

Name:

Student ID:

Section:

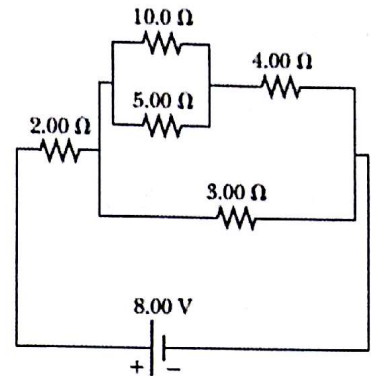
1. A  $2.00 \mu\text{F}$  capacitor with an initial charge of  $5.10 \mu\text{C}$  is discharged through a  $1.30 \text{ k}\Omega$  resistor.
- (a) (3 marks) Calculate the current in the resistor  $9.00 \mu\text{s}$  after the resistor is connected across the terminals of the capacitor.
- (b) (2 marks) What charge remains on the capacitor after  $8.00 \mu\text{s}$ ?
- (c) (2 marks) What is the maximum current in the resistor?

2. Consider the circuit shown in Figure.

(a) (3 marks) Find the voltage across each of the resistors.

(b) (3 marks) Find the current through each of the resistors.

(c) (2 marks) Find the energy stored in the  $3.00 \Omega$  resistor.



$$\boxed{1} \text{ a) } I = \frac{Q_0}{RC} e^{-t/RC}$$

$$= \frac{5.1 \times 10^{-6}}{1.3 \times 10^3 \times 2 \times 10^{-9}} e^{-\frac{9 \times 10^{-6}}{1.3 \times 10^3 \times 2 \times 10^{-9}}}$$

$$= 0.06 \text{ Amp.}$$

$$\text{b) } q = Q_0 e^{-t/RC} = \frac{8 \times 10^{-6}}{1.3 \times 10^3 \times 2 \times 10^{-9}}$$

$$= 5.1 \times 10^{-6} \times e^{-\frac{8 \times 10^{-6}}{1.3 \times 10^3 \times 2 \times 10^{-9}}} = 2.35 \times 10^{-7} \text{ C}$$

$$\text{c) } I_{\text{max}} = \frac{Q_0}{RC} = \frac{5.1 \times 10^{-6}}{1.3 \times 10^3 \times 2 \times 10^{-9}}$$

$$= 1.96 \text{ Amp.}$$

(Ans.)

$$\boxed{2} \quad R_{\text{eq}} = 2 + \frac{1}{\frac{1}{7.33} + \frac{1}{3}} = 4.13 \Omega$$

$$\therefore I_{\text{eq}} = 1.94 \text{ A} = I_2 = I_{10,5,4,3}$$

$$V_{10,5,4,3} = 2.13 \Omega \times 1.94 = 4.13 \text{ V}$$

$$= V_3 = V_{10,5,4}$$

$$I_{10,5,4} = 0.56 \text{ A} = I_4 = I_{10,5}$$

$$V_{10,5} = 3.33 \Omega \times 0.56 = 1.86 \text{ V} = V_{10} = V_5$$

$$\therefore I_2 = 1.94 \text{ A} \quad ; \quad V_2 = 3.88 \text{ V}$$

$$I_{10} = 0.186 \text{ A} \quad ; \quad V_{10} = 1.86 \text{ V}$$

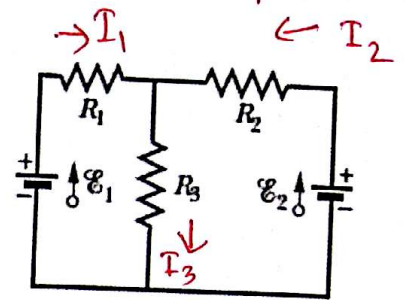
$$I_5 = 0.37 \text{ A} \quad ; \quad V_5 = 1.86 \text{ V}$$

$$I_4 = 0.56 \text{ A} \quad ; \quad V_4 = 2.24 \text{ V}$$

$$I_3 = 1.38 \text{ A} \quad ; \quad V_3 = 4.13 \text{ V}$$

$$\text{c) } P_3 = I_3^2 R_3 = (1.38)^2 \times 3 = 5.7 \text{ W. (Ans.)}$$

3. The ideal batteries have emfs  $\mathcal{E}_1 = 10V$  and  $\mathcal{E}_2 = 0.50\mathcal{E}_1V$ . The values of resistances in each resistor  $4\Omega$ . What is the current in  
 (a) (3 marks) resistance 2 and  
 (b) (2 marks) resistance 3?



$$I_1 + I_2 = I_3$$

$$\mathcal{E}_1 - I_1 R_1 - I_3 R_3 = 0$$

$$\mathcal{E}_2 - I_2 R_2 - I_3 R_3 = 0$$

$$I_1 + I_2 - I_3 = 0 \quad \text{--- (i)}$$

$$-4I_1 - 4I_3 = -10 \quad \text{--- (ii)}$$

$$0 - 4I_2 - 4I_3 = -5 \quad \text{--- (iii)}$$

Solving (i), (ii), (iii)  $\Rightarrow$

$$I_1 = 1.25 \text{ Amp}$$

$$I_2 = 0 \text{ Amp}$$

$$I_3 = 1.25 \text{ Amp.}$$

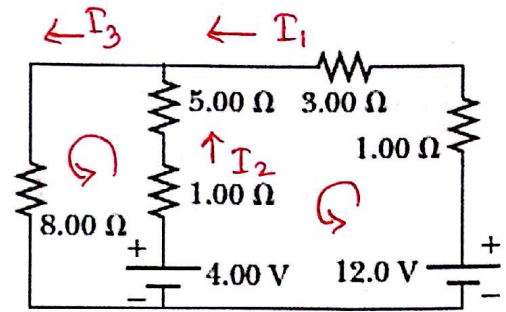
(Ans.)

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1. Consider the circuit shown in Figure.
- (a) (3 marks) Find the voltage across each of the resistors.
- (b) (3 marks) Find the current through each of the resistors.
- (c) (2 marks) Find the energy stored in the  $3.00\Omega$  resistor.



2. A  $4.00\text{ nF}$  capacitor with an initial charge of  $7.10\text{ }\mu\text{C}$  is discharged through a  $2.30\text{ k}\Omega$  resistor.
- (a) (3 marks) Calculate the current in the resistor  $8.00\text{ }\mu\text{s}$  after the resistor is connected across the terminals of the capacitor.
- (b) (2 marks) What charge remains on the capacitor after  $7.00\text{ }\mu\text{s}$ ?
- (c) (2 marks) What is the maximum current in the resistor?

$$\boxed{1} \quad I_1 + I_2 = I_3 \quad \text{--- (i)}$$

$$12 - 4I_1 + 5I_2 + I_2 - 4 = 0$$

$$\Rightarrow -4I_1 + 6I_2 = -8 \quad \text{--- (ii)}$$

$$4 - I_2 - 5I_2 - 8I_3 = 0$$

$$\Rightarrow -6I_2 - 8I_3 = -4$$

$$\left. \begin{aligned} I_1 + I_2 - I_3 &= 0 \\ -4I_1 + 6I_2 + 0 &= -8 \\ 0 - 6I_2 - 8I_3 &= -4 \end{aligned} \right\}$$

$$\boxed{b)} \quad I_1 = 1.3\text{ A}; \quad I_2 = -0.46\text{ A};$$

$$I_3 = 0.846\text{ Amp.}$$

$$\boxed{a)} \quad V \text{ across } 8\Omega = 8 \times 0.846 = 6.77\text{ V}$$

$$V \text{ u } 5\Omega = 5 \times 0.46 = 2.3\text{ V}$$

$$V \text{ u } 1\Omega = 1 \times 0.46 = 0.46\text{ V}$$

$$V \text{ u } 3\Omega = 3 \times 1.3 = 3.9\text{ V}$$

$$V \text{ u } 1\Omega = 1 \times 1.3 = 1.3\text{ V}$$

$$\boxed{c)} \quad P \text{ across } 3\Omega = I^2 R = (1.3)^2 \times 3$$

$$= 5.07\text{ W}$$

(Ans.)

$$\boxed{2} \quad a) \quad I = \frac{Q_0}{RC} e^{-t/RC}$$

$$\Rightarrow I = \frac{7.1 \times 10^{-6}}{2.3 \times 10^3 \times 4 \times 10^{-9}} e^{-\frac{8 \times 10^{-6}}{2.3 \times 10^3 \times 4 \times 10^{-9}}}$$

$$= 0.32\text{ Amp}$$

$$b) \quad Q = Q_0 e^{-t/RC}$$

$$= 7.1 \times 10^{-6} \times e^{-\frac{7 \times 10^{-6}}{2.3 \times 10^3 \times 4 \times 10^{-9}}}$$

$$= 3.32 \times 10^{-6}\text{ C}$$

$$c) \quad I_{\text{max}} = \frac{Q_0}{RC}$$

$$= \frac{7.1 \times 10^{-6}}{2.3 \times 10^3 \times 4 \times 10^{-9}}$$

$$= 0.77\text{ Amp.}$$



3. Calculate:

(a) (3 marks) the current in  $2\Omega$  resistor.

(b) (2 marks) the current in  $6\Omega$  resistor?

$$I_1 = I_2 + I_3$$

$$12 - 2I_3 - 4I_1 = 0$$

$$8 - 6I_2 + 2I_3 = 0$$

$$I_1 - I_2 - I_3 = 0 \quad \text{--- (i)}$$

$$-4I_1 - 2I_3 = -12 \quad \text{--- (ii)}$$

$$-6I_2 + 2I_3 = -8 \quad \text{--- (iii)}$$

Solving (i), (ii), (iii)  $\Rightarrow$

$$I_1 = 2.55 \text{ Amp}$$

$$I_2 = 1.64 \text{ Amp} \quad \text{across } 6\Omega$$

$$I_3 = 0.91 \text{ Amp} \quad \text{across } 2\Omega$$

(Ans.)

