

41

a)

$$(32500)_{10}$$

$$(011111101110100)_2$$

=

$$\begin{array}{r}
 2 \overline{) 32500} \\
 \underline{2 162500} \\
 2 \overline{) 81250} \\
 \underline{2 40621} \\
 2 \overline{) 20310} \\
 \underline{2 10151} \\
 2 \overline{) 5071} \\
 2 \overline{) 2531} \\
 2 \overline{) 1261} \\
 2 \overline{) 630} \\
 2 \overline{) 311} \\
 2 \overline{) 151} \\
 2 \overline{) 71} \\
 2 \overline{) 31} \\
 2 \overline{) 11} \\
 \underline{0 } 1
 \end{array}$$

↑

b)

$$(-12345)_{10}$$

=

$$-(0011000000111001)_2$$

$$= (110011111000110)_{10}$$

$$\begin{array}{r}
 2 \overline{) 12345} \\
 \underline{2 61721} \\
 2 \overline{) 30860} \\
 \underline{2 15430} \\
 2 \overline{) 7711} \\
 2 \overline{) 3851} \\
 2 \overline{) 1921} \\
 2 \overline{) 960} \\
 2 \overline{) 480} \\
 2 \overline{) 240} \\
 2 \overline{) 120} \\
 2 \overline{) 60} \\
 2 \overline{) 30} \\
 2 \overline{) 11} \\
 \underline{0 } 1
 \end{array}$$

$$\begin{aligned} \underline{11}_{10} & - (2)_{10} = -(10)_2 = -(000000000000000010)_2 \\ & = (1111111111111101)_{15} \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 2} \\ 2 \overline{) 10} \uparrow \\ 01 \end{array}$$

a)

$$120_{10} = (000000001111000)_{25}$$

$$\begin{array}{r} 2 \overline{) 120} \\ 2 \overline{) 600} \\ 2 \overline{) 300} \\ 2 \overline{) 150} \\ 2 \overline{) 75} \\ 2 \overline{) 37} \\ 2 \overline{) 18} \\ 2 \overline{) 9} \\ 01 \end{array}$$

b)

$$\begin{aligned} -(12)_{10} & = -(0000000000001100)_2 \\ & = (1111111111110011)_{15} \\ & = (1111111111110100)_{25} \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 12} \\ 2 \overline{) 60} \\ 2 \overline{) 30} \\ 2 \overline{) 15} \uparrow \\ 01 \end{array}$$

c)

$$\begin{aligned} -(120)_{10} & = -(00000000001111000)_{25} \quad \text{From (2a)} \\ & = (11111111110000111)_{15} \\ & = (11111111110001000)_{25} \end{aligned}$$

$$\begin{aligned}
 \underline{3)} \quad \underline{a)} \quad & (10101010)_{1's} \\
 & = - (01010101)_2 \\
 & = -(1 \times 2^6 + 2^4 + 2^2 + 2^0)_{10} \\
 & = -85
 \end{aligned}$$

$$\begin{aligned}
 \underline{3)} \quad \underline{b)} \quad & (01000010)_{1's} \\
 & = (01000010)_2 \\
 & = 66
 \end{aligned}$$

$$\begin{aligned}
 \underline{c)} \quad & (11111111)_{1's} \\
 & = -(00000000)_2 \\
 & = 0
 \end{aligned}$$

$$\begin{aligned}
 \underline{4)} \quad \underline{a)} \quad & (01010101)_{2's} \\
 & = (01010101)_2 \\
 & = (2^6 + 2^4 + 2^2 + 2^0)_{10} \\
 & = (85)_{10}
 \end{aligned}$$

$$\begin{aligned}
 \underline{b)} \quad & (10111100)_{2's} \\
 & = (01000100)_2 \\
 & = -(2^6 + 2^2)_{10} \\
 & = -68
 \end{aligned}$$

$$\begin{aligned}
 \underline{c)} \quad & (11111111)_{2's} \\
 & = -(00000001)_2 \\
 & = -(2^0)_{10} \\
 & = -(1)_{10}
 \end{aligned}$$

5 | a)

$$\begin{array}{r}
 2 \overline{) 525} \\
 \underline{2621} \\
 2 \overline{) 1310} \\
 \underline{651} \\
 2 \overline{) 321} \\
 \underline{160} \\
 2 \overline{) 80} \\
 \underline{40} \\
 2 \overline{) 20} \\
 \underline{10} \\
 01
 \end{array}$$

$$(525)_{10} = (001000001101)_2$$

it is same for 1's and 2's

$$\begin{array}{r}
 2 \overline{) 321} \\
 \underline{1601} \\
 2 \overline{) 800} \\
 \underline{400} \\
 2 \overline{) 200} \\
 \underline{100} \\
 2 \overline{) 50} \\
 \underline{21} \\
 2 \overline{) 10} \\
 01
 \end{array}$$

$$\begin{aligned}
 -(321)_{10} &= -(000101000001)_2 \\
 &= (111010111110)_{1s} \\
 &= (11101011111)_{2s}
 \end{aligned}$$

$$\begin{array}{r}
 (001000001101)_{1s} \\
 (111010111110)_{1s} \\
 \hline
 1000011001011 \\
 +1 \\
 \hline
 (000011001100)_{1s}
 \end{array}$$

$$\begin{array}{r}
 (001000001101)_{1s} \\
 (111010111111)_{2s} \\
 \hline
 1000011001100 \\
 (000011001100)_{2s}
 \end{array}$$

5 | b)

$$\begin{array}{r}
 2 \overline{) 753} \\
 \underline{3761} \\
 2 \overline{) 1880} \\
 \underline{940} \\
 2 \overline{) 470} \\
 \underline{231} \\
 2 \overline{) 111} \\
 \underline{51} \\
 2 \overline{) 21} \\
 \underline{10} \\
 01
 \end{array}$$

$$(753)_{10} = (001011110001)_2$$

$$\begin{array}{r}
 2 \overline{) 864} \\
 \underline{4320} \\
 2 \overline{) 2160} \\
 \underline{1080} \\
 2 \overline{) 540} \\
 \underline{270} \\
 2 \overline{) 131} \\
 \underline{61} \\
 2 \overline{) 30} \\
 \underline{11} \\
 01
 \end{array}$$

$$\begin{aligned}
 -(864)_{10} &= -(001101400000)_{10} \\
 &= (110010011111)_{1s} \\
 &= (110010100000)_{2s}
 \end{aligned}$$

$$\begin{array}{r}
 (001011110001)_{1s} \\
 (110010011111)_{1s} \\
 \hline
 (111100100000)_{1s}
 \end{array}$$

$$\begin{array}{r}
 (001011110001)_{2s} \\
 (110010100000)_{2s} \\
 \hline
 (11110010001)_{2s}
 \end{array}$$

51 c1

$$(20)_{10} = (000000010100)_2$$

$$\begin{aligned} -(100)_{10} &= -(000001100100)_2 \\ &= (111110011011)_{15} \\ &= (111110011100)_{25} \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 20} \\ 2 \overline{) 10} 0 \\ 2 \overline{) 5} 0 \\ 2 \overline{) 2} 1 \\ 2 \overline{) 1} 0 \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{) 100} \\ 2 \overline{) 50} 0 \\ 2 \overline{) 25} 0 \\ 2 \overline{) 12} 1 \\ 2 \overline{) 6} 0 \\ 2 \overline{) 3} 0 \\ 2 \overline{) 1} 1 \\ 0 \end{array}$$

$$\begin{array}{r} (0000000010100)_{16} \\ -(111110011011)_{15} \\ \hline (111110101111)_{15} \end{array}$$

$$\begin{array}{r} (000000010100)_{25} \\ -(111110011100)_{25} \\ \hline (111110110000)_{25} \end{array}$$

51 d1

$$(35)_{10} = (00000100011)_2$$

$$\begin{aligned} -(210) &= -(00011010010)_2 \\ &= (111100101101)_{15} \\ &= (111100101110)_{25} \end{aligned}$$

$$\begin{array}{r} 2 \overline{) 35} \\ 2 \overline{) 17} 1 \\ 2 \overline{) 8} 1 \\ 2 \overline{) 4} 0 \\ 2 \overline{) 2} 0 \\ 2 \overline{) 1} 0 \\ 0 \end{array}$$

$$\begin{array}{r} 2 \overline{) 210} \\ 2 \overline{) 105} 0 \\ 2 \overline{) 52} 1 \\ 2 \overline{) 26} 0 \\ 2 \overline{) 13} 0 \\ 2 \overline{) 6} 1 \\ 2 \overline{) 3} 0 \\ 2 \overline{) 1} 1 \\ 0 \end{array}$$

$$\begin{array}{r} (000000100011)_{15} \\ -(111100101101)_{15} \\ \hline (111101010000)_{15} \end{array}$$

$$\begin{array}{r} (000000100011)_{25} \\ -(111100101110)_{25} \\ \hline (111101010000)_{25} \end{array}$$

$$\begin{aligned}
 &1.8 \\
 &= (000001010101)_2 \\
 &= (11110101010)_B \\
 &= (11110101011)_{25}
 \end{aligned}$$

$$\begin{aligned}
 &= (000000111000)_2 \\
 &= (11111000111)_B \\
 &= (11111001000)_{25}
 \end{aligned}$$

$$\begin{aligned}
 &= (000000000001)_2 \\
 &= (11111111110)_B \\
 &= (11111111111)_{25}
 \end{aligned}$$

$$\begin{aligned}
 &= (000000010000)_2 \\
 &= (11111110111)_B \\
 &= (11111110000)_{25}
 \end{aligned}$$

$$\begin{aligned}
 &= (000000000000)_2 \\
 &= (11111111111)_B \\
 &= (00000000000)_{25}
 \end{aligned}$$

1-12

a)

$$\begin{array}{r} (011010)_2 \\ - (001101)_2 \\ \hline (001101)_2 \end{array}$$

$$\begin{array}{r} (011010)_{15} \\ (110010)_{15} \\ \hline 001100 \\ +1 \\ \hline (001101)_{15} \\ = (001101)_2 \end{array}$$

$$\begin{array}{r} (011010)_{25} \\ (110011)_{25} \\ \hline (001101)_{25} \\ = (001101)_2 \end{array}$$

b)

$$\begin{array}{r} (011010)_2 \\ - (010000)_2 \\ \hline (001010)_2 \end{array}$$

$$\begin{array}{r} (011010)_{15} \\ (101111)_{15} \\ \hline 001001 \\ +1 \\ \hline (001010)_{15} \\ (001010)_2 \end{array}$$

$$\begin{array}{r} (011010)_{25} \\ (110000)_{25} \\ \hline (001010)_{25} \\ (001010)_2 \end{array}$$

c)

$$\begin{array}{r} (010010)_2 \\ - (010011)_2 \\ \hline - (000001)_2 \end{array}$$

$$\begin{array}{r} (010010)_{15} \\ (101100)_{15} \\ \hline (111110)_{15} \\ - (000001)_2 \end{array}$$

$$\begin{array}{r} (010010)_{25} \\ (101101)_{25} \\ \hline (111111)_{25} \\ - (000001)_2 \end{array}$$

d)

we have to do this in 7 bit

$$\begin{array}{r} 0000100 \\ - 0110000 \\ \hline -0101100 \end{array}$$

$$\begin{array}{r} (0000100)_{15} \\ (1001111)_{15} \\ \hline (1010011)_{15} \\ - (0101100)_2 \end{array}$$

$$\begin{array}{r} (0000100)_{25} \\ (1010000)_{25} \\ \hline (1010100)_{25} \\ - (0101100)_2 \end{array}$$

Rough

$$\begin{array}{r} 010011 \\ - 010010 \\ \hline 000001 \end{array}$$

$$\begin{array}{r} 110000 \\ - 000100 \\ \hline 101100 \end{array}$$

1-15

$$(8620)_{10} \rightarrow (1000011000100000)_{BCD}$$

For excess 3

$$(8620)_{10} \rightarrow (1011100101010011)_{\text{excess 3}}$$

$$(8620)_{10} \rightarrow (1110110000100000)_{2421}$$

$$(8620)_{10} = 10000110101100$$

2	8620
2	43100
2	21550
2	10771
2	5381
2	2690
2	1341
2	670
2	331
2	161
2	80
2	40
2	20
2	10
2	01

- 0 0
- 1 01
- 2 10
- 3 11
- 4 100
- 5 101
- 6 110
- 7 111
- 8 1000
- 9 1001

- (A) 10 1010
- (B) 11 1011
- (C) 12 1100
- (D) 13 1101
- (E) 14 1110
- (F) 15 1111

- | | |
|----|------|
| 1 | 0001 |
| 2 | 0010 |
| 3 | 0011 |
| 4 | 0100 |
| 5 | 0101 |
| 6 | 0110 |
| 7 | 0111 |
| 8 | 1000 |
| 9 | 1001 |
| 10 | 1010 |
| 11 | 1011 |
| 12 | 1100 |
| 13 | 1101 |
| 14 | 1110 |
| 15 | 1111 |

2.11

$$(18)_{10} = (00010010)_2$$
$$= (00010010)_{16}$$
$$= (00010010)_{25}$$
$$\begin{array}{r} 2 \overline{) 18} \\ 2 \overline{) 90} \\ 2 \overline{) 41} \\ 2 \overline{) 20} \\ 2 \overline{) 10} \uparrow \\ 01 \end{array}$$

$$(115)_{10} = (01110011)_2$$
$$= (01110011)_{16}$$
$$= (01110011)_{25}$$
$$\begin{array}{r} 2 \overline{) 115} \\ 2 \overline{) 571} \\ 2 \overline{) 281} \\ 2 \overline{) 140} \\ 2 \overline{) 70} \\ 2 \overline{) 31} \\ 2 \overline{) 11} \\ 01 \end{array}$$

$$(79)_{10} = (01001111)_2$$
$$= (01001111)_{16}$$
$$= (01001111)_{25}$$
$$\begin{array}{r} 2 \overline{) 79} \\ 2 \overline{) 391} \\ 2 \overline{) 191} \\ 2 \overline{) 91} \\ 2 \overline{) 41} \\ 2 \overline{) 20} \\ 2 \overline{) 10} \\ 01 \end{array}$$

$$-(49)_{10} = -(00110001)_2$$

$$= (11001110)_{16}$$

$$2 \overline{) 49} = (11001111)_{26}$$

$$\begin{array}{r} 2 \overline{) 49} \\ 2 \overline{) 241} \\ 2 \overline{) 120} \\ 2 \overline{) 60} \\ 2 \overline{) 30} \\ 2 \overline{) 11} \\ 01 \end{array}$$

$$-(3)_{10}$$

$$2 \overline{) 3} = -(00000011)_2$$

$$2 \overline{) 11} \uparrow = (11111100)_{16}$$

$$01 = (11111101)_{26}$$

$$-(100)_{10} = -(01100100)_2$$

$$= (10011011)_{16}$$

$$= (10011100)_{26}$$

$$\begin{array}{r} 2 \overline{) 100} \\ 2 \overline{) 500} \\ 2 \overline{) 250} \\ 2 \overline{) 121} \\ 2 \overline{) 60} \\ 2 \overline{) 30} \\ 2 \overline{) 11} \\ 01 \end{array}$$

2.12

a)

$$\begin{array}{r} (11010100)_{25} \\ (10101011)_{25} \\ \hline (01111111)_{25} \end{array}$$

Not Overflow

b)

$$\begin{array}{r} (10111001)_{25} \\ (11010110)_{25} \\ \hline (10001111)_{25} \end{array}$$

Not Overflow

c)

$$\begin{array}{r} (01011101)_{25} \\ (00100001)_{25} \\ \hline (01111110)_{25} \end{array}$$

Not Overflow

d)

$$\begin{array}{r} (00100110)_{25} \\ (01011010)_{25} \\ \hline (10000000)_{25} \end{array}$$

Overflow

2.15

$$(61453)_{10} = \text{FOOD}$$

16	61453	
16	3840	13
16	240	0
16	15	0
	0	15

↑

2.16

a)

$$\begin{array}{r} 1234 \\ 5432 \\ \hline 6666 \end{array}$$

is true for 7 bits and above

b)

$4\frac{1}{3} = 13$ is true for 8 base

$$(4 \times n + 1) / 3 = (1 \times n + 3)$$

$$\Rightarrow 4n + 1 = 3n + 9$$

$$\Rightarrow n = 8$$

c) $33/3 = 11$ is true for 4 bits and above.

$$(3 \times n + 3) / 3 = (1 \times n + 1)$$

$$\Rightarrow 3n + 3 = 3n + 3$$

d)

$$23 + 44 + 14 + 32 = 223$$

$$2n + 3 + 4n + 4 + n + 4 + 3n + 2 = 2n^2 + 2n + 3$$

$$\Rightarrow 10n + 13 = 2n^2 + 2n + 3$$

$$\Rightarrow 2n^2 - 8n - 10 = 0$$

$$n = 5 \text{ or } n = -1$$

so, the operation is true for 5 base

e) $302/20 = 12.1$

$$(3 \times n^2 + 0 \times n + 2) / (2n) = n + 2 + n^{-1}$$

$$\Rightarrow 3n^2 + 2 = 2n^2 + 4n + 2$$

$$\Rightarrow n^2 - 4n = 0$$

$$n = 4 \text{ or } n = 0$$

so, the operation is true for 4 bit.

f)

$$14 = 5$$

$$n + 4 = 5$$

$$\Rightarrow n = 1$$

So, apparently it seems to be base 1.

But the use of different bases. As it not possible to satisfy this case with 1 base.