



**KING FAHD UNIVERSITY OF PETROLEUM &  
MINERALS**

**BUSINESS SCHOOL**

**DEPARTMENT OF INFORMATION SYSTEM &  
OPERATIONS MANAGEMENT**

**MANAGEMENT SCIENCE OM 511**

**02 – Optimization Modelling – Graphical Method**

**DHAHRAN, SAUDI ARABIA**

# amazon logistics



## SUPPLY CHAIN

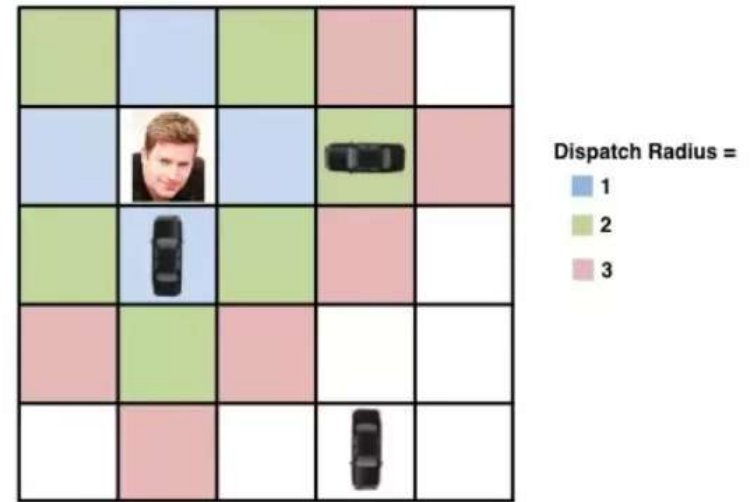
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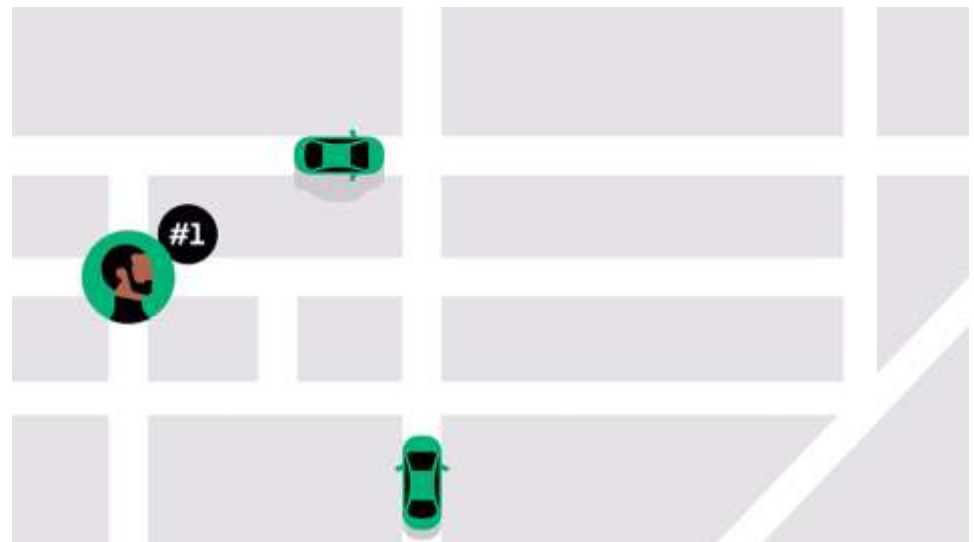
## Uberg



Good morning, Sergio

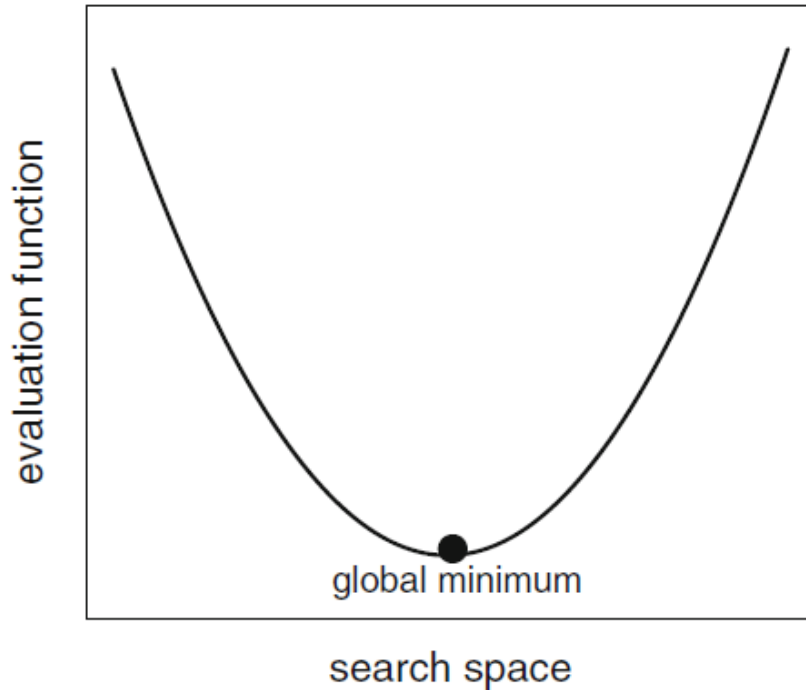
Where to?

Now





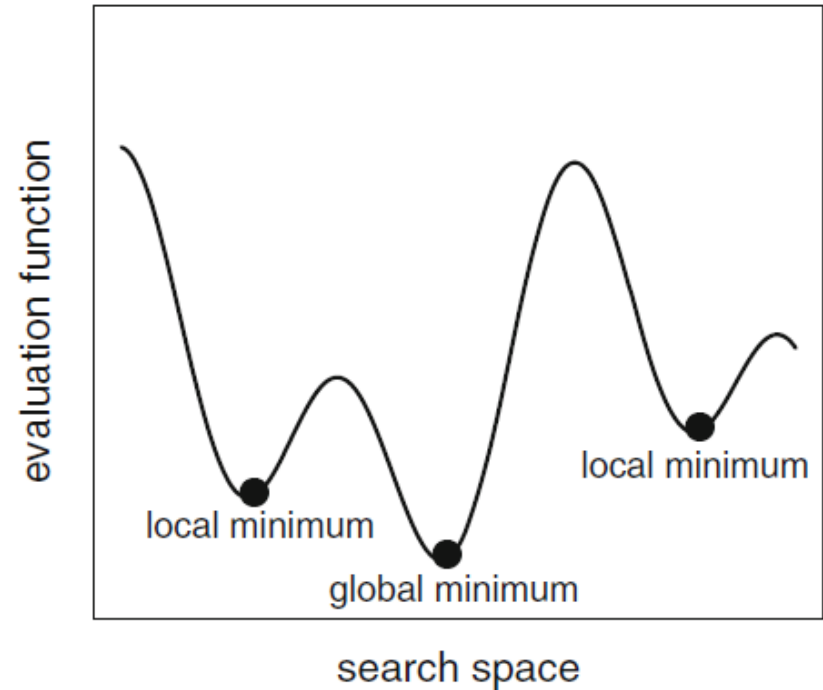
Convex



Linear programming

A convex function curves upwards, and any local minimum is also a global minimum.

Non - Convex



Non - Linear programming

A non-convex function may have regions where it curves downwards or contains multiple local minima and maxima



# Problem formulation

The process of translating the **verbal statement of a problem into a mathematical statement.**

Formulating models is an art that can only be mastered with practice and experience.

Even though every problem has some unique features, most problems also have common features

# Problem formulation

Some practical advices before starting

- Understand the problem thoroughly
- Describe the objective (max, min, punctual?)
- Identify the number of constraints
- Describe each constraint
- Define the Decision Variables
- Write the Objective in Terms of the Decision Variables
- Write the Constraints in Terms of the Decision Variables



# Practical example

The director of manufacturing analysed each of the operations and concluded that if the company produces a medium-priced standard model, each bag will require  $\frac{7}{10}$  hour in the cutting and dyeing department, 1.0 hour in the sewing department, 1.0 hour in the finishing department, and  $\frac{1}{10}$  hour in the inspection and packaging department. The more expensive deluxe model will require 1.0 hour for cutting and dyeing,  $\frac{5}{6}$  hour for sewing,  $\frac{2}{3}$  hour for finishing, and  $\frac{1}{4}$  hour for inspection and packaging.

Department	Production Time (hours)	
	Standard Bag	Deluxe Bag
Cutting and Dyeing	$\frac{7}{10}$	1
Sewing	$\frac{1}{2}$	$\frac{5}{6}$
Finishing	1	$\frac{2}{3}$
Inspection and Packaging	$\frac{1}{10}$	$\frac{1}{4}$



# Practical example

$$\text{Max } 10S + 9D$$

subject to (s.t.)

$$\frac{7}{10}S + 1D \leq 630 \quad \text{Cutting and dyeing}$$

$$\frac{1}{2}S + \frac{5}{6}D \leq 600 \quad \text{Sewing}$$

$$1S + \frac{2}{3}D \leq 708 \quad \text{Finishing}$$

$$\frac{1}{10}S + \frac{1}{4}D \leq 135 \quad \text{Inspection and packaging}$$

$$S, D \geq 0$$

# Graphical method



- **What is Linear Programming?**
  - A mathematical technique for optimizing (maximizing or minimizing) a linear objective function, subject to a set of linear constraints.
- **Purpose of the Graphical Method:**
  - A visual approach to solving linear programming problems **with two decision variables**.
  - Helps in finding the optimal solution by visually representing constraints and identifying the feasible region.

# Graphical method

## Five step approach for solving LP problems through the graphical method



### Step 1: Define the Problem

- Identify the objective function and constraints.



### Step 2: Plot the Constraints

- Convert each inequality constraint into an equation.
- Plot each equation on a graph with decision variables



### Step 3: Identify the Feasible Region

- The feasible region is where all the constraints overlap.
- Represents all possible solutions that satisfy the constraints.



### Step 4: Locate the Corner Points

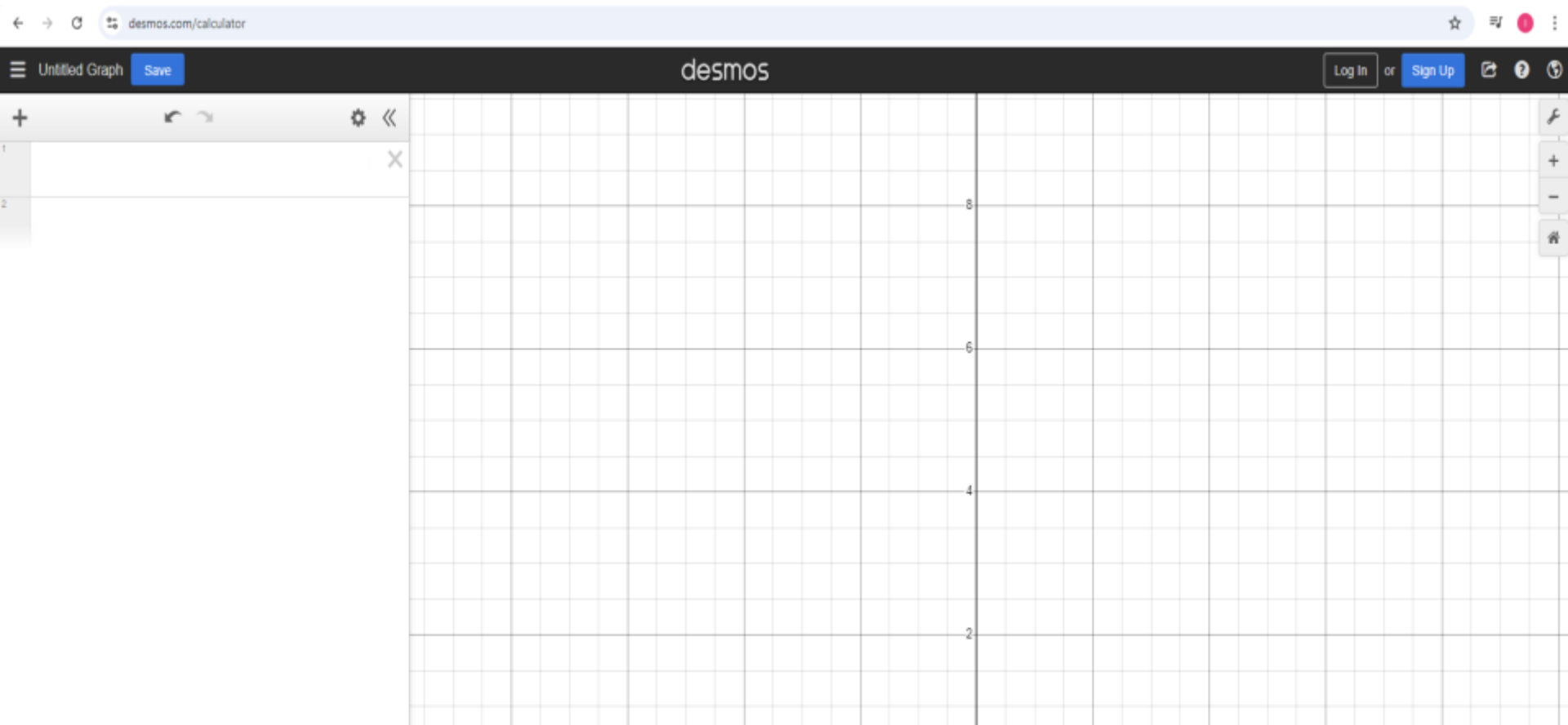
- The optimal solution lies at one of the corner points (vertices) of the feasible region.
- Find these points by calculating the intersection of the constraint lines.



### Step 5: Evaluate the Objective Function

- Calculate the value of the objective function at each corner point.
- The point that gives the highest (or lowest, if minimizing) value is the optimal solution.

# Graphical method



<https://www.desmos.com/calculator>

# Graphical method

- **Problem Statement:**

- Maximize  $Z=10S + 9D$

- Subject to:

$$\frac{7}{10}S + 1D \leq 630 \quad \text{Cutting and dyeing}$$

$$\frac{1}{2}S + \frac{5}{6}D \leq 600 \quad \text{Sewing}$$

$$1S + \frac{2}{3}D \leq 708 \quad \text{Finishing}$$

$$\frac{1}{10}S + \frac{1}{4}D \leq 135 \quad \text{Inspection and packaging}$$

$$S, D \geq 0$$

- **Graphical Representation:**

- Show a simple graph with constraints plotted as lines.
- Highlight the feasible region where all constraints overlap.

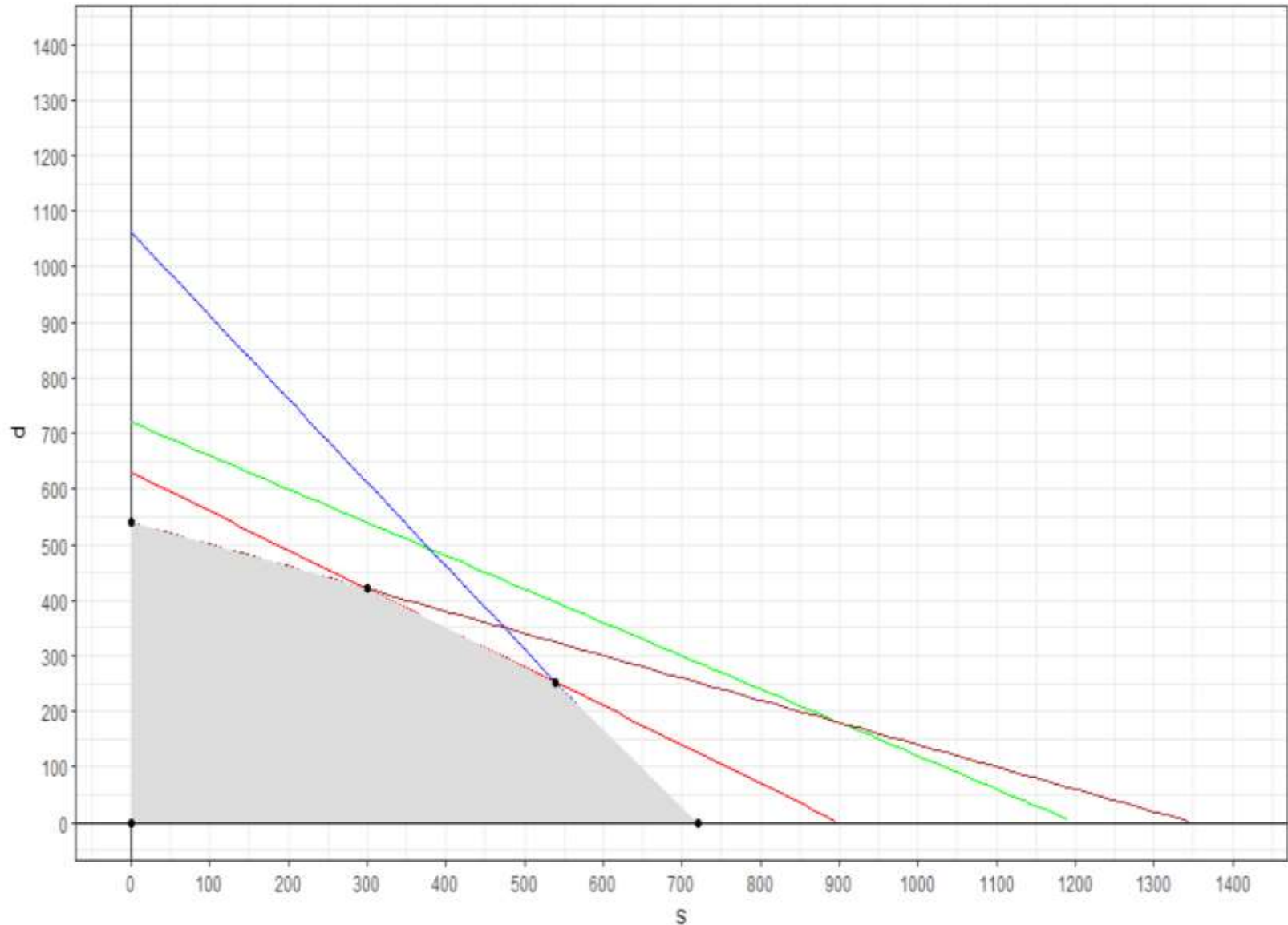
- **Solution:**

- Indicate the corner points of the feasible region.
- Show the calculation of the objective function at each point.
- Identify the optimal solution based on the highest value of  $Z$ .

<https://www.desmos.com/calculator>

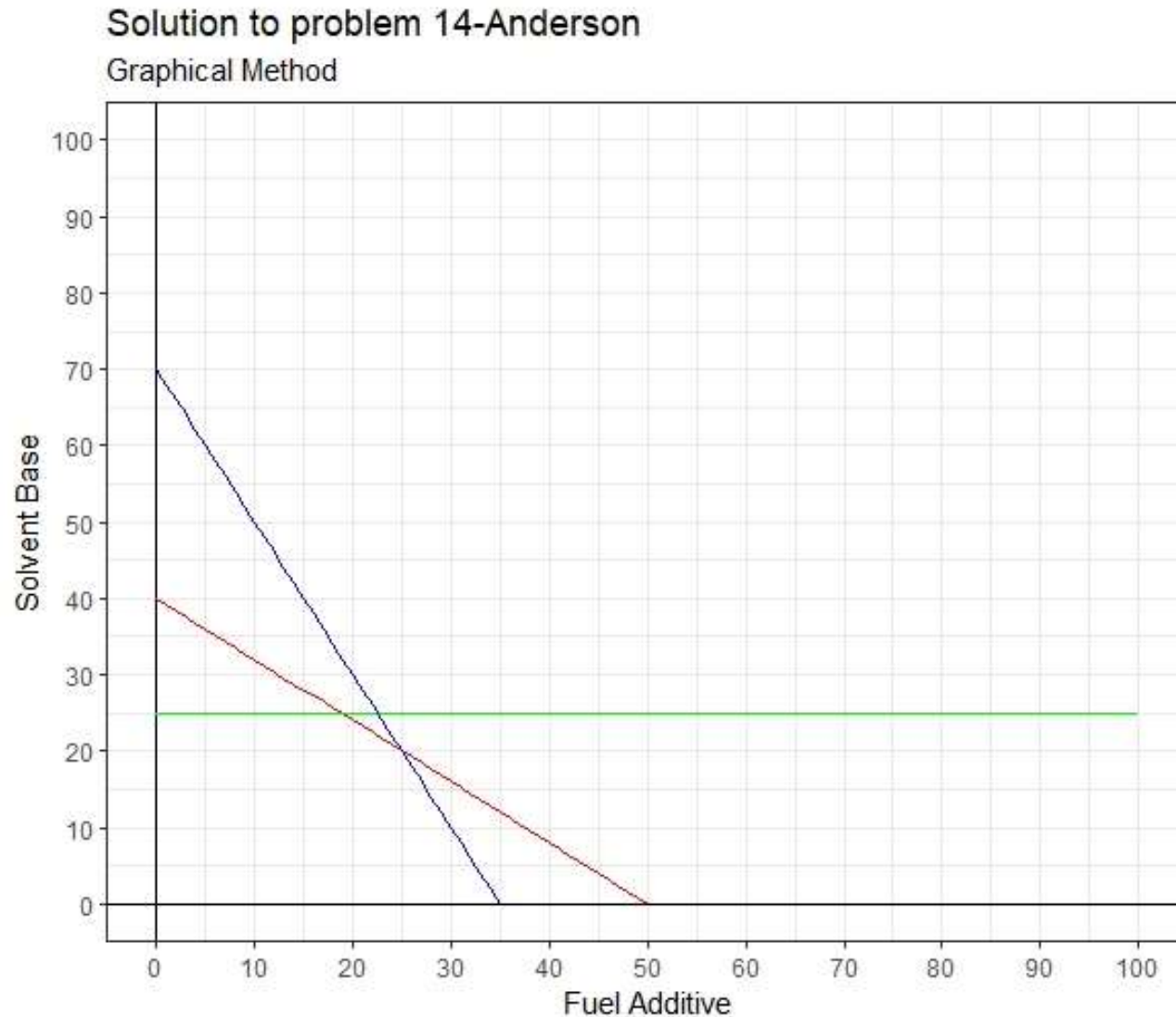


# Solution problem in page 33, chapter 2, Anderson book. Graphical method

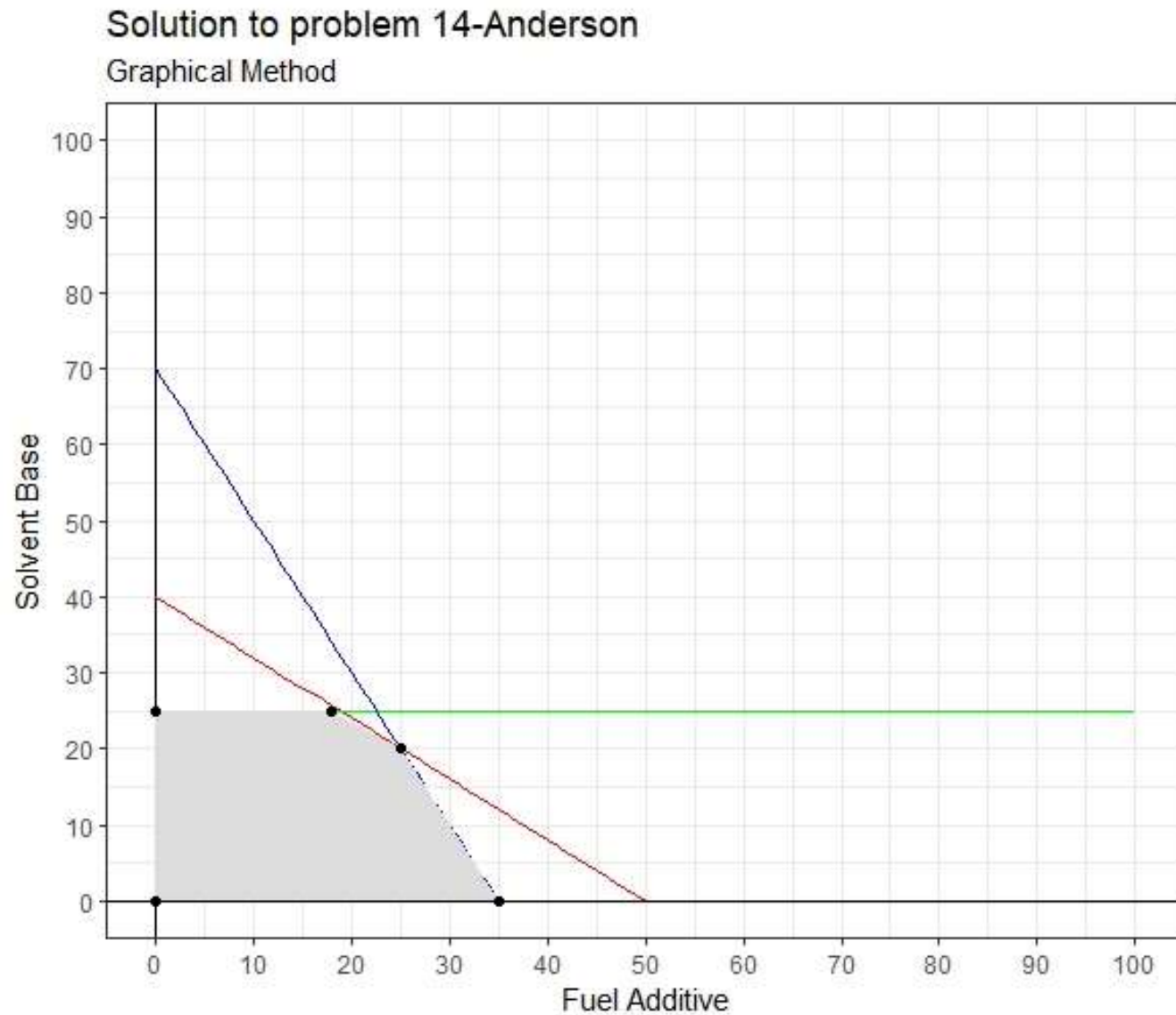




# Solution to problem 14 Anderson book. Graphical Method



# Solution to problem 14 Anderson book. Graphical Method



# Exercise in classroom

Chapter 2. Anderson. Pp 70 #14

RMC, Inc., is a small firm that produces a variety of chemical products. In a particular production process, three raw materials are blended (mixed together) to produce two products: **a fuel additive (F)** and **a solvent base (S)**.

Each ton of **fuel additive (F)** is a mixture of  $\frac{2}{5}$  ton of material 1 and  $\frac{3}{5}$  of material 3. A ton of **solvent base (S)** is a mixture of  $\frac{1}{2}$  ton of material 1,  $\frac{1}{5}$  ton of material 2, and  $\frac{3}{10}$  ton of material 3.

The profit contribution is \$40 for every ton of **fuel additive (F)** produced and \$30 for every ton of **solvent base (S)** produced.

RMC's production is constrained by a limited availability of the three raw materials. For the current production period, RMC has available the following quantities of each raw material:

Raw Material	Amount Available for Production
Material 1	20 tons
Material 2	5 tons
Material 3	21 tons

# Exercise in classroom

Chapter 2. Anderson. Pp 74 #24

Kelson Sporting Equipment, Inc., makes two different types of baseball gloves: a **regular model (R)** and a **catcher's model (C)**. The firm has 900 hours of production time available in its **cutting and sewing department**, 300 hours available in its **finishing department**, and 100 hours available in its **packaging and shipping department**. The production time requirements and the profit contribution per glove are given in the following table:

Model	Production Time (hours)			Profit/Glove
	Cutting and Sewing	Finishing	Packaging and Shipping	
Regular model	1	$\frac{1}{2}$	$\frac{1}{8}$	\$5
Catcher's model	$\frac{3}{2}$	$\frac{1}{3}$	$\frac{1}{4}$	\$8