp\\_and\\_R](https://github.com/mmollina/Cpp_and_R)



# Gamete formation in polyploids\*



$$\psi_4$$

In this case: 15 possible configurations. For any ploidy level  $p$

$$\frac{1}{\frac{p}{2}!} \prod_{i=1}^{\frac{p}{2}} \binom{2i}{2}$$

\*no double reduction

# Expected gametic frequency given a bivalent configuration

$$\begin{array}{ccccc}
 & A_1 & B_1 & & \\
 \textcolor{darkred}{\rule{1cm}{0.5mm}} & & \textcolor{darkred}{\rule{1cm}{0.5mm}} & & \\
 & A_6 & B_6 & & \\
 & & & A_2 & B_2 \\
 & & & \textcolor{brown}{\rule{1cm}{0.5mm}} & \textcolor{brown}{\rule{1cm}{0.5mm}} \\
 & & & A_5 & B_5 \\
 & & & & \\
 & & & A_3 & B_3 \\
 & & & \textcolor{olive}{\rule{1cm}{0.5mm}} & \textcolor{red}{\rule{1cm}{0.5mm}} \\
 & & & A_4 & B_4
 \end{array}$$

$$\begin{bmatrix} \frac{1-r}{2} & \frac{r}{2} \\ \frac{r}{2} & \frac{1-r}{2} \end{bmatrix} \otimes \begin{bmatrix} \frac{1-r}{2} & \frac{r}{2} \\ \frac{r}{2} & \frac{1-r}{2} \end{bmatrix} \otimes \begin{bmatrix} \frac{1-r}{2} & \frac{r}{2} \\ \frac{r}{2} & \frac{1-r}{2} \end{bmatrix}$$

In general:

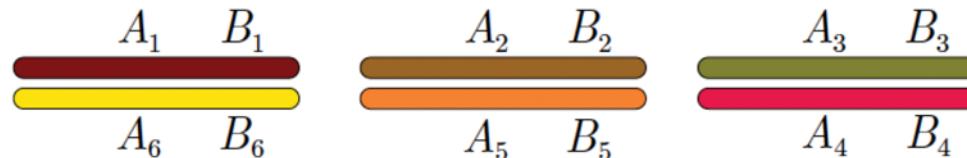
$$\mathbf{V}_1 \otimes \mathbf{V}_2 \otimes \cdots \otimes \mathbf{V}_{\frac{p}{2}}$$

All elements of this product are of the form

$$\Pr(G_A, G_B \mid \psi_j, r) = \frac{(1-r)^{(\frac{p}{2}-l)} p^l}{2^{\frac{p}{2}}}$$

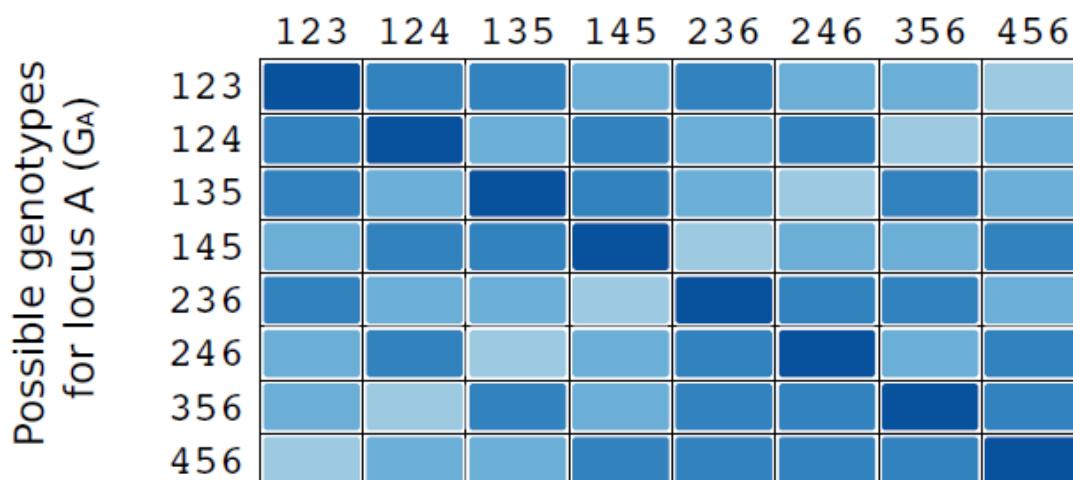
$l$  : known number of recombinant bivalents between loci A and B

# Gametic probability for $\psi_1$



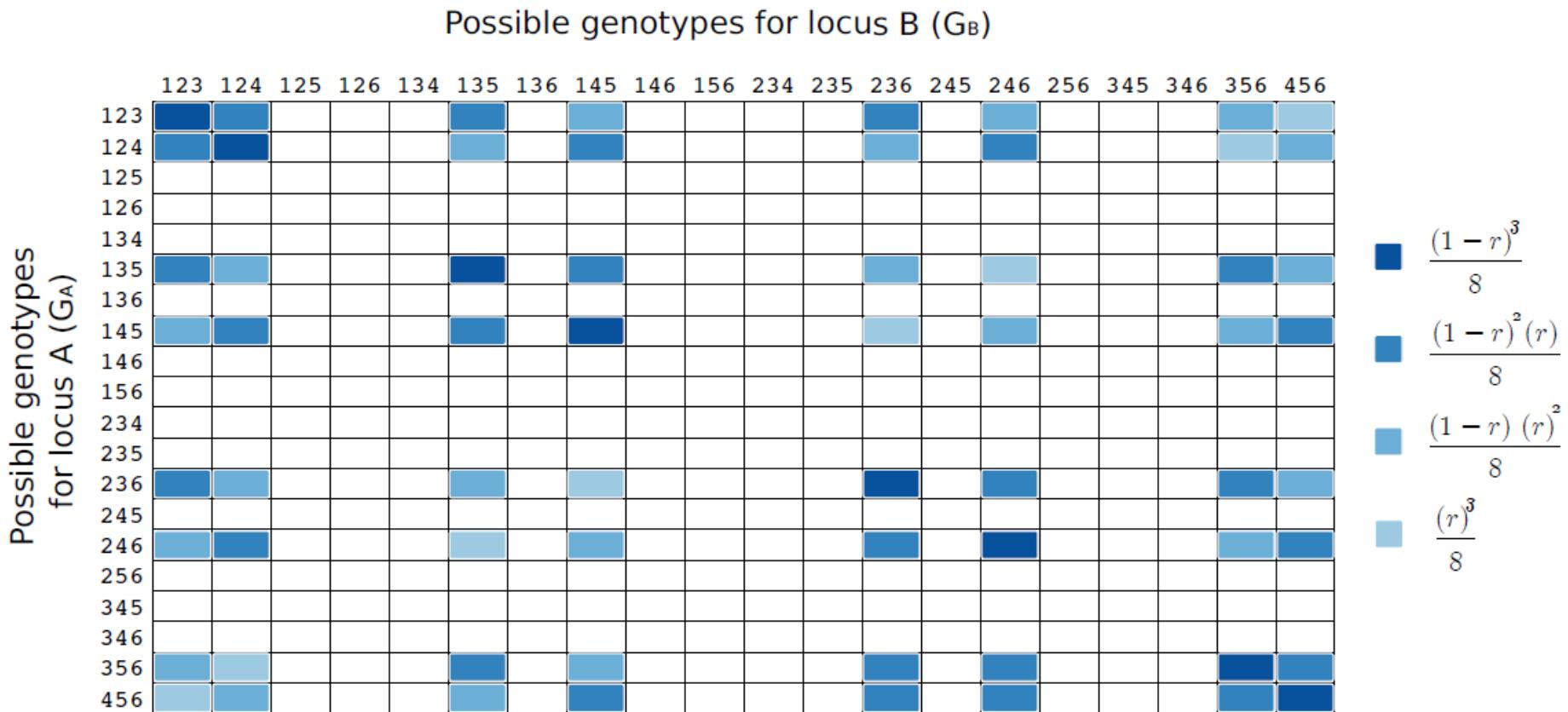
$$\begin{bmatrix} \frac{1-r}{2} & \frac{r}{2} \\ \frac{r}{2} & \frac{1-r}{2} \end{bmatrix} \otimes \begin{bmatrix} \frac{1-r}{2} & \frac{r}{2} \\ \frac{r}{2} & \frac{1-r}{2} \end{bmatrix} \otimes \begin{bmatrix} \frac{1-r}{2} & \frac{r}{2} \\ \frac{r}{2} & \frac{1-r}{2} \end{bmatrix}$$

Possible genotypes for locus B ( $G_B$ )

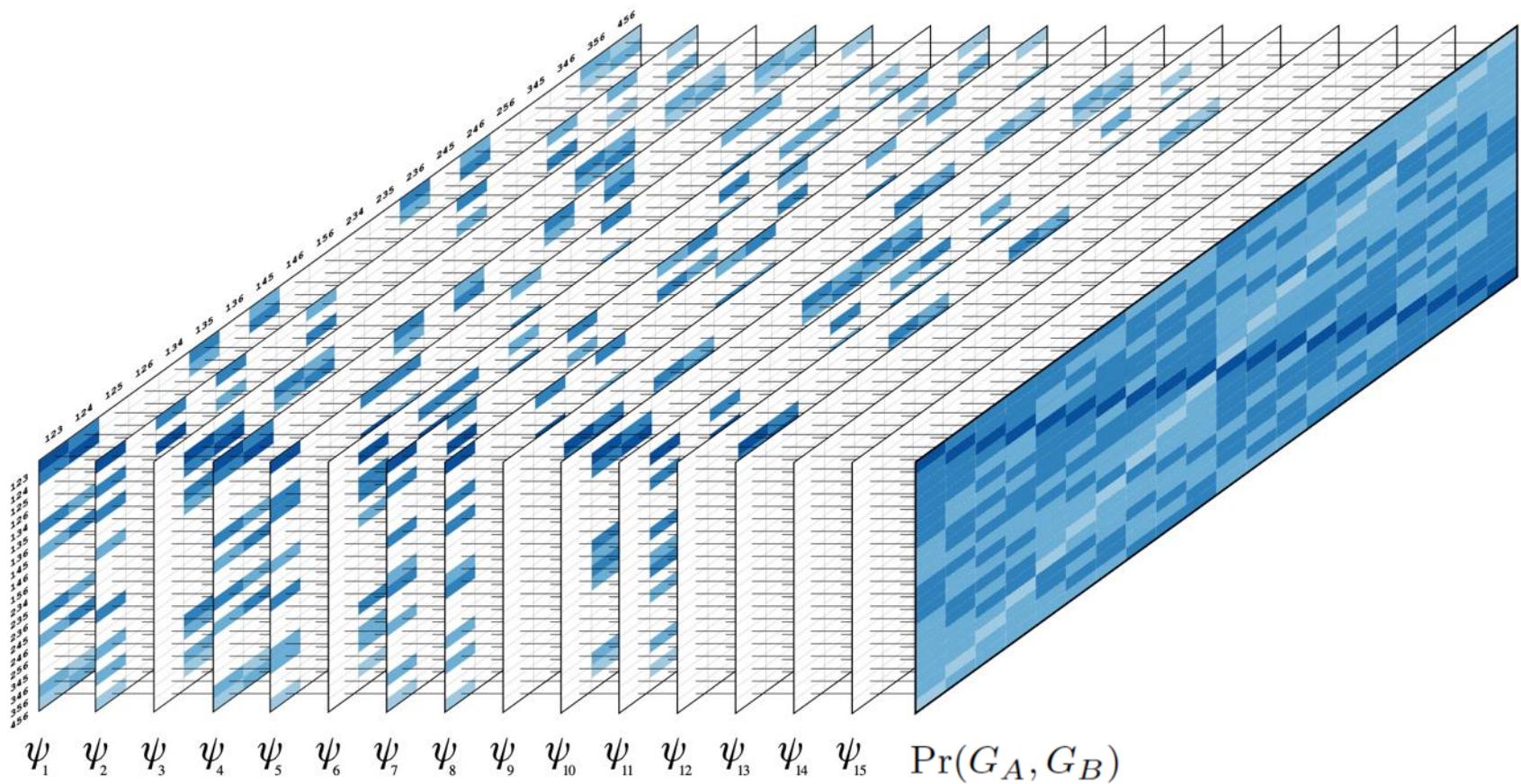


- $\frac{(1-r)^3}{8}$
- $\frac{(1-r)^2(r)}{8}$
- $\frac{(1-r)(r)^2}{8}$
- $\frac{(r)^3}{8}$

# Gametic probability for $\psi_1$



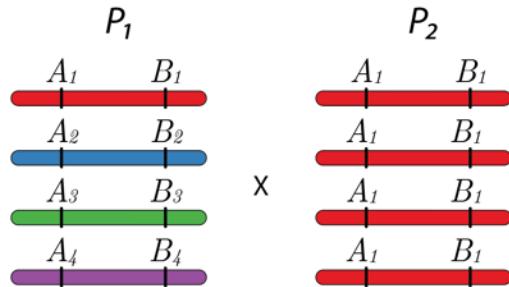
# Unconditional gametic probability



$$\begin{aligned}\Pr(G_A, G_B) &= \sum_j \Pr(G_A, G_B \mid \psi_j) \Pr(\psi_j) \\ &= \frac{l! \left(\frac{m}{2} - l\right)!}{w_m} \frac{(1 - r_k)^{\frac{m}{2} - l} (r_k)^l}{2^{\frac{m}{2}}}\end{aligned}$$

# Recombination Fraction – Autotetraploid

Fully informative marker



$$\Pr(G_A, G_B \mid r)$$

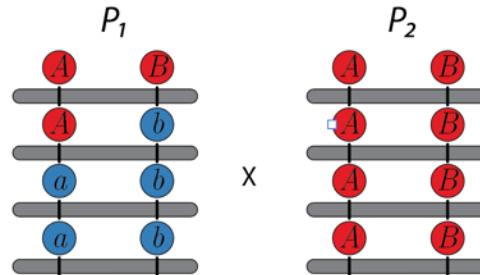
	$B_1B_2$	$B_1B_3$	$B_1B_4$	$B_2B_3$	$B_2B_4$	$B_3B_4$
$A_1A_2$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$
$A_1A_3$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$
$A_1A_4$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$
$A_2A_3$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$
$A_2A_4$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$
$A_3A_4$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$

$$L(r) = \left[ \frac{(1-r)^2}{6} \right]^{n_1} \left[ \frac{(1-r)r}{12} \right]^{n_2} \left[ \frac{r^2}{6} \right]^{n_3}$$

$$\hat{r} = \underset{r}{\operatorname{argmax}} L(r)$$

# Recombination Fraction – autotetraploid

Partially informative marker – Duplex/simplex – Association



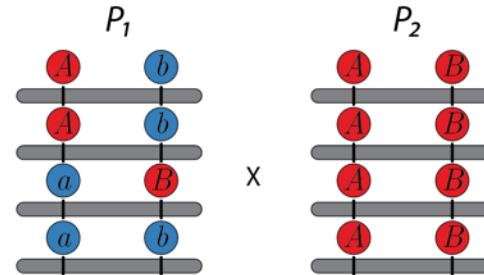
$$\Pr(G_A, G_B \mid r)$$

	$Bb$	$Bb$	$Bb$	$bb$	$bb$	$bb$		$Bb$	$bb$
$AA$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$AA$	$\frac{(1-r)}{6}$	$\frac{r}{6}$
$Aa$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$Aa$	$\frac{1}{3}$	$\frac{1}{3}$
$Aa$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$a a$	$\frac{r}{6}$	$\frac{(1-r)}{6}$
$Aa$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$			
$aa$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$			

$$L_1(r) = \left[ \frac{(1-r)}{6} \right]^{n_1} \left[ \frac{1}{3} \right]^{n_2} \left[ \frac{r}{6} \right]^{n_3}$$

# Recombination Fraction – autotetraploid

Partially informative marker – Duplex/simplex – **Repulsion**



$$\Pr(G_A, G_B \mid r)$$

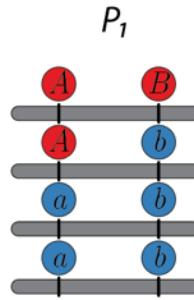
	$bb$	$Bb$	$bb$	$Bb$	$bb$	$Bb$
$AA$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$
$Aa$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$
$Aa$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$
$Aa$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$
$Aa$	$\frac{(1-r)r}{12}$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$	$\frac{(1-r)r}{12}$
$aa$	$\frac{r^2}{6}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)r}{12}$	$\frac{(1-r)^2}{6}$



	$Bb$	$bb$
$AA$	$\frac{r}{6}$	$\frac{(1-r)}{6}$
$Aa$	$\frac{1}{3}$	$\frac{1}{3}$
$a a$	$\frac{(1-r)}{6}$	$\frac{r}{6}$

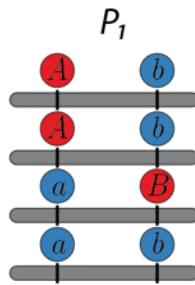
$$L_2(r) = \left[ \frac{r}{6} \right]^{n_1} \left[ \frac{1}{3} \right]^{n_2} \left[ \frac{(1-r)}{6} \right]^{n_3}$$

# Recombination Fraction – assessing linkage phases



$$\hat{r}_1 = \operatorname{argmax}_r L_1(r) \implies L_1(\hat{r}_1)$$

Compare likelihoods  
choosing the **most likely**  
configuration

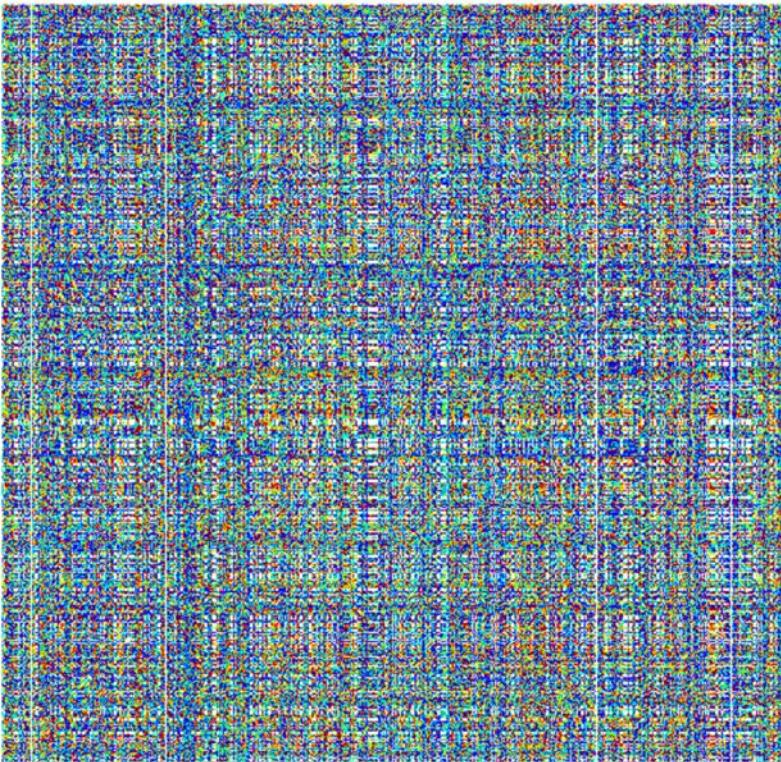


$$\hat{r}_2 = \operatorname{argmax}_r L_2(r) \implies L_2(\hat{r}_2)$$

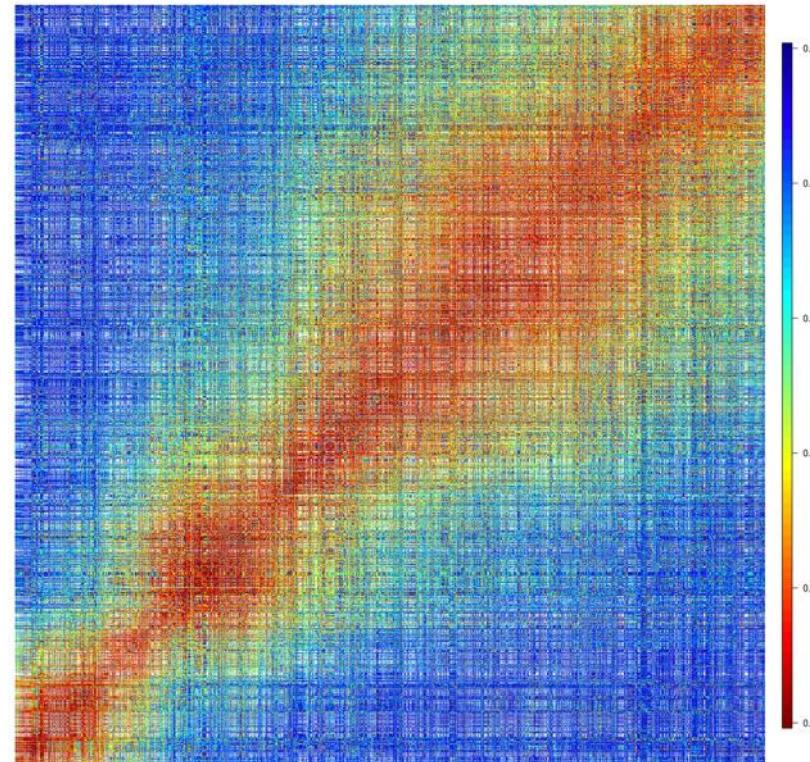
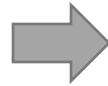
- Pairwise MLE of r are used to group markers into linkage groups and order markers within each linkage group using optimization algorithms such as MDS
- Given a sequence of ordered markers, it is possible to extend the idea of comparing likelihoods of competing linkage phases throughout multiple markers

# Multidimensional Scaling Algorithm (MDS)

- Reduce data from many dimensions preserving the observed distances between points by minimizing a loss function  $L$ .

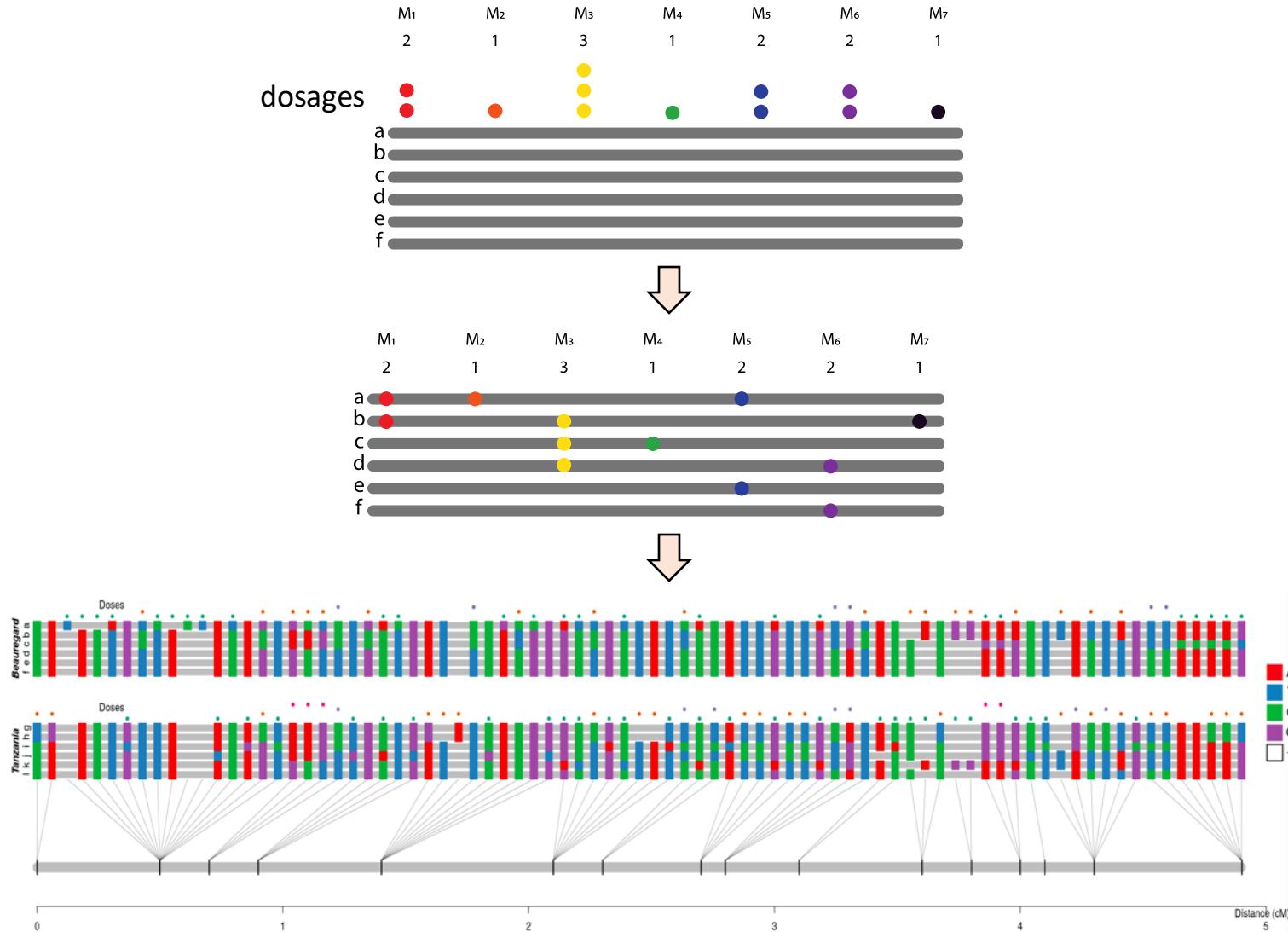


Sweetpotato linkage group 1: 2745 markers



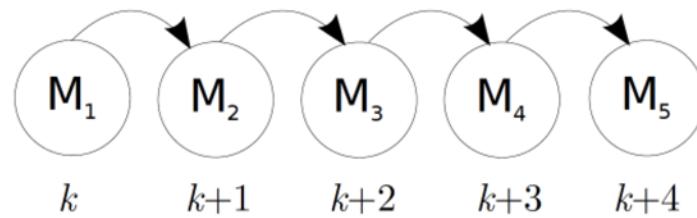
# Haplotyping in polyploids

- Disposition of allelic variants in the homologs in a homology group



# Multilocus linkage analysis in polyploids

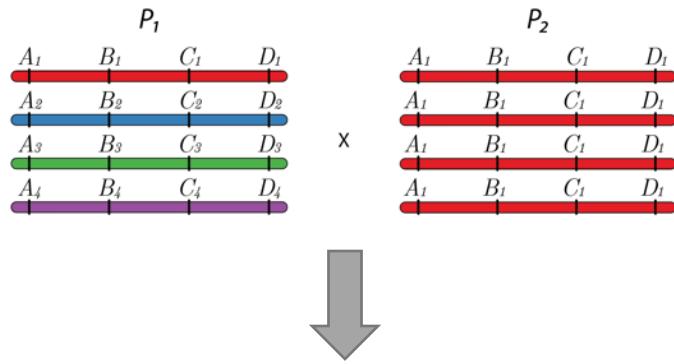
Markov Model: conditional independence



$$\Pr(G_{k+1}|G_k) = \frac{(1 - r_k)^{\frac{p}{2} - l}(r_k)^l}{\binom{\frac{p}{2}}{l}}$$

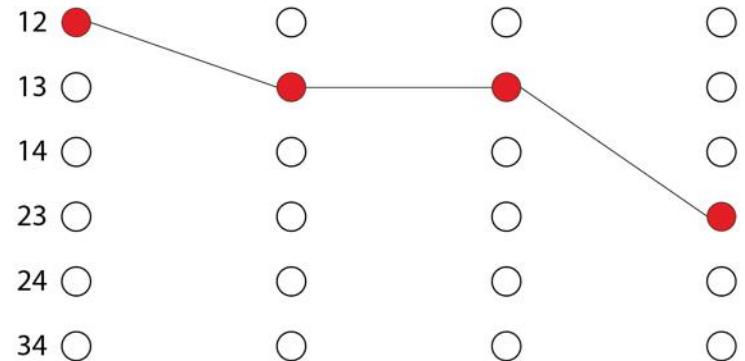
where  $r_k$  is the recombination frequency between loci  $k$  and  $k+1$ ,  $p$  is the ploidy level and  $l$  is the number of recombinant events between  $k$  and  $k+1$ .

# Markov model



	M <sub>1</sub>	M <sub>2</sub>	M <sub>3</sub>	M <sub>4</sub>
Ind <sub>1</sub>	{A <sub>1</sub> , A <sub>2</sub> }	{B <sub>1</sub> , B <sub>3</sub> }	{C <sub>3</sub> , C <sub>4</sub> }	{D <sub>3</sub> , D <sub>4</sub> }
Ind <sub>2</sub>	{A <sub>1</sub> , A <sub>2</sub> }	{B <sub>1</sub> , B <sub>3</sub> }	{C <sub>1</sub> , C <sub>3</sub> }	{D <sub>3</sub> , D <sub>4</sub> }
Ind <sub>3</sub>	{A <sub>1</sub> , A <sub>2</sub> }	{B <sub>1</sub> , B <sub>3</sub> }	{C <sub>1</sub> , C <sub>3</sub> }	{D <sub>2</sub> , D <sub>3</sub> }
:	:			
Ind <sub>n</sub>	{A <sub>2</sub> , A <sub>3</sub> }	{B <sub>2</sub> , B <sub>3</sub> }	{C <sub>2</sub> , C <sub>3</sub> }	{D <sub>2</sub> , D <sub>3</sub> }

Individual 3 → {A<sub>1</sub>, A<sub>2</sub>}   {B<sub>1</sub>, B<sub>3</sub>}   {C<sub>1</sub>, C<sub>3</sub>}   {D<sub>2</sub>, D<sub>3</sub>}

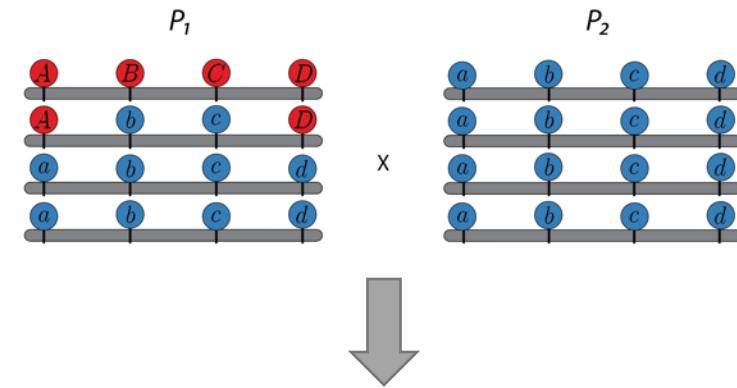


$$L(\mathbf{r}) = \prod_n \Pr(G_A, G_B, G_C, G_D \mid \mathbf{r})$$

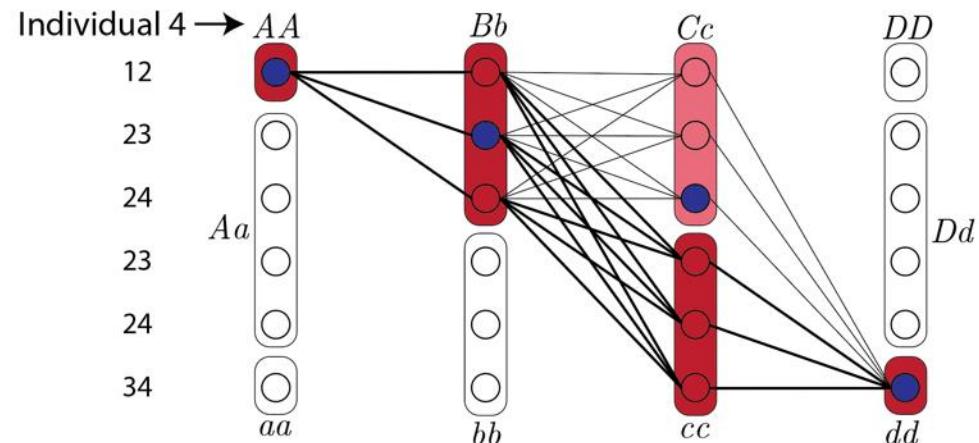
$$\hat{\mathbf{r}} = \underset{\mathbf{r}}{\operatorname{argmax}} L(\mathbf{r})$$

# Hidden Markov Model - HMM

$$b_j(O) = \Pr\left(O \mid \mathcal{G}_{k,j}^m, \varphi_P^k, \varphi_Q^k\right) = \begin{cases} 1 - \epsilon & \text{if } O = \delta(k, j) \\ \frac{\epsilon}{m} & \text{otherwise} \end{cases}$$



	M <sub>1</sub>	M <sub>2</sub>	M <sub>3</sub>	M <sub>4</sub>
Ind <sub>1</sub>	AA	Bb	cc	dd
Ind <sub>2</sub>	AA	Bb	Cc	dd
Ind <sub>3</sub>	AA	Bb	Cc	Dd
Ind <sub>4</sub>	AA	Bb	Cc/cc 0.2 0.8	Dd
⋮	⋮	⋮	⋮	⋮
Ind <sub>n</sub>	Aa	Bb	Cc	Dd

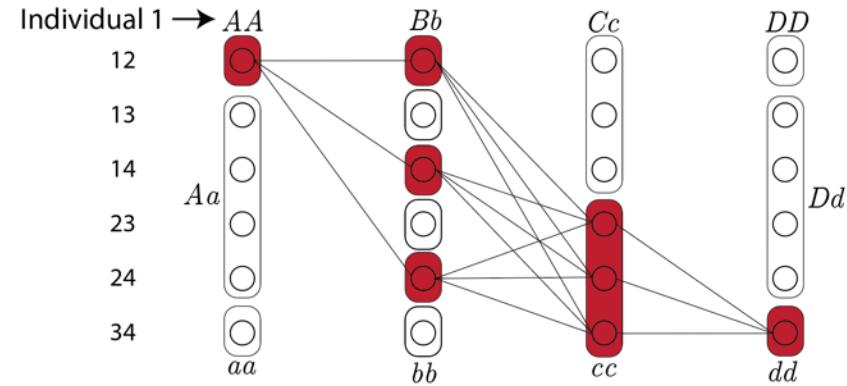
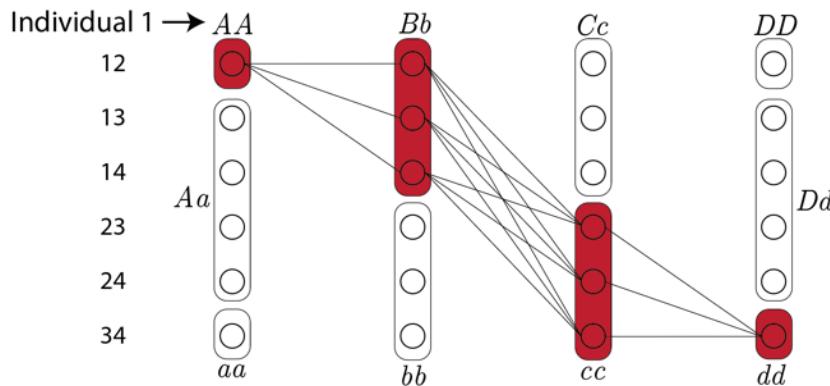
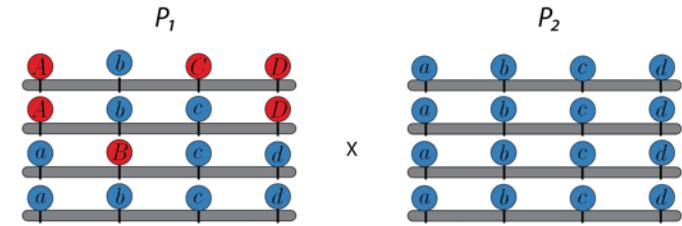
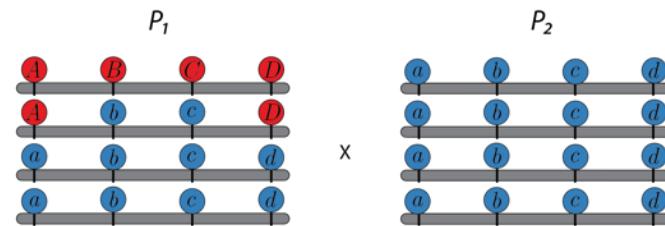


$$L(\mathbf{r}) = \prod_n \Pr(G_A, G_B, G_C, G_D \mid \mathbf{r})$$

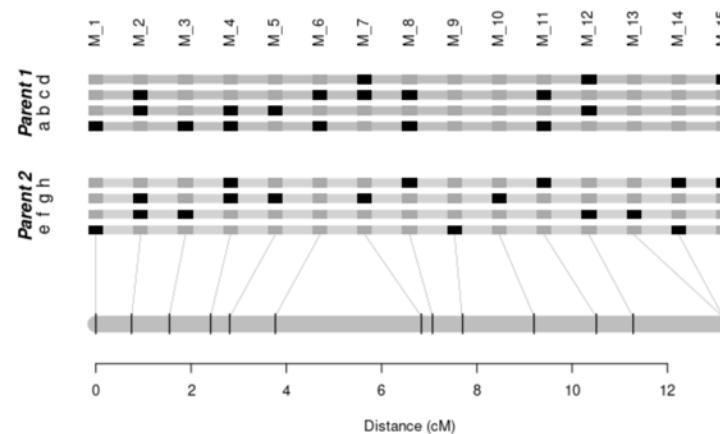
$$\hat{\mathbf{r}} = \operatorname{argmax}_{\mathbf{r}} L(\mathbf{r})$$

# Hidden Markov Model - HMM

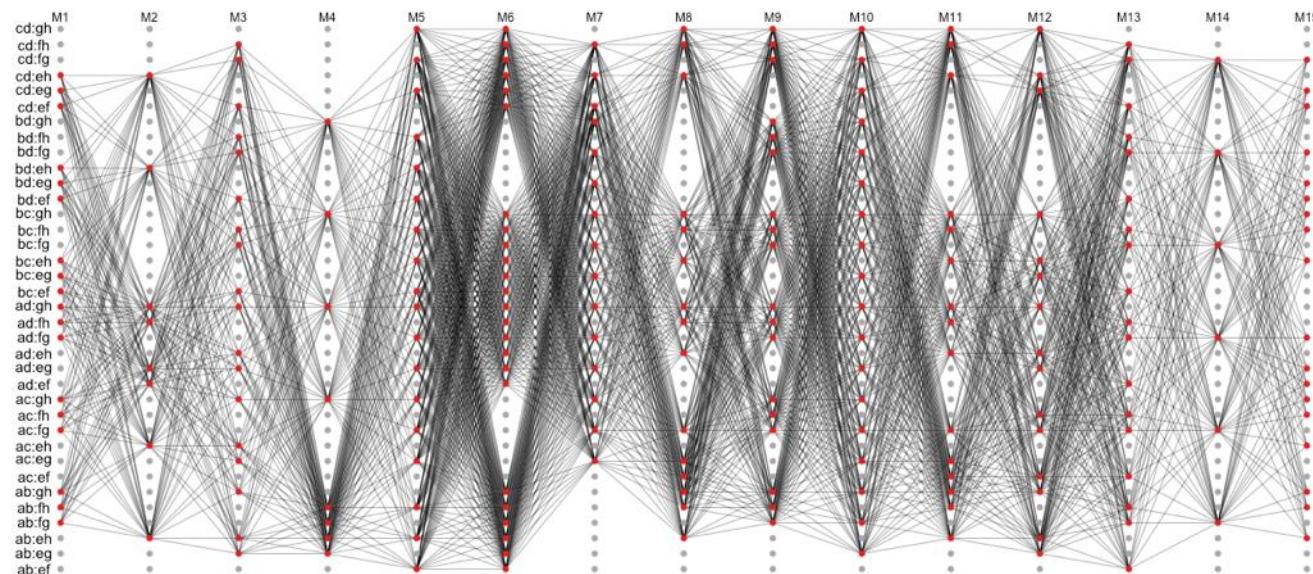
Assessing *different linkage phases* using multilocus analysis



# Hidden Markov Model - HMM

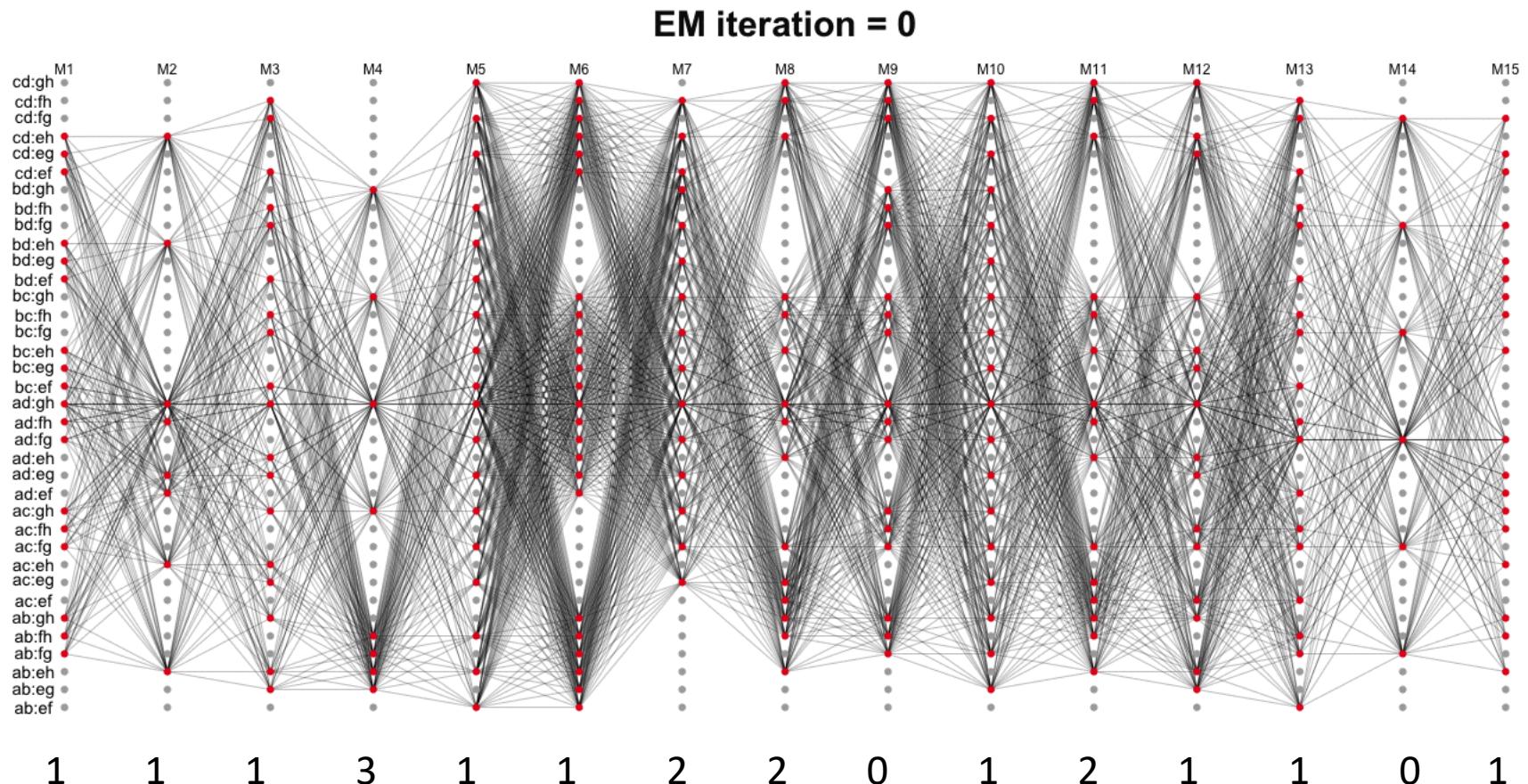


Individual 64: 1 1 1 3 1 1 2 2 0 1 2 1 1 0 1



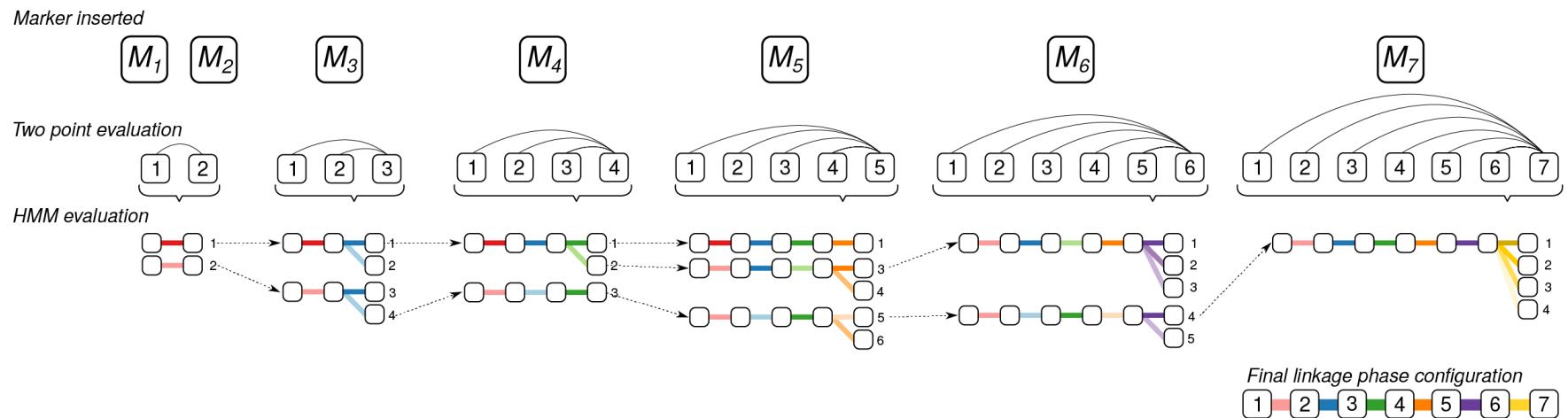
# Hidden Markov Model - HMM

- Tetraploid example, one individual, 15 markers



# Haplotype phasing – MAPpoly strategy

- Step 1: Use of two-point information to reduce the search space
- Step 2: Evaluate the remaining configurations, using HMM likelihood



# Biparental Population - BT

- Beauregard x Tanzania
- 315 individuals
- GBS – GBSpoly protocol (Bode Olukolu – U Tennessee)
- Two reference genomes *I. trifida* and *I. triloba* (Zhangjun Fei's group – BTI Cornell)



Beauregard



Tanzania



# Biparental Population - BT



Beauregard

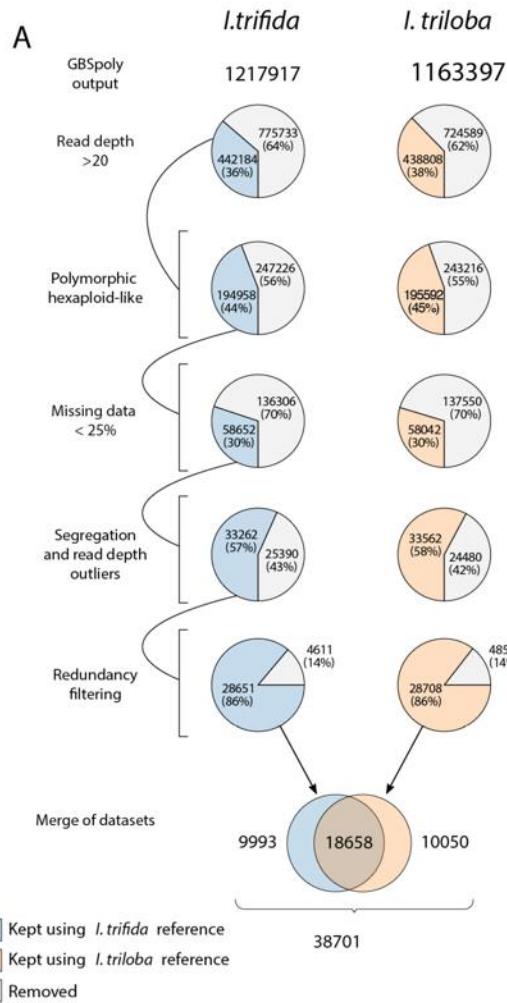


Tanzania

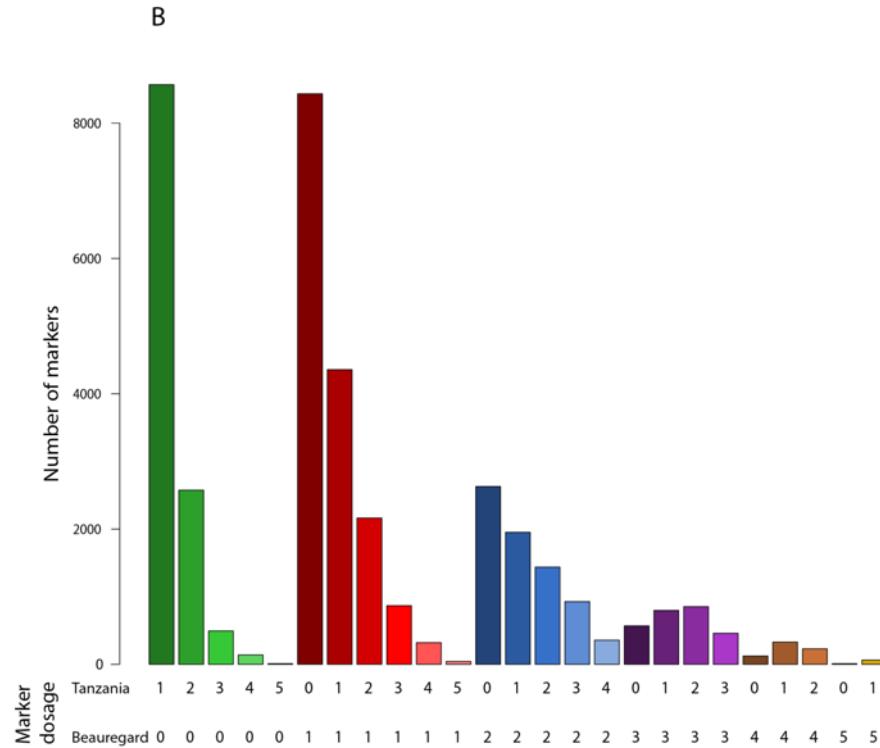


# Results - Genotyping Calling - BT population

## Filtering process

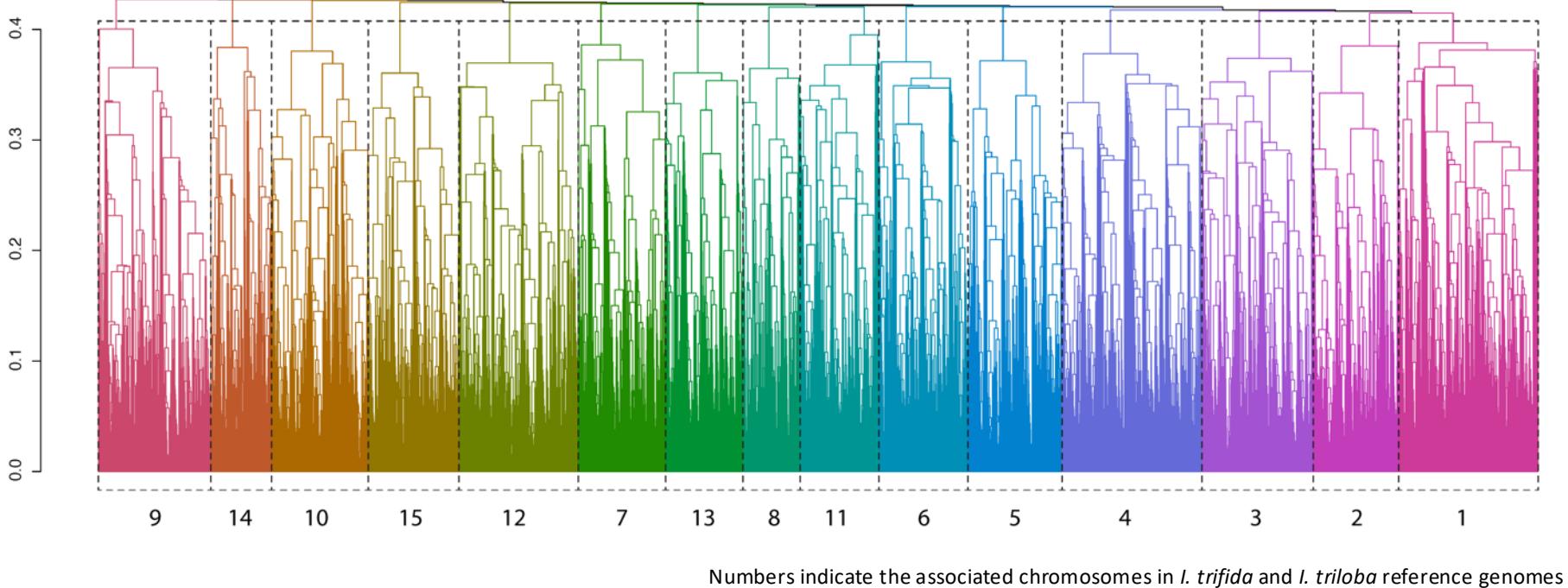


**Distribution of the marker doses in *Beauregard* and *Tanzania* (38,701 SNPs).**



# Two – point analysis and grouping

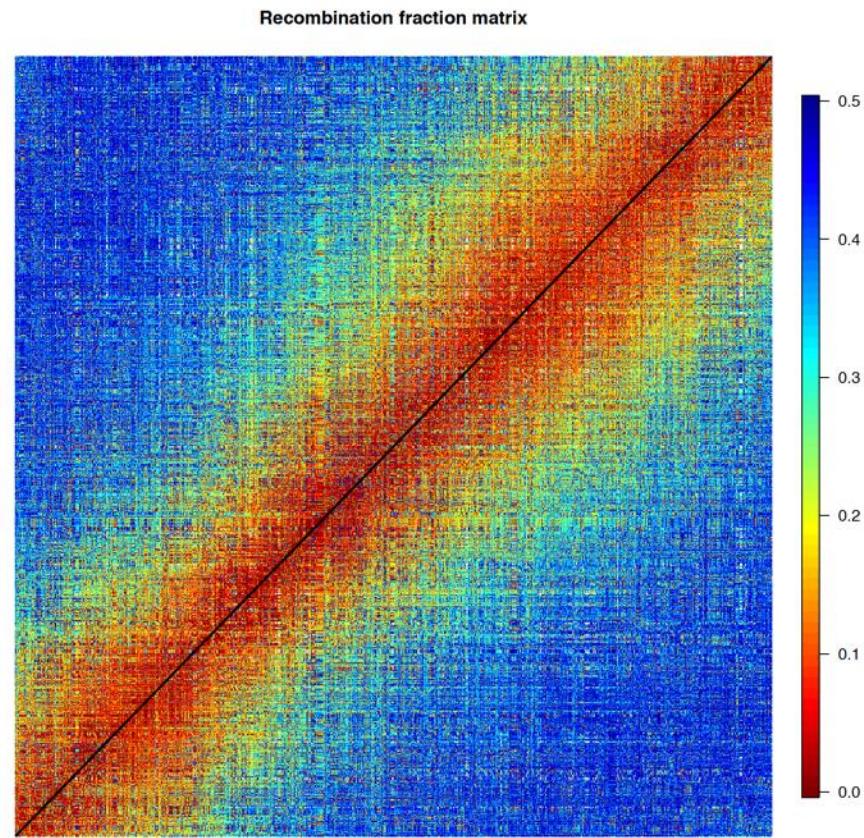
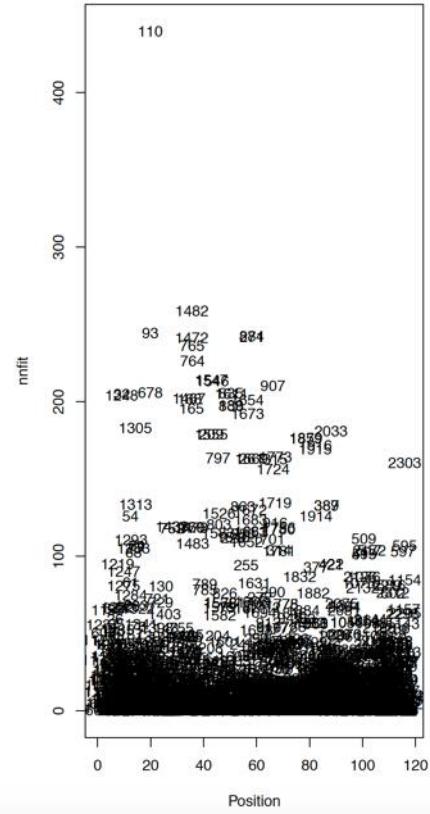
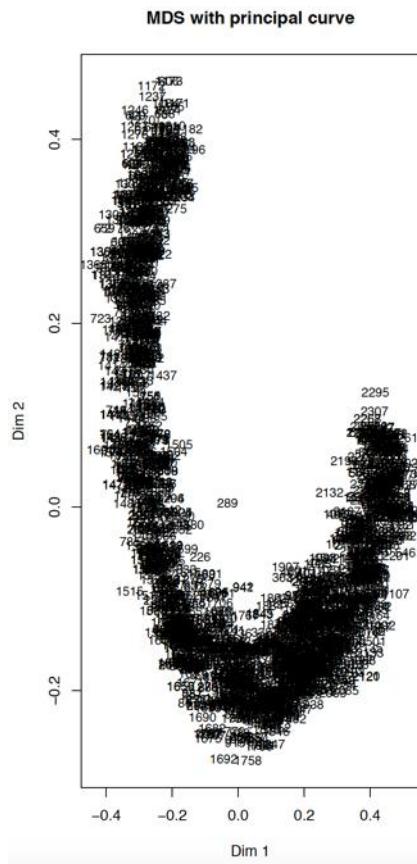
- Number of markers: 38,701
- Number of recombination fractions: ~749 million pairs



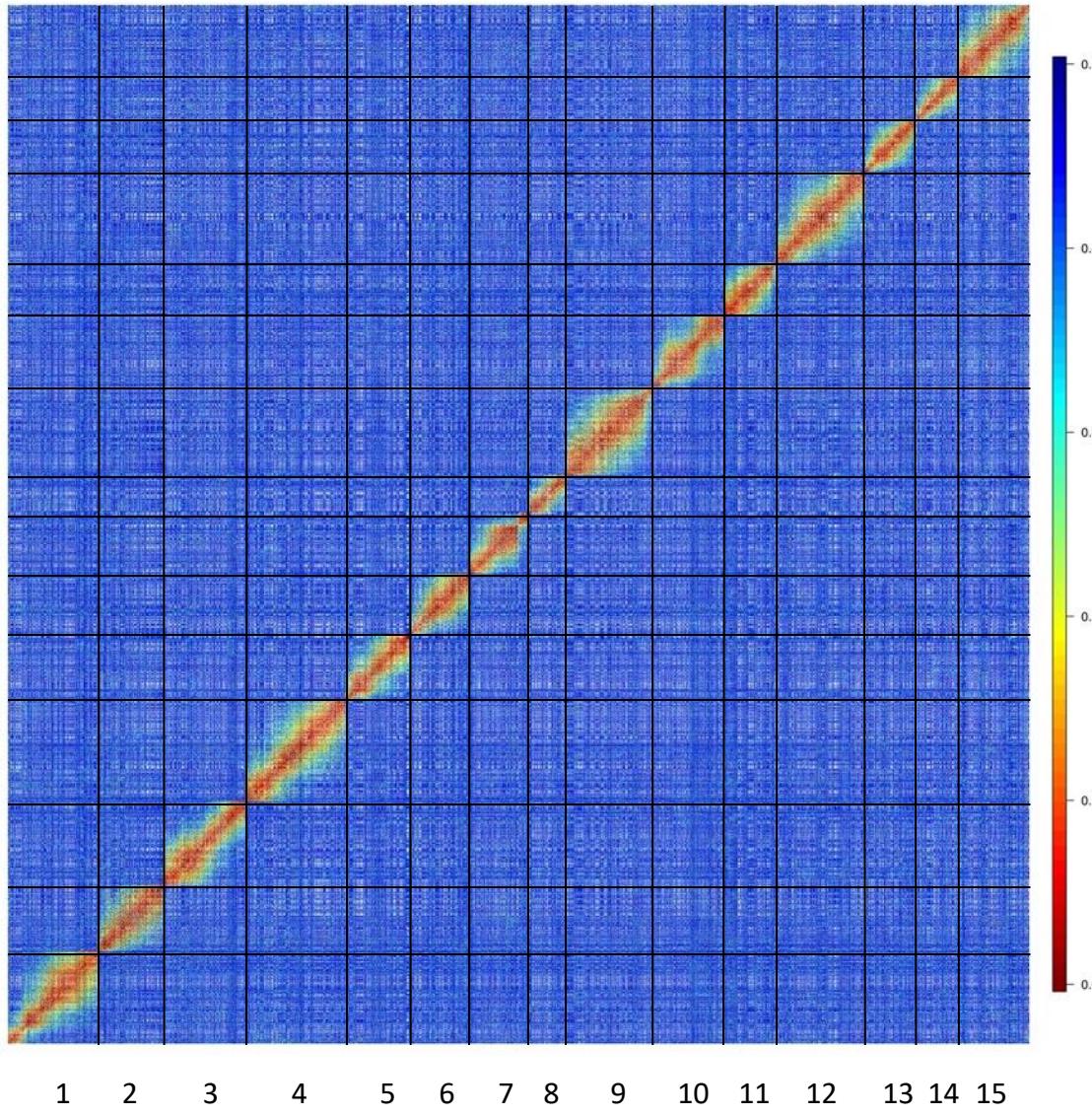
# Ordering - Multidimensional Scaling Algorithm (MDS)

- Projects the information contained in the recombination fraction matrix in two (or more) dimensions. It provides a visual representation of the pattern of proximities among markers (Preedy and Hackett, 2016).

Linkage group 1: 2745 markers



# Ordering with MDS – 15 linkage groups



# Linkage and Haplotyping in polyploids

## Linkage Analysis and Haplotype Phasing in Experimental Autopolyploid Populations with High Ploidy Level Using Hidden Markov Models

2019

Marcelo Mollinari\* and Antonio Augusto Franco Garcia<sup>†,1</sup>

\*Department of Horticultural Science, Bioinformatics Research Center, North Carolina State University, Raleigh, North Carolina, and <sup>†</sup>Department of Genetics, University of São Paulo/ESALQ, Piracicaba, São Paulo, Brazil

[doi:10.1534/g3.119.400378](https://doi.org/10.1534/g3.119.400378)

## Unraveling the Hexaploid Sweetpotato Inheritance Using Ultra-Dense Multilocus Mapping

2020

Marcelo Mollinari,<sup>\*†,1</sup> Bode A. Olukolu,<sup>‡</sup> Guilherme da S. Pereira,<sup>\*,†</sup> Awais Khan,<sup>§</sup> Dorcus Gemenet,<sup>\*\*</sup>

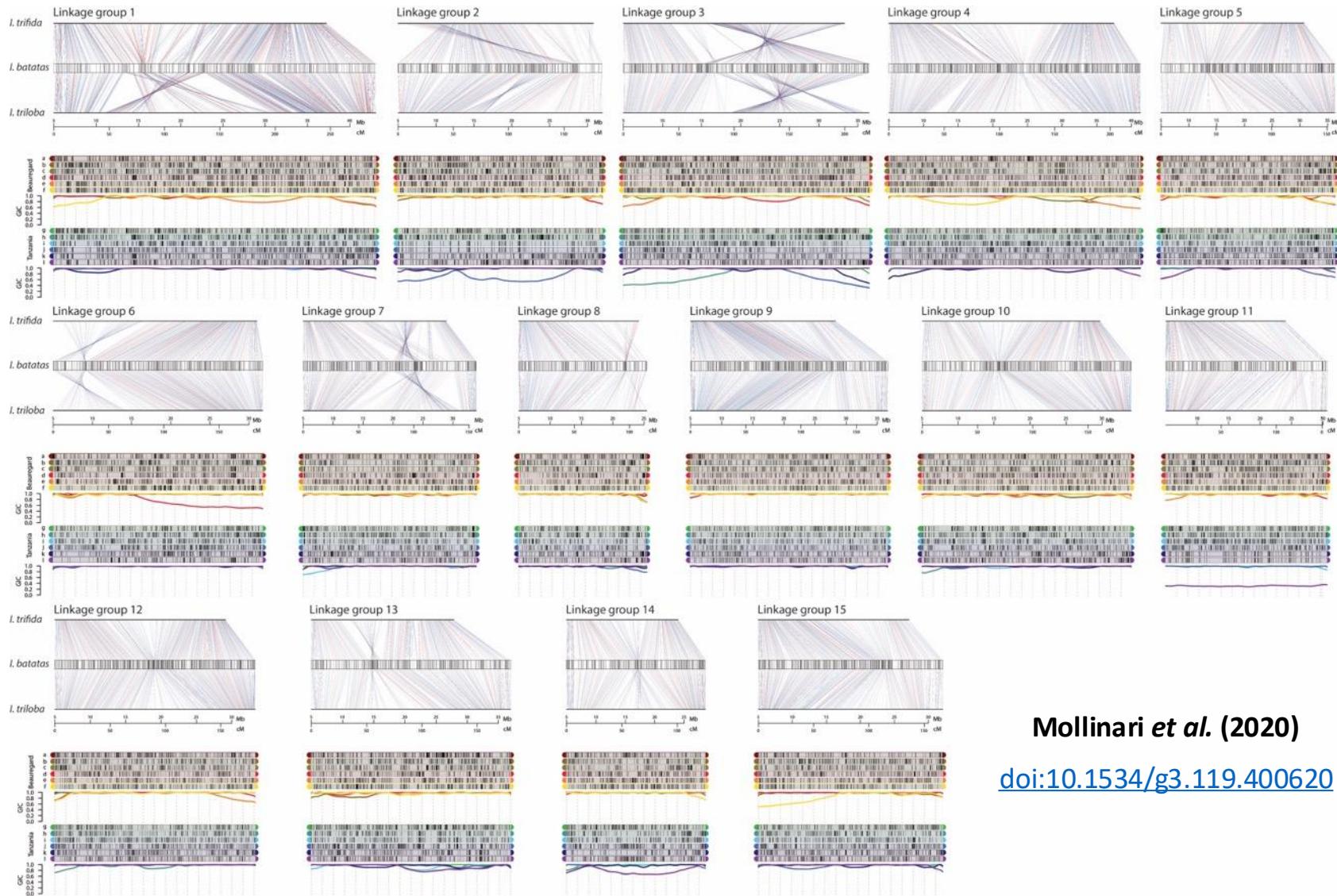
G. Craig Yencho,<sup>†</sup> and Zhao-Bang Zeng<sup>\*,†</sup>

\*Bioinformatics Research Center, North Carolina State University, Raleigh, North Carolina, <sup>†</sup>Department of Horticultural Science, North Carolina State University, Raleigh, North Carolina, <sup>‡</sup>Department of Entomology and Plant Pathology, University of Tennessee, Knoxville, Tennessee, <sup>§</sup>Plant Pathology and Plant-Microbe Biology Section, Cornell University, Geneva, New York, and <sup>\*\*</sup>International Potato Center, ILRI Campus, Nairobi, Kenya

[doi:10.1534/g3.119.400620](https://doi.org/10.1534/g3.119.400620)



# Sweetpotato genetic map

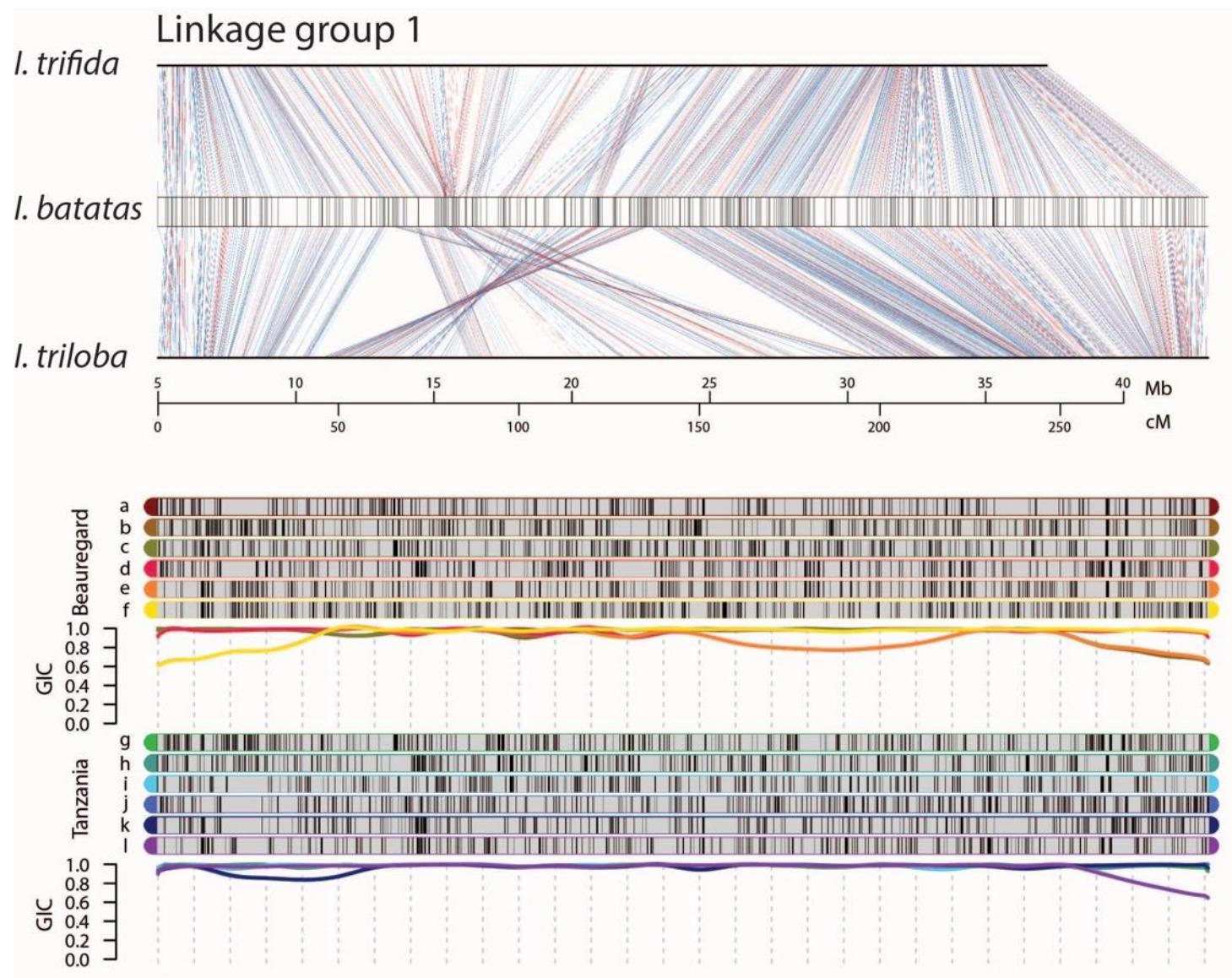


Molinari *et al.* (2020)

[doi:10.1534/g3.119.400620](https://doi.org/10.1534/g3.119.400620)



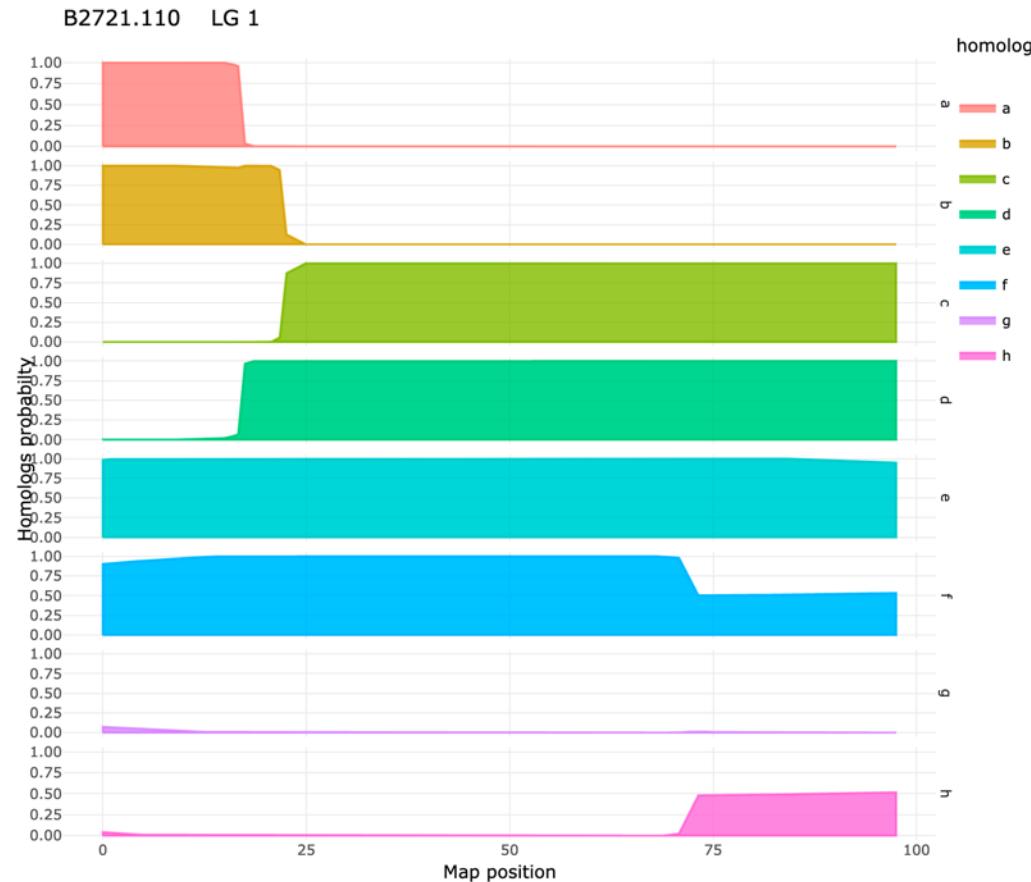
# Sweetpotato genetic map



# Probabilistic haplotype reconstruction

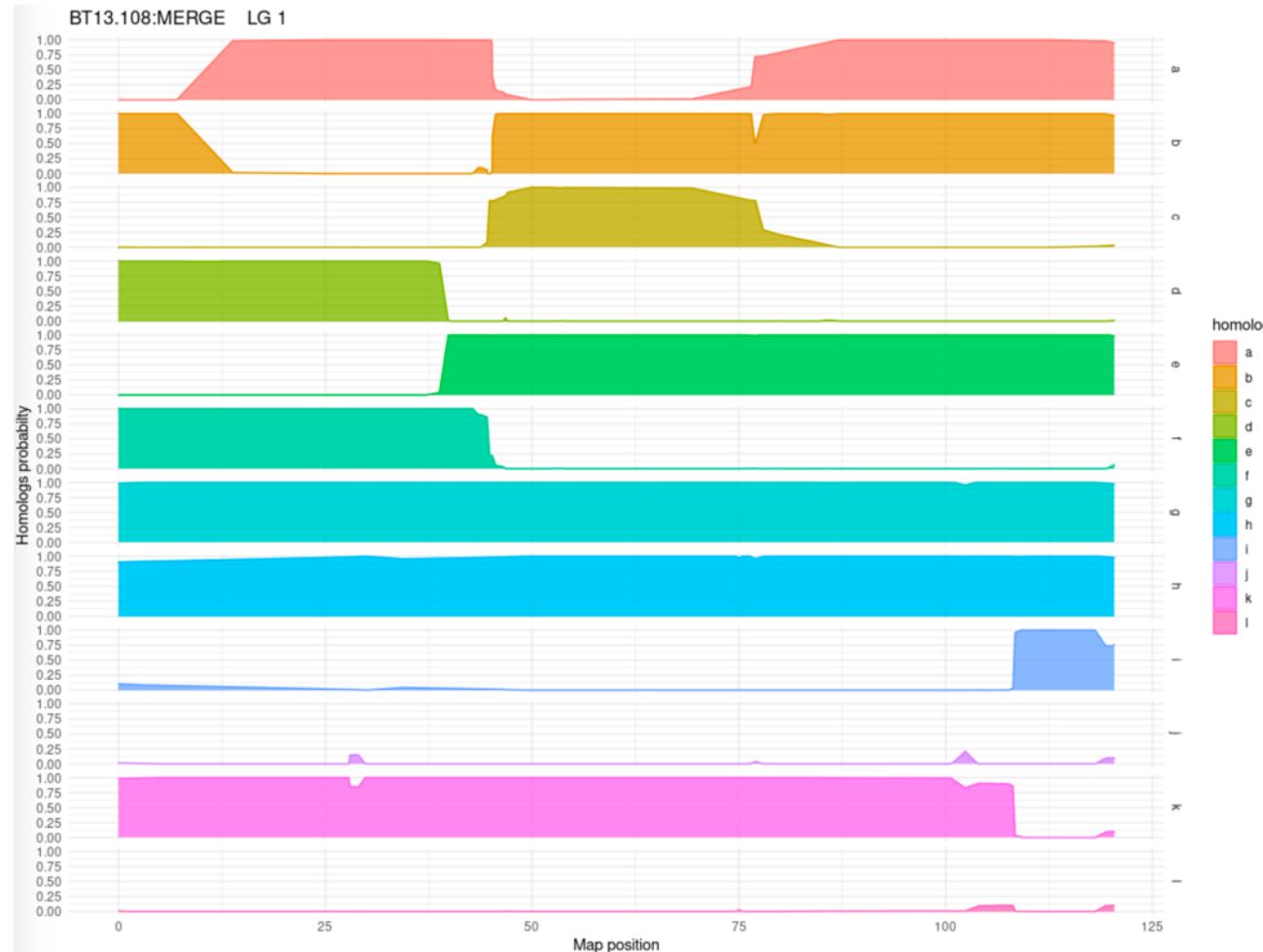
- When assuming a *prior probability* distribution of the genotypes, multilocus strategies can improve the quality of the inferred haplotypes

Tetraploid potato



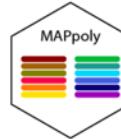
# Probabilistic haplotype reconstruction

Hexaploid sweetpotato



# MAPpoly – R package to construct multipoint genetic maps in polyploids

[build passing](#) [build passing](#) [development active](#) [License GPL v3](#) [codecov 77%](#) [CRAN 0.2.0](#)



## Introduction

MAPpoly (v. 0.2.0) is an R package to construct genetic maps in autopolyploids with even ploidy levels. In its current version, MAPpoly can handle ploidy levels up to 8 when using hidden Markov models (HMM), and up to 12 when using the two-point simplification. When dealing with large numbers of markers (> 10,000), we strongly recommend using high-performance computation.

In its current version, MAPpoly can handle three different types of datasets:

1. CSV files
2. MAPpoly files
  - Dosage based
  - Probability based
3. VCF files (beta)

The derivation of the HMM used in MAPpoly can be found in [Mollina and Garcia, 2019](#). Recently, we used MAPpoly to built an ultra-dense multilocus integrated genetic map containing ~30k SNPs and characterized the inheritance system in a sweetpotato full-sib family ([Mollina et al., 2019](#)). See the resulting map [here](#) and the haplotype composition of all individuals in the full-sib population [here](#).

MAPpoly is not available from CRAN, but you can install it from GitHub. Within R, you need to install and load the package `devtools`:

```
install.packages("devtools")
```

To install MAPpoly from GitHub use

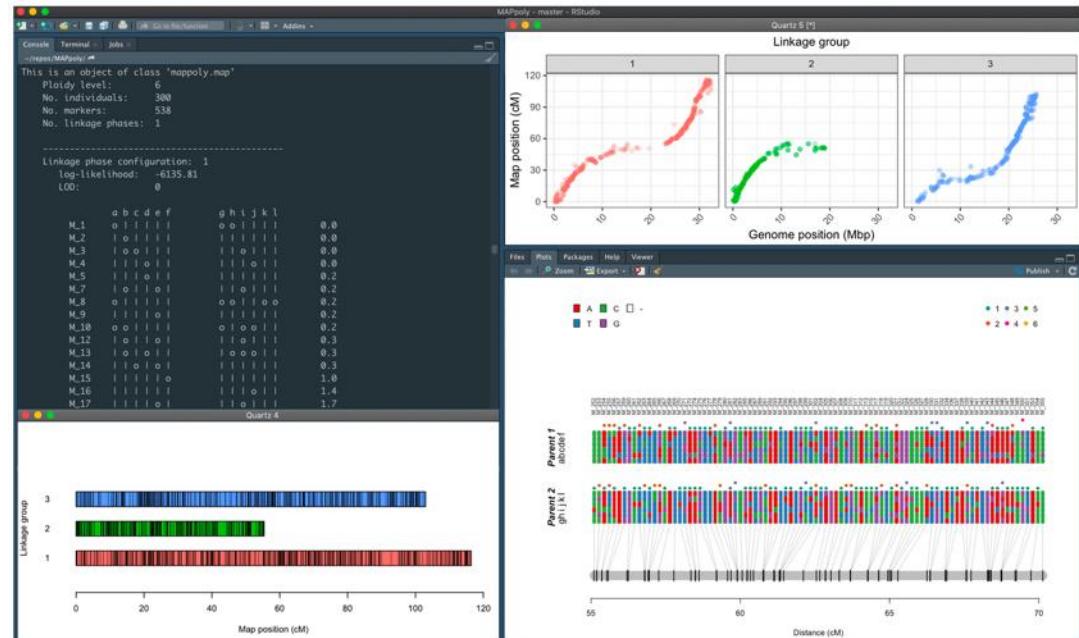
```
devtools::install_github("mmollina/mappoly")
```

## Vignettes

- Building a genetic map in an hexaploid full-sib population using MAPpoly
- Building a genetic map using potato genotype data from SolCAP
- Dataset examples
  - Hexaploid simulation with dosage call in MAPpoly format
  - Hexaploid simulation with dosage probabilities in MAPpoly format
  - Tetraploid potato with dosage call in MAPpoly format
  - Tetraploid potato with dosage call in CSV format
  - Tetraploid potato with dosage probabilities in MAPpoly format

## Acknowledgment

This package has been developed as part of the [Genomic Tools for Sweetpotato Improvement project \(GT4SP\)](#), funded by [Bill & Melinda Gates Foundation](#).



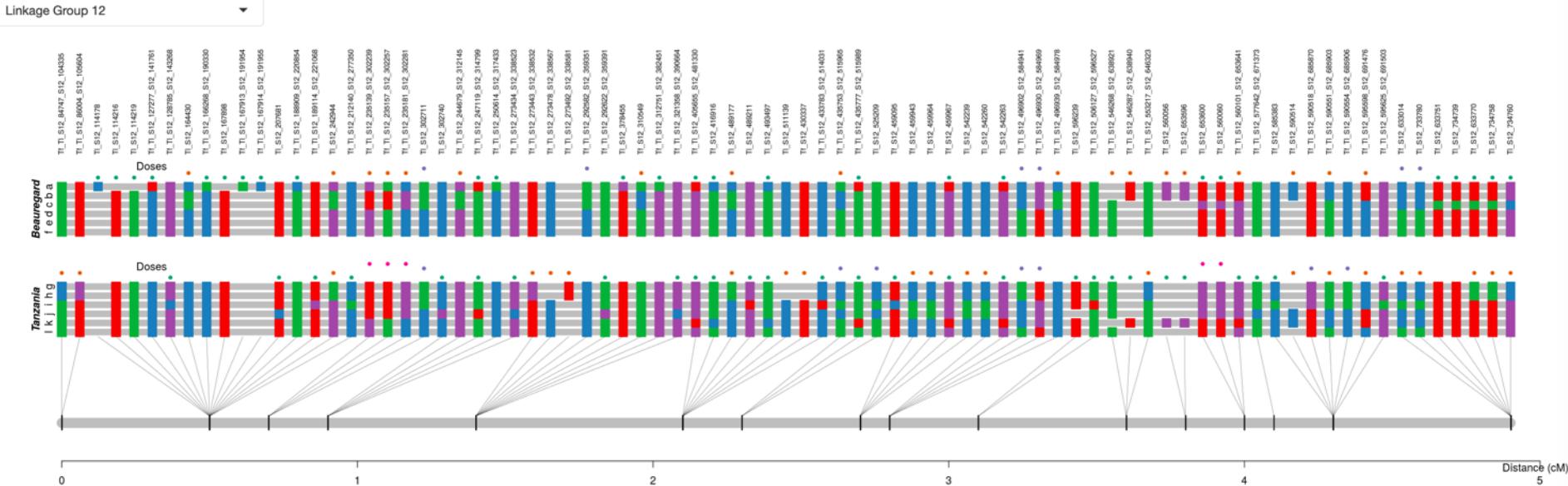
stable: <https://CRAN.R-project.org/package=mappoly>

development: <https://github.com/mmollina/MAPpoly>



# Genetic mapping – Linkage group 12 – 2661 SNPs

## Sweetpotato genetic map - Beauregard x Tanzania (BT)



Show SNP names?

### Legend

Nucleotide	Doses
A	6
T	5
C	4
G	3
-	2
	1

### Number of SNPs per dosage

\$doses	0	1	2	3	4	5	6
0	0	16	12	3	0	0	0
1	14	7	3	0	2	0	0
2	4	5	5	1	3	0	0
3	1	0	2	3	0	0	0
4	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0

### Summary

```
$number.snp
[1] 81

$length
[1] 4.9

$cM.per.snp
[1] 0.06
```

### Notes

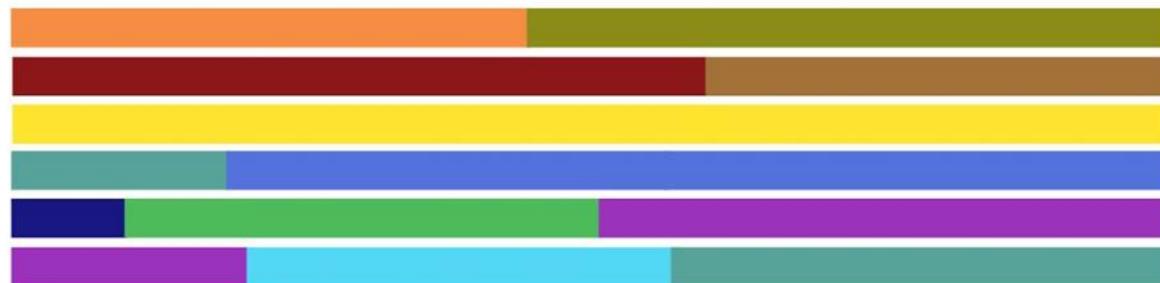
- The detailed mapping procedure is described in Mollinari et al. (2019)
- Use the slide bar to resize or move through the map.
- The estimation of the offspring haplotype is available [here](#)

Interactive version: [https://gt4sp-genetic-map.shinyapps.io/bt\\_map/](https://gt4sp-genetic-map.shinyapps.io/bt_map/)

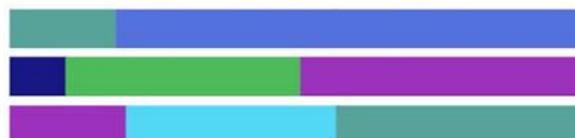
# Haplotype reconstruction in the offspring



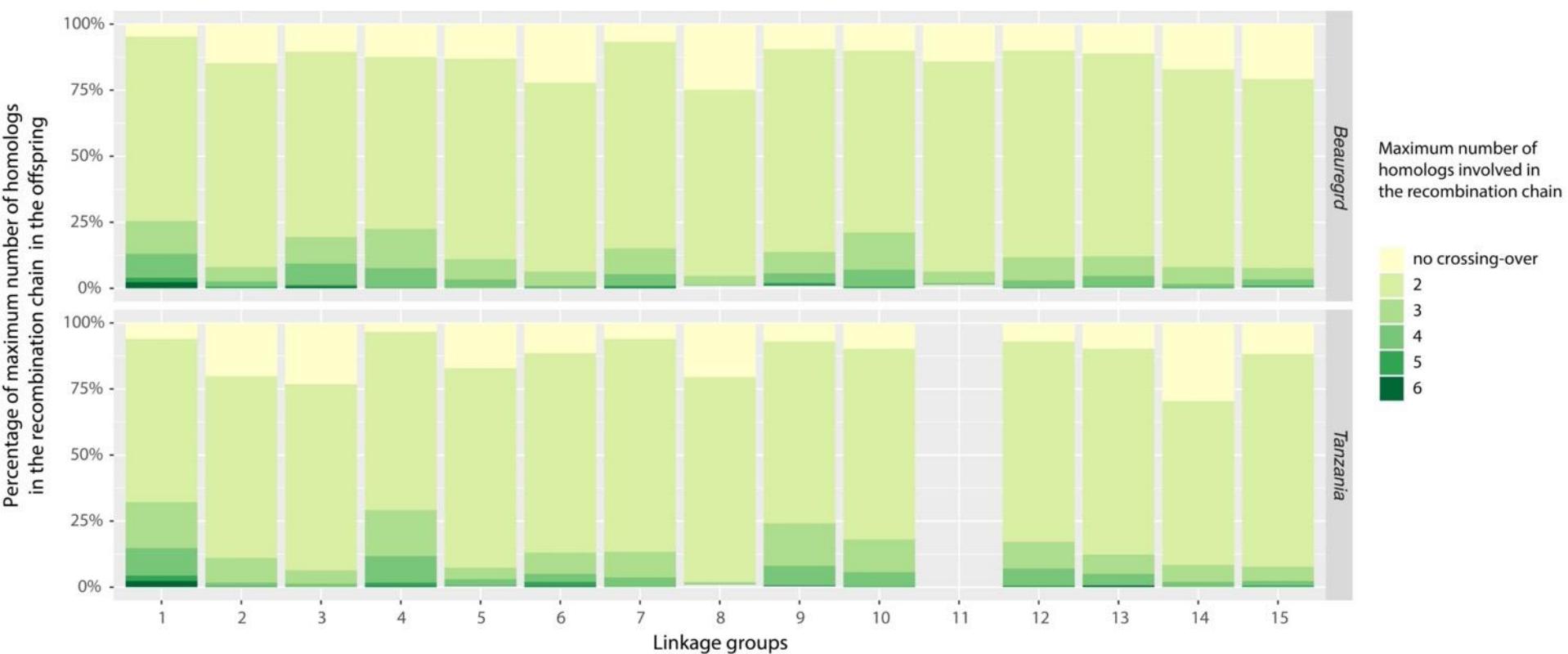
Haplotype of individual BT05:320



Resulting gametes

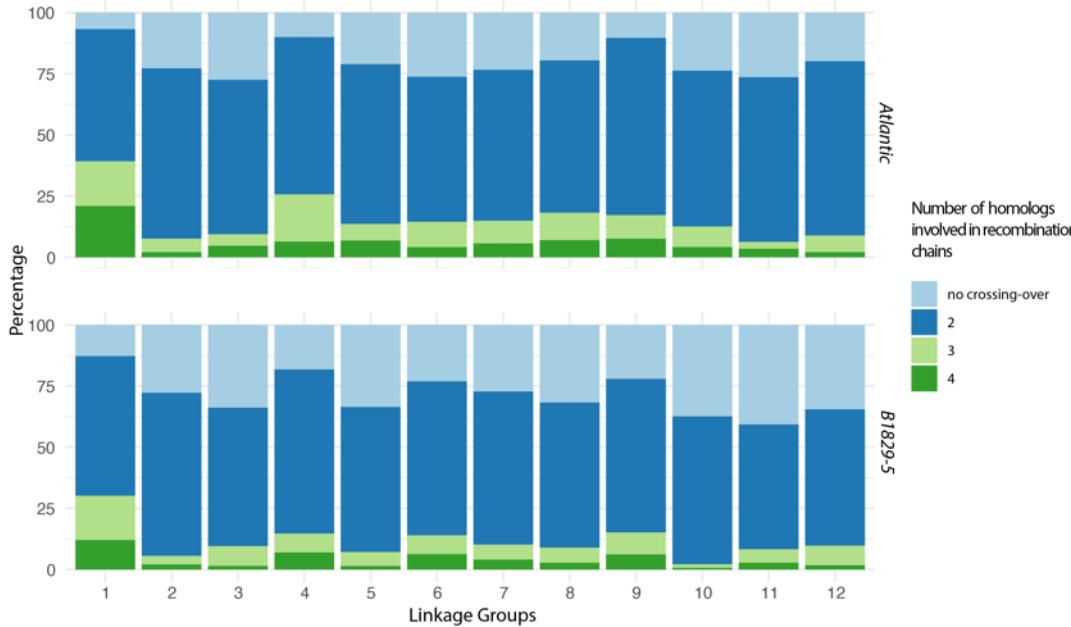


# Number of homologs involved in recombination chains



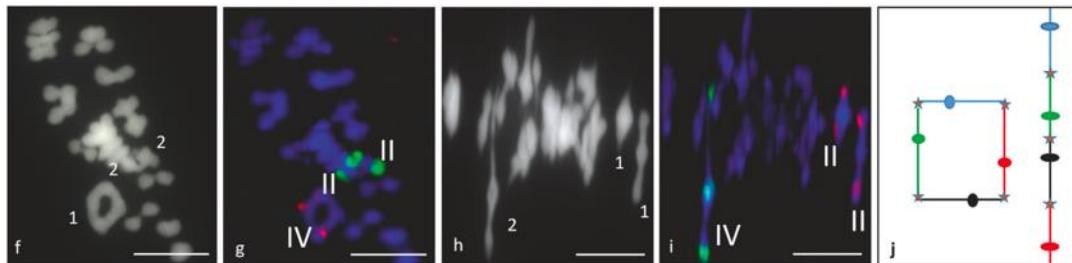
# Homologs in recombination chains – potato

**Pereira et al. (2020)** - Recombination landscape in a *Solanum tuberosum* cv.

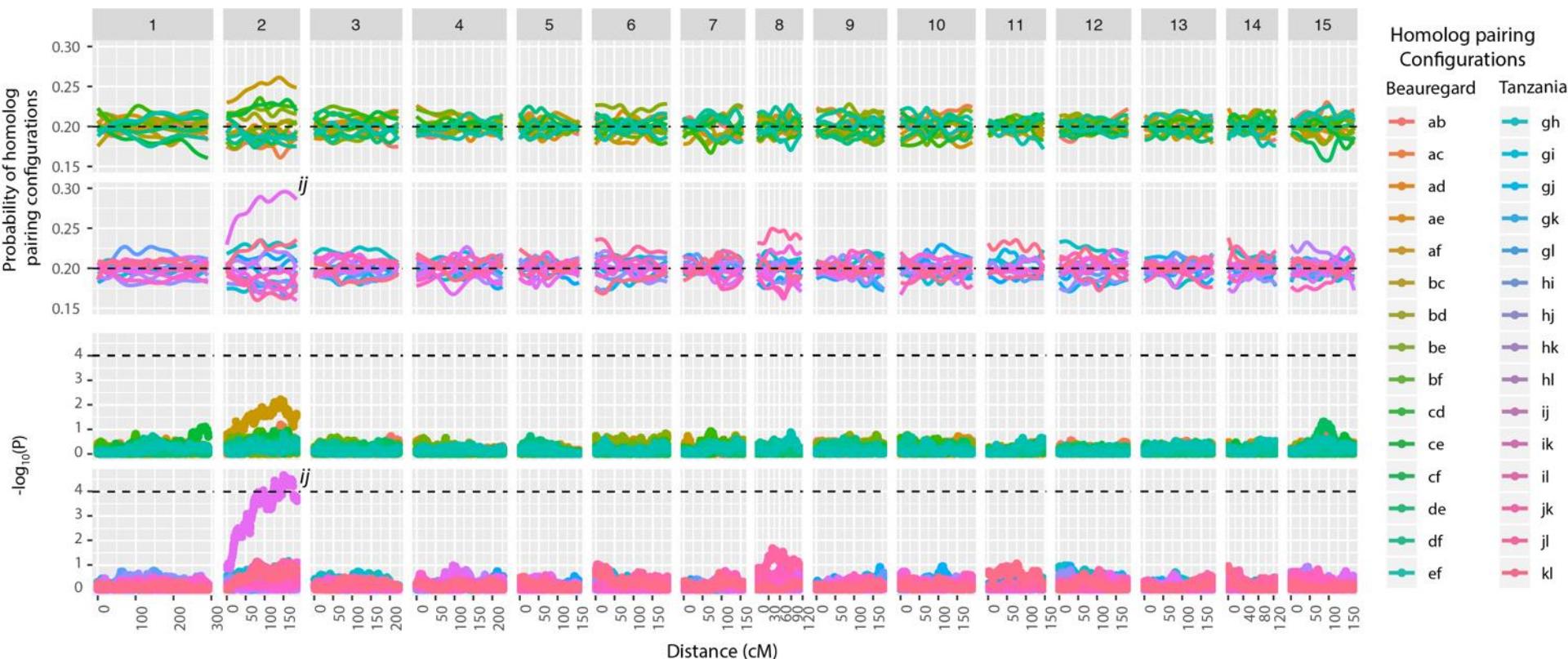


	Choudhary et al. (2020)	Pereira et al. (2020)
bivalents	predominant	62.3 %
multivalents	7~48%	2.2~39.2%

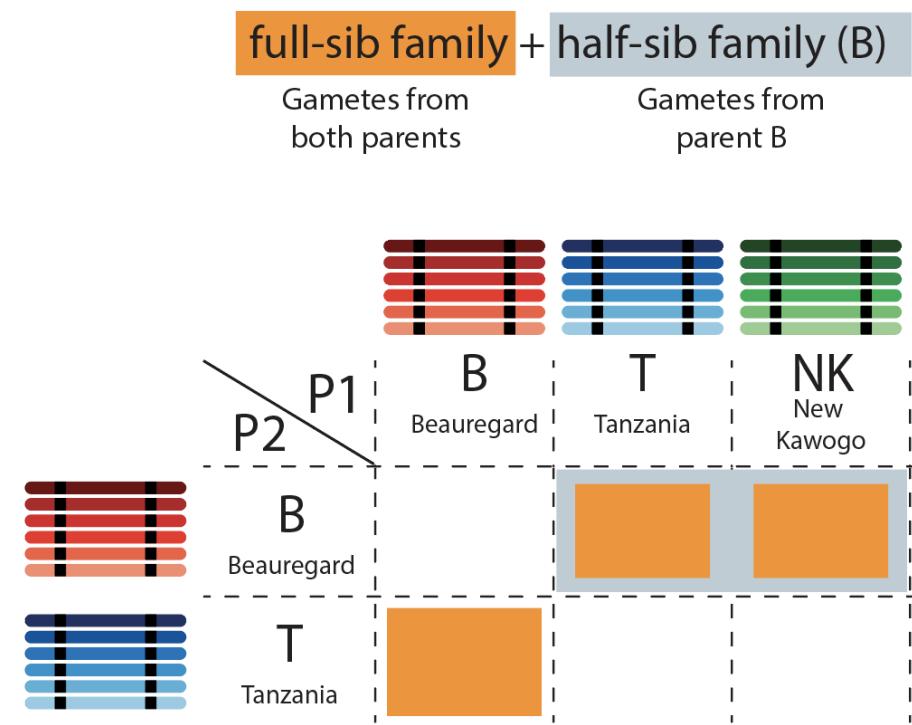
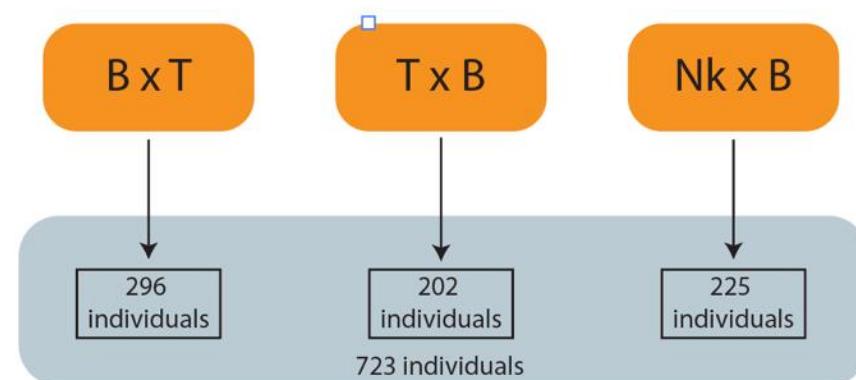
**Choudhary et al. (2020)** – Using fluorescence *in situ* hybridization (FISH)  
5S rDNA probe (red) and 45S rDNA probe (green)



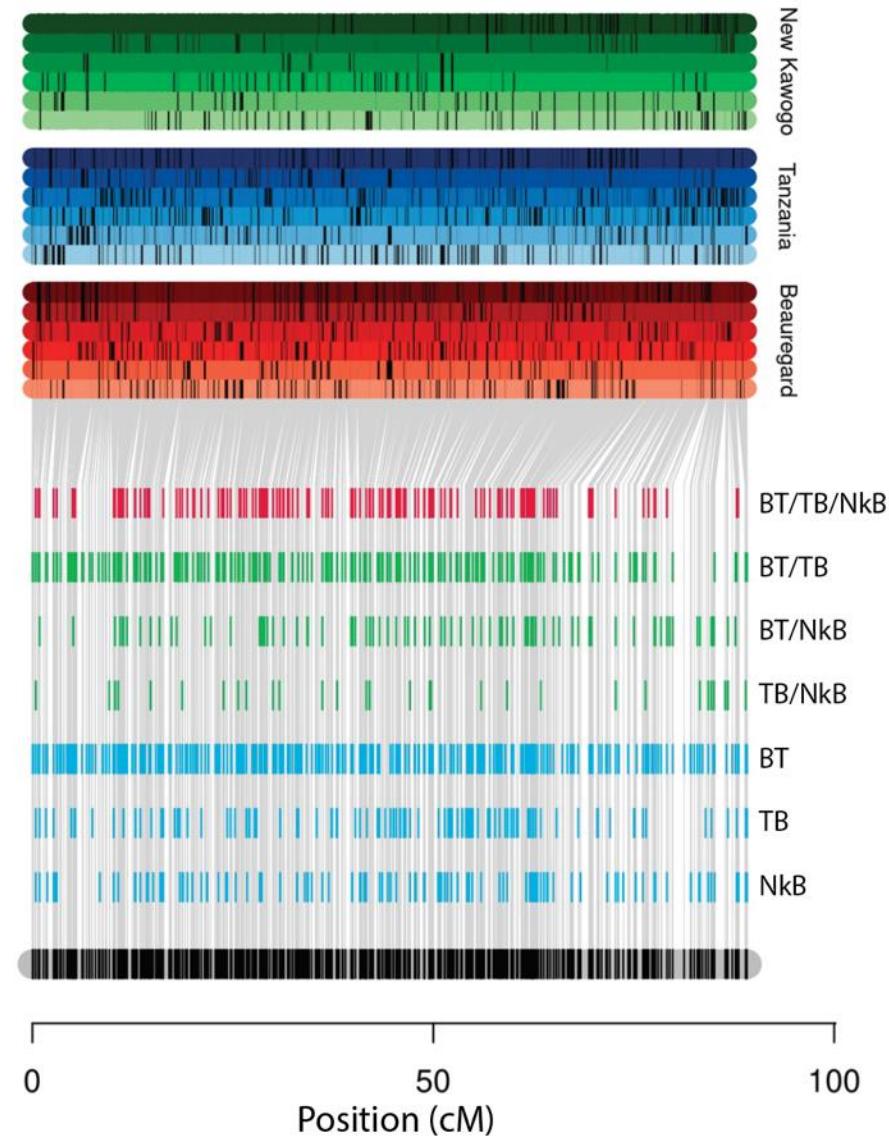
# Preferential pairing profiles: Sweetpotato is vastly **autohexaploid**



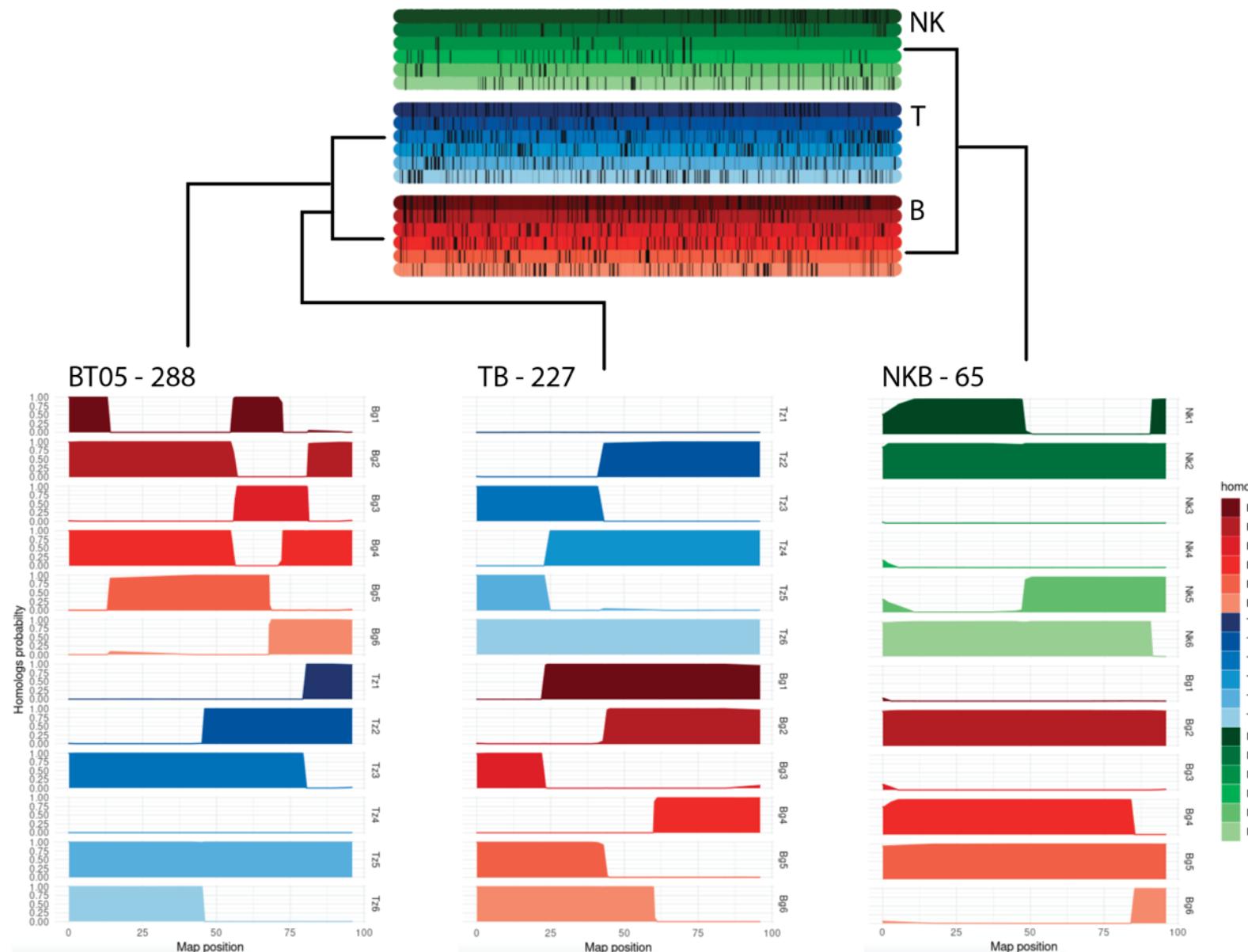
# Linkage analysis in multiple inter-connected families



# Multi-parental map BT-TB-NkB – Chromosome 15

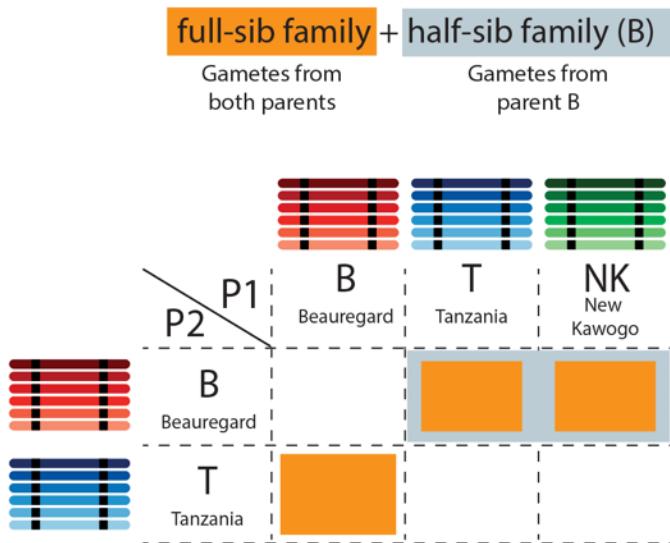


# Haplotyping in BT-TB-NKB – Chromosome 15

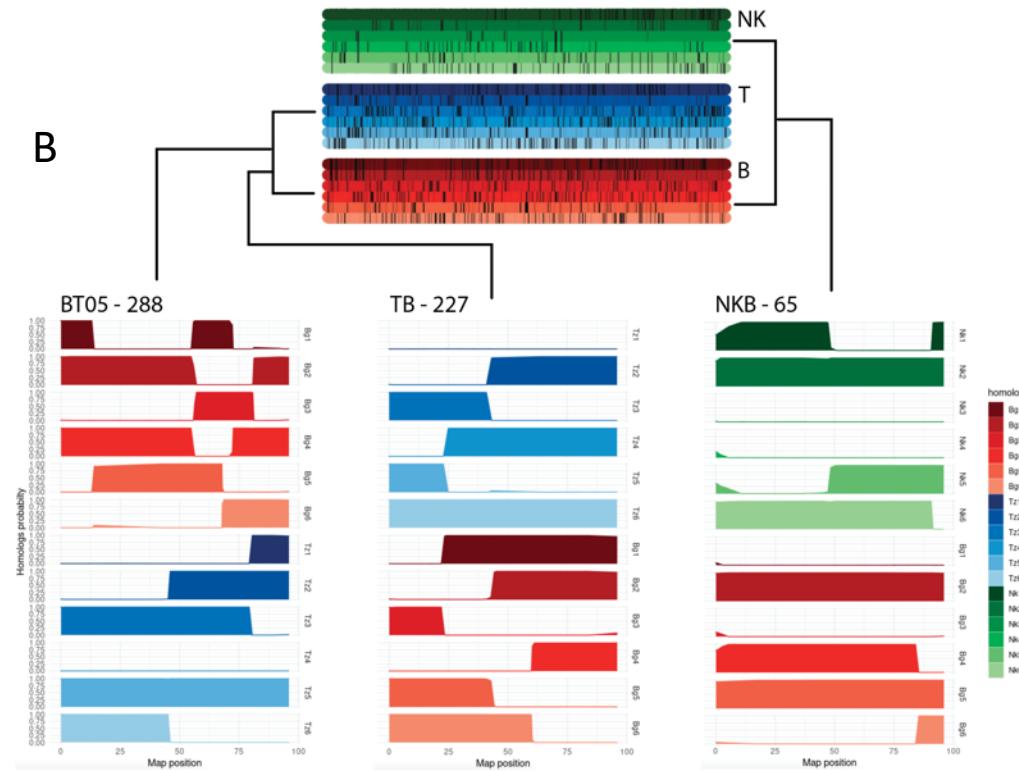


# Haplotyping in BT-TB-NKB – Chromosome 15

A



B



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