Various Homology and Cohomology Theories

We list various cohomology/homology theories in this document.

Sheaf Cohomology

$$H(X, \mathcal{F}) = H(\Gamma(X, \mathcal{E}))$$

Commutative Algebra

$$\operatorname{Tor}_{R}(A,B) = \operatorname{H}(A \otimes_{R} Q) = \operatorname{H}(P \otimes_{R} B) = \operatorname{H}(P \otimes_{R} Q)$$

$$\operatorname{Ext}_{R}(A,B) = \operatorname{H}(\operatorname{Hom}_{R}^{\star}(A,E)) = \operatorname{H}(\operatorname{Hom}_{R}^{\star}(P,B))$$

$$\operatorname{H}(x,M) = \operatorname{H}(\mathcal{K}(x) \otimes_{R} M)$$

$$\operatorname{H}(x^{\infty},M) = \operatorname{H}(\widehat{\mathcal{K}}(x,M)) = \varinjlim_{I} \operatorname{H}(\mathcal{K}^{\star}(x^{n},M))$$

$$\operatorname{H}_{I}(M) = \operatorname{H}(\Gamma_{I}(E))$$

Sheaf Cohomology

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