Cache: Direct Mapping Address Structure

Direct Mapping Fundamentals

- · Main Memory Structure:
- Memory is divided into blocks (eg. 64 blocks)
- Cache is made of lines
- · Cache Mapping Formula:
 - A memory block maps to a specific cache line cache line index = (block #) mod (# of lines)

Example:

- Main Memory has 32 blocks (0-31), cache has 4 lines (0-3) * Unrealistic Example
- Block 25 maps to line 1 (25 mod 4 = 1)
- Block 4 and block 16 both map to line 0
- Consequence: If block 4 is in line 0, and block 16 is loaded, then block 4 gets evicted

Tag and Line Number: Address Breakdown

- · When we store to cache, we want to store the block # alongside the data data, to better be able to check the cache for hits/misses
- · But we don't want to store the entire block # since that would take up too much space

If we have a 4-line cache, any block # that is a multiple of 4 will map to line 0 Likewise, any mem block # that is a (multiple of 4) + 1 will map to cache line 1

	Mem block #	block # binary		Mem block #	block # binard
line 0:	block 0	0 0 0 0 0	line 1:	block 1	00001
	block 4	00100		block 5	00101
	block 8	0 1 0 0 0		block 9	0 1 0 0 1
	610cK 12	0 1 1 0 0		block 13	0 1 1/01
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We notice that the last 2 digits are the same, so we can simply store the first 3 digits and add back the last 2 digits on the fly when we want to access the cache. This "truncated" block # is called the tag

When a block is loaded into a cache line, its identity must be memoized using a tag

- · Tag = top bits of the address (unique identifier)
- · Line Number = lower bits (used to index into the cache)

General Formula

- · Address size: S bits (memory size = 25)
- · Cache size: 2 lines (line index size = B bits)
- · Tag size = 5 B

Example:

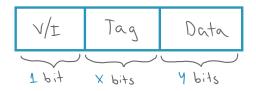
- · Memory has 32 blocks = 5 bit address (S = 5)
- · Cache has 4 lines = 2 bit line # (R=2)
- · Tag = 5-2 = 3 bits

Cache Structure

Each cache line contains:

- · Valid/invalid bit (V/I): Indicates if the data is valid
- · Taq: Used for identifying the block stored
- · Dafa: The contents of the block

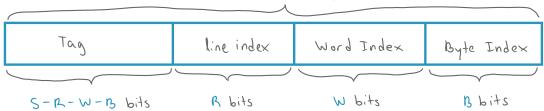
Cache Line Format



Tag and data bit width will depend on the system being described

Direct Mapping Address Structure





- · 5 = Total address bits
- · n = Bits for line index
- · W = Bits for word index (If multiple words per block. If only 1 word per block, we don't include a partition for the word index)
- · B = Bits for byte index (if the system uses byte addressing, otherwise we don't include this partition for the byte index)

Address Decomposition for Word and Byte Addressing

Scenarios:

· Word Addressing, I word per block

Tag line index

· Byte Addressing, I word per block, word size = 4 bytes

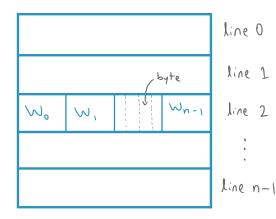
Tag	line index	byte offset (2 bits)

· Word Addressing, multiple words per block

tag line index word index

· Byte Addressing, multiple words per block

Tag line index word index byte offset



Cache Initialization and Context Switching

· On program startup: all cache lines are marked invalid

· On context switch:

- Previous process's cache data becomes irrelevant

- All cache lines are again marked invalid

· Valid bit is set to I only when new block data is loaded

Total Cache Size Calculation

Formula:

Total cache size = # of lines x (1 + Tag Bits + Data bits)

· Find the total # of bytes for a direct mapping cache to store 64 KB in 1-word blocks assuming a word size of 32 bits and MIPS addressing

& Break down the specifications:

- Word size = 32 bits -> 32 bit address

- Block size = 1 word

- Addressing mode: byte addressing (from what we know of MIPS)

* B = bytes

* h = bits

- Data: 64 KB

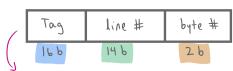
Block size = 1 word = 20 words We don't need to allocate any bits for word select

word size = 32 bits > 4B = 22B -> Allocate 2 bits for addressing byte # (byte addressing) Data = 64 KB = 64 x 210 B = 26 x 210 B = 216 B

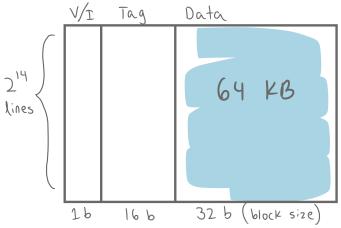
(s # of lines =
$$\frac{\text{Data size}}{\text{block size}} = \frac{2^{16} \text{ B}}{2^{2} \text{ B}} = 2^{14} \text{ lines}$$

Tag = 32 - (14 + 2) = 16 bits

Address Structure



Cache Structure



Total cache size

$$2^{14}$$
 lines x 39 bits/line = $(39 \cdot 2^{14})$ bits
= $(39 \cdot 2^{4})(2^{10})$ bits = $(39 \cdot 16)(1 \text{ Kb}) = (39 \cdot 16) \text{ KB}$
= $(39 \cdot 2) \text{ KB} = 78 \text{ KB}$