

Labor Market Analysis

Revised Econometric Model

Marjorie Blanco, Joe Thomson, Haodi Tu

Research Questions

- 1) How do earnings vary by education level?
- 2) How does the premium for education vary by gender?

Revised Model

$$\text{Earning} = \beta_0 + \text{Divorced} * \beta_1 + \text{NeverMarried} * \beta_2 + \text{Female} * \beta_3 + \text{RaceBlack} * \beta_4 + \text{RaceOther} * \beta_5 + \text{SomeCollege} * \beta_6 + \text{Associate} * \beta_7 + \text{Bachelor} * \beta_8 + \text{Master} * \beta_9 + \text{Professional} * \beta_{10} + \text{Doctoral} * \beta_{11} + \text{Age} * \beta_{12}$$

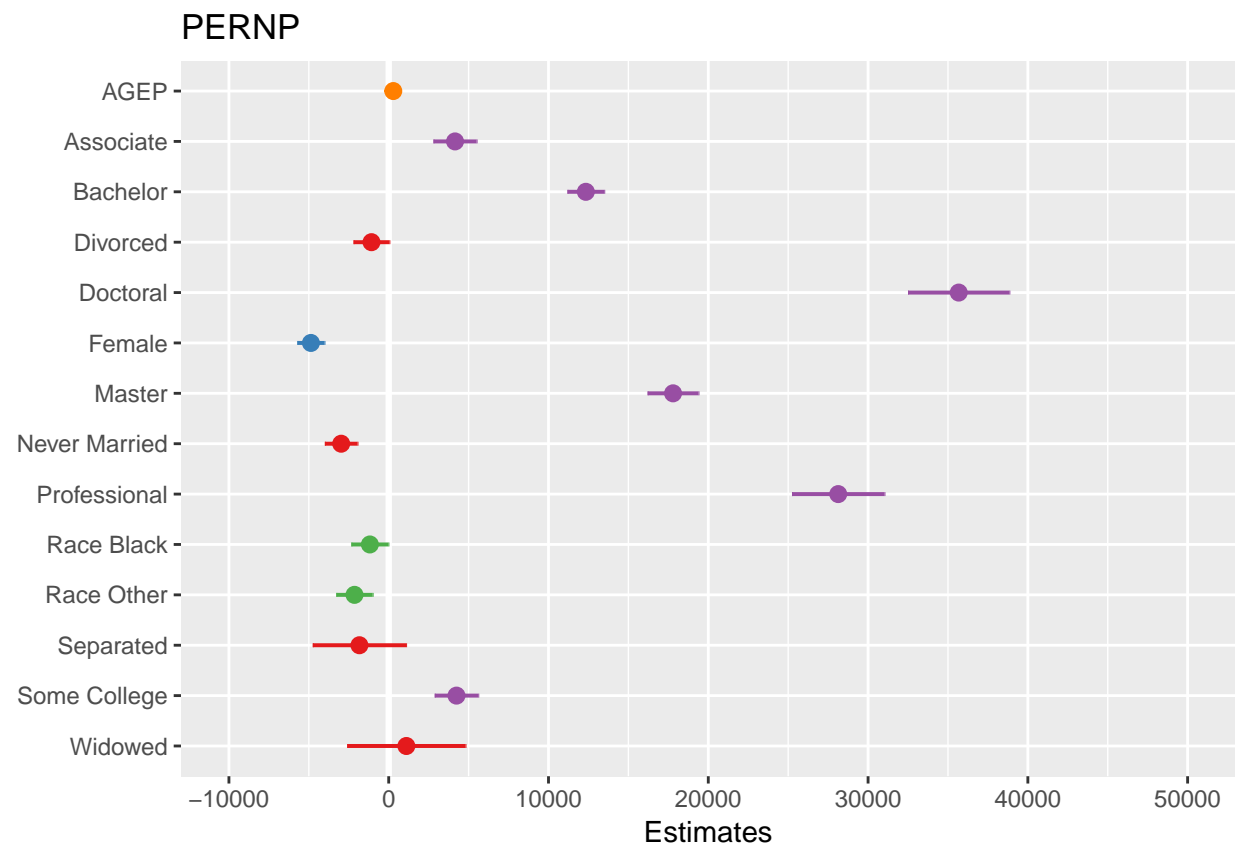
```
##
## Call:
## lm(formula = PERNP ~ Widowed + Divorced + Separated + NeverMarried +
##      Female + RaceBlack + RaceOther + SomeCollege + Associate +
##      Bachelor + Master + Professional + Doctoral + AGE, data = ss16ppr)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -43683  -9228  -2919   5341   98762
##
## Coefficients:
##              Estimate Std. Error t value      Pr(>|t|)
## (Intercept)  12598.97    1110.28  11.348 < 0.0000000000000002 ***
## Widowed       1104.92    1888.02   0.585     0.558422
## Divorced     -1078.74     571.98  -1.886     0.059353 .
## Separated    -1833.17    1489.22  -1.231     0.218393
## NeverMarried -2974.75     520.48  -5.715  0.00000001155 ***
## Female      -4868.47     432.66 -11.252 < 0.0000000000000002 ***
## RaceBlack   -1178.01     591.36  -1.992     0.046421 *
## RaceOther   -2141.04     579.98  -3.692     0.000225 ***
## SomeCollege  4241.63     694.73   6.105  0.00000000110 ***
## Associate    4150.43     688.45   6.029  0.00000000177 ***
## Bachelor    12337.16     587.07  21.015 < 0.0000000000000002 ***
## Master       17795.40     812.61  21.899 < 0.0000000000000002 ***
## Professional 28133.37    1476.36  19.056 < 0.0000000000000002 ***
## Doctoral     35674.46    1617.08  22.061 < 0.0000000000000002 ***
## AGE          284.94       21.12  13.488 < 0.0000000000000002 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 14920 on 5179 degrees of freedom
## Multiple R-squared:  0.2466, Adjusted R-squared:  0.2446
## F-statistic: 121.1 on 14 and 5179 DF,  p-value: < 0.00000000000000022
```

Interpretation

- Coefficients Explanation

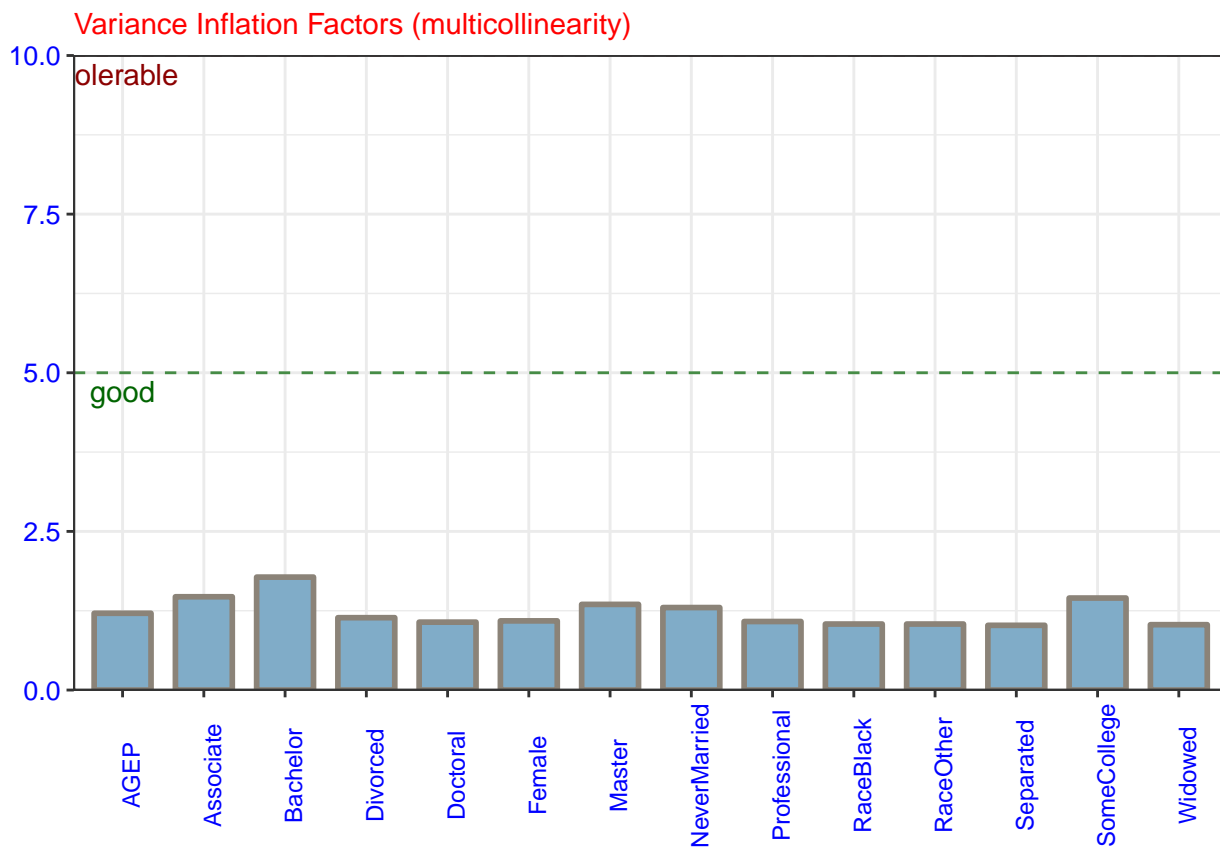
- Holding gender, race, education and age constant, married people makes \$1104.92 less than people who widowed on average.
- Holding gender, race, education and age constant, married people makes \$1078.74 more than people who divorced on average.
- Holding gender, race, education and age constant, married people makes \$1833.17 more than people who separated on average.
- Holding gender, race, education and age constant, married people makes \$2974.75 more than people who never married on average.
- Holding marriage, race, education and age constant, male makes \$4868.47 more than female on average.
- Holding marriage, gender, education and age constant, White makes \$1178.01 more than Black on average.
- Holding marriage, gender, education and age constant, White makes \$2141.04 more than Other race on average.
- Holding marriage, gender, race and age constant, people have high school education makes \$4241.63 less than people have some college education on average.
- Holding marriage, gender, race and age constant, people have high school education makes \$4150.43 less than people have associate education on average.
- Holding marriage, gender, race and age constant, people have high school education makes \$12337.16 less than people have bachelor's degree on average.
- Holding marriage, gender, race and age constant, people have high school education makes \$17795.4 less than people have master's degree on average.
- Holding marriage, gender, race and age constant, people have high school education makes \$28133.37 less than people have Professional education on average.
- Holding marriage, gender, race and age constant, people have high school education makes \$35674.46 less than people have doctor's degree on average.
- Holding marriage, gender, race and education constant, people make \$284.94 more as age increases on average between the age of 18 to 64.

Model Diagnostics



Variables	Tolerance	VIF
Widowed	0.9729050	1.027850
Divorced	0.8808670	1.135245
Separated	0.9756434	1.024965
NeverMarried	0.7702636	1.298257
Female	0.9159123	1.091808
RaceBlack	0.9633247	1.038072
RaceOther	0.9650376	1.036229
SomeCollege	0.6878124	1.453885
Associate	0.6814727	1.467410
Bachelor	0.5604312	1.784341
Master	0.7394234	1.352405
Professional	0.9238792	1.082393
Doctoral	0.9320203	1.072938
AGEP	0.8267426	1.209566

[[1]]

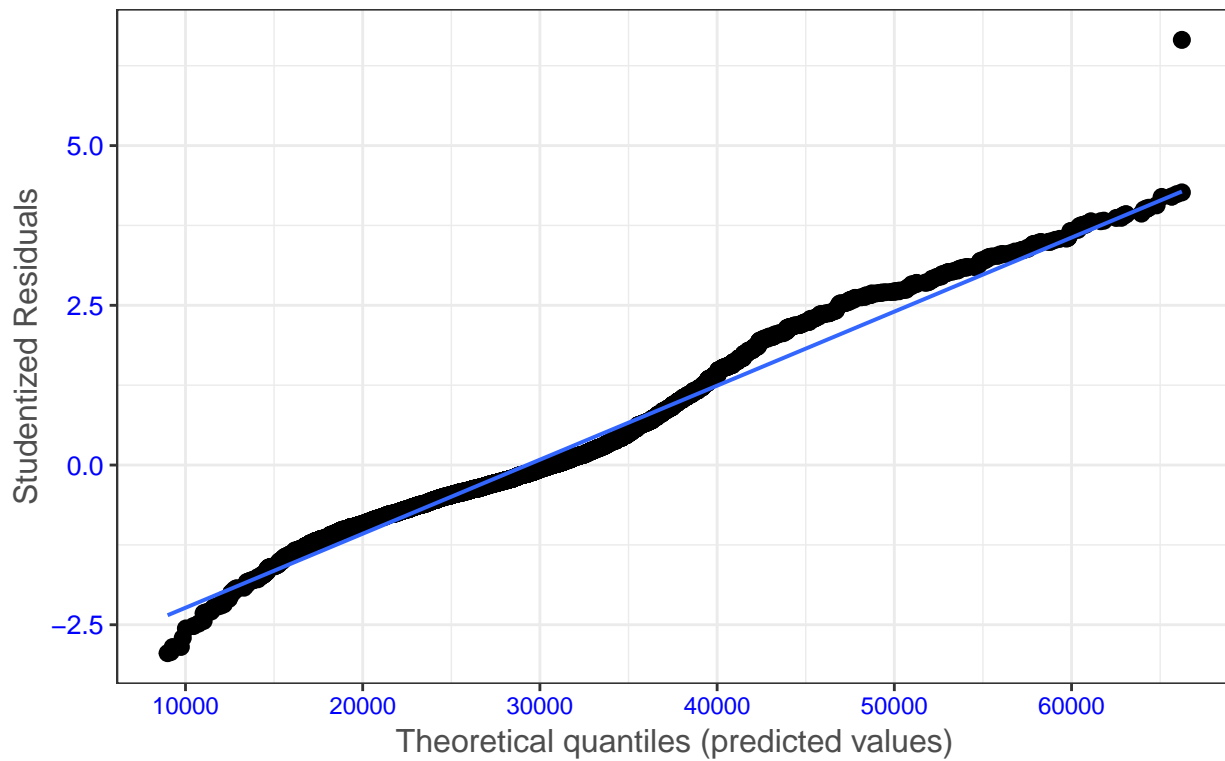


A VIF chart shows that there is no correlation among the kth predictor and the remaining predictor variables.

```
## [[1]]
```

Non-normality of residuals and outliers

Dots should be plotted along the line

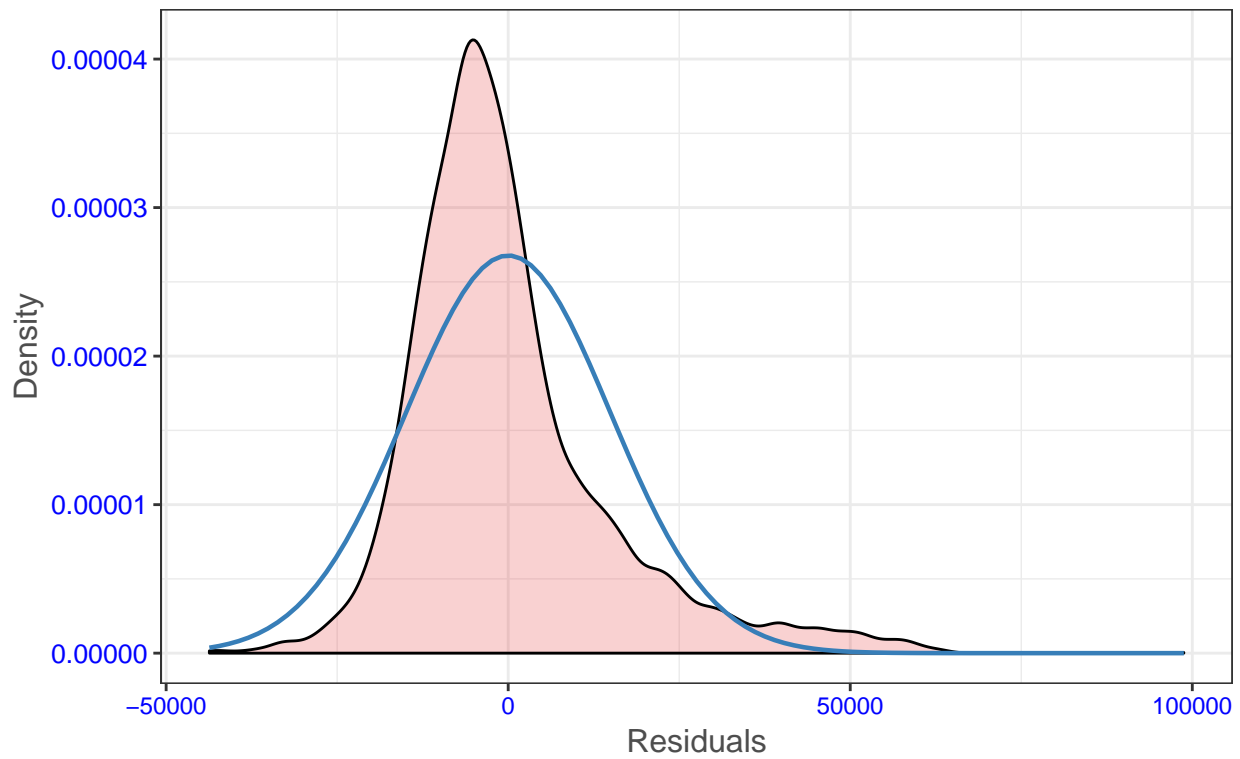


The plot shows that the distribution of the residuals are approximately normally distributed. The “thin tails” correspond to the first quantiles occurring at less than expected values and the last quantiles occurring at larger than expected values.

```
## [[1]]
```

Non-normality of residuals

Distribution should look like normal curve

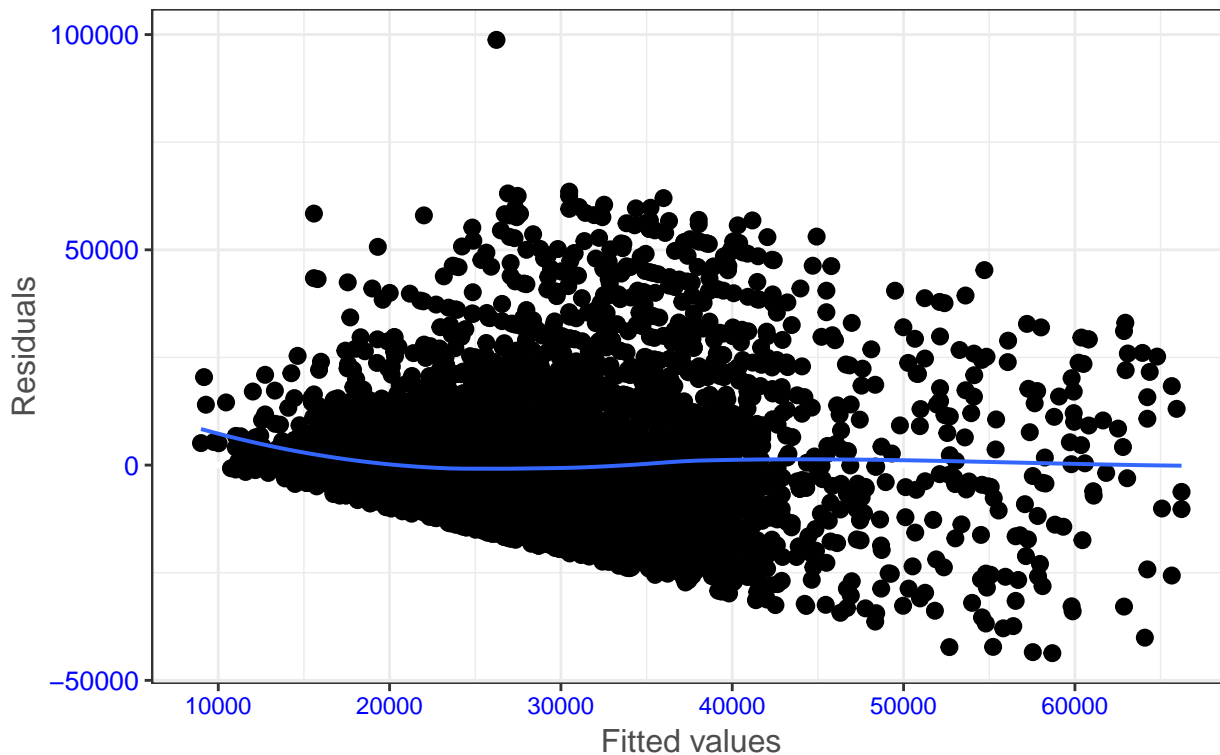


The plot shows that the distribution of the residuals are approximately normally distributed.

```
## [[1]]
```

Homoscedasticity (constant variance of residuals)

Amount and distance of points scattered above/below line is equal or randomly spread



The plot shows heteroscedasticity as the variance of the residuals are not constant.

Breusch-Pagan test

H_0 : Variance is unchanging in the residual

H_1 : Variance is changing in the residual

```
##
## studentized Breusch-Pagan test
##
## data: Model_1
## BP = 297.55, df = 14, p-value < 0.00000000000000022
```

The p-Value < 0.05 which indicates that the null hypothesis (the variance is unchanging in the residual) can be rejected and therefore heteroscedasticity exists.

Revised Model with robust standard errors

```
##
## Call:
## lm(formula = residuals(Model_1) * residuals(Model_1) ~ Widowed +
##     Divorced + Separated + NeverMarried + Female + RaceBlack +
##     RaceOther + SomeCollege + Associate + Bachelor + Master +
##     Professional + Doctoral + AGEp, data = ss16ppr)
##
## Residuals:
```

```

##           Min           1Q           Median           3Q           Max
## -620286278 -187332480 -89004449 -6623206 9554893533
##
## Coefficients:
##           Estimate Std. Error t value      Pr(>|t|)
## (Intercept) -22272288  35096119 -0.635      0.5257
## Widowed      10526294  59680719  0.176      0.8600
## Divorced     -9634464  18080343 -0.533      0.5941
## Separated    -74925738  47074515 -1.592      0.1115
## NeverMarried -41219294  16452372 -2.505      0.0123 *
## Female       -86614125  13676418 -6.333 0.00000000026057555 ***
## RaceBlack    -30492334  18693117 -1.631      0.1029
## RaceOther    -56411117  18333200 -3.077      0.0021 **
## SomeCollege   54139584  21960626  2.465      0.0137 *
## Associate     38592334  21762198  1.773      0.0762 .
## Bachelor     167802881  18557574  9.042 < 0.0000000000000002 ***
## Master       240588080  25686793  9.366 < 0.0000000000000002 ***
## Professional 363259303  46668182  7.784 0.00000000000000843 ***
## Doctoral     283832422  51116425  5.553 0.00000002953675723 ***
## AGEP         4843548    667752    7.254 0.00000000000046605 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 471600000 on 5179 degrees of freedom
## Multiple R-squared:  0.05729,    Adjusted R-squared:  0.05474
## F-statistic: 22.48 on 14 and 5179 DF,  p-value: < 0.00000000000000022

##           (Intercept)      Widowed      Divorced      Separated NeverMarried
## (Intercept)  1007933.05   58087.062 -81847.4203 -49419.377 -267638.579
## Widowed      58087.06  3995751.368 105877.9224  111739.704   61877.649
## Divorced     -81847.42  105877.922 349056.7354  102495.813   95360.449
## Separated    -49419.38  111739.704 102495.8126 1565899.963   91581.434
## NeverMarried -267638.58   61877.649  95360.4487   91581.434  242152.106
## Female       -24269.36 -37296.786 -22584.5663  -9502.521   3535.426
## RaceBlack    -54050.20   4154.512  -261.2336  -1778.827  -1474.294
## RaceOther    -43361.05 -17198.587   3064.7362  28165.922  -2030.508
## SomeCollege  -164587.00   5864.731   2716.6330 -30536.341  -9191.626
## Associate    -156276.57  28238.641  14270.5777  26369.734  16901.438
## Bachelor     -140253.26  58869.676  15822.7991  22192.750  11420.935
## Master       -98238.23  19298.737   4166.7095 -29561.887   4120.858
## Professional -178405.52  47377.351 -9202.0646  36275.425 -25373.156
## Doctoral     -51307.89  115905.356  47855.5908  140337.165  29949.062
## AGEP         -18128.79  -3587.834  -293.0243  -1156.124   3781.175
##
##           Female      RaceBlack      RaceOther      SomeCollege      Associate
## (Intercept) -24269.3559 -54050.20464 -43361.053 -164587.002 -156276.572
## Widowed     -37296.7857   4154.51196 -17198.587   5864.731  28238.641
## Divorced    -22584.5663  -261.23364   3064.736   2716.633  14270.578
## Separated   -9502.5212  -1778.82702  28165.922 -30536.341  26369.734
## NeverMarried  3535.4265  -1474.29397  -2030.508  -9191.626  16901.438
## Female      194048.3723  -8630.04524  -8397.285  -29487.201 -42117.858
## RaceBlack   -8630.0452  315761.19749  66096.740  -10264.752  -6036.723
## RaceOther   -8397.2851  66096.74016  278637.804   3569.363  -4820.559
## SomeCollege -29487.2014 -10264.75223   3569.363  332091.081  125594.576
## Associate   -42117.8578  -6036.72309  -4820.559  125594.576  319016.024
## Bachelor    -78511.6369   6202.41918 -10349.806  130275.001  135533.527
## Master      -92998.9918  -6855.66175  28720.700  131019.704  135614.524
## Professional -48793.0798  28726.41028  17513.253  130357.805  129838.545

```



```

## Doctoral      -37589.1845    758.93490  80827.611  112338.880  124924.530
## AGEP          -787.2688     -97.32446   -420.435   1437.587   1046.660
##              Bachelor      Master Professional      Doctoral
## (Intercept)  -140253.2646  -98238.2349  -178405.520  -51307.8937
## Widowed      58869.6759   19298.7370    47377.351   115905.3561
## Divorced     15822.7991    4166.7095   -9202.065    47855.5908
## Separated    22192.7500  -29561.8868    36275.425   140337.1654
## NeverMarried 11420.9348    4120.8577   -25373.156   29949.0622
## Female       -78511.6369  -92998.9918   -48793.080   -37589.1845
## RaceBlack    6202.4192   -6855.6618    28726.410    758.9349
## RaceOther   -10349.8064   28720.6998    17513.253    80827.6113
## SomeCollege 130275.0011  131019.7043   130357.805   112338.8799
## Associate    135533.5269  135614.5236   129838.545   124924.5305
## Bachelor     307695.2759  152567.2493   140083.610   133715.9622
## Master       152567.2493  847427.5870   140245.690   140031.3156
## Professional 140083.6102  140245.6899   4394423.380   124345.5782
## Doctoral     133715.9622  140031.3156   124345.578  4770075.3429
## AGEP         949.8206     127.4089     1732.881    -2150.9231
##              AGEP
## (Intercept) -18128.78819
## Widowed     -3587.83358
## Divorced    -293.02429
## Separated   -1156.12421
## NeverMarried 3781.17492
## Female      -787.26885
## RaceBlack   -97.32446
## RaceOther   -420.43504
## SomeCollege 1437.58685
## Associate    1046.66000
## Bachelor     949.82059
## Master       127.40891
## Professional 1732.88105
## Doctoral    -2150.92312
## AGEP        413.64705

## (Intercept)      Widowed      Divorced      Separated NeverMarried
## 1003.95869      1998.93756      590.81024      1251.35925      492.08953
##      Female      RaceBlack      RaceOther SomeCollege      Associate
## 440.50922      561.92633      527.86154      576.27344      564.81504
##      Bachelor      Master Professional      Doctoral      AGEP
## 554.70287      920.55830      2096.28800      2184.05022      20.33831

```

Revised Logarithmic Model

$$\text{Log}(\text{Earning}) = \beta_0 + \text{Divorced} * \beta_1 + \text{NeverMarried} * \beta_2 + \text{Female} * \beta_3 + \text{RaceBlack} * \beta_4 + \text{RaceOther} * \beta_5 + \text{SomeCollege} * \beta_6 + \text{Associate} * \beta_7 + \text{Bachelor} * \beta_8 + \text{Master} * \beta_9 + \text{Professional} * \beta_{10} + \text{Doctoral} * \beta_{11} + \text{Age} * \beta_{12}$$

```

##
## Call:
## lm(formula = log(PERNP, base = exp(1)) ~ Widowed + Divorced +
##      Separated + NeverMarried + Female + RaceBlack + RaceOther +
##      SomeCollege + Associate + Bachelor + Master + Professional +
##      Doctoral + AGEP, data = ss16ppr)
##
## Residuals:

```

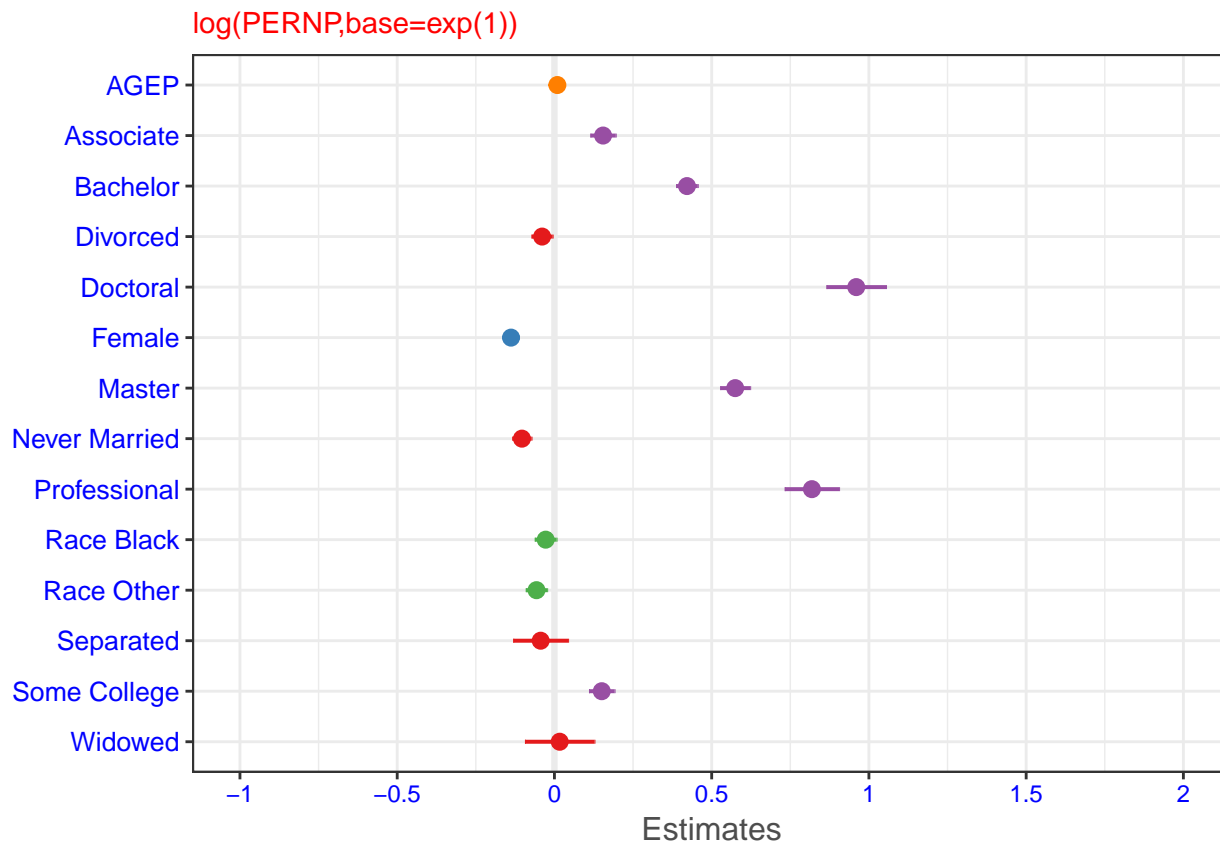
```
##      Min      1Q   Median      3Q      Max
## -1.56195 -0.30715 -0.03111  0.27690  1.69792
##
## Coefficients:
##              Estimate Std. Error t value      Pr(>|t|)
## (Intercept)   9.5841704  0.0331471 289.140 < 0.0000000000000002 ***
## Widowed       0.0167914  0.0563665   0.298    0.765794
## Divorced      -0.0391735  0.0170763  -2.294    0.021829 *
## Separated     -0.0437489  0.0444603  -0.984    0.325162
## NeverMarried -0.1033310  0.0155387  -6.650  0.00000000000323503 ***
## Female       -0.1380595  0.0129169 -10.688 < 0.0000000000000002 ***
## RaceBlack    -0.0278297  0.0176550  -1.576    0.115017
## RaceOther    -0.0570606  0.0173151  -3.295    0.000989 ***
## SomeCollege   0.1505241  0.0207411   7.257  0.00000000000004534 ***
## Associate     0.1546604  0.0205537   7.525  0.00000000000000619 ***
## Bachelor     0.4214137  0.0175270  24.044 < 0.0000000000000002 ***
## Master        0.5748312  0.0242603  23.694 < 0.0000000000000002 ***
## Professional  0.8187333  0.0440766  18.575 < 0.0000000000000002 ***
## Doctoral     0.9597258  0.0482778  19.879 < 0.0000000000000002 ***
## AGE          0.0092656  0.0006307  14.692 < 0.0000000000000002 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4454 on 5179 degrees of freedom
## Multiple R-squared:  0.2556, Adjusted R-squared:  0.2536
## F-statistic: 127 on 14 and 5179 DF, p-value: < 0.00000000000000022
```

Interpretation

- Coefficients Explanation
- Holding gender, race, education and age constant, married people makes 1.69% less than people who widowed on average.
- Holding gender, race, education and age constant, married people makes 3.84% more than people who divorced on average.
- Holding gender, race, education and age constant, married people makes 4.28% more than people who separated on average.
- Holding gender, race, education and age constant, married people makes 9.82% more than people who never married on average.
- Holding marriage, race, education and age constant, male makes 12.9% more than female on average.
- Holding marriage, gender, education and age constant, White makes 2.74% more than Black on average.
- Holding marriage, gender, education and age constant, White makes 5.55% more than Other race on average.
- Holding marriage, gender, race and age constant, people have high school education makes 16.24% less than people have some college education on average.
- Holding marriage, gender, race and age constant, people have high school education makes 16.73% less than people have associate education on average.
- Holding marriage, gender, race and age constant, people have high school education makes 52.41% less than people have bachelor's degree on average.

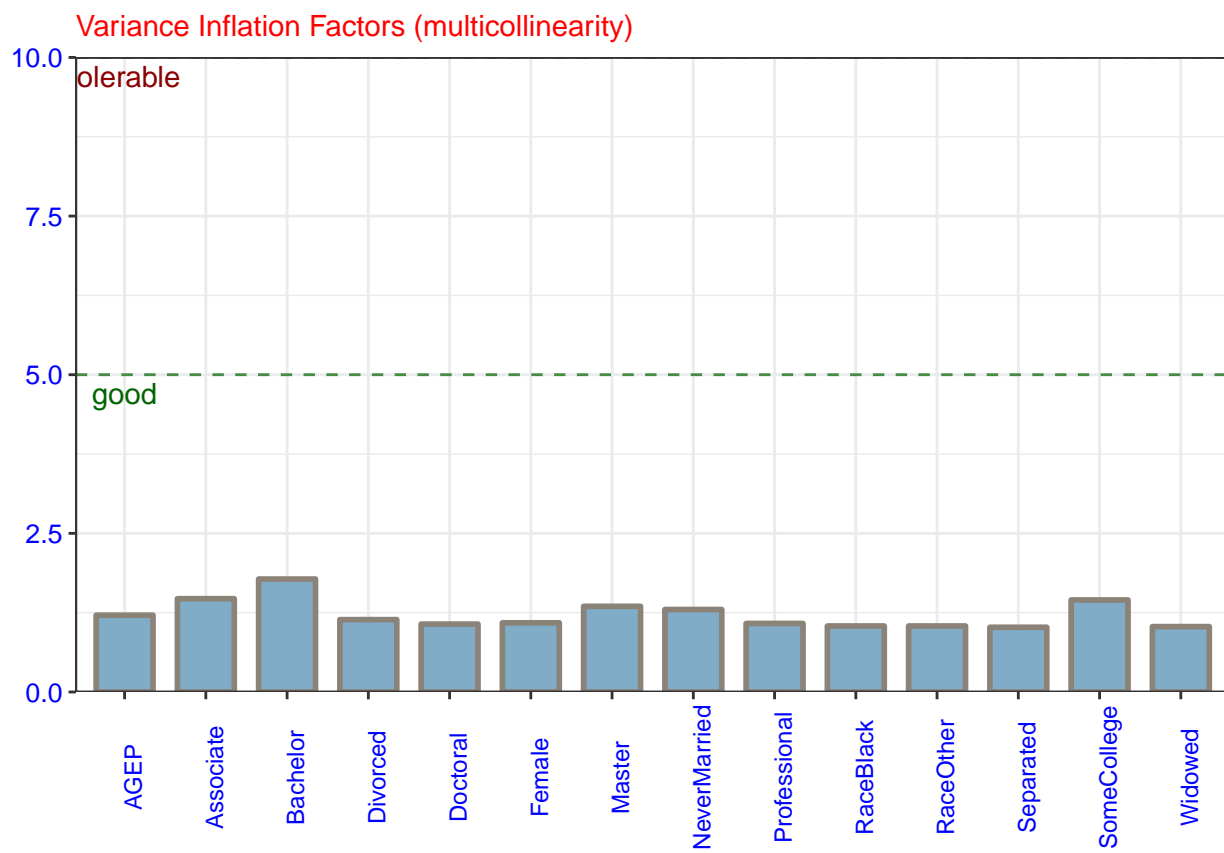
- Holding marriage, gender, race and age constant, people have high school education makes 77.68% less than people have master's degree on average.
- Holding marriage, gender, race and age constant, people have high school education makes 126.76% less than people have Professional education on average.
- Holding marriage, gender, race and age constant, people have high school education makes 161.1% less than people have doctor's degree on average.
- Holding marriage, gender, race and education constant, people make 0.93% more as age increases on average between the age of 18 to 64.

Model Diagnostics



Variables	Tolerance	VIF
Widowed	0.9729050	1.027850
Divorced	0.8808670	1.135245
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```
## [[1]]
```

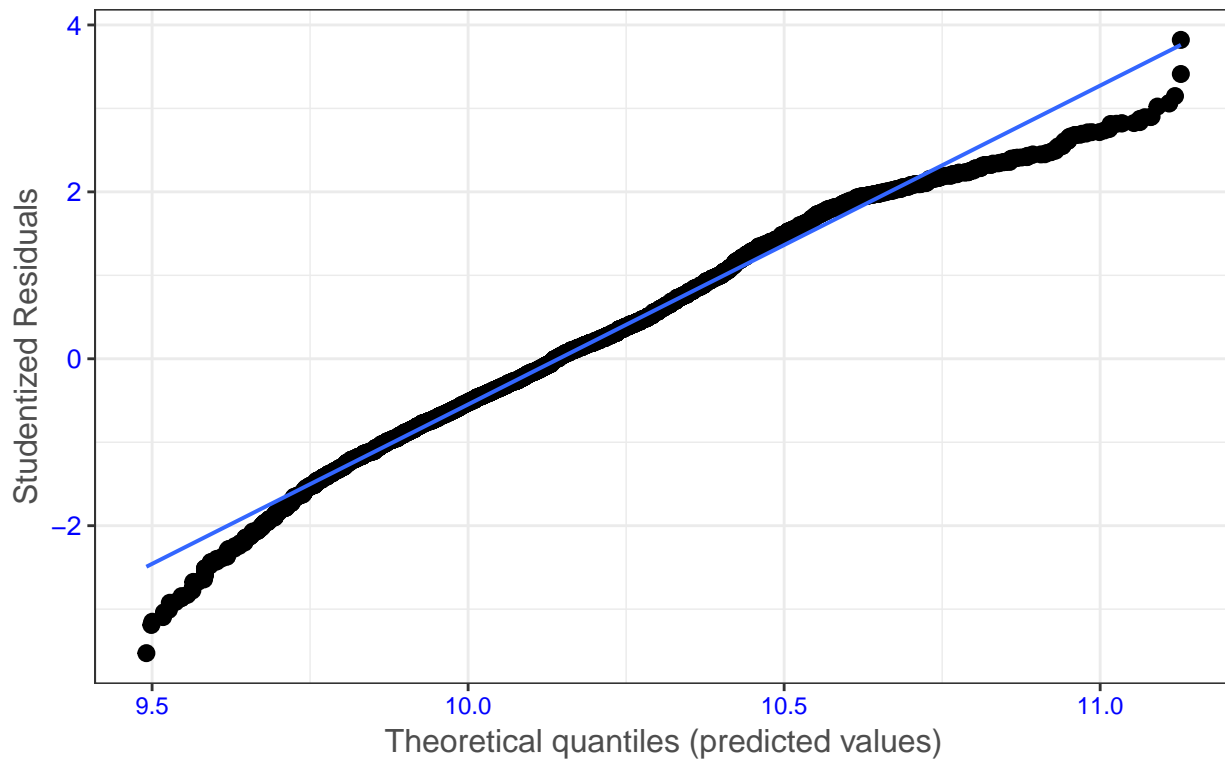


A VIF chart shows that there is no correlation among the kth predictor and the remaining predictor variables.

```
## [[1]]
```

Non-normality of residuals and outliers

Dots should be plotted along the line

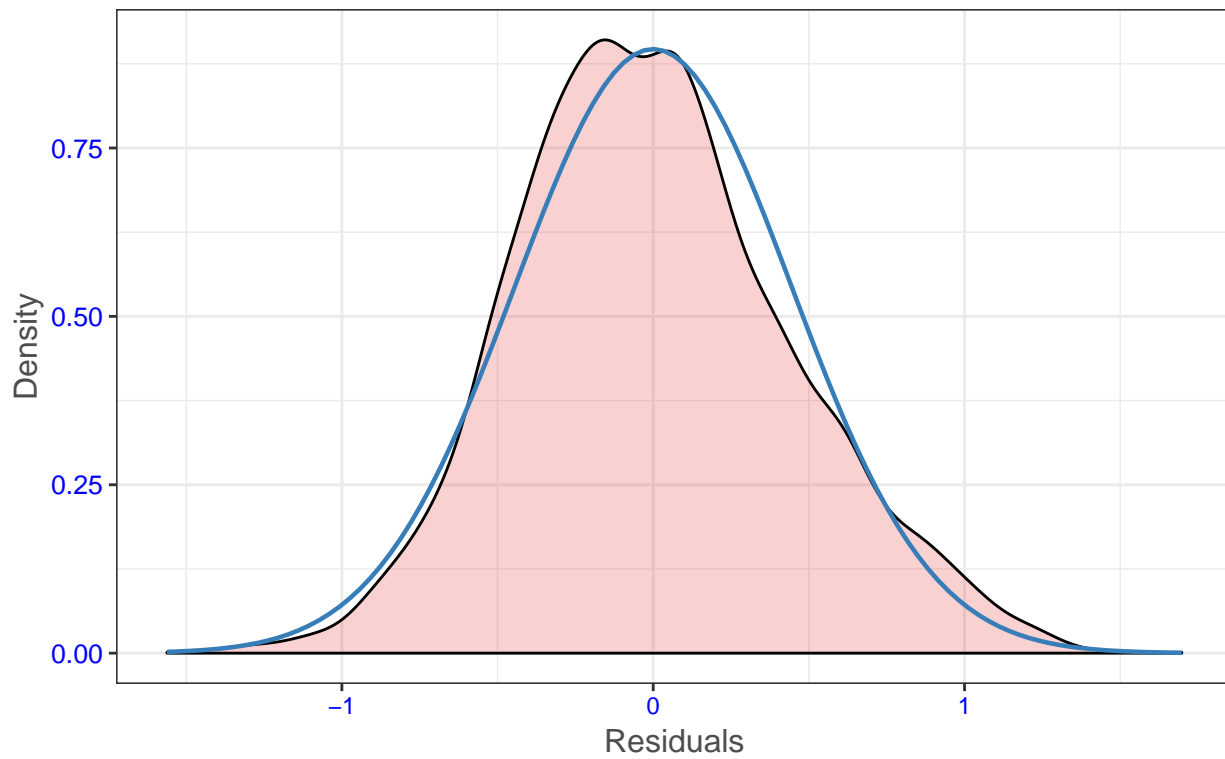


The plot shows that the distribution of the residuals are approximately normally distributed. The “thin tails” correspond to the first quantiles occurring at less than expected values and the last quantiles occurring at larger than expected values.

```
## [[1]]
```

Non-normality of residuals

Distribution should look like normal curve

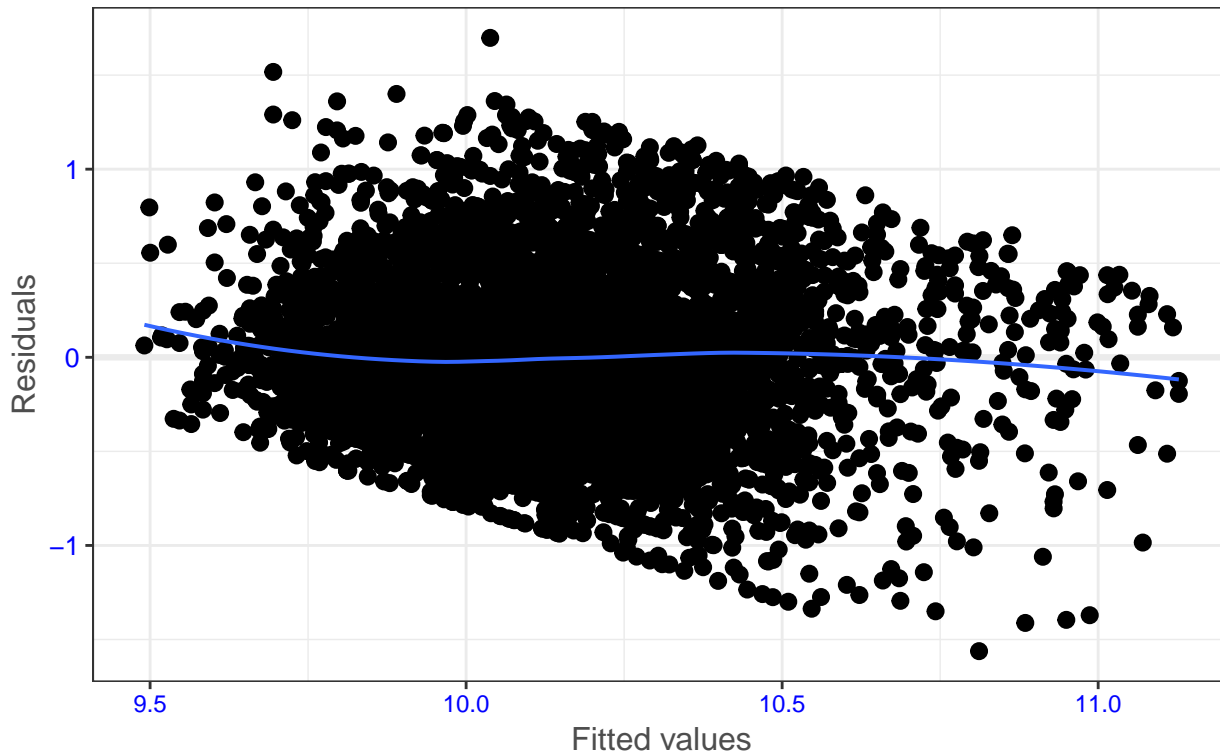


The plot shows that the distribution of the residuals are approximately normally distributed.

```
## [[1]]
```

Homoscedasticity (constant variance of residuals)

Amount and distance of points scattered above/below line is equal or randomly spread



The plot shows heteroscedasticity as the variance of the residuals are not constant.

```
##
## \begin{table}[!htbp] \centering
##   \caption{}
##   \label{}
## \begin{tabular}{@{\extracolsep{5pt}}lcc}
## \hline
## \hline \hline
## & \multicolumn{2}{c}{\textit{Dependent variable:}} \hline
## \cline{2-3}
## \hline & PERNP & log(PERNP, base = exp(1)) \hline
## & (I) & (II) \hline
## \hline & (1) & (2) \hline
## \hline \hline
## Widowed & 1,104.916 & 0.017 \hline
## & (2,001.830) & (0.061) \hline
## & & \hline
## Divorced & $-1,078.738^{*}$ & $-0.039^{**}$ \hline
## & (591.665) & (0.018) \hline
## & & \hline
## Separated & $-1,833.170$ & $-0.044$ \hline
## & (1,253.170) & (0.043) \hline
## & & \hline
## NeverMarried & $-2,974.748^{***}$ & $-0.103^{***}$ \hline
## & (492.802) & (0.015) \hline
## & & \hline
## Female & $-4,868.474^{***}$ & $-0.138^{***}$ \hline
## & (441.147) & (0.013) \hline
##
```

```

##      & & \\
## RaceBlack &  $-\$1,178.008^{\{**\}}\$$  &  $-\$0.028$  \\
##      & (562.739) & (0.017) \\
##      & & \\
## RaceOther &  $-\$2,141.038^{\{***\}}\$$  &  $-\$0.057^{\{***\}}\$$  \\
##      & (528.625) & (0.016) \\
##      & & \\
## SomeCollege &  $4,241.631^{\{***\}}\$$  &  $0.151^{\{***\}}\$$  \\
##      & (577.107) & (0.020) \\
##      & & \\
## Associate &  $4,150.434^{\{***\}}\$$  &  $0.155^{\{***\}}\$$  \\
##      & (565.632) & (0.019) \\
##      & & \\
## Bachelor &  $12,337.160^{\{***\}}\$$  &  $0.421^{\{***\}}\$$  \\
##      & (555.506) & (0.017) \\
##      & & \\
## Master &  $17,795.400^{\{***\}}\$$  &  $0.575^{\{***\}}\$$  \\
##      & (921.890) & (0.026) \\
##      & & \\
## Professional &  $28,133.370^{\{***\}}\$$  &  $0.819^{\{***\}}\$$  \\
##      & (2,099.322) & (0.051) \\
##      & & \\
## Doctoral &  $35,674.460^{\{***\}}\$$  &  $0.960^{\{***\}}\$$  \\
##      & (2,187.211) & (0.045) \\
##      & & \\
## AGEp &  $284.937^{\{***\}}\$$  &  $0.009^{\{***\}}\$$  \\
##      & (20.368) & (0.001) \\
##      & & \\
## Constant &  $12,598.970^{\{***\}}\$$  &  $9.584^{\{***\}}\$$  \\
##      & (1,005.412) & (0.031) \\
##      & & \\
## \hline \\[-1.8ex]
## Observations & 5,194 & 5,194 \\
##  $R^2$  & 0.247 & 0.256 \\
## Adjusted  $R^2$  & 0.245 & 0.254 \\
## Residual Std. Error (df = 5179) & 14,919.810 & 0.445 \\
## F Statistic (df = 14; 5179) &  $121.084^{\{***\}}\$$  &  $127.039^{\{***\}}\$$  \\
## \hline
## \hline \\[-1.8ex]
## \textit{Note:} & \multicolumn{2}{r}{ $^{\{*\}}p < 0.1$ ;  $^{\{**\}}p < 0.05$ ;  $^{\{***\}}p < 0.01$ } \\
## \end{tabular}
## \end{table}

```