Ch5 Lecture Notes

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Contents

1 Units and Light

(Not textbook notes but stuff I added)

Below is a list of words we associate with light, but can we give these proper *physical* definitions?

Brightness, flux, intensity, luminosity, lux, lumens, magnitude, polarization, ...

1.1 Lumens, Luminosity, Lux

We have many **many** ways to quantify light. Example flashlight with adjustable end that concentrates beam or disperses it.

- **Luminosity**: absolute measure of electromagnetic power.

$$[L] = \frac{\text{Joules}}{\text{second}} = \text{Watt}$$

$$L\text{sol} = 3.828 \times 10^{26}\text{W}$$

- **Flux**: How bright does a light source appear? Depends on luminosity, **distance**, and amount of dust between us and the light source.

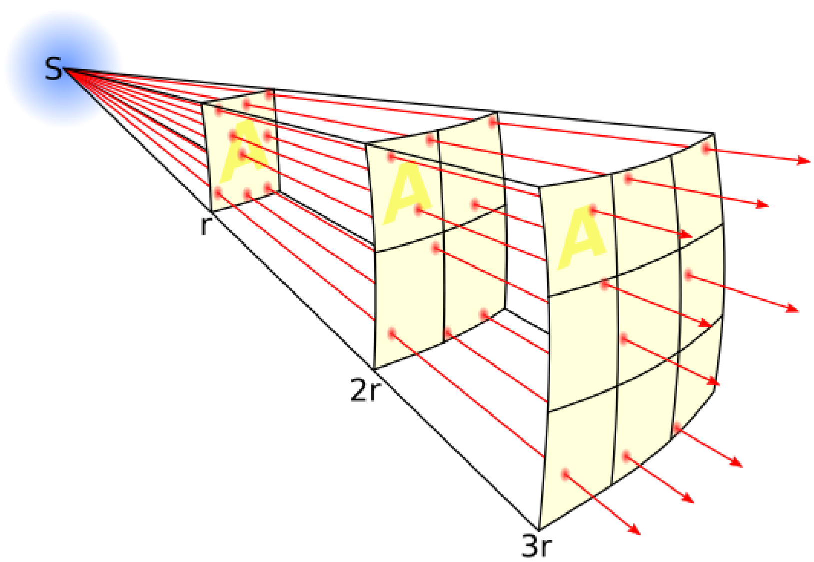

Figure 1: Flux from a point light source.

$$\text{Flux} = \frac{\text{Luminosity}}{\text{Surface Area}}$$

- **Candella**: SI unit for *luminous intensity* (cd) Specifically a measure of luminous power per solid angle, **but** wavelengths are weighted. Weights given by *luminosity function* (model of human eyes sensitivity to different wavelengths)

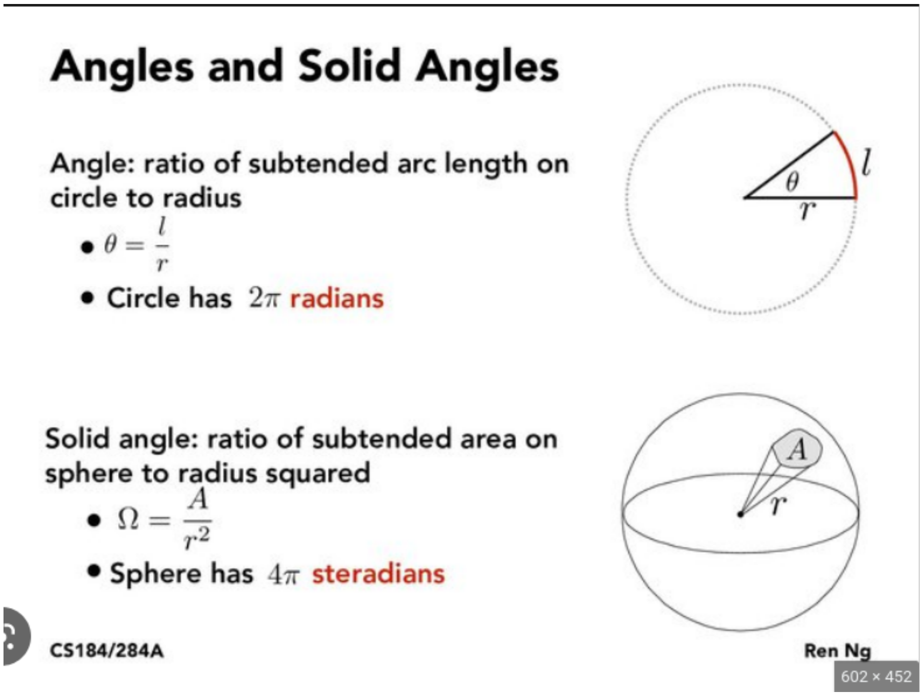

Figure 2: Explanation of what a solid angle is

A wax candle has a luminous intensity of about 1cd.

- **Lumen**: unit of luminous flux (ℓm), a measure of **percieved** power of light. Luminous flux weights the power of different wavelengths based on the human eye sensitivity.

$$1\ell m = 1\text{cd} \times 1\text{sr}$$

- **Lux**: unit of luminous flux per unit area. Example: flashlight same distance from wall but is the beam concentrated or spread out.

$$1\ell x = 1\ell m/m^2$$

2 Random facts about light

- $c = \lambda\nu = 2.998e8$m/s
- Energy of light given by Plank's constant times the frequency

$$E = h\nu \quad h = 6.626\text{e-}34\text{Js}$$

- Information we can get from studying light
  - apparent brightness
  - spectral energy distribution (find example)
  - Doppler shift
  - spectral line broadening (find example)
  - Zeeman line splitting (find example)
  - temporal variations
  - polarization

  Applying physics principles we can also determine
  - light source's **distance**
  - luminosity
  - temperature
  - chemical composition
  - size
  - rotation
  - magnetic fields
  - radial and transverse velocity
  - **intervening absorption by gas and dust**
- Astronomical sources categorized as *point* and *extended*
  - **Point**: most stars
  - **Extended**: sol, nebulae, *resolved* galaxies, diffuse synchotron emission, **CMB**, *IR dust emission in the Solar system.*

  Light measured from the two sources has to be handled differently

3 The Magnitude Scale

A star's **apparent brightness** is referred to as **magnitude**.

Higher number equals fainter object

- "Cumbersome" system inherited from antiquity and still widely used.
- Originally based on appearance of stars between **sunset** and **astronomical twilight** (see figure 3)

  Sunset $\rightarrow$ end of twilight broken into 6 segments. Stars that appear in the first segment were magnitude 1 (the brightest), stars appearing in the second time segment were magnitude 2, . . .
- Human eye the only tool to quantify magnitudes for centuries.
- Invention of photometers revealed two facts

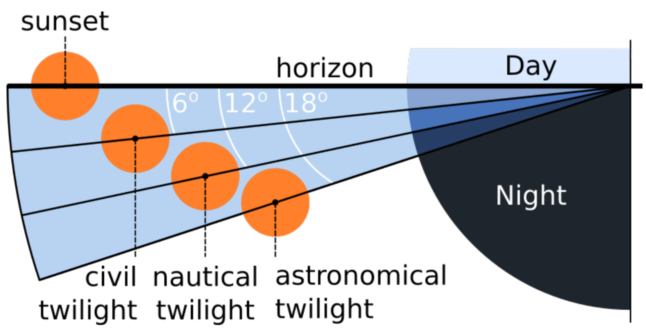

Figure 3: What is twilight

1. Magnitude 1 was too broad. Sirius *much* brighter than Regulus but both are mag1.
2. Ratios of magnitude brightness ≈ 2.5.

$$\frac{B_3}{B_4} \approx 2.5, \quad \frac{B_3}{B_5} \approx 2.5^2$$

   Humans see *equal brightness* ratios as equal steps in *magnitude* $\therefore$ **human vision is logarithmic**

   m = magnitude, F = apparent brightness (flux)

$$\Delta m \propto \log\left(\frac{F_2}{F_1}\right)$$

- 1856 Pogson proposes modern definition of magnitude scale.

$$\boxed{\frac{F_1}{F_2} \equiv \left(\sqrt[5]{100}\right)^{m_2-m_1}} \approx 2.5119^{m_2-m_1}$$

Mag difference of 5 exactly equals ratio of 100 to 1.

$$\log\left[\frac{F_1}{F_2}\right] = \log\left[\left(\sqrt[5]{100}\right)^{m_2-m_1}\right]$$

$$\log\left[\frac{F_1}{F_2}\right] = \log(100^{\frac{m_2-m_1}{5}})$$

$$\log\left[\frac{F_1}{F_2}\right] = \frac{m_2-m_1}{5}\log(10^2)$$

$$-\log\left[\frac{F_2}{F_1}\right] = \frac{m_2 - m_1}{5}\,2$$

$$\boxed{m_2 - m_1 = -2.5\log\left[\frac{F_2}{F_1}\right]}$$

1. Cannot identify magnitude of a single star by itself. Must compare stars through difference in magnitudes.
2. No zero from log $\therefore$

   $$\boxed{\text{Pogson Equation: } m_i = -2.5\log F_i + C}$$

   where C is the *zero-point offset*. Astronomers have to agree a specific star has a specified magnitude (see Bolometric magnitude and IAU 2015 resolution B2 for examples).

- What difference in magnitude results from a *small* difference in apparent brightness?

  $$\Delta m = -2.5\log\left[\frac{F_2}{F_1}\right] \quad \rightarrow \quad f(x) = -2.5\log(x)$$

  Use a Taylor series to expand the log function

  $$f(x) = f(a) + \frac{1}{1!}f'(a)(x-a) + \frac{1}{2!}f''(a)(x-a)^2 + \frac{1}{3!}f'''(a)(x-a)^3 + \ldots$$

  Need to change base to compute derivatives correctly

  $$\log_b(a) = \frac{\log_c(a)}{\log_c(b)}$$

  $$f(x) = -2.5\frac{\ln(x)}{\ln(10)} = -1.086\ln(x)$$

  $$f(a) = -1.086\ln(x)$$

  $$f'(x) = -1.086\frac{1}{x}, \quad f'(a) = -1.086\frac{1}{a}$$

  $$f''(x) = +1.086\frac{1}{x^2}, \quad f''(a) = +1.086\frac{1}{a^2}$$

  Let $a = 1$ (i.e. $F_2 = F_1$)

  $$f(x) = -1.086(x-1) + 1.086\frac{(x-1)^2}{2} + \ldots$$

Evaluate this function at $x = F_2/F_1$ under the condition that $F_2 = F_1 + \epsilon$. $\therefore x \approx 1$ and $(x-1)^n \approx 0$ for $n > 1$.

$$f(x = F_2/F_1) = -1.086\left(\frac{F_2}{F_1} - 1\right) + O(x^2)$$

$$f(x) \approx 1.086\left(\frac{F_2}{F_1} - \frac{F_1}{F_1}\right)$$

$$\boxed{\Delta m \approx -\frac{\Delta F}{F_1}}$$

Suppose star 1 has a magnitude of $m_1 = 3.5$ and star 2 $m_2 = 3.6$. Than

$$\Delta m = 0.1$$

and star 2 is about 10% brighter.

$$0.1 \approx \frac{\Delta F}{F_1}$$

$$0.1F_1 \approx (F_2 - F_1)$$

$$F_2 \approx 1.1F_1$$

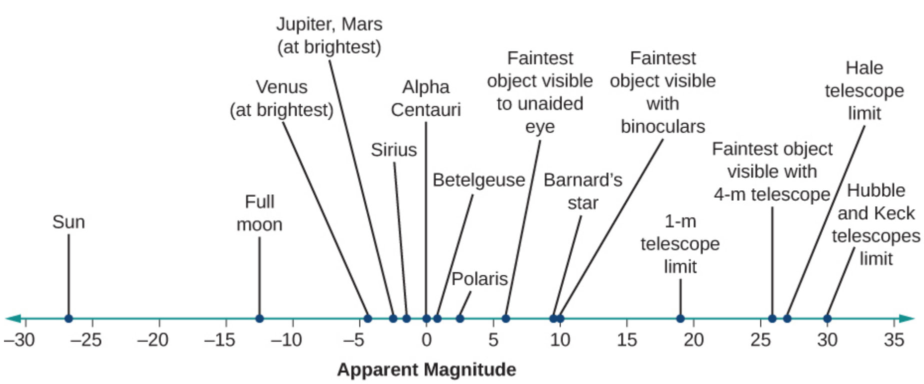

Figure 4: Modern Magnitude system

3.1 Magnitude and Wavelength Dependence

The human eye's sensitivity to to different wavelengths means sources can appear to have different magnitudes, even if they are the same luminosity. Compare a flashlight to the IR beam from a TV remote.

The Pogson equation is an example of the **visual magnitude**.

$$\boxed{\text{Monochromatic Pogson Equation: } m_\lambda = -2.5\log F_\lambda + C}$$

Bolometric magnitude is the opposite of monochromatic, and includes ALL EM radiation emitted by the source.

$$\text{Bolometric correction: } BC_{\text{band}} = m_{\text{bol}} - m_{\text{band}}$$

m_{band} is the magnitude in some passband.

Example: The bolometric correction to the visual magnitude, BC_{V}, for the sun is $BC_{\text{V}} = -0.07$ magnitudes.

3.2 Absolute Magnitude

Absolute Magnitude: The apparent magnitude a star would be *if* it was 10 parsecs away.

Must know the stars apparent magnitude and distance.

$$\textbf{Distance Modulus}: m - M = 5\log\left(\frac{d}{10}\right)$$

Distance Modulus	Distance (parsec)
1	15.8
5	100
10	1000
15	10000

If $d > 10$pc must consider **interstellar absorption**!

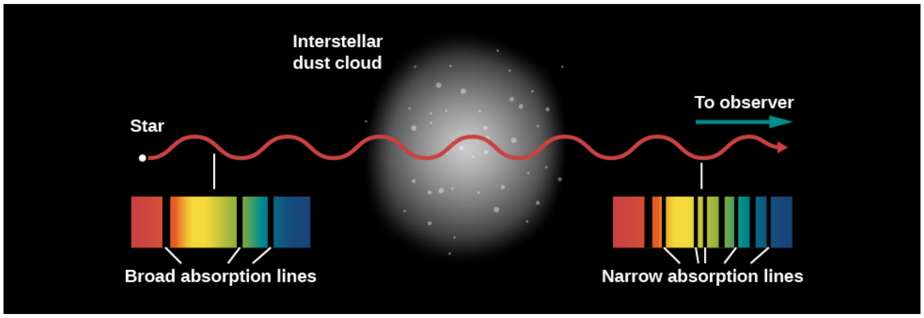

Figure 5: Interstellar absorption

$$\text{Apparent Distance modulus: } (m - M)_\lambda = (m - M)_0 + A_\lambda$$

A_λ is absorption (in magnitude) at that passband (wavelength λ).

Interstellar absorption always makes an object appear further.

4 Color Index

5 Magnitude zero points

6 Filter systems

This one seems important

7 Flux