

# CH-9 GRAPH

$G(V, E)$

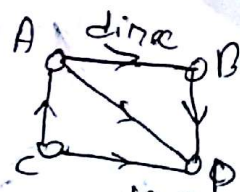
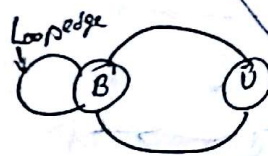
Vertices  $\rightarrow$  Node  
Edge  $\rightarrow$  path

A, B, C, D  $\rightarrow$  vertices

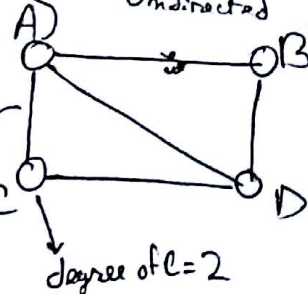
A  $\rightarrow$  B - Edge  
or  
A — B - Edge

Simple graph  
 $\rightarrow$  only one Edge between two vertices

Multigraph  
If more than 1 edge between 2 vertices

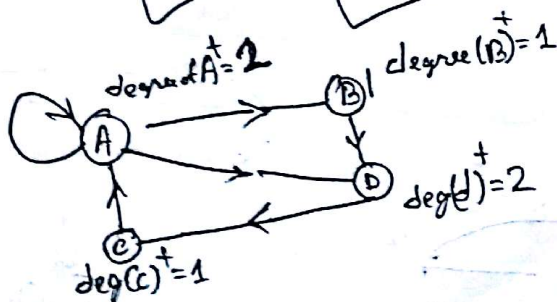
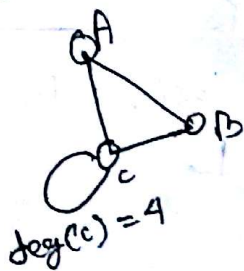


degree of A = 3  
Undirected



Degree } Undirected

Directed graph  
{ In degree  
Out degree

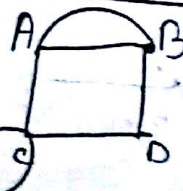


For ~~simple~~ undirected graph  
Add All the degree  
No of Edge =  $\frac{3 + 3 + 2 + 2}{2} = \frac{10}{2} = 5$

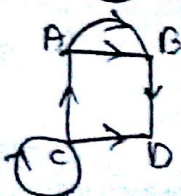
$\circ =$  in degree  
No of edge = sum of degree  $\div 2$

## Graph Representation

- Adjacency list
- Adjacency Matrix
- Incidence list



Adjacency list	
A	B, C, D
B	A, D, C
C	A, D, B
D	B, C

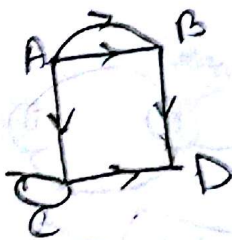


Adj List	
A	B
B	A
C	A, D
D	

# Adjacency Matrix

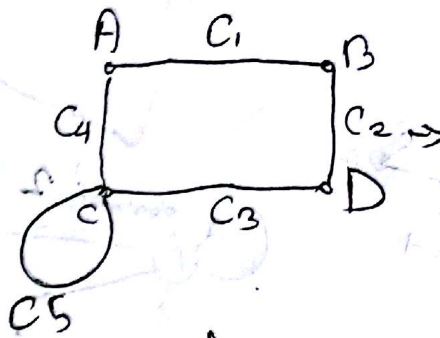


	A	B	C	D
A	0	2	1	0
B	2	0	0	1
C	1	0	1	1
D	0	1	1	0

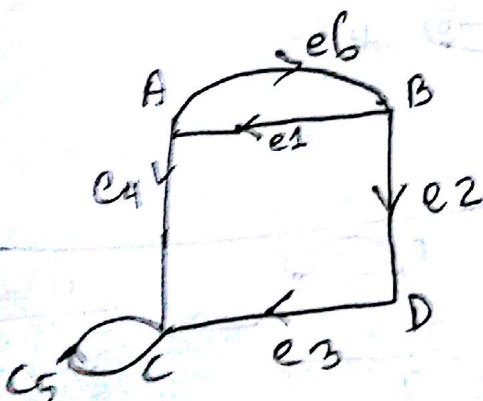


	A	B	C	D
A	0	2	1	0
B	0	0	0	1
C	0	0	1	1
D	0	0	0	0

## Incidence List



	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	C <sub>5</sub>
A	1	0	0	1	0
B	1	1	0	0	0
C	0	0	1	1	1
D	0	1	1	0	0



Let  
out  $\rightarrow$  1  
in  $\rightarrow$  -1

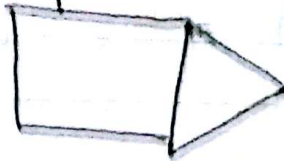
	e <sub>1</sub>	e <sub>2</sub>	e <sub>3</sub>	e <sub>4</sub>	e <sub>5</sub>	e <sub>6</sub>
A	-1	0	0	1	0	1
B	1	1	0	0	0	-1
C	0	0	-1	-1	1	0
D	0	-1	1	0	0	0



Connects graph

edge

Euler path

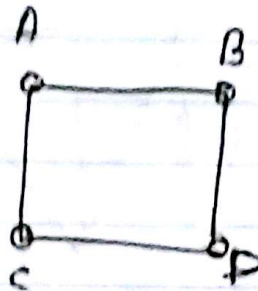


No edge is repeated

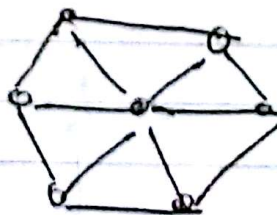
Euler circuit → Visit each <sup>once</sup> edge and come back to start.

Hamilton Circuit

vertex



each vertex visited 1 time and not



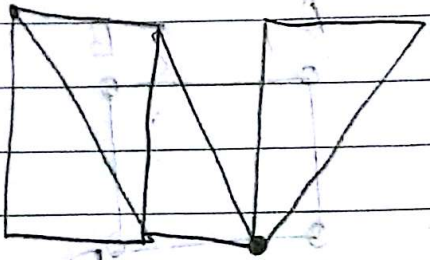
Not Euler Circuit

but Hamilton circuit and not

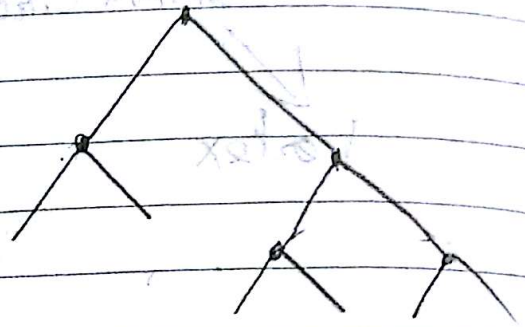
CH-10

Trees

A

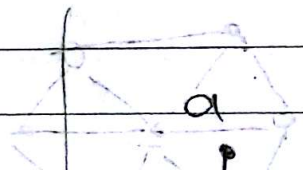


(connected graph, but not tree)



Tree

$G_2$



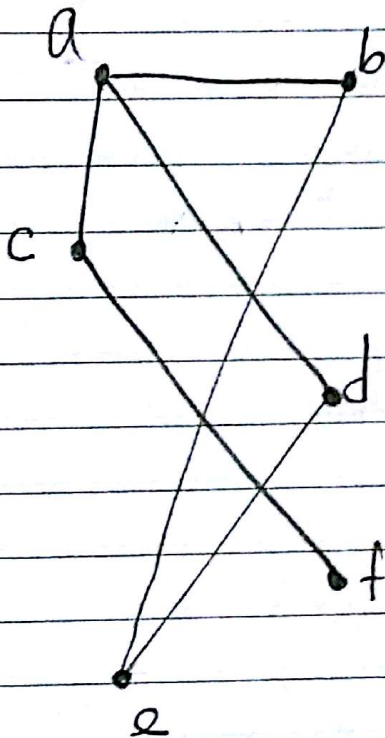
$G_1$

# N 2 and 9 in Mgt 211

Total mark - 40

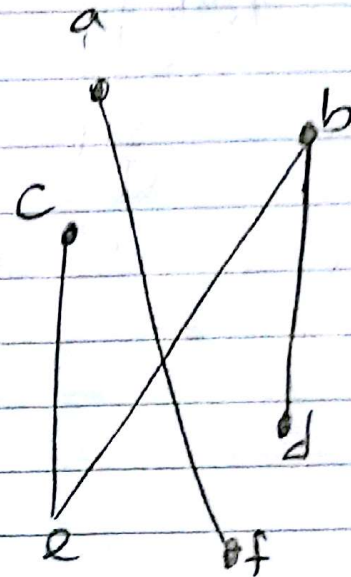
Case:

G3



abcd has cycle  
so not a tree

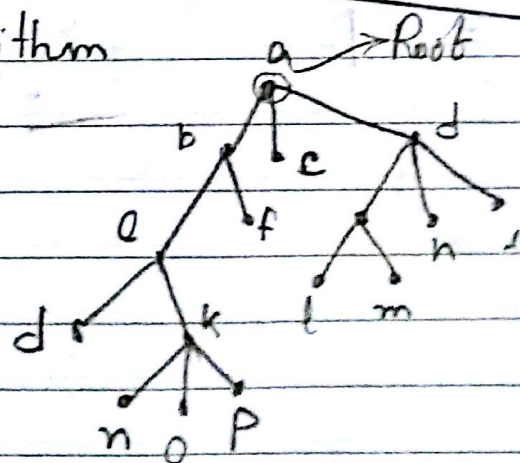
G4



disconnected

so  
not a tree

Traversal Algorithm



Pre-order: root, left, right  
In-order: left, root, right  
Post-order: left, right, root

a b e i k n o p f c d g l m h j



In: j e k n k o p b f a c

l g m d h i

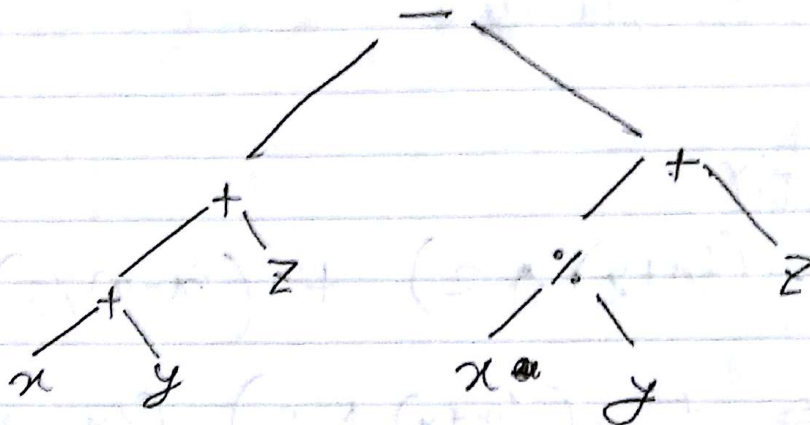
Post  $\rightarrow$  ~~R s t~~

Left Right root

~~root~~  
 $\rightarrow$  self

Rooted tree

$$\{(x+y)+z\} - \{(x\%y)+z\}$$



Infix, prefix, postfix

Date:

Sat ☐ Sun ☐ Mon ☐ Tue ☐ Wed ☐ Thu ☐ Fri

$$\sim x/(y/z)$$

$$\rightarrow = x/(1/yz)$$

$$= 1/x / yz$$



$$\begin{aligned}
 & ((x+y)^2) + ((x-4)/3) \\
 &= ((x+y)^2) + ((x-4)/3) + \\
 &= (x+y)^2 + (x-4)/3 + \\
 &= xy + 2 + x - 4 - 3/ +
 \end{aligned}$$

Pre fix

$$+ - * 235 / \uparrow 2 34$$

$$= + - 65 / 84$$

$$= + 1 / 84$$

$$= + 1 / 84$$

$$= + 1 2$$

$$= 3$$



Post fix

$$723 * - 4 \uparrow 93 / +$$

$$= 76 - 4 \uparrow 3 +$$

$$= 14 \uparrow 3 +$$

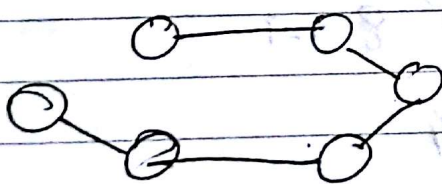
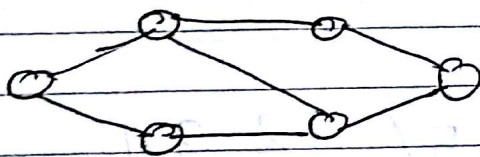
$$= 13 +$$

$$= 4$$

- Spanning tree

- Minimum Cost Spanning Tree

Graph to tree convert



spanning tree

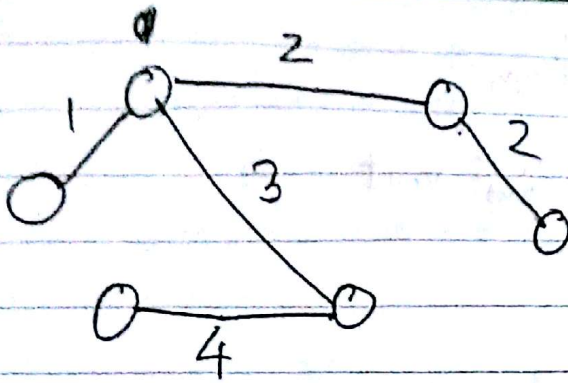
a graph can have  
multiple spanning  
tree



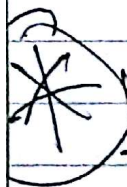
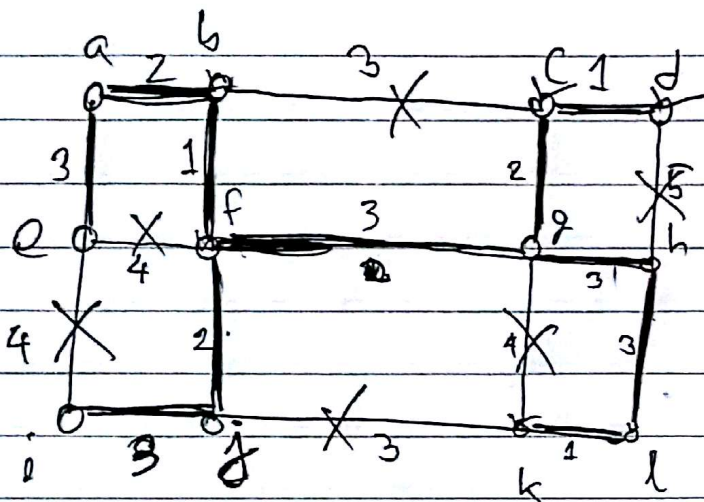
Subject:

Date:

Sat Sun Mon Tue Wed Thu Fri



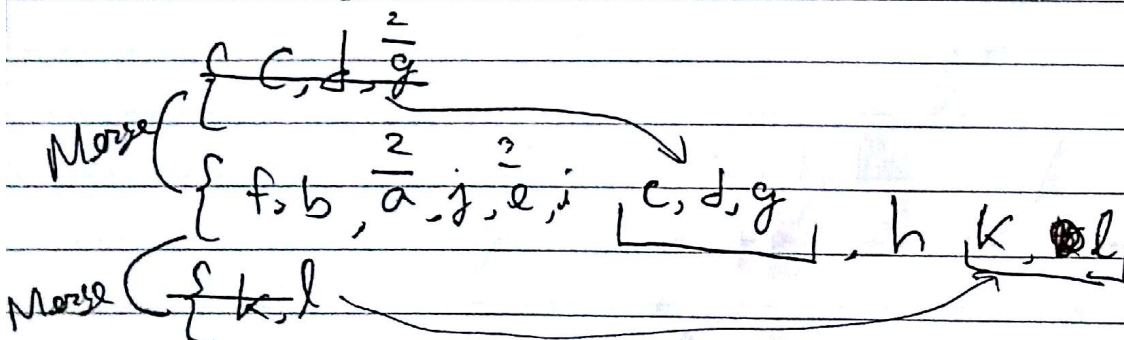
min cost spanning tree



Kruskal Algo

\* go to weight least the start then gradually make sets

1



sum of weights = minimum cost  
can have different type.  
but cost is one.

Papers King

Scanned by CamScanner

Subject:

Date:

Sat ☐ Sun ☐ Mon ☐ Tue ☐ Wed ☐ Thu ☐ Fri

Circuit  $\rightarrow$  has to return to starting node after visiting all nodes

path  $\rightarrow$  don't return <sup>to start node</sup> just visit

all the Nodes