

**Identification of Vertebra Characteristics that  
Determine Different Mechanical Outcomes of  
Vertebroplasty**

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# Chapter 1

## Literature Review

### 1.1 Introduction

#### 1.1.1 Spine

The human spine is a complex structure that has a host of biomechanical functions. At each level, there are three joints (a disc and two facet joints) which, along with two vertebrae, muscle and ligamentous tissue form a functional unit. The functions of the spine are: to protect the spinal cord, to provide stability and mobility, and to allow the transmittance of movement of the upper and lower extremities.

The spinal column (Figure 1.1) consists of 24 articulating vertebrae and nine fused vertebrae, divided into five regions. These regions consist of seven cervical, 12 thoracic, five lumbar, five fused sacral and three to five fused coccygeal vertebrae, which all vary in size, shape and curvature.

The curvature of the spinal column features lordosis (concave curvature, when viewed from the posterior) in the cervical and lumbar regions and kyphosis (convex curvature) in the thoracic and sacro-coccygeal regions. It has been postulated that the curvature exists to increase rotational stability – moving mass away from the centre line increases the centre of inertia about the skull-pelvis axis. The change in curvature during gait cycle reduces the loads on the skull due to absorption of energy in the tendons and musculature of the surrounding areas. The curvature is created by vertebral geometry in the thoracic and sacral regions, while in the cervical and lumbar regions the curvature is created by the intervertebral disc being wedge shaped.

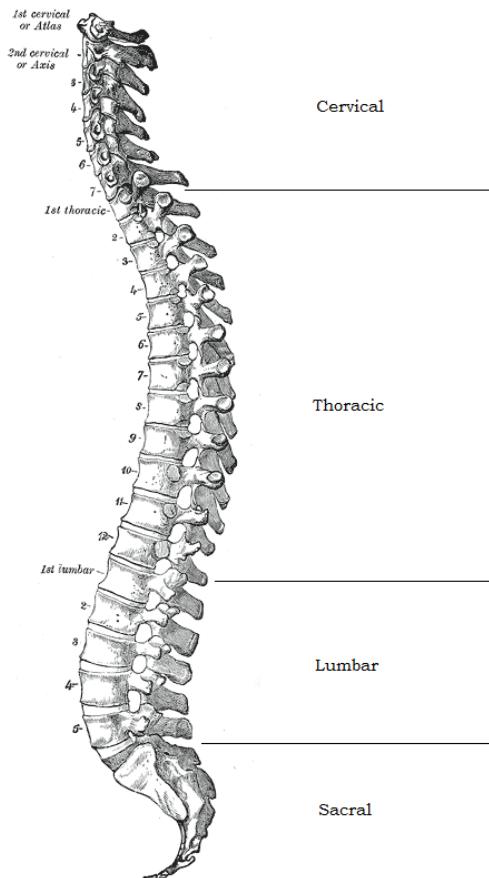


Figure 1.1: Curvature of the vertebral column with the four regions labelled. Adapted from [1].

### 1.1.2 Vertebrae

Vertebrae vary greatly between each region and gradually within them. Generally, vertebrae consist of the vertebral body on the anterior portion and the neural arch on the posterior portion along with pedicles and bony processes (Figure 1.2).

The vertebral body has a similar structure to long bones, with a low-density trabecular structure internally, with a more dense cortical shell. Due to approximately 80 percent of the compressive load of the spine being carried by the vertebral body [2], the trabeculae are orientated vertically to aid load transfer with horizontal trabeculae providing resistance to compressive buckling. Especially in older patients, often with osteoporosis, the vertebral body can be subject to vertebral fracture, more commonly on the anterior portion, causing anterior collapse and a wedge shape when viewed from the side [2].

Vertebral bodies vary between level in terms of cross sectional area, height and strength, with the axial strength of vertebrae increasing from approximately 1300 N at the third cervical level to over 8000 N at the fourth lumbar level [3]. Similar variations have been found in the bone mineral density (BMD) [yoganandan2006], with the BMD varying with

the loads they are expected to carry. While a reduction in BMD is most often associated with osteoporosis, similar increases in the risk of fracture are attributed to metastatic bone disease.

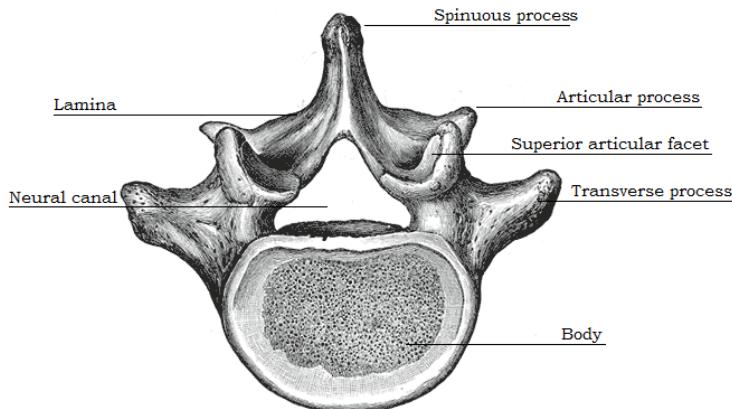


Figure 1.2: Superior view of a lumbar vertebrae, with key features labelled. Adapted from [1].

The posterior region of the vertebrae consists of two pedicles, followed by the neural arch and processes. The spinous and transverse processes allow for greater leveraging by the muscles and ligaments while the superior and inferior articular facets of neighbouring vertebrae form the facet (zygapophysial) joints.

Vertebrae at different levels have differing structures to permit their required role. Cervical vertebrae are considerably smaller and lighter than vertebrae at other levels due to the reduced weight they are required to carry (the head and neck, and forces from stabilising muscles). One identifying feature is the foramen transversarium lateral to the vertebral body which allows for the passage of the vertebral artery and vein [4].

The thoracic vertebrae vary substantially through T1 to T12 with the size of the vertebral body gradually increasing and the pedicles changing in orientation and shape. The addition of adjoining ribs through the thoracic region greatly increase the stiffness of the section due to the ligaments and costovertebral joints.

The lumbar vertebrae carry the greatest load of the spinal regions [3] and consequently have the lowest height to width ratio [5]. The end-plates (at the top and bottom of a given vertebra) of this region are in general parallel, suggesting that the lordosis originates from the disc shape rather than the vertebrae.

The sacral vertebrae are fused to form the sacrum which are followed by three to four elements that form the coccyx and fuse in adulthood.

## 1.2 Vertebral Fractures & Vertebroplasty

### 1.2.1 Vertebral Fracture Types

The two most frequent types of vertebral fracture are the compression fracture and the burst fracture. These types originate from different conditions of both the intact vertebrae and the loads applied. To examine the type of fracture, the vertebra is often categorised into three columns from a sagittal view, with the columns being: the anterior, middle and posterior regions [6].

#### 1.2.1.1 Compression Fractures

A vertebral compression fracture (VCF) is a failure of the vertebral body under the anterior column with the middle column remaining intact, a feature unique to this type of fracture [6]. Such fractures can also be identified through compression of the cancellous bone and lack of fragmentation. The two main types of VCF are anterior and lateral, with the mechanism being anterior flexion and lateral flexion respectively. These types can be further divided based on whether the superior or inferior end-plate experienced failure, however failure of the superior end-plate is more common [6]. Radiographically, the anterior height of the vertebral body is reduced with no visible change or damage to the posterior region of the vertebral body [6], although occasionally in juvenile and osteoporotic vertebrae the damage is limited to end-plate impaction [7]. A more extreme case is a vertebral body collapse, found in osteoporotic spines, where occasionally fragments of bone are produced which can violate the spinal canal especially when both end-plates are impacted (such cases are treated as burst fractures) [7].



Figure 1.3: Types of VCF. Left: Intact FSU. Left-Mid: Anterior wedge fracture. Right-Mid: Posterior wedge fracture. Right: Vertebral body collapse.

A study of 132 anterior VCFs by Denis [6] found that the distribution of fractures favoured the upper lumbar region (L1 was considerably more common) and mid-thoracic (T7 most

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common in the thoracic region). Lateral VCFs accounted for only 16 of the 148 VCFs, which were all found to occur in the lumbar region except one case.

### **1.2.1.2 Demographic**

Patients suffering from vertebral compression fractures (VCFs) can experience severe pain for extended amounts of time, dramatically changing daily activities in addition to the pain, through reducing the lower vital capacity and forced expiratory volume when compared to patients without such fractures [8]. Mortality rates were also reported to increase with VCFs in women, with the rate increasing further with the addition of more fractures [8].

Due to VCFs occurring most commonly through the loads applied to the spine exceeding the axial strength of the vertebral body, the demographic of sufferers is dominated by those with osteoporosis or tumours within the vertebrae [8]. The occurrence of osteoporosis is usually age related with the frequency of VCF increasing from 25 percent of postmenopausal women to 40 percent in women aged 80 years old in the United States [9]. However, as discussed by Melton & Kallmes [10], there is difficulty in defining VCFs due to the number of systems developed to define them and the lack of a clear gold standard for classification. This study found that the prevalence varied from 7% to 19% for women in the age range of 50-80 years depending on the method by which the fracture was defined and 4% to 17% for men in the same age range. The prevalence of osteoporotic VCFs in women was found to be twice that of men in an age-adjusted study [11].

VCFs due to tumour infiltration into the vertebrae is another subset of patients and was the motivation for the first image guided percutaneous vertebroplasty procedure in 1984 [12], however it is difficult to assess the rate of such occurrences. The increasing ability to treat osteolytic metastases and myeloma, leave more patients open to vertebral collapse. This is further increased by possible secondary osteoporosis induced by the treatment of malignant lesions [8]. However, specific pathologies and trauma account for a mere 3% and 14% respectively of all clinically relevant fractures [10].

### **1.2.2 Risk Factors**

Many of the risk factors of VCFs are the same as osteoporosis due to their linked nature and can be categorised into potentially modifiable and non-modifiable risk factors [9]. Non-modifiable factors include age, gender, Caucasian race and history of existing fractures;

modifiable factors include insufficient physical activity, calcium and vitamin D deficiency and alcohol and tobacco use [9].

### **1.2.3 Diagnosis**

Approximately two thirds of VCFs are undiagnosed [13] due to back pain often being regarded as a consequence of aging and not reported by patients. Care is often required to ensure that pain is directly related to a VCF and not another spinal entity such as facet arthropathy, herniated disc and spinal stenosis [8]. Indicators for Percutaneous Vertebroplasty (PVP) are often described as pain localised to the area, which lacks suggestions of nerve or cord compression and includes an increase in pain under weight bearing [8]. Vertebral pain for 1-6 weeks that fails to reduce after oral analgesics has also been defined as an indicator [14].

Due to the strong relationship between BMD and bone strength, with stronger vertebrae exhibiting a higher BMD [15], dual energy X-ray absorptiometry (DEXA) or quantitative CT can be used to predict vertebral fractures. Increasingly the ability to assess the bone structure at the clinical level gives a greater ability to clinicians to predict fractures more accurately, due to BMD effectively being a surrogate for the trabecular structure.

### **1.2.4 Vertebroplasty**

The main group of patients that receive PVP are those with either osteoporotic VCFs or those with tumour infiltration. Early use of PVP was limited to those patients who responded poorly to conservative treatments, including analgesics, bed rest, physical therapy and in some cases bracing [8]. However due to the low complication rate of PVP, indication of an osteoporotic VCF is often enough and helps to reduce further compression of the vertebral body [14]. PVP consists of the injection of bone cement into the vertebral body from the posterior side of the body. The addition of cement into an osteoporotic, fractured vertebral body allows stabilisation of the fracture with the aim of reducing pain for the patient.

#### **1.2.4.1 Vertebroplasty Procedure**

Performing vertebroplasty requires careful monitoring during cement injection and cannula placement; this is carried out with the use of fluoroscopic guidance, which helps to limit the possibility of extravasation (cement leakage from the vertebral body). Biplane fluoroscopy

is often used, allowing the procedure to be carried out more rapidly, while single plane fluoroscopy requires checking both lateral and anteroposterior projections [8].

There are three common approaches to the vertebral body: transpedicular, parapedicular, and oblique, shown in Figure 1.4. Transpedicular vertebroplasty provides a route into the vertebral body through the pedicle, which acts as a tunnel reducing the risk of dural puncture. Depending on patient vertebrae size and level, the pedicle may be insufficient to allow passage of the vertebroplasty needle and hence other approaches may be required. The transpedicular approach also often requires injection from both sides of the vertebrae into the vertebral body to prevent build-up of cement on one side.

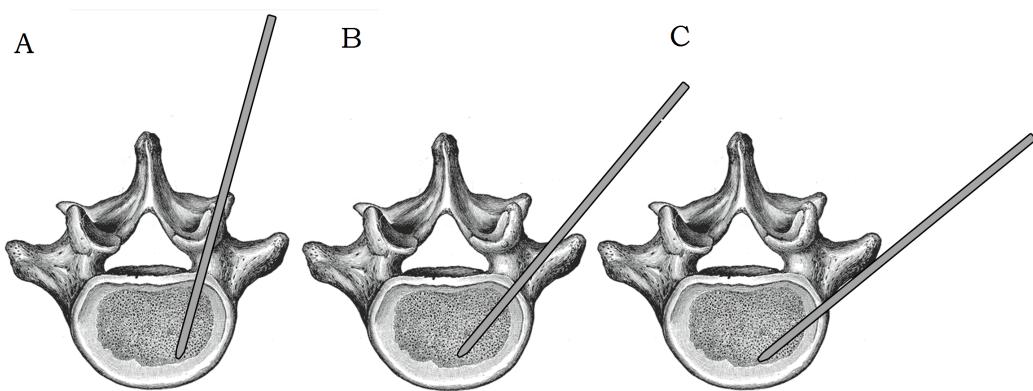


Figure 1.4: Three approaches to vertebroplasty. A, transpedicular approach, B, parapedicular approach, C, oblique approach. Adapted from [1].

The parapedicular approach involves the needle being inserted transversely across the pedicle until the vertebral body wall is reached. It has the advantages of allowing the needle to be positioned ideally for injection, removing the need for multiple injections to evenly distribute the cement. Although allowing ideal positioning of the needle tip, it requires the needle to pass close to the basilar vein, therefore increasing risk of puncturing the vein.

Finally, the oblique approach avoids the pedicle entirely, entering the vertebral body in the posterolateral corner and is often used in the thoracic region where the needle can pass over the top of the rib into the vertebral body. Disadvantages of this approach include difficulties in positioning due to the longer needle required and due to the positioning any extravasation at the needle entry point will be around the exiting nerve root [16].

#### **1.2.4.2 Results of Vertebroplasty and Clinical Trials**

The pain relief reported following vertebroplasty is currently not fully understood; theories include effects on the nerve endings, both thermal and/or chemical, and the general

Table 1.1: Two randomised clinical trials, with their similar inclusion and exclusion criteria and results for the study.

Study Author	Number of patients	Type of pathologies	Inclusion Criteria	Exclusion Criteria	Results for osteoporotic patients
Buchbinder et al. [17]	71 patients, 35 in VP group, 36 in placebo group	Vertebral compression fractures	Pain < 12 months duration and presence of one or two vertebral fractures	> 90 % collapse, presence of spinal cancer, retropulsion of fragments, hip fracture or infection	No beneficial effect of vertebroplasty over a sham procedure at 1 week or at 1, 3, or 6 months among patients
Kallmes et al. [18]	131 patients, 68 VP group and 63 placebo group	Vertebral compression fractures	> 50 years of age 1–3 painful, osteoporotic vertebral compression fractures between vertebral levels T4 and L5. Fracture < 1 year old	Evidence of neoplasm, retropulsion of fragments, hip fracture or infection	No significant difference between groups one month after the procedure on measures of back pain intensity, functional disability, and quality of life

stabilisation of the vertebrae due to the material properties of the cement which can restore the vertebral material properties [19]. The identification of factors that affect pain relief are often difficult to spot, especially with the relatively small patient populations reported in studies, for example the study by Barr et al. [20], with 47 patients was able to find trends showing patients with single level fractures responded better to the procedure. However, the importance of other factors such as degree of kyphosis and compression, age, gender and fracture location require a much larger population in order to obtain any statistical significance.

A large systematic review by Hulme et al. [21] of 69 clinical studies achieved contrasting results to the study described above. A large proportion of patients, 87 %, had pain relief of some degree out of 1552 patients from 32 studies. However, the review also found higher than expected leakage rates, with leakage occurring in 41 % of vertebroplasty procedures and frequent new fractures were found above and below the augmented level. These fractures give an example of the need for larger, comparative, blinded and randomized clinical trials, which could determine whether these fractures are a feature of altered loading,

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increased patient activity or whether the new fractures would have occurred regardless of the vertebral augmentation.

The two studies summarised in Table 1.1 detail blinded randomised and controlled studies by Buchbinder et al. [17] and Kallmes et al. [18]. These studies raised questions over the risks and evidence for vertebroplasty due to their conclusions that there is no difference between the vertebroplasty and placebo groups. The near simultaneous publication of such results caused many to disregard much of the positive evidence [22] for vertebroplasty. However there are some considerations regarding both of the trials: the inclusion and exclusion criteria detailed in Table 1.1 were neither clear nor well defined, failing to take results of MRI scans (Kallmes et al. [18]) and physical examinations (both) into consideration. Such results would link to accepted indications of bone marrow oedema and pain on palpation respectively [23]. In addition to a population bias towards fractures less than six weeks old, there was no statistical significance between chronic and sub-chronic patients (due the small numbers), prohibiting any insight into which subgroups of patients respond best to vertebroplasty. Additionally, the National Institute For Health And Clinical Excellence guidance document suggests that consideration for receiving the treatment should be after six weeks, due to the severity of pain reducing over that time and many patients being pain free at six weeks post fracture [24]. The standard deviation for both pain intensity and Roland–Morris Disability Questionnaire scores were generally high, especially at one month post-procedure. For example the mean ( $\pm SD$ ) RDQ score in the vertebroplasty group was  $12.0 \pm 6.3$ , as compared with  $13.0 \pm 6.4$  in the control group. This highlights the need to understand where this variation originates from and hence which subset of patients the treatment is better suited to.

## 1.3 Experimental Studies

### 1.3.1 Trabecular Structure

The biomechanical properties of the vertebrae are known to rely heavily on the trabecular structure, especially the compressive strength and stiffness which relates to the failure behaviour and elastic behaviour respectively. The compressive strength originates from the architecture of the load-bearing trabeculae, which is characterised by thick trabeculae columns or plates oriented vertically and held in place by much thinner horizontal trabeculae. This internal structure changes with age; the vertical plates are reduced to columns through bone remodelling and horizontal supports are often removed [25], [26]. Osteoporosis is

often defined by a reduction in the Bone Mineral Density (BMD) of 2.5 standard deviations below that of a young, healthy member of the population of the same gender. However, reports of poor correlations between the BMD and vertebral fracture rates suggest that a measure of BMD is not sensitive enough to solely determine fracture risks [27], hence the trabecular architecture must be studied using more sensitive and specialised tests.

Methods for studying the trabecular structure of the vertebral body usually involve mechanical testing of the vertebrae, or trabecular bone samples in conjunction with a study of the bone density. The trabecular structure and bone architecture in general can be identified through calculation of the ash density and comparisons of the trabecular structure through histological and  $\mu$ CT examination. The following measurable parameters are usually measured using  $\mu$ CT and/or histological images of the trabecular bone: the bone volume fraction (BV/TV), connectivity density (Conn.D), Structural Model Index (SMI), degree of anisotropy (DA) and the trabecular separation, number and plate thickness (Tb.Sp, Tb.N and Tb.Th respectively) and are discussed in detail in the following papers by Hulme et al. [28] and Mosekilde et al. [29].

The ash density allows comparison of the densities of bone samples through the removal of water and soft tissue in addition to a calculation of the mineral content using an additional measurement of the dry weight. Bone marrow and other remaining soft tissue (fat) is often removed prior to incineration using high-pressure water jets and acetone washes [30]. The dry weight is measured following drying using a recommended 100°C furnace for an hour [30] and the dry density ( $\text{gcm}^{-3}$ ) is the weight divided by the specimen volume. To ash the specimens, they are usually placed in a muffle furnace at 650°C for 18-24 hours[29], [30], which following cooling can be reweighed. The mineral content can be calculated through dividing the ash weight by the dry weight and ash density by dividing the ash weight by the initial specimen volume. However, with the adoption of  $\mu$ CT in most studies regarding trabecular structure, ash density calculations are rarely used in more recent studies.

Other parameters of bone architecture (BV/TV, Conn.D, SMI, DA, Tb.Th, Tb.N and Tb.Sp) are usually defined through  $\mu$ CT scans of the bone and analysis using accompanying software to the  $\mu$ CT scanner. The bone volume fraction, BV/TV, usually quoted as a ratio or percentage, is a measurement of the proportion of the total volume of interest that is bone tissue. Conn.D indicates the number of trabecular connections per volume of interest. The SMI provides a quantification of numbers of different types of trabecular element, usually on a scale from 0 to 3 (from rods to parallel plates)[31]. Tb.Sp and Tb.Th are measured in length and identify the average separation between trabeculae and the thickness of trabeculae respectively, while Tb.N quantifies the number of trabeculae

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per unit length. Finally, the degree of anisotropy measures the average alignment of the trabeculae along a specific axis, where a value of one usually specifies isotropic behaviour and less than one equates to various degrees of anisotropy[28].

The region of interest for taking specimens from the vertebral body depends on the nature of the study. If the study requires the capture of an average value for the vertebrae, then the largest possible volume of cancellous bone is required, while avoiding the cortical bone and areas where the basivertebral vein intersects [yoganandan2006]. Other studies have included all cancellous bone between the cranial and caudal endplates and have used subsections of the vertebral body to identify differences and changes with age to specific regions [28].

Bone morphology has been shown to vary greatly between different regions of the vertebrae [28], [32] and between different ages of vertebrae [32], [33]. Animal models are commonly used for the in vitro and in vivo biomechanical models of the spine while testing the performance of various treatments. However, despite providing a basic understanding of spinal function, the differences in vertebrae at different levels and the changes that the vertebrae experience with ageing mean a single species cannot be used to model the entire spine. Hence many different large mammals have been used, including bovine, ovine, porcine and cervine vertebrae which have already been characterised in the literature [34, 35, 36]. These studies compare the anatomical variation in terms of vertebral body width, height and depth, spinal canal size and pedicle height and width. Studies detailing similar anatomical properties for human vertebrae also exist, allowing comparison and assessment of whether a particular animal model is appropriate [4, 5]. The anatomical differences found between the animal study papers listed above and the human studies show many differences between all of the parameters, furthering the idea of multiple animals being used for different studies. The studies suggested that sheep spines were much larger than humans, with the vertebral body height being particularly greater [35, 36], while the mean vertebral width and depth of the human spine are greater than that of all the animals in the studies (with the exception of the upper thoracic segments in the deer [36]). Much of the geometric and structural variation between human and animal vertebrae may be due to the orientation during walking and therefore load differences. Despite this large difference, muscle forces may add additional loads to the vertebrae, reducing the total loading differences.

A study regarding the trabecular composition of bone samples from the lumbar spine compared: human, dog, pig, cow and sheep and concluded that care was required when choosing a suitable animal model for a particular study, due to the large interspecies

differences in terms of Bone Mineral Content (BMC), volumetric BMD (vBMD), height and area and finally fracture stress [37]. They found that human BMC and vBMD were significantly lower when compared to the other animals in the study, aligning with the greatly reduced fracture stress also reported; the details of this can be seen in Figure 1.5. However, the study also reports a higher fracture stress in sheep compared to cows, yet similar values for the BMC and vBMD, with a similar trend also found between pigs (higher BMD) and dogs (lower BMD). Having similar density properties yet high fracture stress, aligns with reports of poor correlations between the BMD and vertebral fracture in the study by Hordon et al[27].

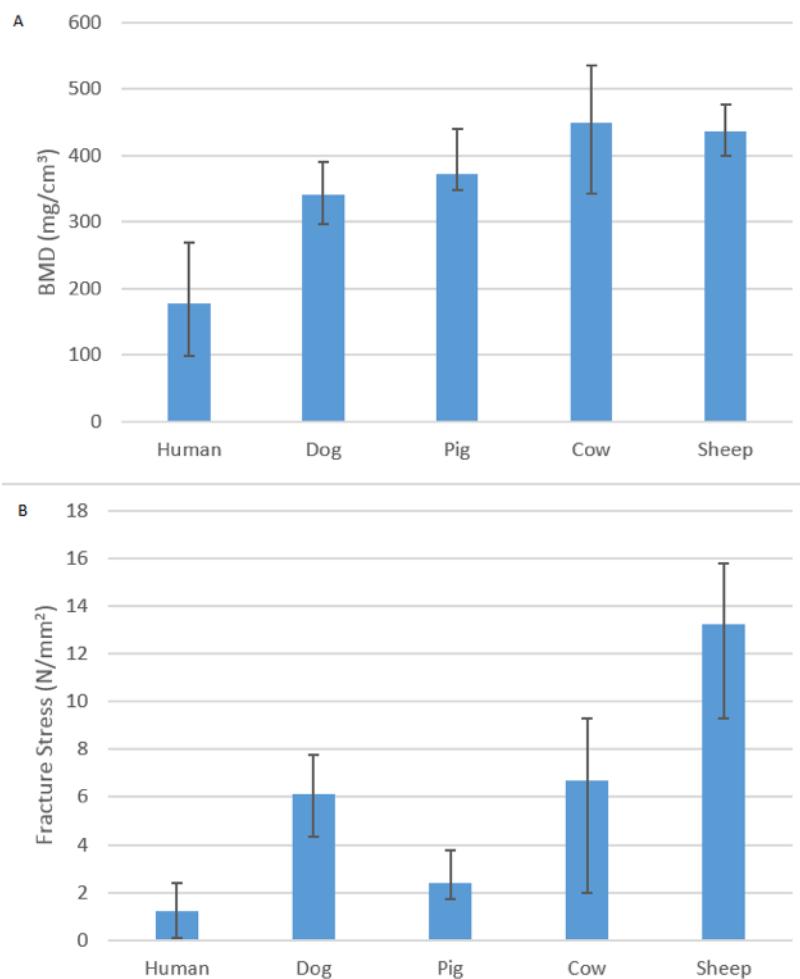


Figure 1.5: A, the mean BMD from cylindrical cores taken from the lumbar spine of five different species. B, the mean fracture stress for the same five samples. Bars indicate the range of values. Adapted from [37].

### 1.3.2 Current Studies on Vertebral Fractures and Vertebroplasty

There have been a considerable number of experimental studies that have investigated the effects of vertebroplasty through mechanical testing. Often these studies are carried out in conjunction with computational studies, where properties are defined experimentally and

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used to validate computational models, for example [38]. These studies are reviewed in the following section, with a focus on the preparation of specimens and methods and with references to notable findings.

### **1.3.2.1 Specimen Preparation**

Capturing as much data as possible for a given specimen is vital for understanding results and allowing those results to be used in many areas of study. Hence, pre and post-mechanical loading  $\mu$ CT scans (including scans before and after cement augmentation) are usually captured.

To simulate physiologic conditions, specimens are often wrapped in phosphate-buffered-solution (PBS, saline) soaked gauze following dissection [20] and are stored at -20°C and thawed for 24 hours before testing at a non-physiological room temperature[39], [40]. This difference between room and body temperature may affect the results, with constituents of the specimens, such as the bone marrow, having different properties at the two temperatures. However, there is a lack of research investigating the effects temperature has on mechanically testing specimens in the literature.

### **1.3.2.2 Mechanical Testing**

The generation of vertebral fractures experimentally attempts to match the natural creation of such fractures; compression fractures are usually generated with an application of force at a low rate, mimicking the gradual creation of fractures in osteoporotic vertebrae over time. Natural burst fractures are usually the result of a traumatic event, high energy impacts causing high rate axial loads through the vertebrae; experimentally burst fractures are usually generated through dropping a load of known mass onto the specimen from a calculated height [39], [41], generating comparative forces to a natural traumatic impact. However, other methods involving biaxial hydraulic testing machines, where high loads (50 – 100 % of the animals body weight) were applied over a short period of time, generating the burst fracture [42].

Mounting of specimens prior to loading in material testing machines allows the position of vertebrae to be maintained during testing, whilst not restricting or confining compression more than necessary. Methods of mounting allow parallel positioning of the exterior surfaces and allow perpendicular loading of the vertebrae along the axis. These requirements for the mounting are usually achieved through potting the specimens in PMMA [39, 40, 43], semi cured moulding material [44] or low viscosity resin [45].

Methods of loading both a pre-fracture and post fracture/augmentation rely on mimicking the natural loading of the spine, with similar methods being used throughout the literature. Loading is carried out with a materials testing machine, applying loads either under pure axial compression or allowing flexion of the upper endplate through various methods. Methods of applying the “natural” load include applying the load or displacement through a steel ball, requiring a specified loading point and allowing natural motion [39], [40]. Applying bilateral loads through pneumatic cylinders and allowing controlled flexion with simultaneous compression [43] and similarly with the application of two anterior and two posterior loads using pneumatic cylinders positioned so that more of the load was applied to the anterior side causing flexion [45] were other methods used in the literature. The positioning of the applied load differs in the literature varying between the mid point of the superior endplate [46] and one quarter of the distance of the vertebral body in from the anterior margin of the superior endplate [19]. With some studies identifying the effect of loading position on the measured stiffness of the vertebrae [38].

The definition of the point of fracture varies in the literature, most commonly the fracture point was defined as the peak on the recorded load-displacement graph. However, Furtado et al. [40] defined the point of fracture creation as 75% of the original vertebral body height, with the failure strength defined as either the value at the end of the experiment (75% of VB height) or the peak on the load-displacement graph. Pneumaticos et al. [45] defined the point of fracture (or maximum fracture load) using the load-displacement graph, where catastrophic failure could be observed through a sudden jump in the displacement.

### **1.3.2.3 Results of Mechanical Loading**

Mechanically loading vertebrae in the study by Furtado et al. [40] showed a significant correlation between failure strength and the product of BMD and endplate area, with the range of failure loads being 900 N to 2200 N for human thoracic vertebrae between T2 and T12. However, the failure load was defined as the load at a deformation of 75 percent of the original vertebral height or the peak load before reaching this deformation, potentially suggesting that the maximum load was not achieved until after 25 percent strain. This may explain the discrepancy between these results and those of Pneumaticos et al. [45] where the average reported failure load was  $6724 \pm 3291$  N for intact specimens using vertebrae between the thoracic levels T2 to T11 from four human cadaveric spines.

#### **1.3.2.4 Experimental Vertebroplasty Compared with Clinical Vertebroplasty**

Experimentally, transpedicular (uni or bi-pedicular) approaches are more common in the literature[40, 43, 45], although extrapedicular approaches have also been used [40].

Although bilateral transpedicular vertebroplasty is the more common clinical procedure[47], unipedicular vertebroplasty is used under some mitigating circumstances often requiring the patient to return for the second injection. A study comparing bilateral and unilateral vertebroplasty found no significant difference between the two procedures in terms of vertebral height and stiffness, possibly attributed to the central positioning of the cement despite the unilateral approach [47]. The authors reached the conclusion that a unipedicular approach is a valid alternative to bipedicular vertebroplasty and may be especially useful during multilevel vertebroplasty by reducing the number of injections and hence risk of cement leaking outside the vertebral walls (extravasation).

#### **1.3.2.5 Results following Experimental Vertebroplasty**

Table 1.2: Comparison of the methods used in studies carrying out vertebroplasty experimentally on cadaveric specimens.

Author	Type of specimen	Procedure type & fill volume	Cement Type	Key Finding
Bellkoff et al. [48]	Five vertebral bodies (L1-L5) from four female cadaveric spines (age, $80 \pm 5$ years)	Transpedicular, 6 ml fill volume throughout	A bioactive cement, Orthocomp (Orthovita, Malvern, PA) & a PMMA based cement, Simplex P (Howmedica, Rutherford, NJ)	Significantly greater strength following injection of cement, compared to the intact vertebrae
Furtado et al. [40]	Twenty-six single vertebrae from 2 female cadavers (age, 88 and 89 years)	Extrapedicular into anterior third of vertebral body, 20 % volume fill, based on height $\times$ endplate surface area	PMMA with 20 % by dry weight of barium sulfate	Increased failure strength by a factor of 1.72 post vertebroplasty compared to the intact vertebrae
Higgins et al. [49]	Human cadaveric, 61 vertebrae from 5 cadavers with mean age of 81 years	Unipedicular, 10% and 20% cement fill by volume, with unfilled as controls	PMMA	A statistically significant 36% strength increase as compared with the unfilled controls regardless of density levels
Pneumaticos et al. [45]	40 vertebrae from four human cadaveric thoracic spines (age range 65-69 years)	Transpedicular, 6 ml fill volume throughout	PMMA, with 5 to 1 ration of barium sulphate	A reduced failure load post vertebroplasty, although non-significant

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The methods used to recreate the vertebroplasty procedure experimentally vary considerably between studies, especially given the sensitivity that certain studies suggest factors such as fill volume have on outcomes. Table 1.2 shows the methods and some of the more important variables used in a selection of studies carrying out vertebroplasty on cadaveric specimens. Below is discussion of some of the finer points of the studies, including comparisons to clinical studies.

Identifying the effect of vertebroplasty on intact specimens in the thoracolumbar region, Higgins et al. [49] found the strength was increased by a statistically significant amount of ~36% using 20% fill volume and that when comparing the strength increases with BMD, it was found that those vertebrae with a lower BMD showed a more dramatic increase in the strength. Conversely Graham et al. [50], found that highly osteoporotic vertebrae showed the least improvement compared to intact vertebrae in terms of strength and stiffness.

Higgins found that the upper thoracic vertebrae failed to show any significant result following augmentation of both 10 % and 20 % compared to the intact controls. Belkoff et al. [51] suggested that 7.7 mL of cement was required to restore the original strength of fractured osteoporotic vertebrae, this corresponded to ~24 % volume fill in the lumbar vertebrae tested.

When comparing different cements Belkoff [48] found that in order to obtain a significant increase in the strength 6 mL or approximately a fill of 18 % was required. Similarly, Lee et al. [52], found that between 25 % and 30 % volume fill was required to restore strength to the intact level for lower thoracic and lumbar vertebrae in a clinical study. Graham et al. [50], required a fill volume of 24 % (average 7 mL) to achieve statistical significance, however this did not return the stiffness to the intact level, and only returned the strength to the intact level in those specimens with the highest BMD of their group.

An increase in strength following fracture and augmentation is a desirable outcome especially for osteoporotic vertebrae where returning the strength to that of the intact vertebrae may not prevent fractures. This is often carried out as prophylactic percutaneous vertebroplasty, where the procedure is carried out on vertebrae that are likely to fracture or on levels adjacent to fractured vertebrae already undergoing PVP. Restoring the stiffness however is believed to be responsible for pain relief due to the internal stabilisation and prevention of micro motion, providing a more suitable environment for healing. A study examining the quantity of cement required to restore the strength and stiffness of osteoporotic vertebrae having undergone a compression fracture found that as little as 2 mL of cement is enough

to restore the strength of the vertebrae to the intact value, with the quantity required to restore the stiffness being between 4 mL and 6 mL depending on the level (lumbar vertebrae requiring more cement)[19].

Regarding extravasated cement during the vertebroplasty procedure, Higgins et al. [49] found that an increase in the BMD greatly increased the tendency for cement to leak, however, this typically was from the anterior wall of the vertebra (more favourable than into the spinal canal) and was independent of vertebral level.

Despite previous studies suggesting BMD alone could not be used as an indicator for vertebral fracture [27], Higgins et al. concluded that it was one of the most important factors, conceding however that the BMD measured ex-vivo is not directly comparable to that measured in a clinical setting. This was due to differences in the BMD calculation due to the surrounding soft tissue for the *in vivo* scans.

The results from Furtado et al. [40] using an extrapedicular vertebroplasty approach achieved approximately 25 % fill for specimens which had previously undergone loading to generate a compression fracture, equating to an average volume of cement of approximately 4.5 ml. This augmentation caused a significant increase in the failure load, a factor of 1.72 increasing the average failure load from  $1.61 \text{ kN} \pm 0.49 \text{ kN}$  to  $2.63 \text{ kN} \pm 0.85 \text{ kN}$ . A similar result was achieved by Tohmeh et al. [47], showing that the post augmentation strength is significantly higher than the fractured and intact vertebrae. Pneumaticos et al. [45] found no significant difference between intact and post augmentation intact vertebrae, with an average failure load of  $5.77 \pm 2.13 \text{ kN}$  for the augmented intact specimens with 6 mL of cement injected.

## 1.4 Finite Element Modelling (FE)

The use of finite element models of the spine, spinal segments and vertebrae has been rising rapidly over the past decades. They are being used to model a range of interventions and devices along with being used to aid our understanding of spinal biomechanics. The main benefit of such studies is the ability to test a range of variables and properties for the same model or specimen, with an additional benefit of assessing parameters that cannot easily be measured experimentally, such as stress and strain fields.

Important factors for the generation of biomechanical finite element models have been discussed previously [53]–[54] and include verification, sensitivity testing and validation of models created. The first of these factors is an assessment of the numerical accuracy

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of the model; given that most studies use commercially available software for FEA this verification has usually already been carried out, with documentation available. Additional verification can be carried out regarding mesh sensitivity and convergence, where the level of detail of the model is investigated with considerations of accuracy and computational cost. Sensitivity testing determines the sensitivity of a model to various input variables and the errors that these input variables have on the system. Such tests may include the response of the system to various boundary conditions and material properties. Validation of models is a proof that the computational results agree with either *in vitro* or *in vivo* results, however, proof that the results agree with the *in vitro* model do not mean that the model is a valid representation of the *in vivo* scenario.

Due to the importance of trabecular bone in many aspects of bone and spinal research, the methods used to model it are quite detailed throughout the literature. There are currently two dominant approaches to modelling trabecular bone using FEA, discussed in detail by Mengoni et al. [55]. These are  $\mu$ -FE, which expresses the micro structure of the bone explicitly, and continuum level FE models which represent the trabecular structure through a continuous model using an inhomogeneous material property to represent the micro-structure. The increased computational cost of  $\mu$ -FE models, especially for full sized vertebrae and larger functional spinal units, means that many studies use continuum level FEA, despite the reduced level of detail. However, the development of continuum level models allows the use of much larger CT scan data sets, given that the resolution of clinical  $\mu$ CT scanners is upwards of  $1.2\text{ mm}^3$ .

The studies summarised in Table 1.3 use various methods to acquire vertebrae geometry, generate models and apply appropriate material properties, either from combinations of scan data and experimental data, or homogenous experimentally defined properties. The variations between methods and results which can be drawn from these studies is described below.

#### 1.4.1 Geometry & Meshing

With the growing availability of  $\mu$ CT scanners and the increasing resolution available with them, studies using *in vitro* measurements and handcrafted geometries such as the study by Higgins et al. [49] in 2007 are being replaced with geometries developed from  $\mu$ CT data. One of the more common methods of generating specimen specific models of vertebrae is the conversion of voxels from down-sampled  $\mu$ CT images into hexahedral elements. The direct conversion of voxels into elements has the advantage of increasing the simplicity of

model generation, however, this requires real specimens (in the form of animal or human tissue) which can be difficult to acquire and scan.

Table 1.3: The geometry generation, meshing and material property assignment methods for 7 studies modelling single vertebrae to acquire stiffness and strength data.

Author	Geometry Generation	Meshing	Material Properties
Brown et al. (2014) [56]	Used $\mu$ CT with resolution of $0.074 \times 0.074 \times 0.074$ mm	Using ScanIP software, segmented CT images down sampled to $1 \times 1 \times 1$ mm and meshed in ScanFE using hexahedral elements and tetrahedral elements for the smooth vertebral surface	Material properties assigned using density values from $\mu$ CT. No division between cortical and cancellous bone. Relationship between elastic modulus and BV/TV value investigated
Buckley et al. (2006) [57]	Used $\mu$ CT data with resolution of $1 \times 1 \times 1$ mm	Conversion of voxels to hexahedral elements of size $1 \times 1 \times 1$ mm	Material properties assigned using density values from $\mu$ CT. No division between cortical and cancellous bone
Chevallier et al. (2009) [58]	Used HR-pQCT data with resolution of $0.082 \times 0.082 \times 0.082$ mm	Used $\mu$ CT data to find cortical wall thickness. Surface meshes defined through local triangulation for each cell for the surface and interior cortical wall boundary. Trabecular bone modelled with hexahedrons of size $1.312 \times 1.312 \times 1.312$ mm using GMSH software	Elastic and yield properties assigned to each trabecular element from $\mu$ CT density data

Eswaren et al. (2007) [59]	Used $\mu$ CT data with resolution of $0.03 \times 0.03 \times 0.03$ mm	Conversion of voxels to hexahedral elements of size $0.06 \times 0.06 \times 0.06$ mm. 8 node hexahedral elements using in-house software. Endplates and cortical shell modelled with higher definition using thickness from $\mu$ CT. Bone within $180 \mu\text{m}$ of the outer structure was identified as belonging to the cortical shell.	Used a constant material property for entire model
Higgins et al. (2007) [49]	Taken from in vitro measurements of L1 vertebrae, using flat endplates and curved side walls	Composed of 12 node brick elements using in-house code. Used separate mesh for cortical walls and different thicknesses for the endplates and posterior and anterior cortical shell.	Anisotropic through model, using different material properties for cortical shell, endplates and vertebral body.
Kinzl et al. (2012) [60]	Used $\mu$ CT with resolution of $0.082 \times 0.082 \times 0.082$ mm	Used $\mu$ CT data to find cortical wall thickness. Surface meshes defined through local triangulation for each cell for the outer and interior cortical wall boundary, meshed using pentahedrals. Trabecular bone modelled with tetrahedrals	Material Mapping based on porosity (density). Uses parameters for elastic, plastic and damage behaviour. Uses elasto-plastic material for the cement augmented region
Wijayathunga et al. (2008) [38]	Taken from $\mu$ CT data with resolution $0.074 \times 0.074 \times 0.074$ mm	Hexahedral and tetrahedral elements using ScanFE software, smoothing is applied to vertebral surface to improve geometry	Material properties assigned using density values from $\mu$ CT. No division between cortical and cancellous bone

The cortical surfaces of these models are often rough when just using voxel to element meshing, for example the models created by Buckley et al. [57] in Figure 1.6. However, many studies introduce smoothing to the surface of a vertebra model. The error introduced from possible stress raisers when omitting smoothing from the model was questioned by Chevalier et al. [58]. This study suggested that smoothing, in the form of surface meshes representing the cortical walls, successfully removed the stress raisers and artificial damage zones from their models. The studies by the group that produced the Chevalier et al. and Kinzl et al. papers in Table 1.3 use methods for fitting the vertebrae surface of the model to that of the scanned specimen, rather than simply smoothing the voxel to element mesh. Kinzl et al. [60] used a “marching tetrahedral” method to extract the surface of the scanned vertebrae from Treecce et al. [61], which uses an adaption of the popular marching cubes method to obtain an iso-surface from discretised three-dimensional data (from  $\mu$ CT data).

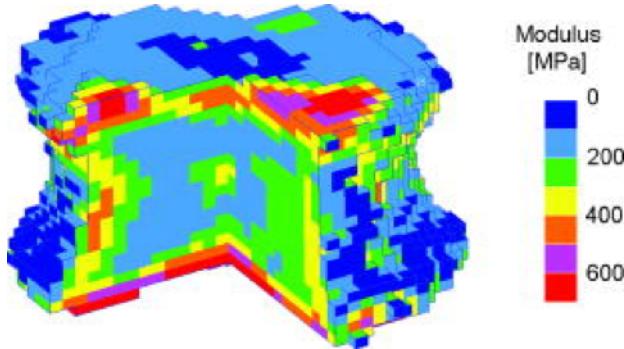


Figure 1.6: Voxel finite element mesh of L2 vertebrae used by Buckley et al. with voxel size of 2 mm [57].

There is a reduced difference between the structure of the cortical shell and the cancellous bone structure of the vertebra when compared to other human bones [62]. Despite this, the cortical walls have been shown to share a significant quantity of the load, especially in the axial midsection, where the cross section is narrowest and the load carried by the cortical wall is greatest [62]. An understanding and correct modelling of the load sharing between the cortical wall and trabecular bone becomes more important when considering the variation of the cortical wall with age, location, level and osteoporotic nature of the vertebrae in question [63]. Chevalier et al. [58] found that adding a surface faced cortical shell to their models unloaded the centre trabecular bone and increased the strength and stiffness values of their models to that of their experimental results. Approaches that rely on the  $\mu$ CT greyscale values to assign material properties to elements, give additional stiffness to the cortical walls due to the denser and therefore brighter cortical regions in the  $\mu$ CT images, without the need for modelling the regions separately.

The increased resolution of the Eswaran et al. [59] study allowed for a uniform element size and material assignment for the cortical shell and trabecular bone, relying on the resolution to represent the higher density of bone within this region. In this case, separate meshes were used for the two bone types (cortical and trabecular) to extract information about load sharing between them. However, the required use of a supercomputer to analyse the FE models limits such models being used within research, especially where large datasets are required to investigate population variation.

#### 1.4.2 Material Properties

Material properties for continuum level FE models are in general derived from BV/TV values from  $\mu$ CT greyscale data for each voxel and assigned to the matching element. These density values are used to derive elastic modulus values using a conversion equation. This conversion equation is often optimised to choose the best values for the conversion equations such that the error between experimental and computational results are minimised. Robson Brown et al. [56] performed an investigation into the effect of a linear or non-linear relationship between the elastic modulus and BV/TV. However, due to lower order errors in the form of the tissue modulus and degree of anisotropy, no benefit was found when using the higher order relationship. A good agreement was found with the linear relationship in the Robson Brown et al study when using a similar method in the study by Wijayathunga et al.[38].

Chevalier et al. [58] and Kinzl et al. [60] used other methods of representing the material properties. In these studies an enhanced continuum FE model was used where, rather than using the more common method of converting  $\mu$ CT voxels directly into hexahedral elements, they used high-resolution CT images, which included the cortex and used fabric-elasticity relationships to describe bone morphology. This deviation away from the more common methods used by others [38, 56], potentially allows  $\mu$ CT at lower resolutions to be used, which both reduces computational cost and introduces possibilities for the use of clinically relevant resolutions. The use of lower resolutions was achieved by using 82  $\mu\text{m}$  scans and coarsening them to 1.312 mm to mimic common clinical CT scans. With a focus on identifying modelling errors, a study by Pahr and Zysset [64] compared this enhanced continuum FE models with standard methods. This study looked at both the effect of smooth cortex modelling (also used by Chevalier and Kinzl) and the morphology-elasticity relationship. Pahr and Zysset concluded that this method of modelling provided statistically equivalent results for the stiffness of two different models when compared to the more common method, whilst analysing the model at least 100 times faster. This reduction in

time to analyse the models was due to the reduced sensitivity to mesh size, meaning mesh density and therefore number of nodes / elements could be reduced.

### 1.4.3 Modelling Vertebroplasty

The methods used to model vertebroplasty from a selection of studies are summarised in Table 1.4. The variation in geometry generation can be seen to vary similarly to studies modelling vertebrae alone, however, in addition to this, the generation of cement geometry and material properties is also presented due to the range of methods used.

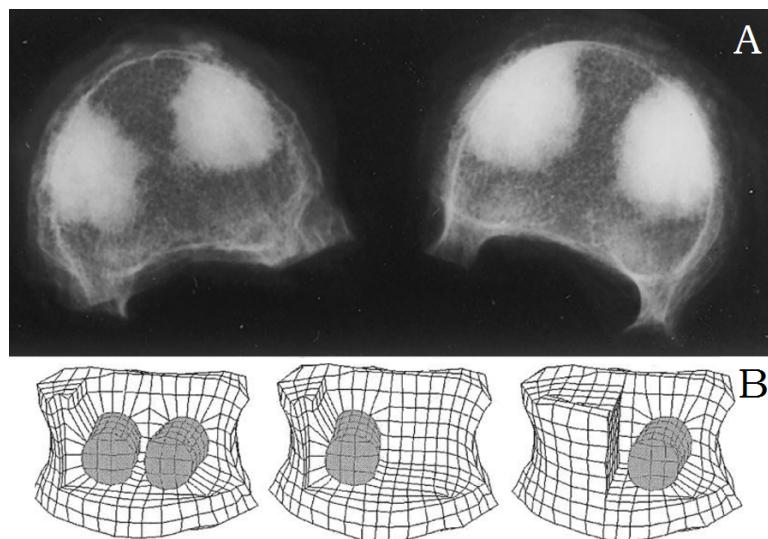


Figure 1.7: A: Top view  $\mu$ CT scans of human vertebrae augmented *in vitro*, showing gradual reduction of cement opacity to the edges of the internal cement volume, adapted from Belkoff et al. [19]. B: The augmented model generation for the study carried out by Liebschner et al. [65].

Methods of modelling vertebroplasty usually involve using  $\mu$ CT scans of augmented vertebrae, masking the internal volume of cement though thresholding the greyscale background. However, the methods used in the studies by Liebschner et al., Polikeit et al. and Baroud et al. [65, 66, 67] used approximations of the cement distribution, with the former modelling the distribution according to images from *in vitro* experiments and clinical trial CT scans, while the other studies modelled the cement more approximately. Such approximations of the internal volume of cement can be seen in Fig. 1.7:B. The  $\mu$ CT scans in Fig. 1.7:A show the much more loosely defined boundaries of the more random internal cement regions, which are created by the trabecular bone that the cement is injected into. The voxels within the defined cement region are often given linear orthotropic elastic properties described by a rule of mixture [68], or more basic material properties with constant elastic modulus and Poisson ration [38, 65, 66, 67].

Table 1.4: Method of geometry generation, cement position, location and materials used for five finite element studies of vertebroplasty.

Author	Geometry	Cement position & shape	Cement material
Baroud et al. [66]	Hand modelled , described in Smit et al. 1997, two level model	Used 70% fill of cement	Used previously obtained values for cement infiltrated bone, 46 times stronger, 12 times stiffer than surrounding trabecular bone.
Chevalier et al. [68]	$\mu$ CT scanned pre and post augmentation, model of vertebroplasty combined cement region with non-augmented scan.	Cement position and structure taken directly from $\mu$ CT scans	Bone-cement mixture described by a rule of mixture using a tensor for the isotropic stiffness and for bone stiffness.
Liebschner et al. [65]	Taken from $\mu$ CT data	Cement capsule design, cylinder with rounded edges. Positioned to investigate uni/bipedicular vertebroplasty and centred cement positioning.	Unspecified, PMMA
Polkeit et al. [67]	Taken from CT scans at 1 mm resolution, manually constructed details not visible. Two level model	Cement modelled as barrels using radiographs as guides. Positioned to investigate uni/bipedicular vertebroplasty including one model with 100 % fill	Constant Young's modulus (3000 MPa) & Poisson ratio (0.41)
Wijayathunga et al.[38]	$\mu$ CT scanned post augmented vertebrae	Identified from $\mu$ CT scan using constant threshold value based on greyscale	Used constant properties for Young's modulus and yield stress. Examined effect of lowering cement modulus to align with that of cement impregnated bone

The studies by Chevalier [68] and Wijayathunga [38] were the only ones to use experimental cement distributions in their FE models. The other studies listed in Table 1.4 rely on previously validated models of non-augmented vertebrae, with approximately shaped and placed cement. While such studies can report changes in the overall stiffness, it is difficult to identify how the load is transferred through the internal cement and whether it has been modelled with the correct material properties and boundary conditions for the cement-bone interface. Wijayathunga et al. [38] found large errors between experimental and computational augmented vertebral behaviour, concluding that the representation of the internal cement region as a homogenous material were possibly inadequate. In light of these results the lack of a comparison to in vitro results in the Chevalier et al. [68] study (in order to study prophylactic vertebroplasty) generates questions of the accuracy of cement modelling, in both material properties and boundary conditions.

#### 1.4.3.1 Bone-Cement Interface

Studies have shown that simple approaches to modelling augmentation do not accurately describe the results seen experimentally [38]. Hence, modelling the bone-cement interface is a vital step in portraying the experimental results.

Zhao et al. and Tozzi, Zhang & Tong [69], [70], used a  $\mu$ FE method to investigate the bone-cement interface. They assigned homogenous and orthotropic elastic-plastic properties respectively along with examining the effect of friction between the two surfaces (coefficient of friction 0.3 and 0.4 respectively). Both studies used stepwise compression testing of their trabecular bone-cement samples (open cell rigid polyurethane foam, similar to osteoporotic human trabecular bone and bovine trabecular samples from the iliac crest, Zhao et al. and Tozzi, Zhang & Tong respectively) within a  $\mu$ CT scanner to assess the evolution of stress in a stepwise fashion. These studies found good agreement with computational and experimental data, with Zhao et al. showing that a composite of bone and cement was considerably lower than what would be expected by cement alone or predicted by a rule of mixtures, such as that used in other studies described above [68]. Tozzi, Zhang & Tong found that greater cement penetration or contact area did not increase the compressive strength contradicting the results of Janssen, Mann & Verdonschot [71] in a FE study of cemented total hip arthroplasty. This study examined friction coefficients and morphology under both compression and tension, which along with the results of Tozzi, Zhang & Tong potentially suggest that cement penetration is more important for failure under tension rather than compressive loading. This advocates the idea of buckling trabeculae at the boundary of the cement region and a lack of load transfer into the cement-bone

interdigitated region.

In a similar study to those by Zhao et al. and Tozzi, Zhang & Tong [69], [70], Kinzl et al. [72] examined the effect of PMMA shrinkage due to polymerisation and different interface properties. The shrinkage of PMMA upon polymerisation affects the bone-cement interface due to gaps developing between the two materials caused by the volume change of the PMMA. Kinzl et al. showed that the shrinkage affected their models in two ways, firstly, the loss of volume and creation of gaps reduced the load transmission between the materials and secondly it created residual stresses in the PMMA, causing bone damage at trabecular connections from compressive and shear loading.

Sikora [73] used FE models generated from  $\mu$ CT images of ovine lumbar vertebra to investigate the bone–cement interface. An analytical model of the behaviour of trabecular bone struts embedded in cement was used to impose properties on an interface region defined in the model. The analytical model was used to predict the interdigitation between the two materials and forecast the characteristics of failure between them, it was then used to determine the plastic and elastic properties to apply to the defined interface mesh. The use of the interface layer with explicitly defined properties produced a good agreement with the experimentally determined results for the sample under compression. However, the study was carried out using cylindrical specimens of height 25 mm and diameter 13 mm, hence a further investigation would be required to identify whether this method would prove useful for modelling whole vertebrae.

#### 1.4.4 Discussion of FE studies

Finite element studies modelling vertebrae are currently producing accurate models for single intact vertebrae. The methods employed by Chevalier et al. [58] to reduce the need for high resolution  $\mu$ CT scans and instead use more clinically relevant resolution, present a valuable tool for clinicians. Problems arise however when attentions are turned to modelling vertebroplasty, specifically, modelling how the two materials interact while under compression.

Despite the well validated results for the three  $\mu$ FE interface studies [69], [70], [72], which examined more accurate methods of modelling the boundary between materials, the computational cost of running such simulations on whole vertebrae restricts further research. Especially given the 700 hours on a high performance computer reported by Zhao et al. [69] for a trabecular sample. Hence, methods employed by Sikora [74] require further testing and validation for whole vertebrae in order to strike a balance between agreement

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with experimental data and computational cost.

## 1.5 Capture of Population Variation

There is an increasing need for patient variation to be taken into account in pre-clinical testing; however, experimentally there can be difficulties in controlling this variation. Obtaining large quantities of varied tissue can be problematic and time consuming, along with the problems of characterising the variation. Relating to the spine: in vitro studies are limited by tissue availability and controlling and understanding its variability (especially for human studies) and in vivo studies are heavily limited by the invasiveness of any measuring methods. Hence, FE studies present a vital method in assessing the spine. Currently however, the main advantage of FE studies is the ability to run multiple scenarios for the same model (for example using different material properties for implants or different quantities of cement in vertebroplasty studies); this removes variability from the study. In order to use FE studies to examine patient variability across the population then there is a need for large quantities of patient specific models, similarly to experimental work.

Variability in terms of shape, size and density of vertebrae is high between individuals, with even greater variability for those with various pathologies. The effects that this variation has of vertebroplasty is very important, whether certain variables result in more positive outcomes or others suggest more conservative treatments are more suitable. Hence, large sets of models that cover the whole range of variation across the population and then categorised based of vertebroplasty effectiveness, could be used to predict outcomes clinically.

However, these large datasets are difficult to gain access to, for ethical reasons among others [75] and current FE studies usually do not attempt to model population variation and instead use vertebrae specific models from a limited selection of experimental specimens [38, 57, 60, 68].

Parameterised finite element models are often used to understand the effect of variables on a system, however, understanding which variables are important and how to set the limits of these variables becomes difficult with the increasing complexity of the system. Statistical approaches that are able to determine the main modes of variation and therefore reduce the number of variation types to those that have the greatest impact can aid such parameterised approaches.

Statistical shape modelling (SSM) and statistical shape and appearance modelling (SSAM)

approaches describe the geometric variation and the material property variation across an input set of models that describe the population [76]. Such models usually describe a mean shape and the main modes of variation found within the population.

### 1.5.1 Principal Component Analysis Methods

The purpose of Principal Component Analysis (PCA) is to capture the variation within a given dataset. It allows an understanding of how different variables interact and what variables control the greatest variation. Here, there is a focus on using PCA for shape analysis, but the algorithm can be used for many other types of data. The variation in data is expressed as eigenvalues which become the principal components for the data-set. These eigenvalues or principal components can then be ranked, allowing an understanding of what variables describe the greatest variation in the data-set (for example the general size or length of a bone). With regard to the biomedical field, it has been applied to sets of data containing similar shapes, such as sets of human femurs and knee joints. In these examples it allows an understanding of how the bones vary across the population contained in the given data-set.

Often the first step for PCA is to normalise scaling, rotational and translation differences between the specimens within the dataset. This is carried out via generalised Procrustes analysis (GPA) and is often referred to as a prepossessing step for PCA, it is described in detail by Grassi et al. [75] and Väänänen et al. [77]. Once normalised, matrices are created from columns containing specimens and rows containing the nodal coordinates for each mesh. Using this matrix and the mean coordinates from it, the PCA algorithm can be applied, from which the principal components can be acquired. These principal components describe each mode of variation, ordered in terms of the largest variance. To determine how much variation is contained within each principal component, the eigenvalue for each component can be divided by the sum of all eigenvalues. The first three modes of shape variation for a femur (used here as a convenient example) can be seen in Figure 1.8, with the minimum and maximum extremes from each mode of variation seen in the wireframe and shaded model respectively [75].

Similar methods can be used for the BMD and how it varies between specimens. Once models were generated with BMD assigned to each element, another matrix is assembled with rows consisting of the BMD of each element in the mesh. From which a similar method to above can be applied to acquire the principal components and the amount of variation contained within each components.

The understanding of the variation of a data-set and its description in terms of a potentially reduced number of components, allows the generation of virtual specimens that fit within the ranges of the input data set. For example principal components could be altered in terms of their standard deviation about the mean specimen (based on the input data). This would allow the generation of virtual specimens that fit within the bounds of variation of the current data, but do not currently exist due to possible gaps in the data set. It also means that the variation can be quantified, allowing effects caused by variation to be studied in an iterative fashion. For example, in the case of vertebrae, if changes to the diameter of the spinal canal correlate with process length (a correlation that would be difficult to identify without PCA), then the effect this has on specimen strength can be examined in depth by altering the component that controls this relationship. Models that are described by this relationship and could be generated and solved through FEA, furthering our understanding of the relationship. However, generating models from the statistical models can produce some problems regarding reliability. For example, the generated models heavily rely on the input database, hence the database is required to evenly represent the entire population. There can also be issues with the generating algorithm's ability to produce shapes and materials not present in the starting database [75], [77].

The Grassi et al. study [75] into whether PCA based modelling can be used for the femur concluded that such generated models were able to describe the population of femurs using generated FE models. They found that 50 modes or the first 50 principal components were required to accurately reconstruct the femur while maintaining errors below that originating from pixel size and another 40 to generate accurate density in the models.

In a study by Fitzpatrick et al. [78] statistical shape models were developed in order to identify the relationship between the shape and function of the patellofemoral joint. Here, 26 magnetic resonance scans of the knee were taken, from which FE models of the joint in question were created. PCA was applied to the set of models, from which the first 15 principal components describing the shape were taken, these 15 components accounted for 97.2% of the total geometric variation, with the first component (PC1) counting for 47.7 %. PC1, as is often the case in biological models, described the variation in the size of the joint components, with the next two components describing the position of the patella and details regarding the conformity and depth of the joint. Following modes of variation described more subtle variations in the geometry of the model.

In order to assess the robustness or ability to accurately predict outcomes of the reconstructed bones or joints, the studies [75, 78] use a leave-one-out approach. This approach neglects one specimen from the development of the shape-function models. The final model,



Figure 1.8: Femoral shape variations for the first three modes from the PCA. From 115 bones the maximum eigenvalue is shown with the minimum eigenvalue shown in wireframe. Taken from [75].

based on the included specimens can be used to predict the mechanics or properties of the left out specimen by using the generated FE models.

### 1.5.2 Discussion

The studies described above present useful workflows of generating virtual subjects from a statistical model acquired from a databases of scans. Such methods allow a variety of population based studies, including those regarding the variation of vertebrae across the population.

The ability to generate models not present in the input dataset and hence create a large set of models representing the population allows us to identify relationships not openly visible. For example in the study by Fitzpatrick et al. [78] a 5 mm change in the patella position caused a 25% increase in the contact pressure mid-flexion. This relatively easy quantification of the relationship between geometry and function can easily be transformed to quantify the relationship between vertebral geometry and the mechanical response to vertebroplasty. Equally, such relationships could enable the prediction of vertebral fracture, adjacent level fracture or advise clinicians as to the quantity and location of cement for

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different patients.

## 1.6 Conclusion

Vertebroplasty potentially provides a valuable method to treat patients with osteoporotic compression fractures, however, the uncertainty regarding its effects, especially regarding certain subsets of patients, mean that further research is required. While the mechanisms of pain relief are not fully understood, certain assumptions regarding the mechanical stabilisation and restoration of stiffness can be investigated. Such investigations may help to understand how patient groups respond to the treatment in different ways.

Current experimental studies have provided a range of useful techniques for mechanically testing vertebrae and for carrying out the vertebroplasty procedure itself. However, obtaining enough vertebrae to represent variation across a population in order understand its effects on different patients is a difficult task and has not been attempted. A possible solution is FE modelling in conjunction with PCA. FE models have been shown to represent the intact vertebrae accurately using both  $\mu$ FE and continuum level models.

Problems arise when modelling the augmented vertebrae, with few studies modelling specimen specific augmented vertebrae and instead modelling vertebrae with arbitrary volumes of cement. Studies that have modelled and validated against experimental results have shown poor agreement, owing to the incorrect modelling of the cement-bone interface or incorrect selection of material properties for the cement-bone interdigitated region.

Finally, principal component analysis has shown its value in the literature presented above allowing the variation in a set of specimens to be accurately described and in certain cases models have been spawned at standard variations away from the mean.

## 1.7 Aims & Objectives

The main aim for the project is to examine whether the outcomes for patients undergoing vertebroplasty are due to underlying biomechanical difference in their vertebrae. To achieve this overall aim three objectives have been defined:

1. To model specimen specific vertebrae accurately, initially using bovine tail vertebrae and later human vertebrae.
2. To carry out vertebra augmentation experimentally and accurately model the results of this augmentation in specimen specific models. This will require an investigation

into the cement–bone interface within FE models, allowing the accurate modelling of augmented vertebrae.

3. To use PCA to identify patient subsets that respond differently to the mechanical outcomes of vertebroplasty.

The first objective will require both experimental and computational work-flows. Experimental work will focus on testing methods using bovine tail vertebrae, with an aim to adapt methods to use human vertebrae. Computational work will concentrate on the creation of models of the bovine vertebrae that agree with experimental results for stiffness.

The second objective will involve developing methods of carrying out vertebroplasty on bovine specimens, aiming for clinically relevant volumes of cement using methods similar to those used in a clinical setting. The computational side to this objective is to further the understanding of modelling cement–bone interfaces, allowing accurate models of augmented vertebrae to be made.

To achieve the final objective, an understanding of PCA will need to be developed along with how to apply it to vertebrae. This will include methods of registering the volumes that define the vertebral body, applying the PCA algorithm and producing spawned vertebrae to help understand the variation in vertebrae of the population.

# Chapter 2

## Bovine Tail Vertebrae Study

### 2.1 Introduction

This chapter is split into two main sections discussing initially the development of experimental methods testing bovine tail vertebrae with the second section describing the methods of computationally modelling these vertebrae using FEA@. These main sections are split further into method development, sensitivity tests and the results. In this chapter the experimental and computational work is limited to bovine tail vertebrae due to their plentiful nature and relatively similar geometry to human vertebrae, while not having many of the problems with increased yield strength and density of porcine or other tissue [79]. Allowing translation into using the same or similar methods with human lumbar vertebrae in the following chapter.

### 2.2 Experimental Methods

#### 2.2.1 Introduction

The experimental methods that have been developed and the early results acquired in this sections allow easier transition to using human tissue and provide valuable results for the development of specimen specific finite element models. Studying these bovine tail vertebrae allows the development of methods for material testing, acquiring  $\mu$ CT scans of the specimens and carrying out vertebroplasty on the specimens. This is in addition to developing computational models of the vertebrae discussed in section 2.3. The following section will detail the development of various aspects of the experimental procedure, difficulties encountered and traversed, experimental results and finally a discussion of the

methods, results and future work.

The steps involved in the developed methods involve dissection of the soft tissue from the vertebrae, potting in PMMA end-caps, scanning using a  $\mu$ CT scanner, compression testing and augmentation, the order of which can be seen in fig. 2.1. Specimen preparation, fracture generation and initial  $\mu$ CT scanning was undertaken jointly with Ruth Coe (PhD student, University of Leeds). Vertebroplasty (following initial training attempts carried out with Dr Peter Loughenbury & Dr Vishal Borse from the Leeds General Infirmary) and subsequent loading and scanning was carried out solely by the author.

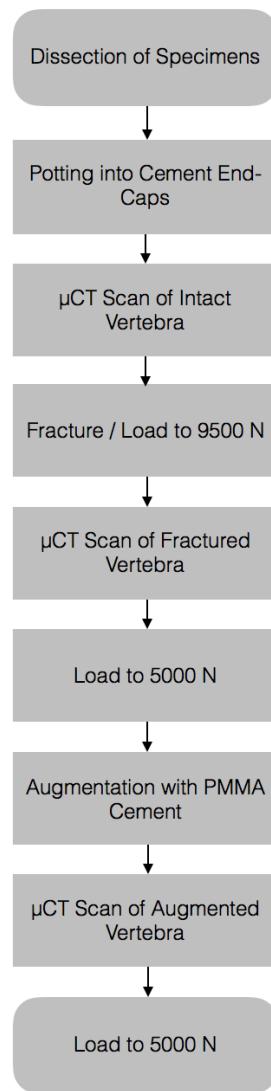


Figure 2.1: Flow-chart detailing the experimental process from initial dissection to final load test.

### 2.2.2 Specimen Preparation

Bovine tails were acquired from a local abattoir and frozen to -20°C prior to use. They were defrosted in a 4°C fridge for approximately 24 hours before the initial dissection. The three most caudal vertebral (CC1 to CC3) were kept, discarding the remainder of the tail due to the elongation of the vertebral body further distal of the first three vertebrae. In addition to the elongation of the vertebral body the spinal canal narrows limiting its ability to house a steel rod used for mounting the vertebrae in PMMA end-caps. Soft tissue was removed from the vertebrae as thoroughly as possible, including the intervertebral disc material and material occupying the spinal canal. This was carried out in order to remove potential error when comparing experimental results of stiffness to the vertebra models developed from  $\mu$ CT scans (due to difficulties modelling the soft tissues) and to allow a metal rod through the spinal canal to aid alignment.

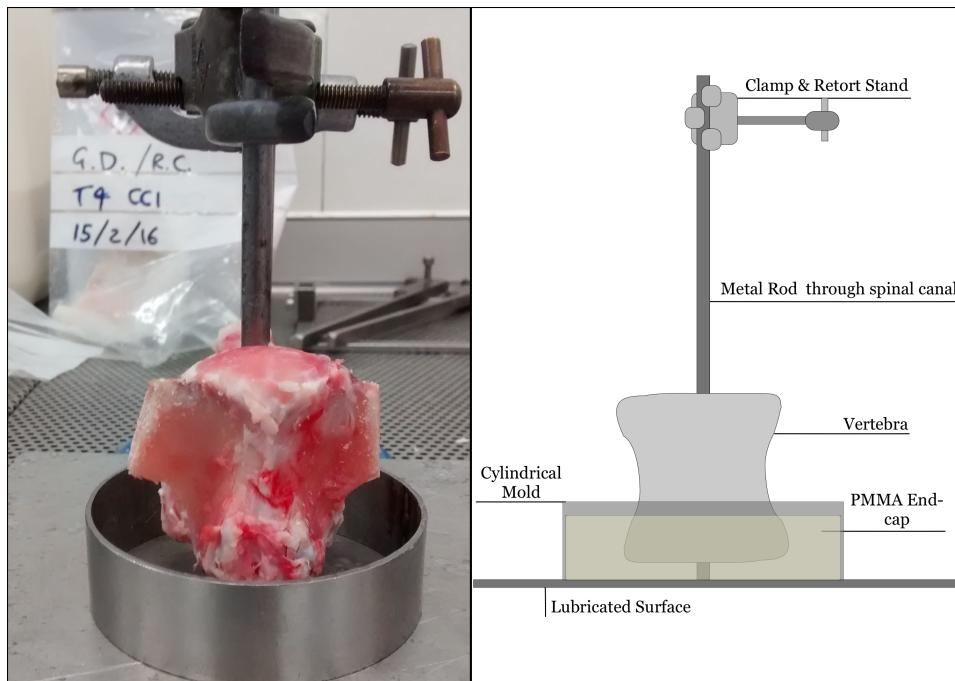


Figure 2.2: Photograph and diagram depicting the method of creating end-caps for the specimens.

Once dissected (and in subsequent breaks between procedure steps) the vertebrae were wrapped in phosphate buffered solution (PBS) soaked tissue, to limit the drying of the vertebral bone. The specimens were potted in PMMA end-caps to allow repeated loading of the vertebrae with the same orientation and positioning, while constraining the vertebrae as little as possible and allowing flexion of the upper endplate. Such flexion (anterior and posterior bending), occurs naturally in the human spine, hence representing this experimentally is important. The setup for potting the vertebrae can be seen in fig. 2.2. Vertebrae were held using retort stands and clamps holding a rod placed through the

spinal canal. Depending on the level of the vertebrae the spinal canal was packed with foam around the rod forming a snug fit while the vertebrae was held approximately 5 mm above a petroleum jelly lubricated metal surface. Also, depending on the level of the vertebrae, any pedicles that protruded past the limits of the metal cylinders were removed with a hacksaw at their base to prevent issues with the loading and scanning tests which followed, most often this was limited to the most caudal vertebrae. The removed pedicles can be seen in fig. 2.2. Lubricated hollow metal cylinders of  $\sim$ 10 cm diameter were used to form the endplate when the 2:1 powder to liquid component PMMA mixture was added. PMMA was added until the endplate of the vertebral body was covered up to the point where the body starts to become concave. After approximately 20 minutes the PMMA had sufficiently set to turn over the vertebra and create the end-cap at the other end using the same process with the addition of a level to ensure the creation of parallel end-caps.

Once the PMMA was set the vertebrae were wrapped in more PBS soaked tissue before being frozen or stored in a fridge until the vertebrae were loaded to fracture. The specimens were frozen only if more than 24 hours would pass before the next stage of testing to reduce the number of freeze thaw cycles.

### **2.2.3 Axial Compression**

#### **2.2.3.1 Fracture Creation**

All specimens underwent axial compression using a material testing machine in order to generate fractures within the vertebral body. Mounted vertebrae were placed between two steel end-plates, the lower of which contains four screws to inhibit lateral motion of the specimen when under load and the upper plate contains similar screws, with the addition of a chamfered hole. This chamfered hole allows the alignment of the specimen so that the loading point was directly below the head of the testing machine using the marker located above the centre of the vertebral body. The steel ball becomes the centre of rotation for the free to rotate upper end-cap. This permitted rotation mimics natural loading of the vertebrae and increases the likelihood of physiological anterior wedge fractures. Details of the setup can be seen in fig. 2.3.

Loading of the vertebrae starts with a preload from 50 N to 300 N for 10 cycles at a rate of 1mm/minute to remove any viscoelastic effects of any remaining soft tissue. Following the preload, displacement was increased by 1 mm/minute until either the load reached 9500 N (a safety limit due to the 10 kN load cell limit) or a visible failure occurred on the real-time load-displacement plot during compression. This failure was observed as a peak

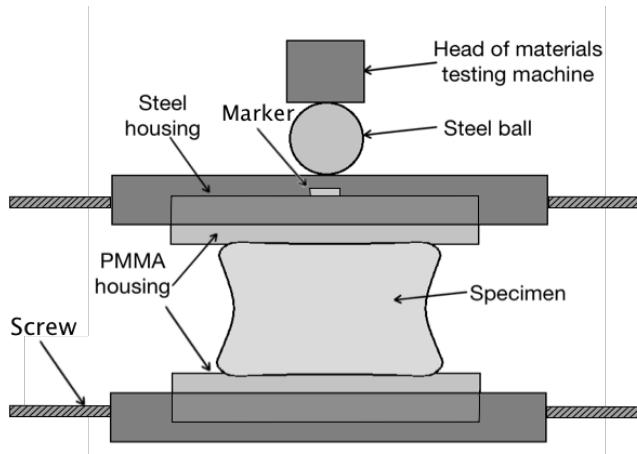


Figure 2.3: The experimental setup for axial loading the vertebral specimens.

in load with the compression being stopped once clear decrease in load was observed. Both scenarios can be seen in fig. 2.4.

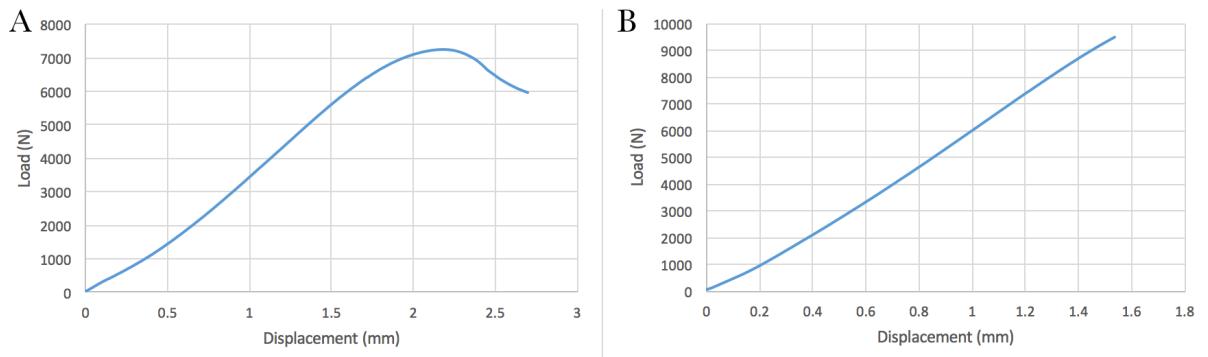


Figure 2.4: The difference between failure (A) and non-failure (B) for bovine tail vertebra compressed to a maximum load of 9500 N or until a peak was observed.

### 2.2.3.2 Post Fracture & Post Augmentation Loading & Stiffness Calculation

In order to find the stiffness of the previously fractured and augmented specimens a similar loading procedure was used. However, following the preload, compression was stopped when the load reached 5000 N as a means to limit additional damage and fractures to the vertebrae. This ensured that the vertebral stiffness across the three stages (intact, post-fracture and post-augmentation) was calculated from the same range of loads (0 - 5000 N). To examine the effect that the initial load to failure has on the following loads, both post-fracture and post-augmentation, a control specimen was used. This control (T1 CC3) was only loaded up to 5000 N before ending the test.

The stiffness of the specimens throughout their tests was calculated using a Python script on the raw data from the materials testing machine. The script allowed the limits of the

range of interest to be set and, using a defined segment size, incremented over the data reporting the greatest stiffness found in a segment. The segment size was set to 0.3 mm. The script iterated over the data in overlapping increments of 0.1 mm and the range of interest was set to 0 - 5000 N, an explanation of this can be seen in fig. 2.5.

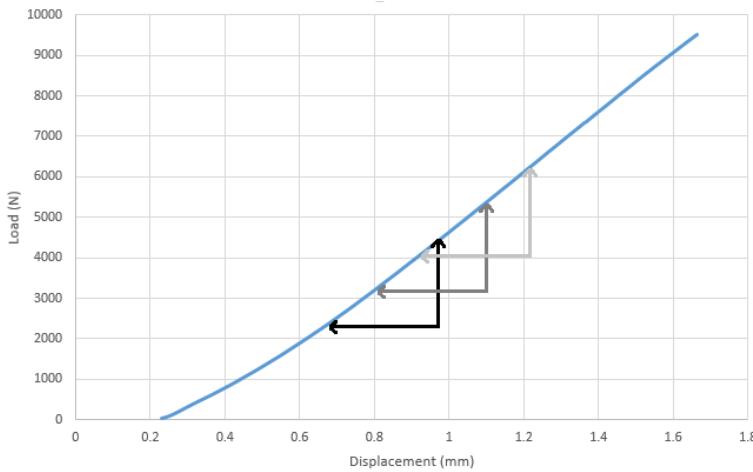


Figure 2.5: A typical load displacement curve showing how the gradient was taken from 0.3 mm long sections incremented at 0.1 mm across the length of the curve.

If the load-displacement curves were perfectly linear within the “linear region” the stiffness in the three ranges of interest in fig. 2.6 (0-1500 N, 0-5000 N and 0-9500 N) would give an equal value for the stiffness or maximum gradient. However, given that these values were found to differ for the three ranges it suggested non-linear behaviour. As shown in fig. 2.6 the recorded maximum stiffness varies greatly depending on what portion of the load displacement graph was being examined. With the maximum stiffness only measurable with the 0-9500 N range. Given that the measured stiffness in the 0 to 5000 N is much closer to the measurement with the full range is included, compared to only including the 0 to 1500 N, it was decided this was a reasonable trade off given the attempt to limit the damage with post fracture tests and the need for a uniform measurement range.

## 2.2.4 Vertebroplasty

The procedure was developed in collaboration with two clinicians (Dr Peter Loughenbury & Dr Vishal Borse) from the Leeds General Infirmary. Subsequent tests of the procedure were undertaken with the aid of Dr Sebastien Sikora, Dr Fernando Zapata Cornelio & Ruth Coe (Research Fellow, Research Fellow & PhD student respectively), while the specimens presented in the results below were augmented solely by the author.

Due to the differences between human and bovine vertebrae it was not possible to perform bi-pedicular vertebroplasty on the bovine specimens using the methodologies established

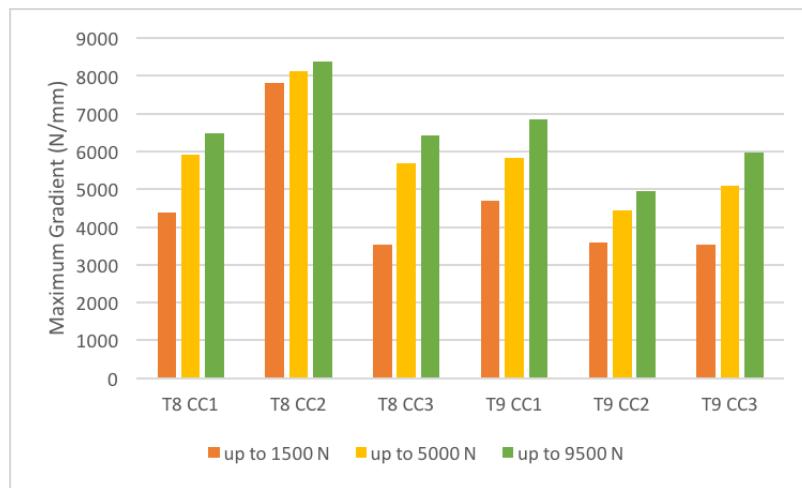


Figure 2.6: The difference seen when measuring the greatest gradient (stiffness) using different portions of the load displacement curve. From 0 to 1500 N, 0 to 5000N and 0 to 9500N.

for human vertebra. The main difficulty was the greatly increased density of the bovine vertebra bone, meaning that rather than pushing the vertebroplasty needle into the vertebra by hand, a mallet and vice to hold the vertebra were required. In addition to this, the force required to inject cement into the vertebral body was greatly increased. The vertebroplasty method for bovine tail vertebra was therefore developed over several iterations due to these difficulties. This sub-section details the initial procedure, the problems encountered and solutions developed to allow a clinically relevant volume of cement to be injected and captured in  $\mu$ CT scans.

#### 2.2.4.1 Initial Procedure

The procedure was initiated by using bone nibblers to remove the rounded end of both posterior pedicles, providing a surface to start the needle entry. While holding the vertebra in a table mounted vice the needle's 1 cm markings were used to estimate the depth and angle needed to reach the anterior quarter of the vertebral body. The placement of the needle required care to ensure the pedicle was not damaged through splitting as it was inserted. A mallet was used to insert the needle until it was at the depth required; the procedure was repeated for the other pedicle, reusing the same needle.

The PMMA cement was mixed 1:1 monomer to powder to ensure that it could be drawn up via the syringe and to allow enough time to inject the cement before it thickened and set. This additional setting time and reduced viscosity is also used by clinicians, who use ratios up to 0.74 monomer to powder with no adverse outcomes associated despite the reduced modulus and strength often reported [80, 81]. While the vertebra was held in the

clamp of a retort stand, the syringe was attached to the needle, which in turn was inserted into one of the pre-made tracks through the pedicle into the vertebral body. Cement was pushed into the vertebrae using the syringe, until 3-4 mL was inserted into both sides of the vertebrae, with cement being used to back fill as the needle was removed to fill the channel created by the needle. The vertebrae were then left for approximately an hour until the cement had set before scanning.

#### 2.2.4.2 Complications and Changes to the Procedure

Various problems were encountered while carrying out the procedure that required the methods to be adapted. These challenges and their solutions are described below.

**Vertebral Temperature:** The first of these was the difficulty found injecting any cement into the vertebra. With the initial specimens, cement was injected but it was mainly limited to the needle tracks rather than the vertebral body. To counter this the vertebrae were warmed to 37°C for an hour or until the internal temperature of the vertebrae had reached this temperature (using a temperature probe in the vertebroplasty needle hole). This meant that the bone marrow inside the vertebrae was no longer solid and therefore could be displaced by the cement making the injection much easier.

**Radio-opacity of Cement:** A second problem was the opacity of the cement on  $\mu$ CT scans, which proved difficult to segment and separate it from the trabeculae in the vertebral body as can be seen in fig. 2.7:A. Here, the cement was indistinguishable from the bone marrow and can only be seen in the needle channel. The solution to this was to mix barium sulphate ( $\text{BaSO}_4$ ) with the PMMA to achieve the radio opacity seen in fig. 2.7:B, where the bright area in the centre of the vertebral body is the injected cement and  $\text{BaSO}_4$  combined. Due to the hydrophilic nature of the  $\text{BaSO}_4$  powder it was important to use a completely dry beaker when thoroughly mixing it with the PMMA powder to limit aggregation of the  $\text{BaSO}_4$ , which can be seen in the bright spots in fig. 2.7:B. The two components were used in a 1:4  $\text{BaSO}_4$  to PMMA powder ratio, mixed 1:1 with the liquid PMMA component.

**Cement Leaking from Vascular Channels:** Preventing the cement from exiting the vertebrae from vascular channels while injecting the cement proved to be another obstacle to achieving a physiologic fill volume for the vertebrae. These channels lead both out the anterior face and from the vertebral body into the spinal canal, this can be seen in fig. 2.8 and 2.9. In the body these channels would be filled with vasculature preventing the cement leaking through them. Two main methods were used to stop cement leaking while carrying

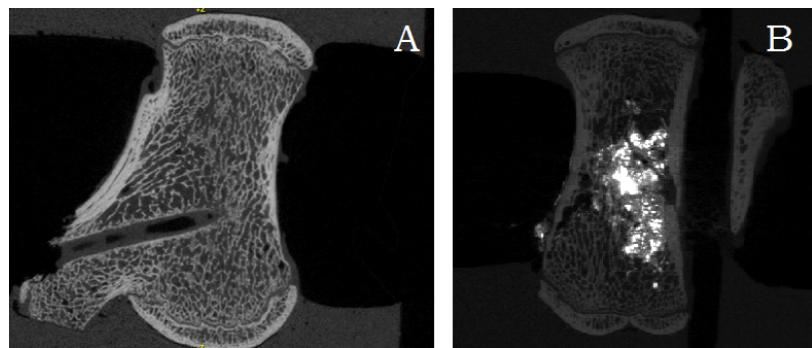


Figure 2.7: A:  $\mu$ CT scan of an augmented vertebrae, with some visible PMMA residing in the needle channel. B:  $\mu$ CT scan of an augmented vertebrae using PMMA mixed with barium sulphate.

out the procedure on the bovine tail vertebra. The first was to use the same rod used for mounting the vertebrae in their end-caps to limit the passage of cement into the spinal canal. The second was to use blu-tac to cover the external vascular channels, wrapped with cling-film to hold it in place. This allowed any bone marrow free passage out of the vertebrae, but enough resistance to limit the flow of cement.

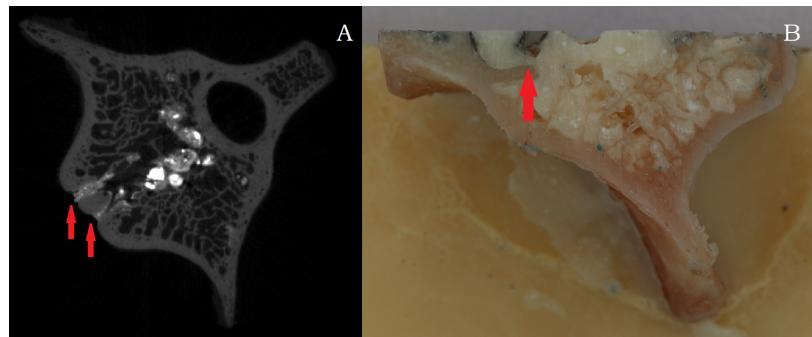


Figure 2.8: A:  $\mu$ CT scan of an augmented vertebrae showing the cement leaking from vascular channels on the anterior side. B: Photograph of an augmented vertebrae cut into four quarters showing a vascular channel leading into the spinal canal.

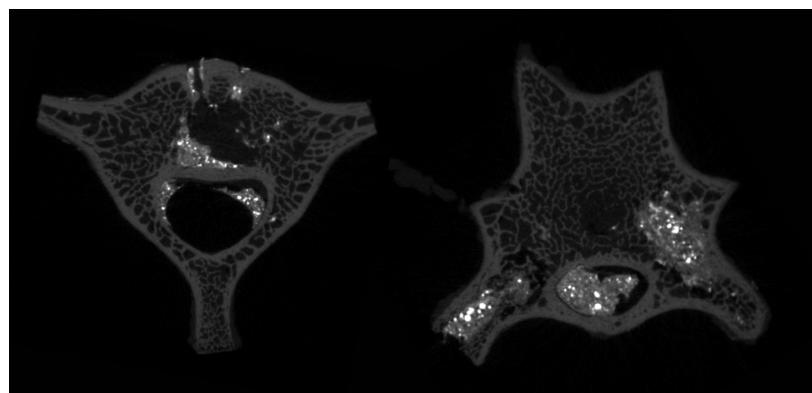


Figure 2.9:  $\mu$ CT scans of two vertebra, showing the cement leaking into the spinal canal and out of the vascular channels and the vertebral surface.

### 2.2.5 MicroCT Scanning

$\mu$ CT scans were taken at three occasions during the experimental process. These scans occur before and after the initial load to failure, then following the augmentation of the specimens. The process requires the vertebrae to be defrosted and at room temperature, given that the radio-opacity of water differs between solid and liquid states, hence vertebrae were usually defrosted overnight in a 4°C fridge. Vertebrae were loaded two at a time in a carbon fibre loading cradle into a HR-pQCT (XtremeCT, Scanco Medical AG, Switzerland) scanner. The settings used for the scans were: an isotropic voxel size of 82  $\mu$ m, energy settings 900  $\mu$ A, 60 kVp and 300 ms exposure time. These settings were based upon previous studies using the same scanner and similar vertebrae carried out in the group [38, 56, 73, 79].

### 2.2.6 Results

The stiffness values for 12 vertebra from 6 bovine tails are shown in fig. 2.10. Of the twelve vertebra only two, the first and second tail vertebra of the second tail (T2 CC1 & T2 CC2), were fractured. The remaining nine (excluding T1 CC3, the control) reached 9500 N and therefore did not fail.

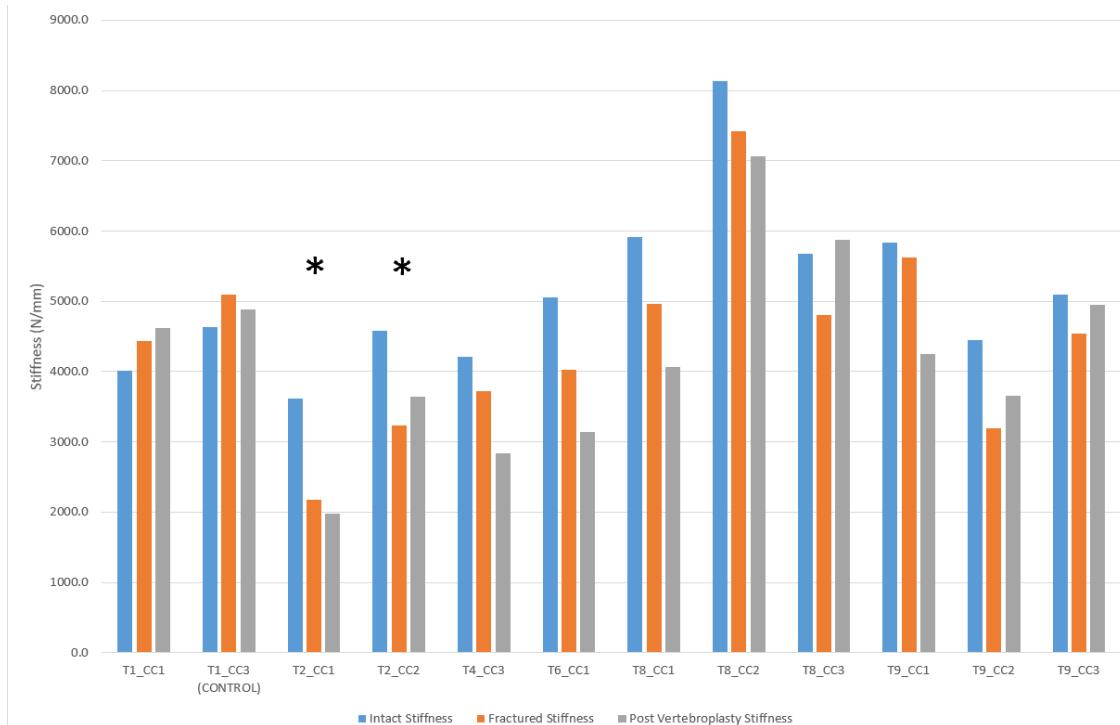


Figure 2.10: The maximum stiffness of 12 bovine tail vertebrae between 0 and 5000 N taken from load - displacement data. Showing the stiffness of the intact vertebrae, a post - fracture stiffness and a post - vertebralplasty stiffness for each. \* Indicates those specimens that achieved a clear failure below 9500 N.

The results for the fill volume of cement in the augmented specimens is presented in table 2.1 and was acquired from the down-sampled, segmented models generated from  $\mu$ CT scans. It shows that fill volume varies between 3% and 17% fill and in addition shows a lack of a correlation between fill volume and increase in augmented specimen stiffness over fractured stiffness with only five vertebrae showing an increase in stiffness. The images in fig. 2.11 shows the extent of the cement fill for the two vertebrae with the largest fill volume.

Table 2.1: The volume of cement and the vertebra volume for the 12 specimens used, along with the percentage cement fill and an indication as to whether the stiffnesses of the augmented vertebrae were greater than the fractured stiffness. This information was measured from the down-sampled models generated from  $\mu$ CT scans of the vertebrae.

Vertebrae	Cement Volume (mm <sup>3</sup> )	Vertebra Volume (mm <sup>3</sup> )	Cement Percentage of Vertebra Volume (%)	Increase in Augmented Stiffness over Fractured Stiffness
T1 CC1	2260	32440	6.97	*
T1 CC3	465	27039	1.72	
T2 CC1	663	23285	2.85	
T2 CC2	3405	20373	16.71	*
T4 CC3	1363	25446	5.36	
T6 CC1	830	29332	2.83	
T8 CC1	1257	37357	3.36	
T8 CC2	4489	29248	15.35	
T8 CC3	1041	28403	3.67	*
T9 CC1	2922	45681	6.40	
T9 CC2	2210	38894	5.68	*
T9 CC3	2437	35840	6.80	*

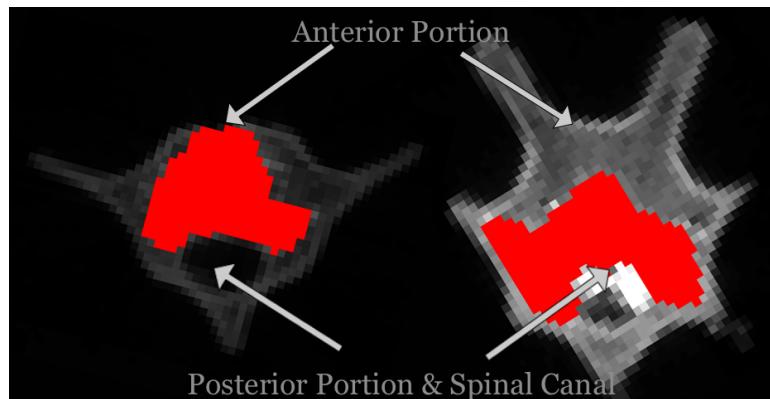


Figure 2.11: Axial  $\mu$ CT slices of T2-CC2 (left) and T8-CC2 (right), with cement masked in red, showing the extend of cement fill at the point where the cement was most anterior.

The attempt to reduce cement leaking through vasculature during the vertebroplasty procedure can be seen in fig. 2.12. The methods employed greatly reduced the the quantity of cement observed in both the spinal canal and around vascular channels at the vertebral

body surface when compared to scans in fig. 2.9.

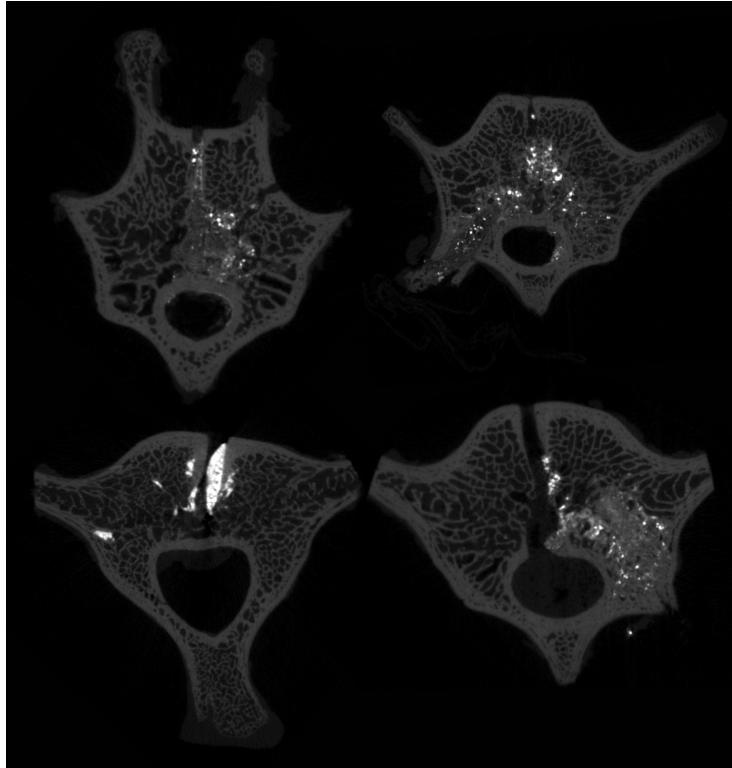


Figure 2.12:  $\mu$ CT scans of four augmented vertebra using a steel rod to fill the spinal canal and blu-tac to cover the external vascular channels. Shows greatly reduced cement content within the spinal canal with less cement at the surface of vascular channels.

The two plots in fig. 2.13 show a lack of correlation between the difference in stiffness after augmentation when compared to both the fractured and intact specimen stiffness and the intact stiffness. Showing that magnitude of any increase or decrease in the vertebral stiffness following augmentation is not caused, or a feature of the initial, intact vertebral stiffness.

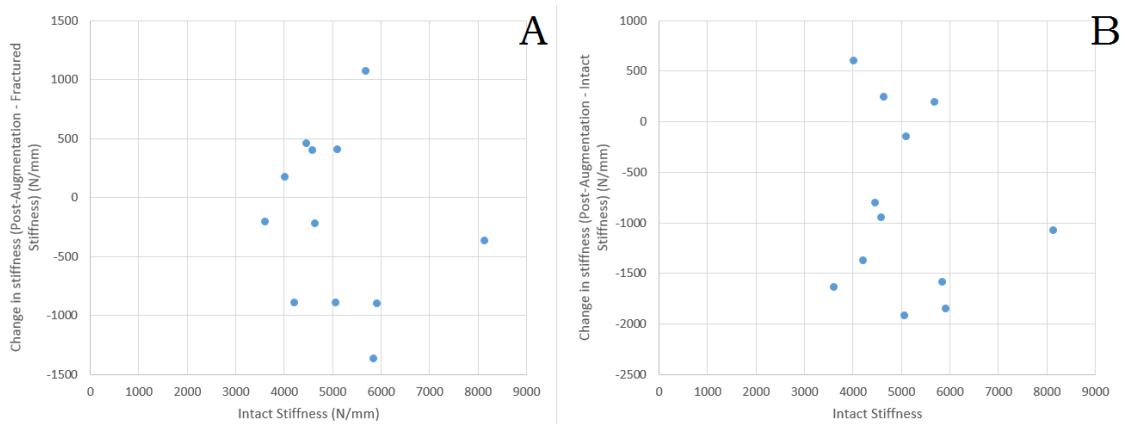


Figure 2.13: A: The difference between the post augmentation and fractured stiffness against the intact stiffness. B: The difference between the post augmentation and intact stiffness against the intact stiffness.

## 2.3 Finite Element Modelling

### 2.3.1 Introduction

The finite element modelling of the bovine tail vertebrae, once validated, allows investigations into various properties of the vertebrae and augmentation process. Such investigations include identification of geometric and material property features, which through the use of FE models can be changed programmatically to pinpoint their effects of certain physical scenarios. Scenarios such as vertebroplasty, where the variation can be extended to augmentation procedure variations, potentially leading to suggestions of best practice depending on the properties of the vertebra in question.

Here, the main aim was to develop methods that enable the creation of specimen specific models of bovine tail vertebrae, allowing creation and generation of the much more clinically relevant human lumbar vertebrae using similar methodologies. Initially the focus was on the generation of models that accurately describe the mechanical behaviour of intact bovine specimens, once this was achieved to a reasonable degree an attempt to model augmented specimens was made. In addition to these larger goals, certain sensitivity tests were carried out, including those to understand the effects that additional meshes, mesh sizes and mesh interactions have on model stiffness. Finally some preliminary investigations were made into the effect of changing augmented region positions, however the majority of this investigation will be reserved for chapter 4.

### 2.3.2 Model Creation

The computational analysis of linear-elastic finite element models was carried out using a combination the segmentation and meshing software, ScanIP (Simpleware, Exeter, UK) and the simulation software, Abaqus (Dassault Systemes, France). The  $\mu$ CT scans were converted into a finite element mesh using the former software package, this was then imported into the second piece of software to be configured and solved.

The scans acquired from the  $\mu$ CT scanner were converted from the ISQ file format, generated by the scanner software, into the more portable TIFF image format files using an existing in-house matlab script that additionally converts the greyscale of the scan into 256 bins. This conversion from 16 bit TIFF files with 65,536 bins to 8 bit TIFF files was required due to the limitation to 255 material properties within Abaqus, this allows one greyscale value per material property (assuming all 255 greyscale values are represented in the scan). Once the scan has been pre-processed it was imported into ScanIP ensuring that

the spacing of voxels was correctly set - in this case  $82 \mu\text{m}$ . Once imported, the location of the loading point was identified to simulate the correct experimental load within ABAQUS; the marker (see fig. 2.3) appears bright on the scan and its centre was taken as the load point, calculated by converting the position into mm. This was achieved by multiplying by the native resolution of  $82 \mu\text{m}$ .

The following parts of model creation were carried out using a Python script from within the ScanIP software. The script carries out the process described below and was generated by the author by carrying out the process manually and in order to understand the steps required and then writing a script to perform those actions. The development of the script removed much of the user variation in the segmentation of each vertebral model. The effect of user variation during the segmentation process is examined in section 2.3.4.5.

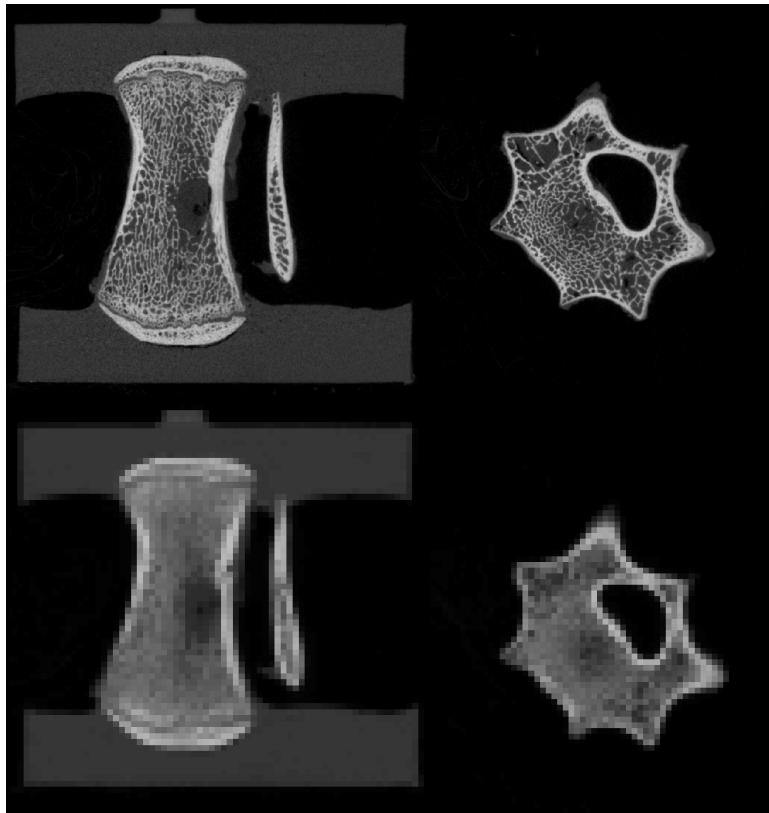


Figure 2.14: Side and top view of a vertebral  $\mu\text{CT}$  scan showing the effect of the downsample from  $82 \mu\text{m}$  to 1mm cubed.

It was easier to down-sample the image stack prior to segmentation, due to the time required for the software to generate high resolution masks and increased memory usage at higher resolution. The effect of down-sampling can be seen in fig. 2.14. However, in certain cases, for example when modelling vertebral augmentation, in order to attempt to capture the intricacies of the structure and the boundaries between cement and trabecular bone it was favourable to generate the mask prior to down sampling, fig. 2.17. The image stack was down-sampled to voxels 1 mm cubed, due to previous studies producing sensitivity

to mesh size results that showed a good trade off between computational cost and model accuracy [82].

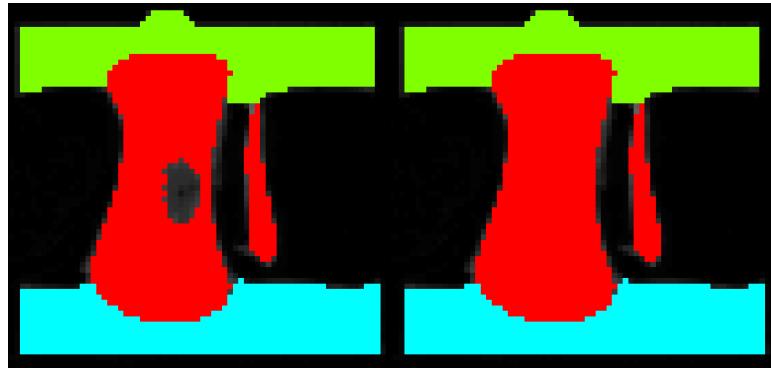


Figure 2.15: Side view of a vertebral model showing segmented vertebra, including the internal void that is filled.

Once down-sampled the image stack was segmented into the constituent parts - the vertebrae and cement end-caps. The different regions that were required to be segmented have different greyscale values, hence the general shape of the masks was created through a thresholding tool that selected volumes of the image stack between two greyscale bounds. For the end-caps these bounds were usually between greyscale values of 12-22 and, if the specimen was not augmented, the vertebrae between 23-255. For augmented specimens these limits change to 23-65 for the vertebrae and 66-255 for internal cement containing barium sulphate. These values were selected by visually limiting the amount of unwanted material selected within the threshold and maximising the wanted material, for example - selecting as much of the end-caps as possible while limiting the selected background and vertebral material to a minimum. This thresholding can be seen in fig. 2.15. It was preferable to avoid internal voids within each mask, due to the potential for errors that may arise from the extra surfaces and contacts created when solved in ABAQUS, these were removed with the use of the morphological close and cavity fill tools within ScanIP (fig. 2.15).

The following parts of the method were carried out manually, following the completion of the automatic segmentation python script. The two end-caps were separated into two separate masks by first duplicating the mask and then flood filling each end-cap to form separate masks.

An FE model was created using the previously generated masks and properties for the volume meshing, materials and contacts were set. The grid size for the model was set to  $1 \times 1 \times 1$  using the FE grid algorithm which uses a mix of tetrahedral and hexahedral elements. Material properties were set to homogenous with a Young's modulus = 2.45 (GPa) and Poisson's ratio = 0.3 for the end-caps. Material properties for the internal

cement regions for the augmented vertebrae are described later. The material properties for the vertebral volume were set to a greyscale based material type using the greyscale background information. The coefficients were set so that both the density and Young's modulus were equal to the greyscale value for that element, allowing the Young's modulus to be set correctly in following steps and as described in Section section 2.3.3.

Contacts were set as placeholders to be edited in Abaqus in the steps following. These were contact pairs between each component and another between the superior end-cap and the upper boundary on the Z-axis. The second contact type was a node set between the inferior end-cap and the lower boundary on the Z-axis used to create an enastre boundary condition for the model base.

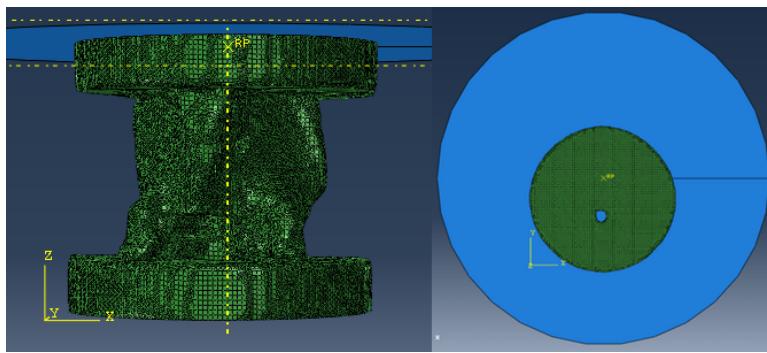


Figure 2.16: Side & top down view of a vertebral model showing the alignment of the analytical rigid plane.

Following this, the FE model was meshed, then exported into an INP file format. This file was imported into Abaqus where the following configuration was completed by a second python script. An analytical rigid plate was created to represent the upper loading platen of the materials testing machine and was centred at the loading point previously found from the marker, this can be seen in fig. 2.16. Once aligned any previous placeholder interactions were removed and a tied interaction was created between the rigid plate and the superior end-cap, along with tied interactions between the vertebra and both end-caps and, if appropriate, to any internal cement volumes. An encastre boundary condition was created at the bottom surface of the inferior end-cap removing all rotational and translational movement and therefore mimicking the experimental setup. A displacement boundary condition was applied to a reference node at the centre of the rigid plate and therefore loading position, the properties were set such that 1 mm of displacement occurs in the negative Z direction; lateral motion in the X and Y planes was restricted, while rotation about the loading point was allowed - mimicking the experimental steel ball setup.

The python script was written to set the material properties of the greyscale dependant vertebral elements by setting the Young's modulus to the greyscale value multiplied by a

conversion factor (which is discussed in section 2.3.3). The script allowed Abaqus to solve the models and outputs the stiffness for each model. This was calculated by dividing the axial reaction force (axis of load application) at the reference point by the 1 mm of displacement.

### 2.3.2.1 Augmented Model Generation

In order to capture the detail of interdigitation between the vertebrae and the injected cement, the masking process was carried out prior to downsampling, seen in fig. 2.17. If masked post-down-sample it became difficult to define the cement boundaries and the masked volume was inaccurate when compared to the full resolution scan. Masking the internal cement region used the same thresholding approach described above.

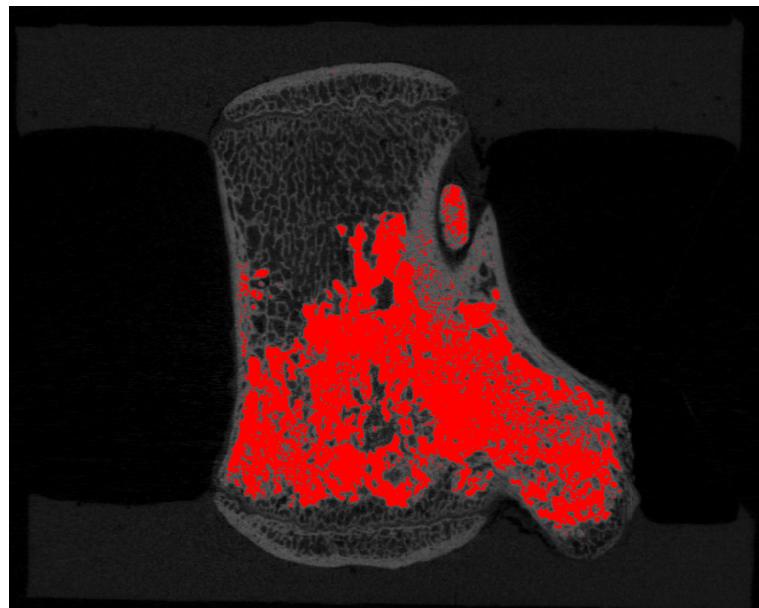


Figure 2.17: A lateral slice through an augmented bovine tail vertebra, showing the cement mask in red at the full  $82 \mu\text{m}$  resolution.

### 2.3.3 Material Properties

#### 2.3.3.1 Bone Material Properties

Material properties for the bone tissue were modelled elastically using a bone element-specific elastic modulus ( $E_{\text{ele}}$ ) that is dependent on the average greyscale value for the element in question ( $\text{GS}_{\text{ele}}$ ) with the conversion factor between the two being  $\alpha$ .

$$E_{\text{ele}} = \alpha \text{ GS}_{\text{ele}} (\text{GPa})$$

This was required due to each element containing differing quantities of bone and bone marrow due to the continuum level modelling carried out. Hence, a homogenous value for the trabecular bone would not have represented the varying average of material properties seen in each element. The conversion factor,  $\alpha$ , was used to convert between the greyscale value for each element and the Young's modulus.

A separate set of 24 bovine tail vertebrae underwent the same experimental and computational methods described previously in order to tune the value of  $\alpha$ . This additional set was split into two groups of 12 and was worked on in collaboration with Dr Sebastien Sikora, Dr Fernando Zapata Cornelio & Ruth Coe (Research Fellow, Research Fellow & PhD student respectively). The groups consisted of a calibration group (used to determine the value of  $\alpha$ ) and a validation group. For the validation group material properties were assigned - multiplying the greyscale for each element by  $\alpha$  prior to compressing the model by 1 mm in Abaqus and was used to validate against the experimental values of stiffness.

The calibration for  $\alpha$ , the conversion factor was carried out using a golden section search scalar optimisation process. Specifically using the Brent method within the opti4Abq toolbox [83]. The objective of this toolbox was to find the root mean square normalised difference between the experimental specimen stiffness and the finite element stiffness and iterate until the objective function achieved a value of  $10^{-3}$ .

### 2.3.3.2 Augmented Specimen Material Properties

For convenience the values for the Young's modulus for the interior cement volume were initially set to that of the inferior and superior end-caps. However, from previous studies into modelling bone cement interactions [38, 60, 68, 70, 71, 72, 73, 84], simple material properties of PMMA do not accurately describe the environment. Due to the rule of mixtures and the results found in the literature [72, 85], the effect of reducing the Young's modulus was investigated. This was carried out by reducing the Young's modulus in 10 percent increments from a value of 2.45 GPa to 1.225 GPa.

Additionally, a preliminary investigation was carried out, identifying the effect of a yielding material interface between the bone and the cement, following the work by Sikora [73]. Here, a small interface layer (1 mm in thickness due to the model resolution) represents buckling that occurs in the trabeculae partially captured in the cement volume. This investigation identified the effect of different yield stress values in combination with different Young's moduli for both the interface and the main cement volume.

The yielding region was created through the duplication and then erosion of the cement

mask within Simpleware ScanIP, shown in fig. 2.18. This gave two masks, where one acts as the internal cement volume and the other as an interface layer. Generic material properties were set to the region within ScanIP, allowing the values of the yield stress and Young's moduli values to be changed within the python setup script. The properties tested included changing the yield stress and Young's modulus of the region, whilst maintaining the properties of the internal cement volume at 1.225 GPa. Values for the yield stress in the interface region were varied between 1 MPa and 0.001 MPa, with the material become perfectly plastic beyond this. Young's modulus values for the interface region were varied between 1.225 GPa and 0.1 GPa. These values were manually tuned to find the optimum values with respect to the CCC of the set.

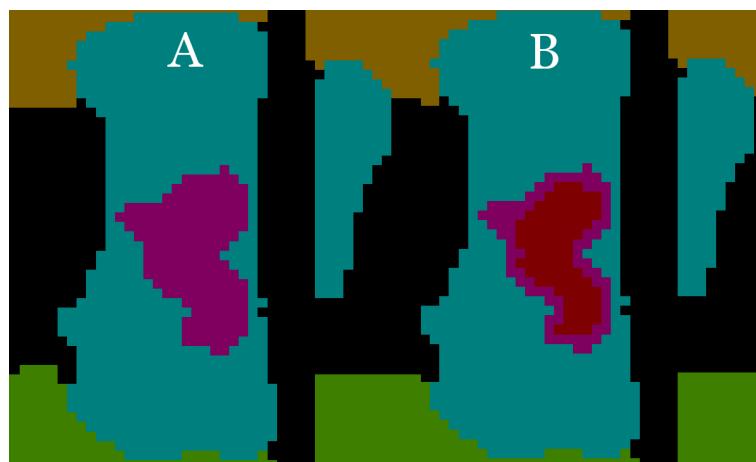


Figure 2.18: Creation of the interface layer: A, showing the initial description of the cement region in pink and B, showing the interface in pink and cement region in red, following the duplication and erosion.

### 2.3.4 Sensitivity Tests

#### 2.3.4.1 Mesh Size Sensitivity

Element sizes of  $1 \times 1 \times 1$  mm were used throughout, following previous convergence studies on porcine vertebrae [82]. The results of the convergence study on porcine vertebrae showed that reducing the element size below  $2 \times 2 \times 2$  mm led to changes in the model that were smaller than predicted errors originating from other factors, such as experimental errors and the simplification of boundary conditions. However, reducing the element size to  $1 \times 1 \times 1$  mm allows greater resolution when modelling the intricacies of the cement mesh for augmented specimens, the difference between the two resolutions can be seen in fig. 2.19.

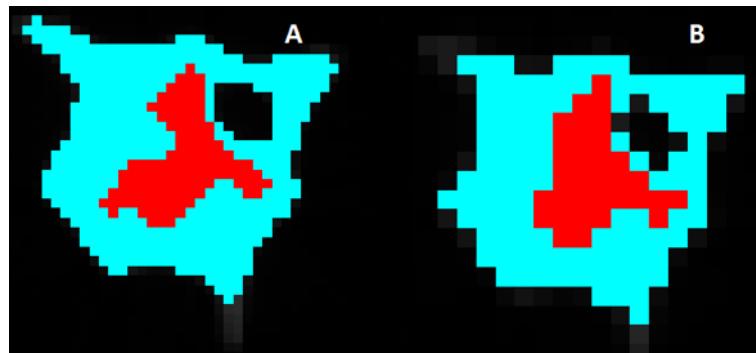


Figure 2.19: Mid-slice through an augmented vertebra, cyan: vertebral body, red: cement. A, element size of  $1 \times 1 \times 1$  mm. B, element size of  $2 \times 2 \times 2$  mm.

### 2.3.4.2 Sensitivity to an Additional Mask

The addition of cement into the vertebral body created an extra mesh boundary within the mesh containing the vertebral elements. In order to test what effect this may have on the stiffness of models containing an extra mesh boundary, an un-augmented specimen was tested with an extra mesh representing the cement, but with the material properties of its elements set based on their greyscale as with the other bone elements. The mask was created by duplicating the vertebral mask and eroding it until the volume was approximately 20 % of its original volume. This allowed testing to be carried out on the effect of the extra mesh alone, while using an augmented specimen would allow a more accurate cement shape, it would hinder setting material properties to that of the bone greyscale and create an additional level of uncertainty. Mesh interactions between the two meshes (internal vertebral surface and the cement mask surface) were set using the contact pair interaction and treated similarly to the interaction between the end-caps and the vertebrae. Following model setup in ABAQUS as outlined in section 2.3.2 the model was loaded in compression to 1 mm and its stiffness was recorded.

There was no difference between the two models, with and without the internal cement mesh, meaning that any changes to the augmented model stiffness was due to the material properties of the cement.

### 2.3.4.3 Mesh Interactions

The effect of mesh interaction between the vertebral body and the internal cement mesh were tested by comparing a) tied interactions between the two surfaces and b) removing any interaction and merely changing the material properties of the internal cement region (neglecting the contact pair steps described earlier). This was carried out for four augmented specimens following the same setup within ABAQUS as described earlier.

The results can be seen in table 2.2, showing a negligible difference between tied and non-tied (single mesh) models. This difference falls well below the difference between experimental and computation, especially for the augmented specimens, hence the effect of this interaction can be neglected from further test.

Table 2.2: The difference between interaction properties, tied and not tied for four augmented vertebrae specimens.

Vertebrae (Tail Number, Vertebral Level)	Tied Interaction (N/mm)	No Tied Interaction (N/mm)	Difference (%)
T2 CC1	5496	5496	0
T2 CC2	8086	8086	0.001
T6 CC1	3686	3686	0.001
T4 CC3	6059	6059	0.0005

#### 2.3.4.4 Augmentation Location Sensitivity

Another preliminary study was carried out (preliminary given the limited nature of the agreement between computational and experimental results and aims to improve this with the use of human tissue) to identify the sensitivity of the models to the position of the cement volume. Tests were carried out to identify the effect of moving a 12 % fill cement volume axially and sagittally in 2 mm increments. This utilised the yielding interface described in section 2.3.3.2 along with the +CAD tools built into Simpleware ScanIP to move a surface based description of the cement volume in the two anatomical planes. A sphere surface of volume equivalent to 12 % fill volume for the T12 CC2 vertebra was created within the +CAD software and imported into the project file for the vertebra, where it was positioned in it's first position. This first position was 1 mm from the top of the vertebral body, ensuring 1 mm of bone surrounded the sphere. It was then converted into a mask, duplicated and eroded in the same method described in section 2.3.3.2 to create the yielding material interface and set with optimum material properties. Following this the mesh was generated and the abaqus input file was exported. The sphere surface was then moved 2 mm in the inferior direction, the previous masks deactivated and the process repeated through the use of a python script to carry out the operations until the bottom of the vertebra had been reached. This was also carried out in the sagittal plane.

The results of moving the cement volumes through the T12 CC2 vertebra are shown in figs. 2.20 and 2.21. For the sagittal plane a reduced stiffness is seen when the volume of cement is positioned most anterially, where the yielding interface of the cement volume encroaches on the denser bone of the cortical shell. Centrally the stiffness is greatest, where

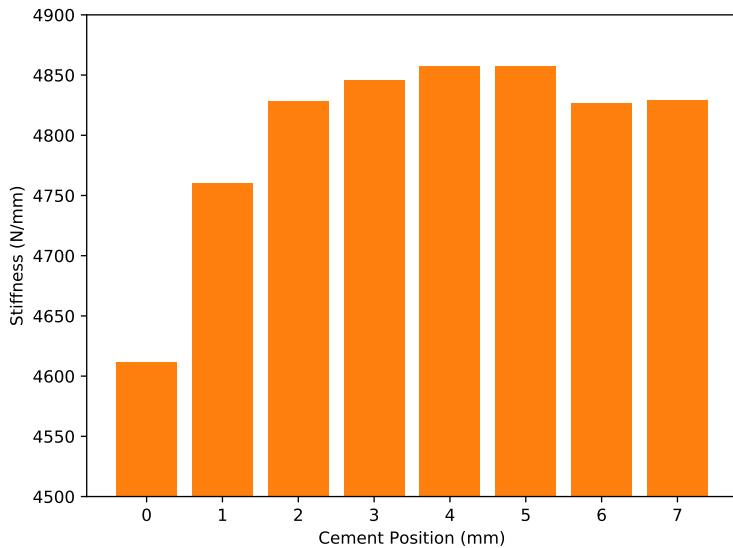


Figure 2.20: The effect of moving the cement volumes from the most anterior position to the most posterior position on the recorded stiffness of the vertebra, when using uniform 12 % fill volume of cement.

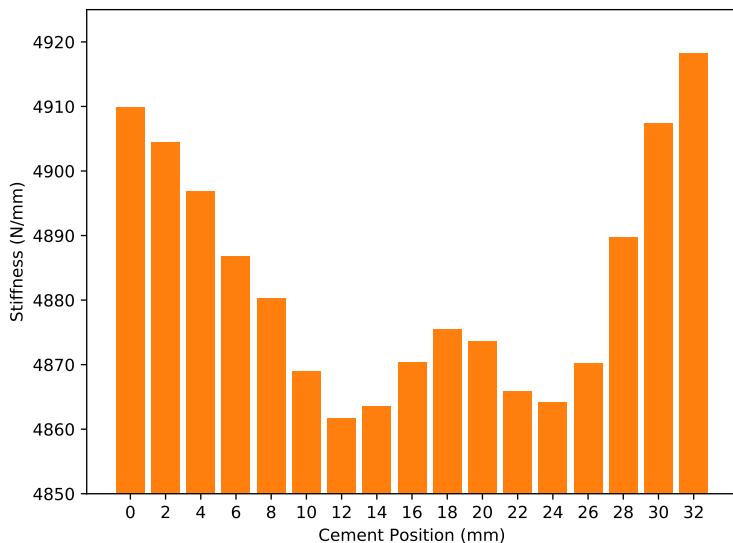


Figure 2.21: The effect of moving the cement volumes from the most superior position to the most inferior position on the recorded stiffness of the vertebra, when using uniform 12 % fill volume of cement.

the cement volume replaces the least dense bone, which can be seen in fig. 2.22, where the least dense (blue) parts are “hidden” by the cement volume in certain positions. Little change to the stiffness at the posterior side of the vertebra is seen due to the additional support from the posterior elements.

Axial movements of the cement volumes show that the most inferior and most superior positions resulted in the greatest stiffness and central positions resulted in the least stiff models. This is potentially due to the greater quantity of bone surrounding the cement volumes at top and bottom where the vertebral body is wider. The peak in the central

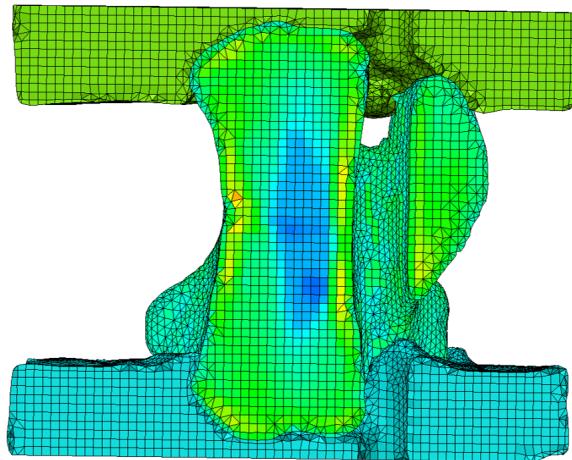


Figure 2.22: A density map of the T12 CC2 vertebra. Yellow/orange elements are the most dense, while blue elements are the least.

loading positions is again likely due to the “hiding” of the weaker bone in the centre of the vertebra.

Finally, despite the changes to the stiffness when moving the cement volume, these changes are smaller than five percent between the most and least stiff result, suggesting cement volume movement at these small volumes is not significant. It may also suggest that cement shape may play a more important role, where endcap to endcap distributions show much larger effects as shown in [68, 86, 87].

#### 2.3.4.5 User Variability Sensitivity

A user variability study was conducted to identify the variation in the modelling approaches, specifically masking the bone and endcap regions. Four users each masked the bone and endcaps for eight vertebrae using thresholding and other morphological filters (which would later be automated using the best approach as described previously). The FE models were then generated and the material properties were optimised using the greyscale optimisation process separately for each users models.

The results for the variability can be seen in table 2.3 showing the mean, maximum, minimum and range as well as the mean for each. The mean range of values was 158, with a mean model stiffness across the four users of 1928 N/mm. The maximum difference between users was for specimen six where a range of 246 was found. This equates to a maximum possible error of 14 % for different users carrying out the same models creation process.

While 14 % error between users if relatively high, the models used in this chapter and

Table 2.3: The variability the modelling approaches of four users with 8 models, each users models undergoing separate greyscale optimisation and FE model solving

Specimen	Stiffness (N/mm)			
	Mean	Maximum	Minimum	Range
1	2457	2567	2379	188
2	2298	2368	2218	150
3	2374	2463	2261	202
4	1600	1659	1545	114
5	2281	2324	2218	106
6	1899	1990	1744	246
7	1330	1398	1236	162
8	1183	1219	1119	100
Mean	1928	1998	1840	158

subsequent chapters were all build by the author. Users tended to produce consistent differences in the stiffness of generated models, for example user one had consistently lower stiffness values and user three had consistently higher stiffness values (means of 1876 N/mm and 1952 N/mm respectively). This, in addition to the fact that the models are built using a python script within Simpleware ScanIP, means that the single user variability should become zero.

### 2.3.5 Result Analysis

The statistical approach to quantifying the agreement between the computational results and the experimental results for the measured stiffness uses the concordance correlation coefficient (CCC). CCC measures the agreement between two variables and is described by Lin [88] as a method to evaluate reproducibility. The CCC is calculated as:

$$CCC = \frac{2\rho\sigma_x\sigma_y}{\sigma_x^2 + \sigma_y^2 + (\mu_x - \mu_y)^2}$$

Where  $\mu_x$  and  $\mu_y$  are the means for the two variables and  $\sigma_x^2$  and  $\sigma_y^2$  are the corresponding population variances.  $\rho$  is the Pearson correlation coefficient between the two variables. For  $n$  independent pairs of samples:

$$CCC = \frac{2S_{12}}{S_1^2 + S_2^2 + (\bar{Y}_1 - \bar{Y}_2)^2}$$

Where,

$$\bar{Y}_j = \frac{1}{n} \sum_{i=1}^n Y_{ij}, \quad S_j^2 = \frac{1}{n} \sum_{i=1}^n (Y_{ij} - \bar{Y}_j)^2, \quad j = 1, 2;$$

and

$$S_{12} = \frac{1}{n} \sum_{i=1}^n (Y_{i1} - \bar{Y}_1)(Y_{i2} - \bar{Y}_2)$$

Specifically, this quantifies the degree to which pairs sit on the  $x = y$  line. Departures from this perfect agreement line result in a  $CCC < 1$  even in cases where the Pearson correlation coefficient would equal 1.  $CCC = 0$  corresponds to no agreement and a value of  $-1$  would be perfect negative agreement.

### 2.3.6 Results

The optimisation process gave a value for the conversion factor of 0.012529, allowing conversion between greyscale values for elements and their elastic modulus. This value was used for the bone constituents of the intact and augmented vertebrae presented in fig. 2.23, which shows the agreement between the *in vitro* and *in silico* results for the specimen specific models. The agreement of intact vertebrae achieved a concordance correlation coefficient (CCC) of 0.49 compared with 0.14 for the augmented vertebrae (simple tied interaction) (table 2.4). The non-augmented CCC value increased to 0.60 if the uncharacteristically stiff T8-CC2 was removed.

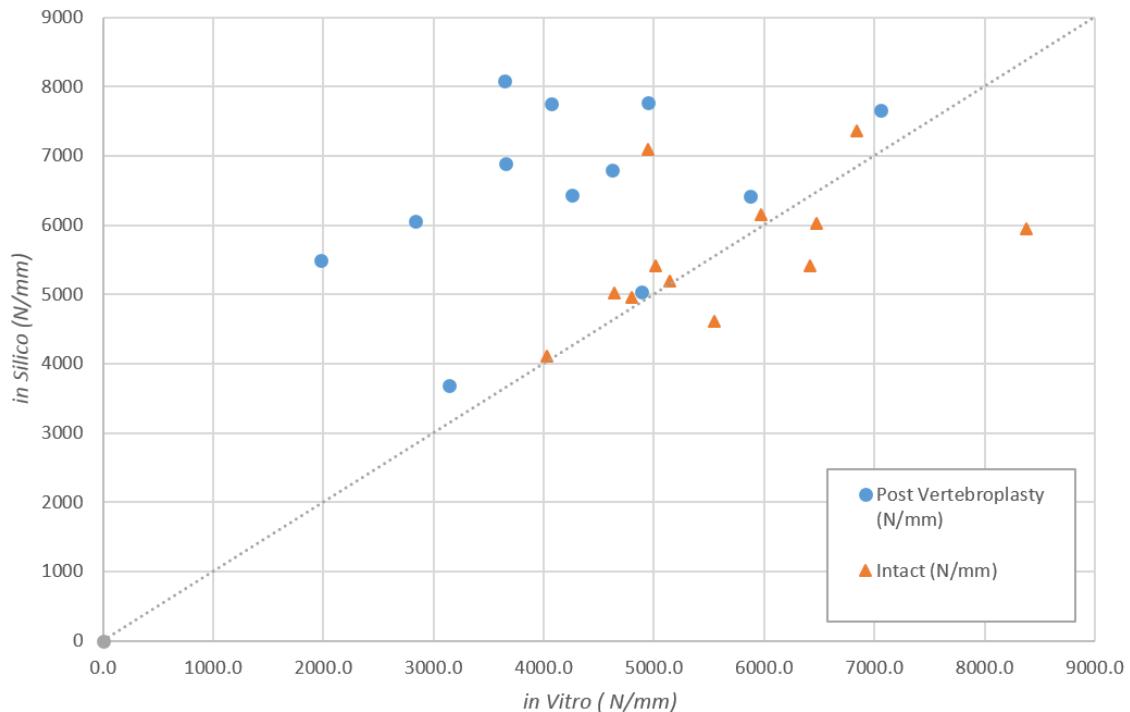


Figure 2.23: The *in silico* compared with *in vitro* stiffness for intact specimens (triangles) and augmented specimens (circles). The dotted line shows a one-to-one correspondence.

Table 2.4: The mean, standard deviation and concordance correlation coefficient (CCC) of the intact and augmented vertebrae (simple tied interaction) for *in vitro* and *in silico* results.

Intact Specimens	Mean Stiffness	Standard Deviation	CCC
<i>in vitro</i>	5684	1196	
<i>in silico</i>	5610	958	0.4895
Augmented Specimens			
<i>in vitro</i>	4246	1371	
<i>in silico</i>	6507	1298	0.14

The effect of changing the modulus of the cement volume in the augmented specimens is presented in fig. 2.24. There was a linear decreases in the stiffness of vertebrae with the reduction of the elastic modulus for the internal cement volume. The two vertebrae that show more prominent decreases in stiffness were those vertebrae that contained larger volumes of cement following their augmentation.

The effect that this has on the data with regard to the *in vitro* stiffness results can be seen in fig. 2.25, where the reduction in *in silico* stiffness moves the data points closer to the  $x = y$  line of perfect agreement between the experimental and computational results. This gave a CCC of 0.18.

The increasing agreement with increasing sophistication of modelling the augmentation can be seen in fig. 2.26, comparing the simple tied interaction, the reduced modulus approach and the combination of this and the yielding material interface. The CCC improves when using the reduced modulus at 50 % (1.225 GPa) from the simple tied interaction with an improvement to 0.18 from 0.14. Another improvement is seen when combining the reduced modulus for the cement with the yielding interface (Young's modulus 1.225 GPa, yield stress 0.005 MPa), with the CCC improving to 0.23. The effect of changing these interactions and properties is not uniform, also shown in fig. 2.24, the vertebral models respond differently to different interactions, with increases and decreases seen within the same set of vertebrae when changing the same interaction.

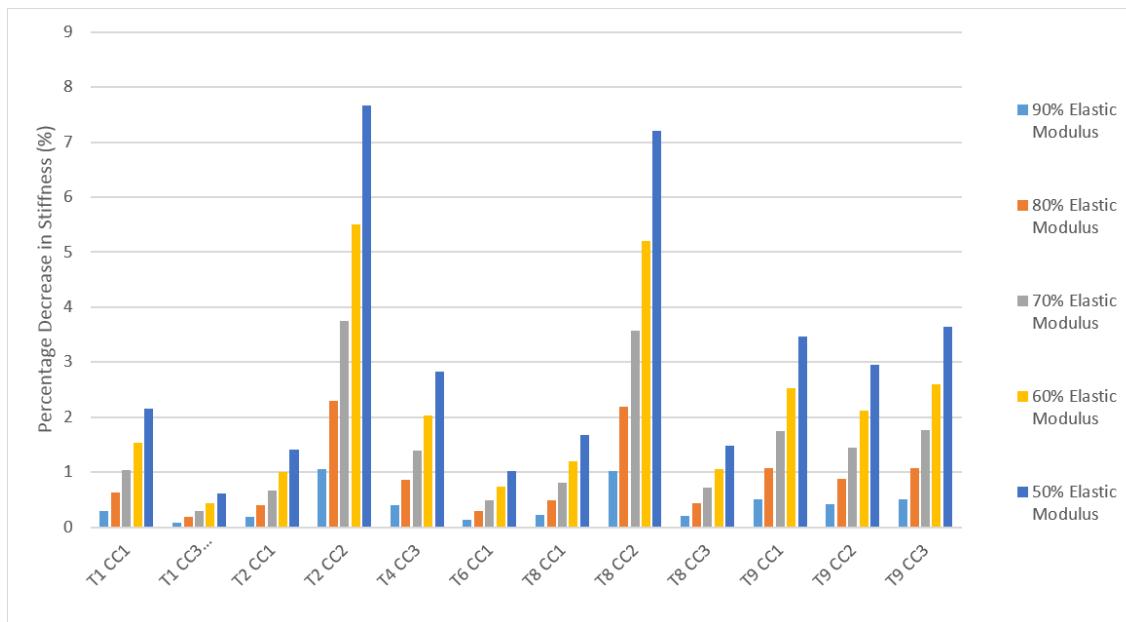


Figure 2.24: The percentage decrease in the vertebral stiffness after reducing the elastic modulus of the cement volume within 12 augmented vertebrae.

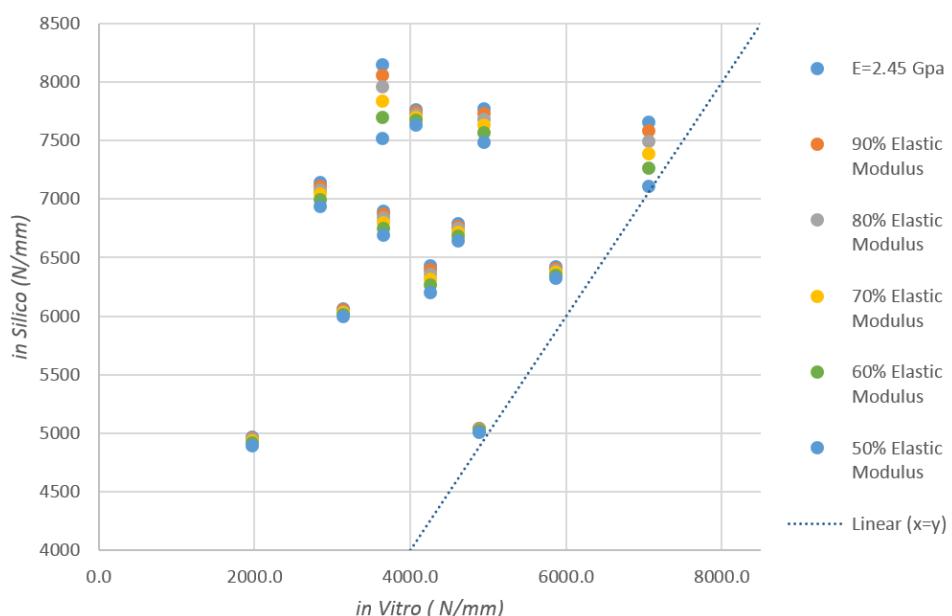


Figure 2.25: The effect of reducing the elastic modulus of the cement volume within 12 augmented vertebrae. Shows the in silico stiffness for the six elastic moduli tested against their in vitro stiffness.

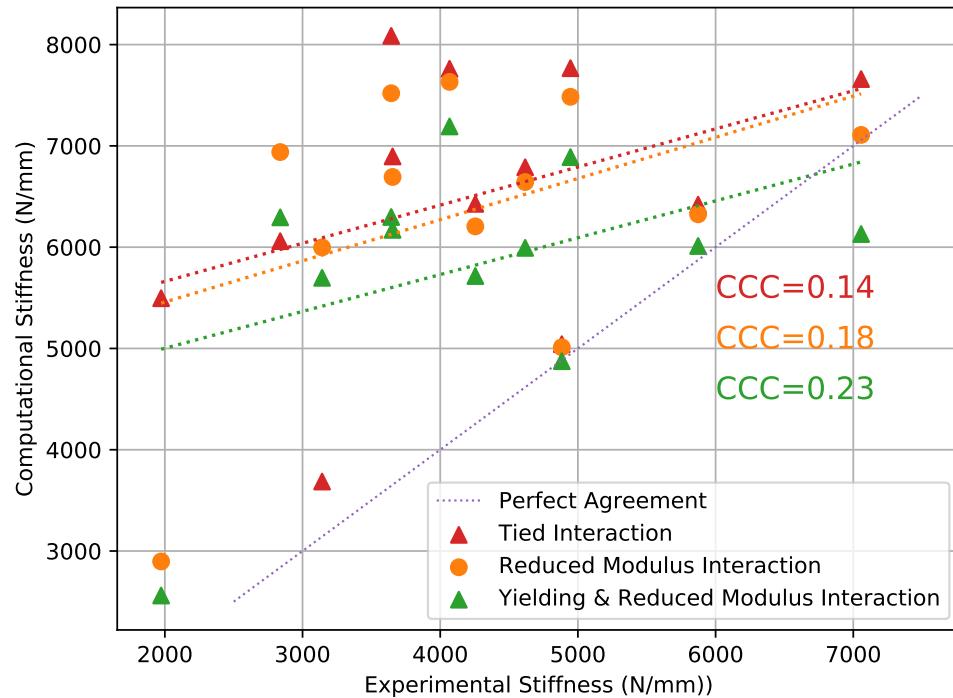


Figure 2.26: A comparison of the different approaches to modelling augmentation in the bovine tail vertebrae. Comparing a simple tie between the bone and cement, a reduced modulus for the cement region and a reduced modulus in combination with a yielding interface layer between the bone and cement.

## 2.4 Discussion

### 2.4.1 Experimental Discussion

The experimental section aimed to develop the various aspects of the experimental methodology on a set of bovine tail vertebrae, allowing for an easy transition into using human lumbar vertebrae, which is discussed in the following chapter. Previously developed methods of  $\mu$ CT scanning have been verified for the bovine tail vertebrae. Methods of performing vertebroplasty and dealing with the unique challenges arising from the bovine vertebrae have been created. The experimental part of this chapter provides a good basis for both the continued modelling of vertebroplasty (especially modelling the cement - trabecular interface) and to continue the experimental work using human tissue. Understanding the challenges of vertebroplasty, will be invaluable when transitioning onto the much more limited source of human vertebrae.

Regarding the results of stiffness at the intact, fractured and augmented stages, the expected trends were not always clear. Most commonly the intact vertebrae have the greatest stiffness with the fractured stiffness showing a reduced value following the damage created with the initial load to failure. The variation of the decrease (and increase) in stiffness for the fractured vertebrae may have a variety of reasons, although the most likely cause is level of damage caused in the initial “load to failure”. These tests varied between the typical load displacement that includes a failure (fig. 2.4:A) and those that show no sign of failure up to the limit of the load cell (fig. 2.4:B). It is difficult to observe any correlation between these vertebra that showed clear failure (T2-CC1 and T2-CC2), those that reached 9500 N and a reduction in the fractured stiffness. It is not to say that the vertebra that reached 9500 N experienced no damage, with the gradient of the load displacement curve often reducing and plateauing as the 9500 N limit approached. The interesting increase in the fractured stiffness for T1-CC1 compared to the intact stiffness may be explained if it is assumed that the compacted trabeculae following the first load to 9500 N result in a stiffer material for the following tests. Other possibilities that may explain the increase in stiffness include a change in the seating of the vertebra within the PMMA endcap. If the initial load changed how the vertebra was positioned in the endcaps it would change the response to loading, even when loaded at the same point.

The cement fill volume information shows that a small percentage of cement is injected into the vertebrae on average, with only two vertebrae approaching the clinically relevant 20% fill. Unexpectedly, only one of these two vertebrae showed an increase in augmented stiffness over the fractured stiffness. A possible explanation is that it is not only the fill

volume that is important in restoring the vertebral stiffness but the placement or shape of the cement fill volumes. This is shown when comparing the segmented scans of the two vertebrae with the greatest fill volume with the T2-CC2 specimen showing cement extending to the anterior wall of the vertebral body, while the cement is limited to the posterior and centre of the vertebral body for T8-CC2. This may help to explain why the stiffness of T8-CC2 did not increase following augmentation. The reduction in stiffness following augmentation for seven of the twelve vertebrae may be due to damage caused by the insertion of vertebroplasty needles. Clinically this damage left behind from the needle channels would heal, most likely restoring the stiffness of the vertebrae back to its intact properties. Additionally, needle insertion into the dense bone of the bovine tail vertebrae required a mallet to reach the anterior portion of the vertebral body, clinically this would not be required due to the much less bone of the human lumbar vertebrae [37]. Such a violent approach would damage the bone surrounding the needle entry, causing micro-fractures not visible on the  $\mu$ CT scans.

Another possible area of inconsistency is the temperature at which the vertebra were mechanically tested, while it is ensured that the specimens were fully defrosted they were tested at both fridge temperature ( $4^{\circ}\text{C}$ ) and room temperature ( $20^{\circ}\text{C}$ ). The effect of this variation in temperature needs to be identified or a consistent temperature needs to be used for subsequent tests.

Despite encouraging results regarding the vertebroplasty methodologies it was difficult to achieve the desired quantity of the cement in the vertebral body. This was mainly due to the difficulty injecting the cement in a smooth manner, which may have been caused by either the tip of the needle becoming blocked following its reinsertion into the needle track, more viscous marrow stopping the displacement of less viscous marrow by the cement or compacted trabeculae around the needle channel that limit the flow of cement past them. One option to test in future work would be side opening needles, which would help guide the cement more accurately to the regions required while circumventing issue with the needle becoming blocked. Additionally, the shape of the vertebrae adds to the difficulty of performing vertebroplasty, with the narrow cylindrical shape of the vertebrae meaning the cement has to travel large distances axially through the trabecular bone to achieve clinically relevant cement fill volumes. In contrast the much wider human lumbar vertebrae used in latter chapters give much more space to inject larger volumes of cement. This, multiplied with a greatly reduced average trabecular density for the osteoporotic human vertebrae (see fig. 1.5 and [34, 37] should allow for greater volumes of cement to be injected.

When attempting to identify trends between the pre and post augmented and pre and post

fractured vertebral stiffness, no relationships were found. It was expected that initially weaker vertebra would show a larger change in stiffness between the fractured state and the augmented state and similarly between the intact and augmented states. However, no such trends were found, suggesting that properties other than the stiffness or bulk material properties are the cause of the variation. Properties such as the vertebral geometry and trabecular structure, which are investigated through the use of statistical shape models in chapter 4.

The experimental methods currently developed will be of great value when starting experimental work using human tissue albeit many will require adaption due to the differences between the tissue types. These include the density of the bone and methods of inserting the needles, where with the available human tissue being from the elderly, the bones will be most likely be osteoporotic.

#### **2.4.2 Computational Results Discussion**

The aims of the computational part of this chapter were to develop methods to build models of vertebrae using automated approaches and to carry out sensitivity tests. These sensitivity tests were to identify the best methods to use when carrying out similar model creation and simulation of the set of human lumbar vertebrae in chapter 3. This was achieved, with automation of the segmentation process within ScanIP and automation of the model setup within Abaqus carried out using a series of python scripts. These scripts require no conversion to be used with the modelling of human lumbar vertebrae, with the exception of the thresholding carried out in scanIP. The preliminary sensitivity tests give a first idea of what variations the vertebrae are sensitive to and will allow further investigation in subsequent chapters.

The computational methods developed and results acquired, as with the experimental results, provide a good base for using human vertebrae and for the continued development of augmented vertebra modelling. The methods and automation of the creation of models both greatly reduce the time spent on model generation and reduce human error. This allows a relatively easy translation to human vertebrae, with only minor adjustments to the thresholds that define materials.

The current methods of masking and meshing the internal volumes of cement in the augmented models provide a good method of creating augmented models. The sensitivity tests carried out on the additional mask inside the vertebrae shows that any effects seen are due to the volume of cement and not a simulation problem. Similarly the

inclusion of a tied interaction between the two meshes failed to affect the result, something especially useful when considering alternative mesh interaction to model the cement - trabeculae interaction. This may be explored further with an expanded sensitivity test identifying whether alternative contacts are more appropriate to model the bone-cement interface.

Augmented volume location sensitivity tests suggests little influence of the position of the cement volume on the reported stiffness when loaded. It does highlight a potential source of error, where anteriorly placed volumes of cement would be expected to increase the stiffness of the vertebrae, given the reduced support and density on the anterior side. However, due to the yielding interface replacing the dense cortical shell, the result is a reduced stiffness. Therefore care needs to be taken when investigating cement volume movement as to not create unnatural simulations. When modelling experimentally augmented models this is not a problem as the cement does not replace the bone when injected, therefore preserving the cortical shell in the vertebral model. Additionally, moving the cement volumes highlights the importance of filling or replacing the weakest, least dense parts of the vertebrae with cement. Although in this case the change of replacing the central “void” in the vertebra is small compared to placing the cement volume elsewhere, as cement volume size increases (and modelling accuracy improves) the effect may become more pronounced. This is investigated further in chapter 4, where cement volumes are moved within statistical shape models of osteoporotic human lumbar vertebrae, which exhibit similarities to the voids found in the bovine tail vertebrae, with much less dense bone in the central portions of the vertebral body.

The intact models agree well with experimental results, with very similar results for the mean and, excluding anomalous results, a good CCC value, showing that the previously validated conversion factor works well with this set of data and that segmentation and model setup works correctly. The poor agreement with the augmented specimen models and their experimental counterparts was an expected result that agrees with similar studies in the literature - [38]. In an attempt to produce a better agreement, the elastic modulus of the cement volume was reduced in accordance with the experimental results of Race et al. [85] and similar methods employed by Wijayathunga et al. [38], where the reduction in modulus is expected due to the greater ratio of monomer to powder used, gaps between the bone and cement and pores within the cement. The reduction in stiffness forms a linear pattern as the elastic modulus is reduced, with those vertebrae that show the greatest reduction being those containing the largest volume of cement. While these results do show a reduction in the stiffness, closer to that of the experimental values, it does not

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explain the disagreement fully. This suggests that a combination of improvements to the augmented models are required. The final increase in the agreement between experiment and model was seen with the addition of the yielding interface. This reduced the stiffness of the set on the whole and also increased the CCC value. Interestingly this was not a uniform or predictable effect with no correlation between yielding interface surface area or volume and the change in stiffness. Suggesting the effect was influenced by the density of the surrounding bone on various regions and therefore was not a bulk effect.

Future work will utilise the results acquired, especially those relating to the cement modulus and the cement - bone interactions, to understand how to model this interface more realistically and achieve good agreement between experimental and computation results of stiffness for augmented specimens.



# Chapter 3

## Human Lumbar Vertebra Study

### 3.1 Introduction

Previous studies and the work in the earlier chapter have used a range of vertebrae, including bovine, ovine and porcine among others. While all of these vertebrae have important uses for developing methodology and understanding certain characteristics, none share the trabecular structure, thickness of cortical shell, axial strength or stiffness with human vertebrae. Hence, to understand the mechanical effects of vertebroplasty in human lumbar vertebrae, human tissue is required.

Here, 14 lumbar vertebrae from four cadaveric spines have been used, with the details shown in table 3.1. These spines were sourced from the Leeds GIFT 2 Research Tissue Project, with consent for the use of tissue being taken by the NHS Blood and Tissue Services. These vertebrae underwent experimental testing, augmentation,  $\mu$ CT scanning and the development of FE models derived from their  $\mu$ CT scans. The goal of the chapter was to develop methodologies to accurately model both augmented and non-augmented human lumbar vertebrae. This chapter details the methods employed, the sensitivity tests carried out, results acquired and a discussion of the implications of those results.

Table 3.1: Details of the lumbar sections used from four cadaveric spines.

Spine Name	Vertebrae	Sex	Age
Spine 1	L1, L2, L3, L4, L5	F	90
Spine 2	L1	F	94
Spine 3	L1, L2, L3	M	86
Spine 4	L1, L2, L3, L4, L5	M	83

## 3.2 Experimental Methods

This section describes the experimental methods used and developed to test and record details of the set of human lumbar vertebrae. This includes an overview of the major changes compared to the methods presented in chapter 2, the specifics of some of the new additions to these methods and the reasons for and results of these improvements.

### 3.2.1 Dissection & Potting

The first step in the experimental setup, as with the bovine tail vertebrae, is the dissection and potting of the vertebrae. As before, potting is required to ensure parallel endcaps to allow repeated axial loading on materials testing machines and dissection was required to remove the soft tissue that would change the results given that only the bone is being tested and modelled. Dissection of the human vertebrae gave added challenge compared to dissecting the bovine tail vertebrae due to the degenerated nature of the vertebrae, with fused facet joints common and difficulties circumventing the bone growths on some of the most degenerated vertebrae.

The geometry of human lumbar vertebrae varies considerably to that of the bovine tail vertebrae from which this methodology is based. This is characterised by much larger posterior elements with the facets extending much lower, below the bottom of the vertebral body. Hence, to correctly pot the human vertebrae much more cement must be used, especially for the posterior end-cap, to cover the bottom of the vertebral body and the extending posterior elements. This would lead to much more of the posterior elements being constrained, therefore restricting the rotation of the vertebral body endplates under axial load. In addition to this the larger posterior elements which are captured within the PMMA end-caps will transmit load and take a greater share of the load when compared to the bovine tail vertebrae. Given that vertebroplasty attempts to restore the stiffness of the vertebral body and that there is no understanding of specifically how the loads are shared between the vertebral body and posterior element, this presents a problem.

A solution to this is to remove the posterior elements, following such methods as [38, 56], where only the vertebral body is modelled. This allows the stiffness of the vertebral body alone to be captured and modelled. The posterior elements were removed by cutting through the pedicles at the narrowest part, limiting damage to the region.

To pot the specimens that now lack a spinal canal (which was used to aid potting the bovine tail vertebrae), a retort stand was used to hold the vertebra, ensuring that both

endplates were level on average, given that lumbar vertebrae do not have parallel endplates. The specimen was then lowered down into the potting container leaving 5 mm between the bottom of the vertebra and the container. PMMA was poured into the container until the entire of the endplate was touching cement, with the edges of the vertebral body covered. Care needed to be taken to ensure all of the endplate was in contact with cement, given the extent of osteophytes creating non-flat surfaces in some of the more degenerated specimens. The other side of the vertebra was potted in a similar manner, however, due to the constraints of the potting container a measured quantity of cement was poured prior to lowering the vertebra into it. A spirit level ensured parallel end-caps.

### **3.2.2 Loading**

Following previous studies [38, 40], the vertebrae were loaded with an initial conservative maximum load of 800 N for similarly osteoporotic vertebrae, rather than the high loads used by Pneumaticos et al. [45]. However, after loading two of the initial set of vertebrae the stiffness continued to increase up to maximum 800 N. Following loads up to 2000 N showed that the stiffness reached a maximum between 1300 and 2000 N, with three of the initial four specimens showing some degree of failure in the final 400 N of loading. Due to this failure, a maximum load of 1600 N was used as a compromise for the remaining vertebrae used, although as presented below, some failure was still observed.

#### **3.2.2.1 Maximum Stiffness Measurement**

The maximum stiffness of the vertebra was found in the same fashion as with the bovine tail vertebrae - measuring the stiffness of segments at increments over the length of the curve. Given that damage, especially for the intact specimens, needs to be avoided if possible the maximum loads used are on the conservative side. This can mean that the maximum stiffness is potentially at the end of the data set or that the stiffness is still increasing at the load cut off. The solution to the latter would require a prediction of the yield point prior to experimental loading, while the former could potentially be solved by using smaller segment sizes when measuring the stiffness from load - displacement results.

To investigate the effect of segment size (the length of each section from which the stiffness is found) and increment size (the size of each increment defining the start point of each segment), the maximum stiffness finding Matlab script used in the previous chapter was rewritten in Python. This function could then be iterated over, reporting the maximum stiffness when using an increment size of between 1 and 100 data points (the distance

between two data points corresponds to 0.0017 mm).

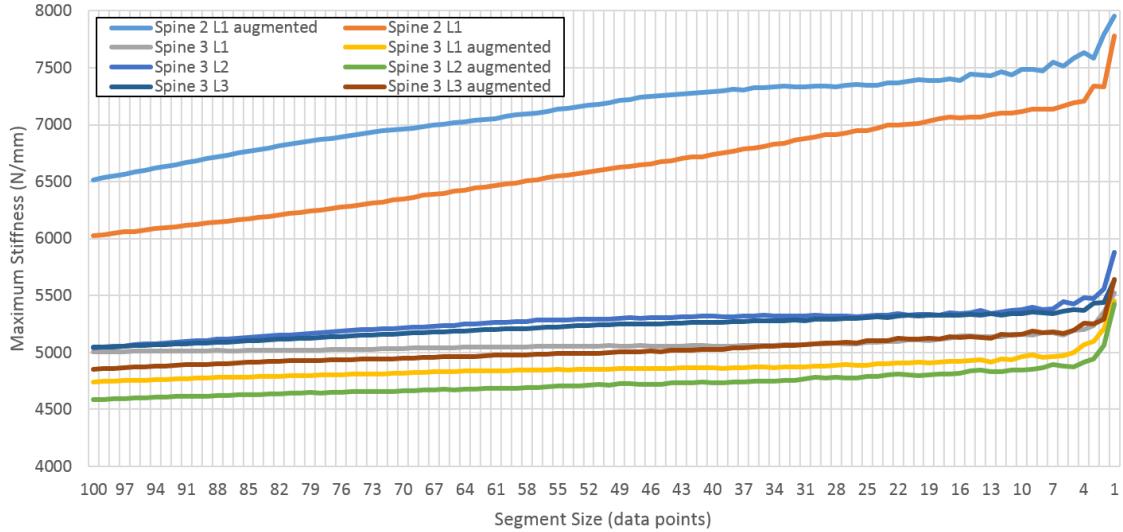


Figure 3.1: The effect of reducing the segment size on the maximum stiffness reported from four human vertebrae loaded to 2000 N pre and post augmentation. Using an increment size of 1 data point (0.0017 mm) and segment sizes of 100 to 1 data point (0.17 mm to 0.0017 mm).

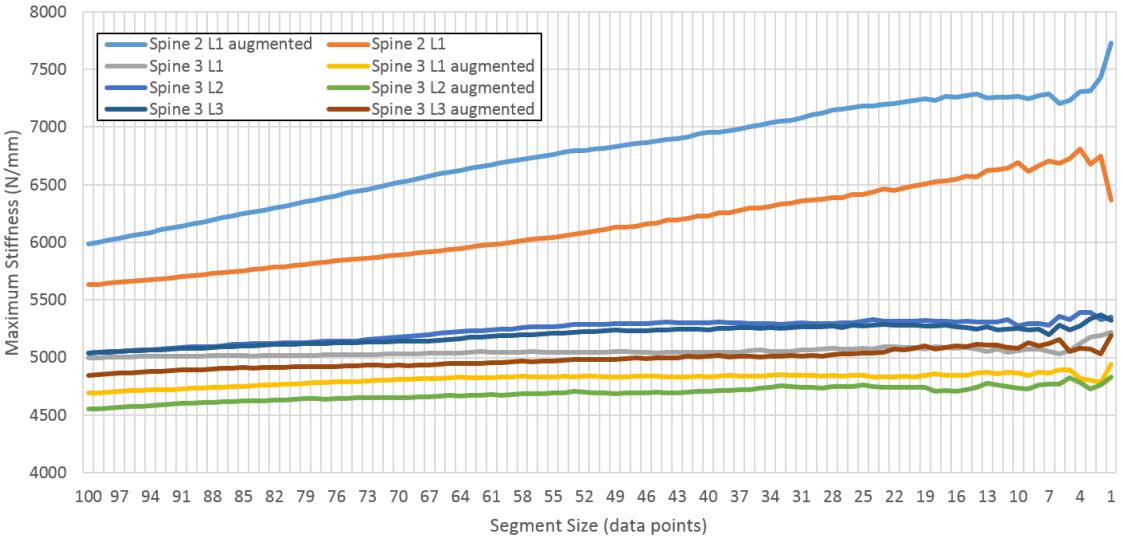


Figure 3.2: The effect of reducing the segment size on the maximum stiffness reported from four human vertebrae loaded to 2000 N pre and post augmentation. Using an increment size of 20 data points (0.0037 mm) and segment sizes of 100 to 1 data point (0.17 mm to 0.0017 mm).

Using an increment size of one data point width, as shown in fig. 3.1 shows a smaller variation across the range of segment sizes compared to using 20 points in fig. 3.2. The effect of both segment size and increment size is especially evident for the two Spine 2 L1 vertebrae both intact and post augmentation where the stiffness continues to increase until the end of the test at 2000 N. Meaning that there is a much smaller linear region for these two specimens and hence a smaller segment size was required to measure the largest gradient.

Choosing values for the segment size to use in the remainder of this study becomes difficult given the large effect it can have on the measured maximum stiffness (a range of over 1000 N/mm in the case the two Spine 2 L1 tests). The segment size needs to be small enough to capture the maximum stiffness while avoiding the noise (seen to the right in figs. 3.1 and 3.2) when using a segment size below 18 data points. Hence, a value of 20 data points was chosen, a value that avoids the noise while being on the plateau of the lines.

### 3.2.2.2 Repeated Loading

Given the nature of the test (attempting to limit damage to the vertebrae especially during their initial non-augmented load), the ability to derive errors becomes difficult especially from a single load. To attempt to understand this error four vertebrae having undergone augmentation were tested three more times in an iterative fashion, removing each from the load testing machine, testing the next specimen in the set and repeating. Removing the vertebrae from their steel housing (instead of three tests while seated in the steel housing) allowed error in loading position and setup to be tested along with repeated loading of the vertebrae.

The results of repeated loading can be seen in fig. 3.3. The majority of specimens show a reduced stiffness for the repeated loads following the initial load, for which there are a few possible reasons. One possibility for the reduction in stiffness is that it is a consequence of the freeze thaw cycle that occurred between these tests. It could be due to damage being caused during the initial load to 2000 N, in fig. 3.4 it is possible to see slight failure in the three Spine 3 vertebrae, although failure cannot be seen in the Spine 2 L1 vertebrae, which also exhibits a reduction in stiffness in the repeats. An option that may explain why for many of the vertebrae the change in stiffness for the first repeat with different trends for the following two repeats is that the vertebrae were seated differently in their endcaps for the first repeat, settling into position for repeats 2 and 3. This trend of a different stiffness for repeat 1 compared to 2 and 3 is evident in spine 1 L3 and L4, spine 2 L1 and spine 4 L1, L2 and L3. A potential cause is the changing temperatures (frozen to room temperature to above room temperature during the  $\mu$ CT scan) causing the vertebrae to expand out of the endcap in some cases, given the scan → freeze → back to room temperature process used for the repeated loads presented.

The iterative reduction in stiffness for the Spine 3 L2 vertebrae can be explained as damage being caused after each iteration. This can be seen in fig. 3.5, with the three repeats each showing a yielding before the 1600 N limit and a smaller maximum load and stiffness after

each repeat.

The figures in figs. 3.4 and 3.5 show the data for the loading, from which the maximum stiffness values are found. This excludes the initial cyclic loading, starts the loading at 50 N and displacement at 0 mm.

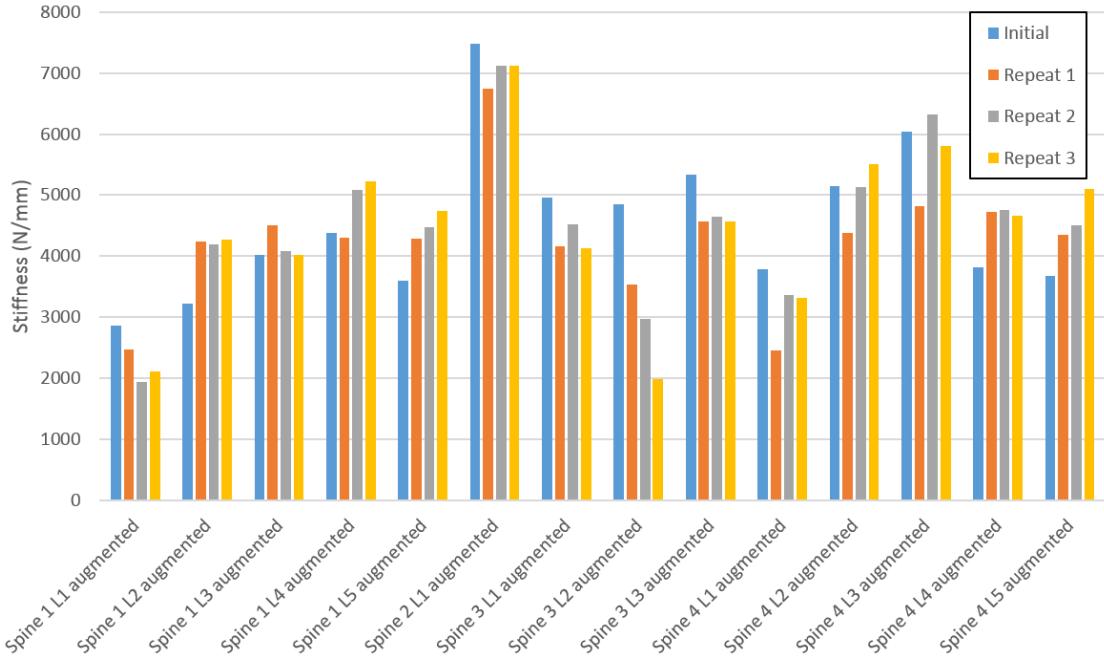


Figure 3.3: The stiffness of the augmented vertebral specimens over the course of an initial load and three repeated loads.

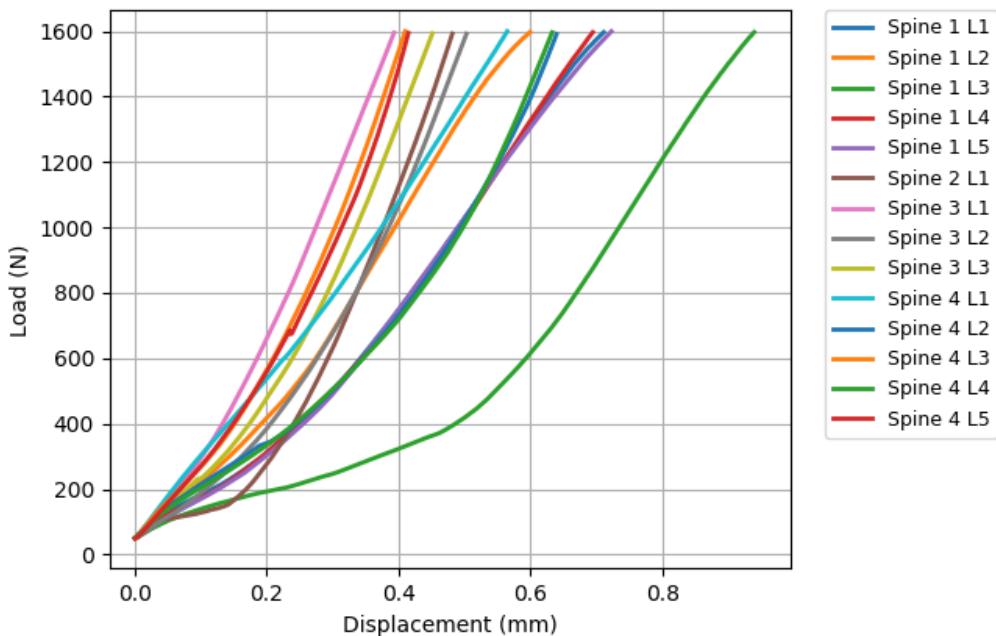


Figure 3.4: The load - displacement results for the initial load for all used vertebra

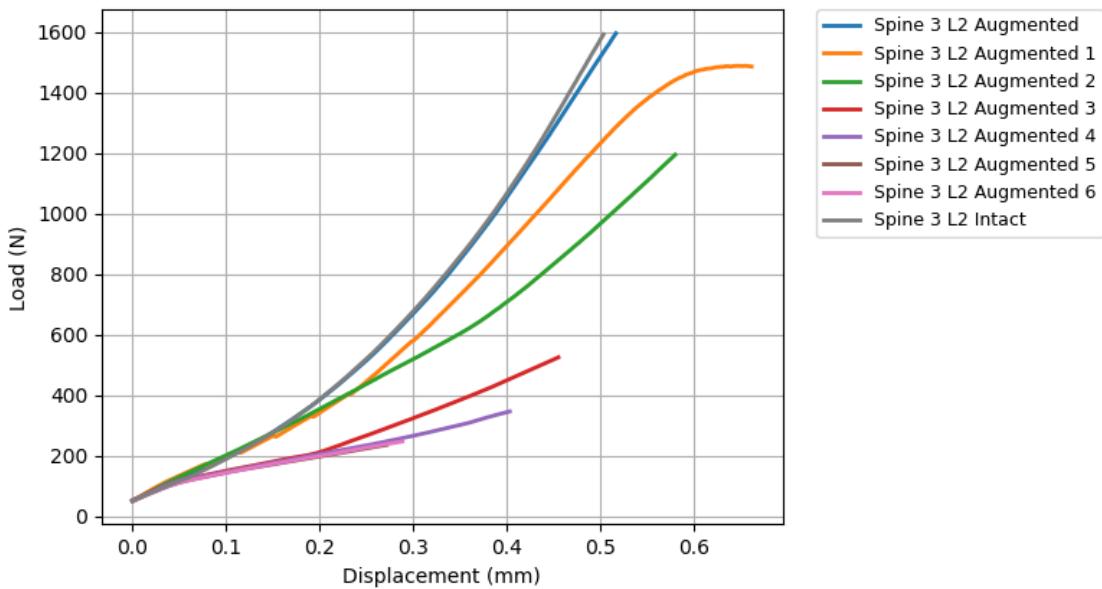


Figure 3.5: The load - displacement results for the Spine 3 L2 vertebra. Showing results of the intact load and post augmentation load as well as the 6 repeats.

### 3.2.3 Vertebroplasty

Despite the development of methods for the augmentation of bovine tail vertebrae, the methods for augmenting human vertebrae were altered due to the different geometry, size and reduced density.

The first change to the procedure was that the human vertebrae, being much less dense, did not require the vertebroplasty needle to be inserted with the aid of a mallet. Instead the needle could be pushed by hand through the cortical shell and into the vertebral body, with the vertebrae being held in a vice to ensure the correct angle and depth was achieved.

A second difference was the approach with the needle, instead of entering the vertebrae through their pedicles an oblique approach was adopted. This was due to variation in pedicle diameter between the L1 - L5 lumbar levels, where the pedicles on the L1 vertebrae were very small and therefore there was potential to damage the region and its load sharing capabilities. The oblique approach therefore avoided damaging pedicle-canal region, especially for the L1 and L2 vertebrae with narrower pedicles. An illustration of this approach can be seen in fig. 3.6 with an example  $\mu$ CT scan shown in fig. 3.7.

A final difference to the needle insertion methods was a change to the needle. Here, a side opening needle was used, allowing the cement to be directed into the anterior-centre region of the vertebral body as opposed to directly out of the needle end. This meant that larger cement volumes were much more achievable given that the injection of cement was not

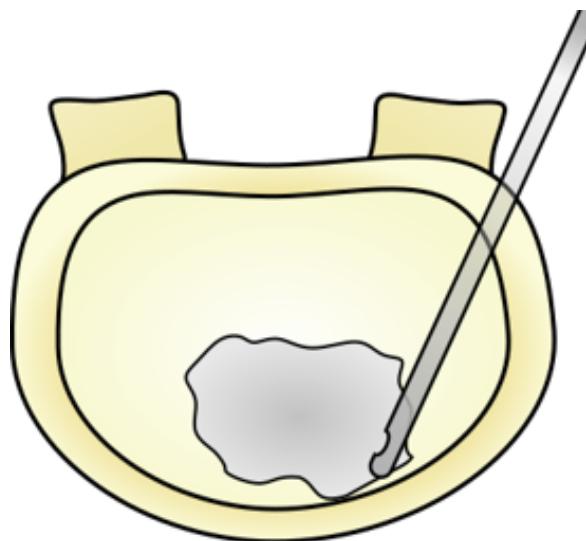


Figure 3.6: An illustration showing the approach to needle insertion and cement position.

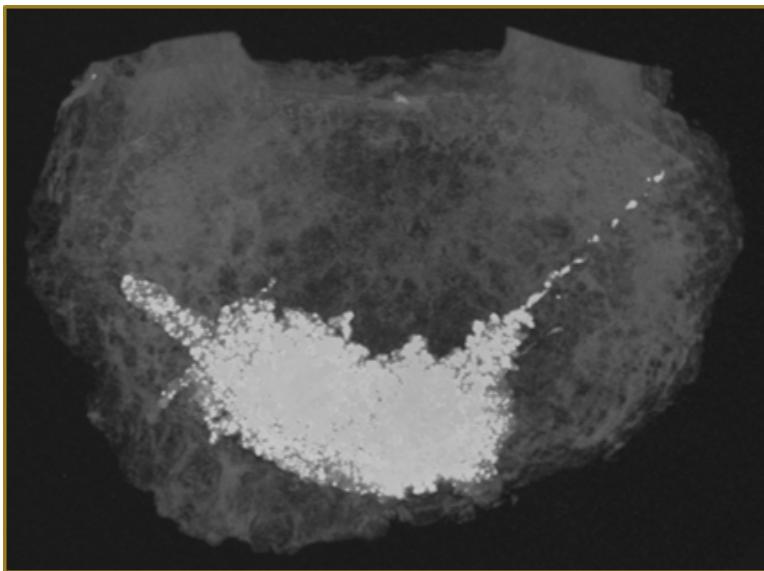


Figure 3.7: A  $\mu$ CT scan showing the injected volume of cement at the anterior of the vertebral body with the cement track from the exiting needle to the right. For this specimen cement leaked through the anterior wall, limiting the quantity of cement injected.

aimed at the anterior wall and instead could be rotated aiming both to the inferior and superior. One limitation that this caused was increased difficulty backfilling the needle tracks when the needle was removed. Future work may utilise a second end-opening needle to perform the backfilling, in this case however there was not enough time to change needles before the cement set, along with the available needles having different gauges.

It was attempted to inject the largest possible volumes of cement into the vertebrae, mimicking the clinical process. Like the clinical procedure the injection was stopped upon cement leakage, which generally occurred through one of the vascular channels at either the posterior or anterior portions of the vertebrae. However, despite stopping the injection upon cement leakage through vascular channels, cement loss still occurred after

the injection was stopped due to pressure build up. In addition to this, cement was also lost in the needle itself, where as the cement set the amount of cement remaining in the needle became difficult to measure. This meant that the cement fill could not be accurately measured though the amount of PMMA leaving the syringe due to both leakage and needle losses. Hence cement fill volume was measured using segmented  $\mu$ CT scans, using the volumes of the masks created to define the injected cement regions. This methodology is described in the computational modelling section (section 3.3).

### 3.2.4 Vertebrae Characteristics

Identifying the different characteristics for the set of lumbar vertebrae has importance in understanding trends and relationships between the experimental and computational results. For example a larger degree of anisotropy and hence more directional and aligned trabeculae would potentially give a more experimentally stiff vertebra, despite otherwise similar characteristics. Given that much of the vertebral characteristics depend on the trabecular structure it is important to understand how this varies between specimens. Furthermore, any calculations originating from a description of the trabecular structure require a correct threshold to be applied to the  $\mu$ CT scan. This threshold describes the limit of the trabecular bone and the start of either marrow or empty space. To enable a fair comparison between vertebrae a region of interest was selected from the vertebral body. Given the large variation in cortical shell thickness, along with certain vertebrae containing large osteophytes and other extra bone growth, the region of interest (ROI) was selected to be the largest cylinder that could fit within the vertebral body while not capturing any of the cortical shell.

#### 3.2.4.1 Histograms

In order to understand the spread of brightness' from the set of lumbar the histograms of the ROIs were plotted (fig. 3.8).

The lower greyscale values represent the empty space within the ROI which translates to regions where the bone marrow has drained from the trabecular bone, most likely during the unavoidable freeze thaw cycles. The peak in the histogram at an approximate greyscale value of 16 is due to the bone marrow. The remaining portion of the histogram represents bone, where variation is due to the differences in the mineral content of the bone, with more mineralised bone appearing brighter on  $\mu$ CT scans. The specimens ROIs that contain the brighter values are those that exhibit more degeneration for example Spine 2 L1, where

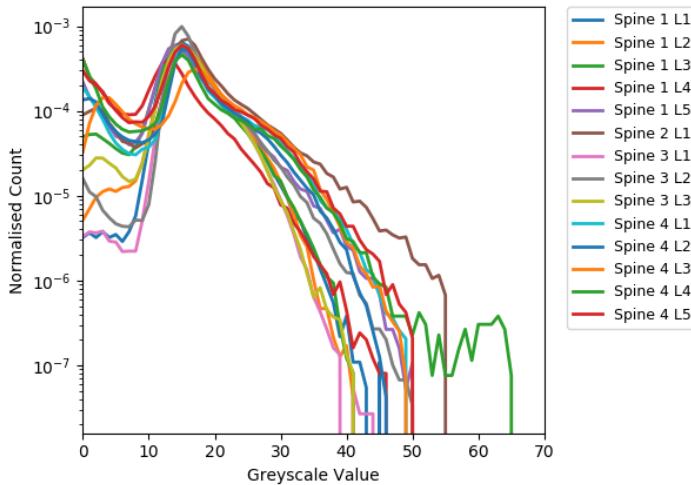


Figure 3.8: The normalised (with respect to the volume of the ROI) histogram data for the 14 lumbar vertebrae.

the histogram is shifted to the right, suggesting many more bright pixels and therefore more bone spurs and other degeneration. This is because the extra bone growths on the degenerated vertebrae is formed of denser cortical shell material.

### 3.2.4.2 Threshold Optimisation

Threshold optimisation or choosing a threshold that defines the limits of the trabecular bone in terms of greyscale values is necessary for various parts of the methods, the first being determination of the bone volume fraction (BV/TV) and secondly for some of the computational modelling methods employed.

The full resolution scan is imported into imageJ where the threshold optimisation is carried out. The BoneJ plugin for imageJ is used for all of the trabecular structure metrics, with the optimise threshold tool being the focus here. The threshold optimisation feature works by optimising the connectivity (Conn.D) against threshold value [89]. This tool is run on the region of interest using the default settings for the connectivity options seen in table 3.2. This chooses a threshold based on the peak in a connectivity against threshold plot and reports that value. These values can be seen in table 3.3, showing some variation across the range of vertebrae. However, the differences in these suggested thresholds can be grouped with the spine, for example: Spine 1 has a range between 15 to 17, while Spine 4 has a range between 18 to 20. This promotes the idea that these differences are due to the bone mineralisation of the bone, especially given that the G17 spine is from a Female and G41 from a male.

However, given that the chosen value for the threshold will directly impact the reported metrics, a consistent value was chosen of 18. Using lower or higher values for the threshold usually results in the trabeculae being described as thicker or thinner respectively. With respect to modelling, the difference in the mineralisation between specimens will still be captured when using a fixed threshold, given that the binary image will be down sampled before material properties are acquired. Here, thicker binarised trabeculae correspond to a brighter continuum level voxel. The results in table 3.7 show the BV / TV data and degree of anisotropy values for the 14 specimens using the fixed threshold of 18. Similar trends to what could be seen from the optimise threshold results can be seen in the BV/TV data, with grouping between the spines evident. This suggests that despite the use of uniform thresholds used across the set of vertebrae the differences are still kept, giving some additional validation and justification for using the uniform threshold. The vertebrae from Spine 1 have a much lower bone volume fraction compared to the other spines, which suggests a more osteoporotic spine, most likely resulting in less stiff vertebra. The remaining discussion of these results is in section 3.5.1.

Table 3.2: Settings used for the ImageJ plugin, BoneJ: Optimise Threshold.

Options	Values
Tests	11
Range	0.2
Subvolume Size	256
Erosian Cycles	0
Dilation Cycles	0

Table 3.3: The suggested threshold from the optimise threshold BoneJ tool for the 14 lumbar vertebrae in the set.

Specimen	Suggested Threshold
Spine 1 L1	17
Spine 1 L2	16
Spine 1 L3	16
Spine 1 L4	15
Spine 1 L5	16
Spine 2 L1	23
Spine 3 L1	18
Spine 3 L2	19
Spine 3 L3	19
Spine 4 L1	20
Spine 4 L2	19
Spine 4 L3	18
Spine 4 L4	19
Spine 4 L5	18

### 3.3 Computational Methods

The methods described in this section describe the process used to model non-augmented and augmented vertebrae, with associated sensitivity tests to understand the most appropriate approach to various aspects of the modelling process.

The methods used in this section broadly follow those used in the previous chapter, with a general process including the segmentation and FE model generation in Simpleware ScanIP, and solving the models in Abaqus using setup scripts written in python. One difference in this chapter is that the models were run on ARC2, part of the High Performance Computing facilities at the University of Leeds. Here, the submission of jobs (simple shell scripts describing the process to be carried out) onto the cluster is carried out using the Sun Grid Engine, a first come first served scheduler for the cluster. By running the FE simulation on the HPC cluster with resources: 10 cores, 1024 MB of memory per core, the time to solve each model was reduced to 5 - 10 minutes compared to 20 - 40 minutes on a desktop PC depending on the model and material properties used with models that included plasticity taking considerably longer to solve. In addition to the time saving benefits this allowed off loading of large (5 - 10 GB per model) Abaqus output files and through the submission system it allowed the iterative testing of material properties, where models could be re-solved using different material properties read from a simple text file.

The methodology of using ARC2, one of the HPC clusters remained much the same as when using a desktop PC. Here, abaqus input files were copied over to a user directory on one of the cluster nodes, along with files detailing the loading positions for the vertebrae, three python scripts and a shell script. The first python script set up the model, importing each abaqus input file, applying boundary conditions, loading position (according to the load position csv file), creation of the loading platen and application of the material properties to the greyscale based material properties of the bone. Settings and values applied in the setup script are read from another file containing: the conversion factor (greyscale to Young's modulus), the displacement and for the augmented models the cement and interface region material properties. The second python script runs the models with values of the number of cores and memory to use matching those of the requested HPC resources. The models are run with an initial increment of 0.1, a minimum increment of 0.0001 and a maximum increment of 1. The final python script runs the post processing; the abaqus output file is read and the axial reaction force (*RF3*) is recorded. The resulting stiffness (reaction force divided by the displacement to give a stiffness) from each model was written

to a results file which could be copied to the desktop PC and analysed. Finally, the shell script describes the resources to be requested from the HPC cluster including a maximum amount of time and then gives the command to be run: `abaqus cae nogui=setup.py && abaqus cae nogui=run.py && abaqus cae nogui=post.py` for the three python scripts. For new tests with potentially unexpected outcomes the abaqus output files were copied to the desktop PC to be viewed, while if incremental material property changes were being made, then only the stiffness results were copied.

### 3.3.1 Non-augmented Vertebrae Modelling Using the BV/TV Method

The methods used here broadly follow those described in the previous chapter with segmentation and model generation carried out in Simpleware scanIP and model simulation carried out in abaqus. Compared here in this chapter are two methods for modelling the non-augmented vertebrae, the first being named the normal method, which follows a near identical procedure to that used to model non-augmented bovine tail vertebrae. The comparison is made to a new method named the bone volume fraction, or BV/TV method. In this section the difference between these modelling methods are outlined with the bone volume fraction method being described in detail.

Given the aims of the project - to include the models generated here into a larger set of vertebral models for use in statistical shape modelling, it is useful to model the vertebrae in a scanner independent method. A method for doing this (BV/TV modelling method) uses a full resolution scan with the bone regions segmented and binarised using a threshold. This full resolution segmented scan is then downsampled to voxels with edge length of 1 mm, meaning that each voxel has a greyscale value proportional to the BV/TV value for the region captured by that voxel. Areas that contain more bone will therefore have a higher greyscale value. This method is purely dependant on the threshold selected to define the bone and hence, given that threshold values can be repeatedly and correctly selected with the methods shown in Section 3.2.4.2 through comparisons using phantoms, it can be scanner independent.

This method gives the opportunity to keep much of the detail that is often lost when downsampling image data. Specifically, the method described gives the vertebral models much more definition of the cortical shell and internal trabecular structure while maintaining the 1 mm cubed resolution and the computational cost benefits associated. The method follows similarly to the method used by Robson Brown et al. [56] with a few minor changes. The scans are converted from the ScanCo proprietary ISQ format into a stack of TIFF

files using an in house Matlab script, which in addition reduces the 16 bit data to 8 bit images.

The BV/TV method was compared to the normal method, described in section 2.3, to understand the effect of the changes made and the use of different greyscale backgrounds. For the bone volume fraction method a threshold was applied at the full  $82 \mu\text{m}$  resolution. This threshold was chosen to be a greyscale value of 18, the mean of the values described in section Section 3.2.4.2 and was applied to the scan stacks in imageJ. Once the binary stack was created a Gaussian filter was applied, also within imageJ, with  $\sigma_{x,y,z} = 1$ . This was applied in order to remove speckling found surrounding the end-caps and some of the other noise visible in the scans. The two stacks of images, binary and non-binary, are then imported into ScanIP; carried out by opening one stack of images (the original stack) and then importing a second background (the binary image stack). Both backgrounds are downsampled to voxel sizes of  $1 \text{ mm}^3$ , with the (originally) binary stack being used to create the mask for the vertebrae and the original stack being used for the segmentation of the end-caps. Greyscale material properties for the vertebral mask are taken from the binary stack, while the remainder of the methods follow the same process as the original method. A comparison of the two approaches can be seen in fig. 3.9, where the improved definition of trabecular structure and cortical shell using the bone volume fraction method can be seen in E and F, following the downsample to  $1 \text{ mm}^3$  resolution.

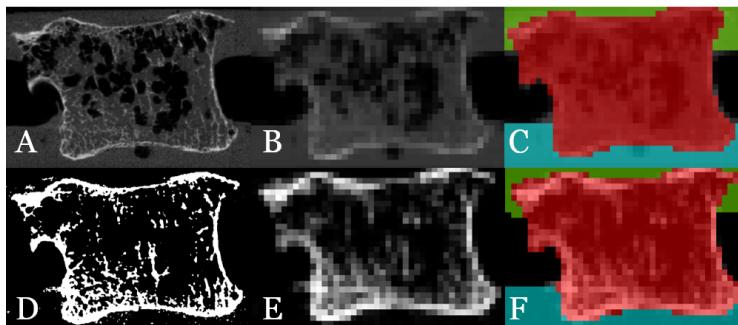


Figure 3.9: A comparison of the normal method (A, B and C) and the bone volume fraction method (D, E and F). A shows the full ( $82 \mu\text{m}$ ) resolution scan, B shows the same image downsampled to  $1 \text{ mm}$  resolution and C shows the segmented scan. D shows the segmented bone at  $82 \mu\text{m}$ , E shows this image downsampled to  $1 \text{ mm}$  and F shows this image after segmentation.

### 3.3.2 Sensitivity Studies

Sensitivity studies other than the main BV/TV tests present difficulties due to the models reliance on the underlying greyscale background. This is due to the greyscale optimisation process required to obtain a new conversion factor between the greyscale values and the

Young's modulus for every change made to the material properties or boundary conditions of the models. This is in order to understand the effect the change has on the agreement between experimental and computational results, and because a change to the material properties or boundary conditions may not have a systematic or uniform effect on the results. Due to this, simple sensitivity tests become difficult, including common convergence studies on voxel size. The sensitivity studies in this section highlight tests that were carried out that either did not require re-calibration of the greyscale conversion factor, or had minimal re-calibrations.

### 3.3.2.1 Load Position Sensitivity

With a dual aim of understanding the error in choosing the load position for the model (aiming to match the experimental loading point as closely as possible) and to understand how the vertebrae respond to different loading positions, 16 different positions were tested, shown in fig. 3.10. These positions included 1 mm and 2 mm aways from the centre in the posterior, anterior, left and right directions along with larger deviations of 10 mm and 20 mm from the centre in the same directions. The same boundary conditions, along with the 1 mm of axial displacement described above were applied to the different loading positions and the change in stiffness was recorded. The two magnitudes of distances from the centre tested, 1 and 2 mm, and 10 and 20 mm, are used to test the error due to the 1 mm resolution and the understand the response to non-central loading respectively.

The results of the load position sensitivity tests (fig. 3.11) show that on average, small posterior loads (above denser bone) result in higher stiffness's while all anterior loads result in a reduced stiffness. Loads lateral to the central loading point (fig. 3.12) resulted in little mean change to the stiffness of the models for the 1 and 2 mm positions. Larger movements away from the central loading position (10 mm and 20 mm) result in almost all vertebrae presenting a reduction in stiffness. Loading positions at 20 mm left and right present the largest reductions, where in the natural body the expected loads are less compared to anterior/posterior loading. Additionally, larger anterior loads resulted in larger reductions in the stiffness, given the less dense nature of anterior portions of the vertebral body

It also shows that the effect of movements of 1 mm away from the experimental loading position only changes the stiffness by approximately 5 %. Given the resolution of the models is limited to 1 mm, the accuracy of the selection of the experimental loading positions is also limited to 1 mm. The maximum 5 % change to the stiffness when posterior or anterior may describe some of the error seen when comparing the experimental and

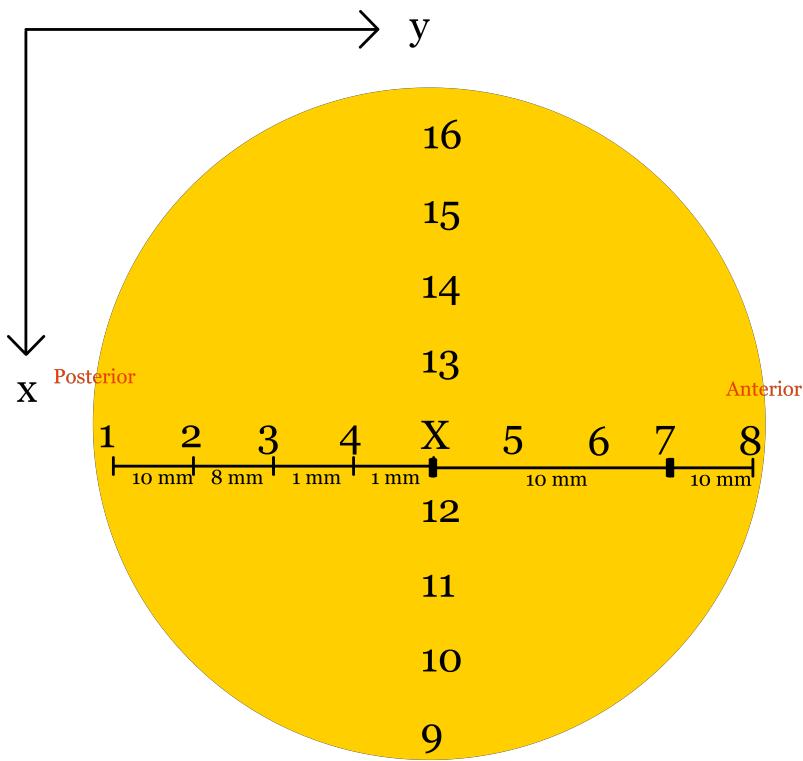


Figure 3.10: The loading positions used for the load variation tests. Position X is the original central loading position for ap and lr loading, other loading positions are 1 mm, 2 mm, 10 mm and 20 mm away from the centre.

computational results. However, as discussed in more detail in section 3.5.3.3, these errors may be negligible compared to the errors in the acquisition of the experimental stiffness from load-displacement data.

### 3.3.2.2 End-cap Depth & Contact sensitivity

This sensitivity test was carried out due to the high regions of stress seen in when removing the endcaps from the scene in the abaqus output viewer. The stress distribution at the surface of the vertebral body shows high stress at the edges of the cement endcaps, at both the top and bottom of these regions, shown in fig. 3.13. Experimentally the endcaps are merely moulded to the shape of the top and bottom of the vertebral body allowing slight motion of the vertebrae within them. However, previous work and other studies have used tied contacts between the bone and endcaps, removing any motion between the two and locking neighbouring nodes together. Additionally, the depth of these endcaps varies between 5 mm and 20 mm depending on the shape of the vertebral endplates. The more concave the vertebral endcap was the more cement was required to fill the space forming a flat cement surface. Hence, those models with larger endcaps may have more error given that more of the model was tied and therefore constrained within the endcaps. However, no relationship between cement endcap depth and the stiffness or error in the stiffness

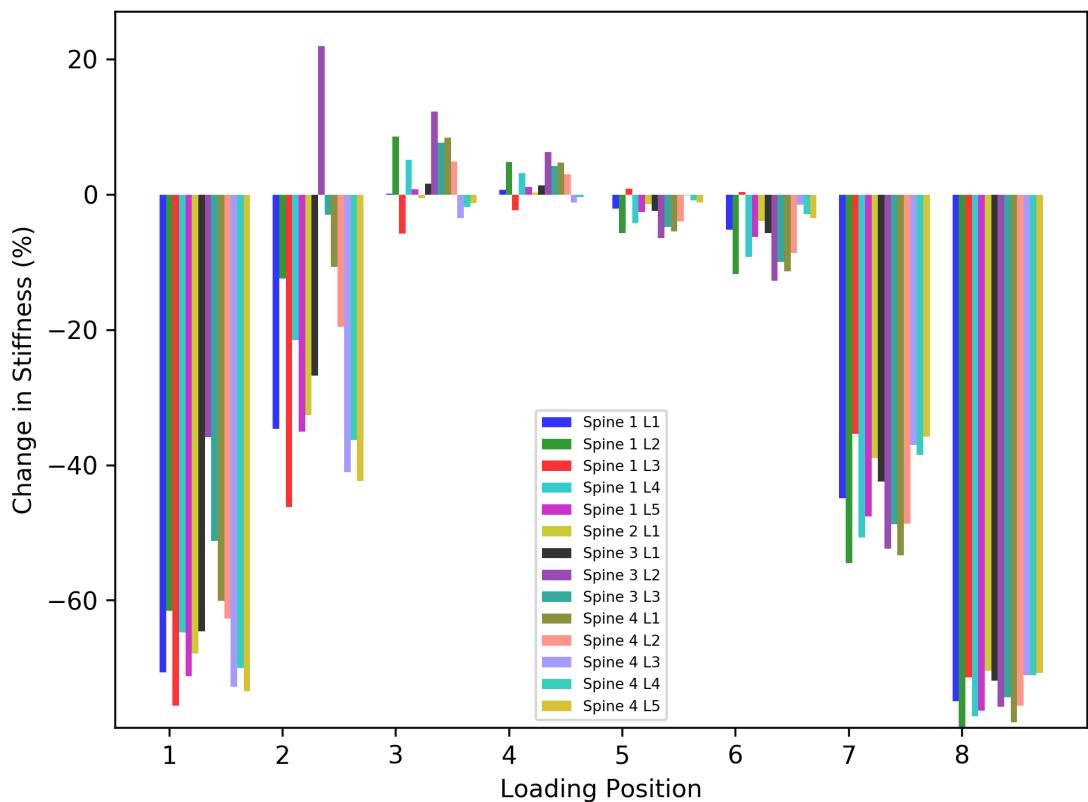


Figure 3.11: The effect of the loading position for the human lumbar vertebrae, shown as a percentage change compared to a central loading position, for load positions from the posterior to anterior according to fig. 3.10

compared to the experimental result was found.

Given this variation, tests identifying the effect of changing the endcap depth were carried out using FEA models with different depths of  $\pm 1$ ,  $\pm 2$  and  $\pm 3$  mm for the top and bottom endcaps independently and together. Additionally, the effect of changing the cement endcap depth with the currently used, tied contact to a frictionless contact was also investigated, along with variations to the properties of the frictionless contacts.

The endcap depth was altered by adding and removing layers within the model file in ScanIP, re-meshing the model and running the files using the same Abaqus python scripts. Endcap contacts were changed within the Abaqus python scripts, by firstly removing the ties between the endcap and the vertebra. An interaction property was created with tangential behaviour set to frictionless and normal behavior with properties: *pressureOverclosure = HARD*, *constraintEnforcementMethod = Default* and the final option was experimented with, *allowSeparation = ON/OFF*. The *allowSeparation* variable determines whether separation is permitted once contact is established and initially models ran correctly with it set to its default of *ON*. However, when experimenting with the effect of loading position, especially with loads applied far from the vertebral centre,

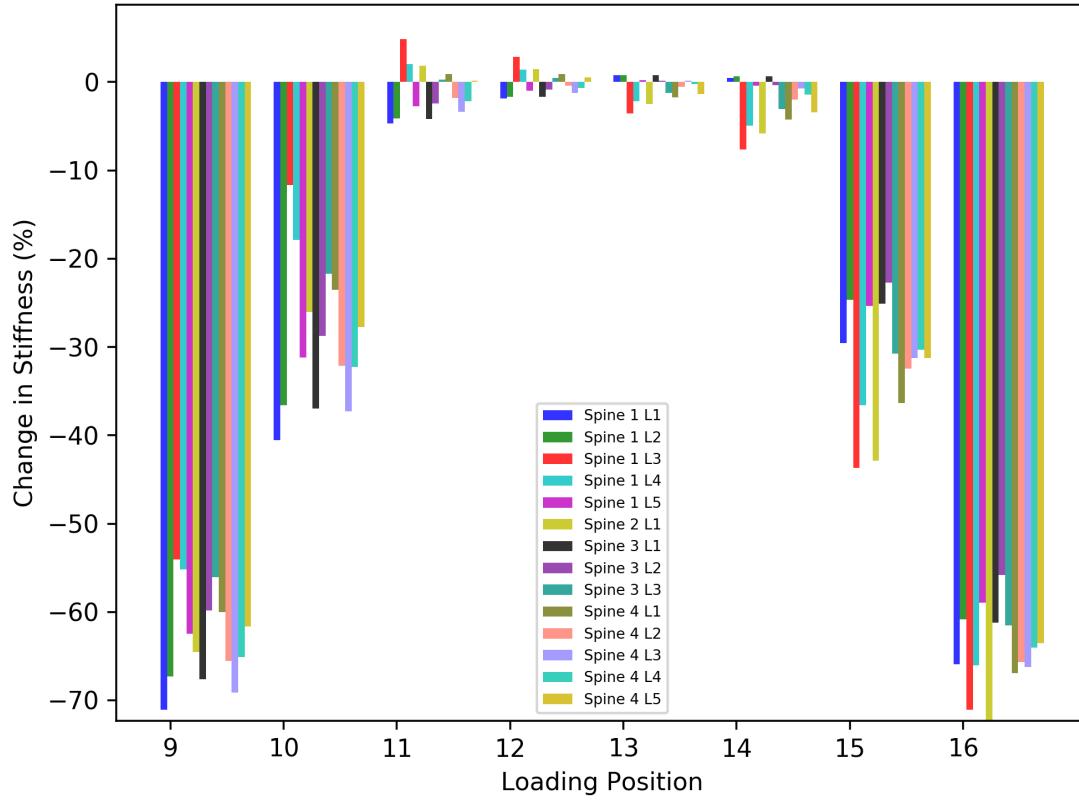


Figure 3.12: The effect of the loading position for the human lumbar vertebrae, shown as a percentage change compared to a central loading position, for load positions from the left to the right according to fig. 3.10

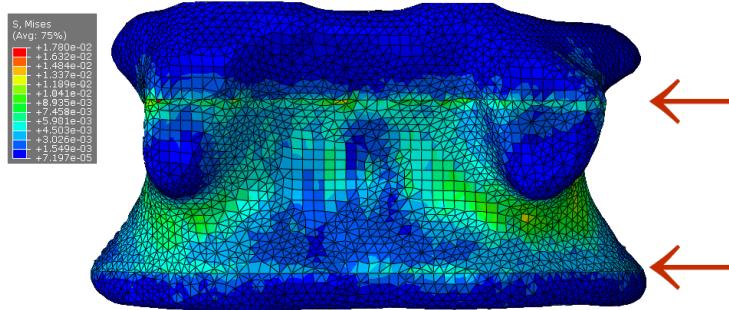


Figure 3.13: The effect of having tied contacts between the endcaps and the bone, with the increases in Von Mises stress indicated.

the solver struggled to converge due to the high stresses this caused at the limits of the vertebral body. Disallowing separation after contact was shown to have a small effect on the results (the outputted stiffness, with a mean increase in stiffness of 63 N) and allowed the models to run to the completion of the job. The remaining settings were set to the default for a generic contact:

*initialClearance = OMIT*

*adjustMethod = None*

*sliding = SMALL*

---

```

enforcement = NODE_TO_SURFACE
thickness = ON
supplementaryContact = SELECTIVE
interactionProperty = contactName
smooth = 0.2
bondingSet = None

```

The results shown in figs. 3.14 and 3.15 show that regardless of the contact, increasing the depth of the endcaps significantly increases the stiffness of the vertebrae, while reducing the depth reduces the measured stiffness. The effect this extra or reduced constraint caused by the changing endcap depth broadly follows the same trends for the two vertebrae tested. However, the response does differ most notably at the extremes of endcap depths ( $\pm 3$  mm), where the spine 4 L5 vertebrae experiences the greater reduction in stiffness when reducing the endcap depth, while the spine 1 L2 vertebrae sees the greater increase following depth increases. This difference is a consequence of the differences in the density of the vertebrae (where spine 4 is, on average, much denser than spine 1 in terms of mean greyscale value) and the differences in the shape (the L5 vertebrae being much wider with greater protruding bone spurs at the bottom of the vertebrae and the narrower L2 vertebrae having the bone spurs at the top of the vertebrae. These shape differences can be seen in figs. 3.25 and 3.28.

The variation in the change to the stiffness within  $\pm 1$ mm change in depth was up to 5 %, for both cases. Given that the maximum error in masking the cement endcaps is 0.5 mm due to the resolution that is used for the segmentation, it suggests that this error has a minimal effect on the end results. As mentioned previously, this is due to the other errors associated with measuring the experimental stiffness.

The effect of changing the contact from tied to frictionless can be seen by comparing figs. 3.14 and 3.15. Excluding the very large change in stiffness seen in the L5 vertebra when reducing the depth of the inferior endcap, the adoption of the frictionless contact reduces the effect of endcap depth on measured stiffness. This is due to a reduction in the constraining nature of the frictionless contact, allowing a more natural measure of the vertebral stiffness rather than a combination of the vertebral and endcap combined stiffness. The anomalous L5 vertebrae here is a function of having less support and the slipping that this allowed, resulting in the reduced measured stiffness. Optimising the greyscale conversion factor for the set of models with a tied constraint and a frictionless contact gave an improved agreement with a concordance correlation coefficients of 0.848

and 0.865 respectively. Therefore the frictionless contact providing a small improvement in the agreement between the computational and experimental results.

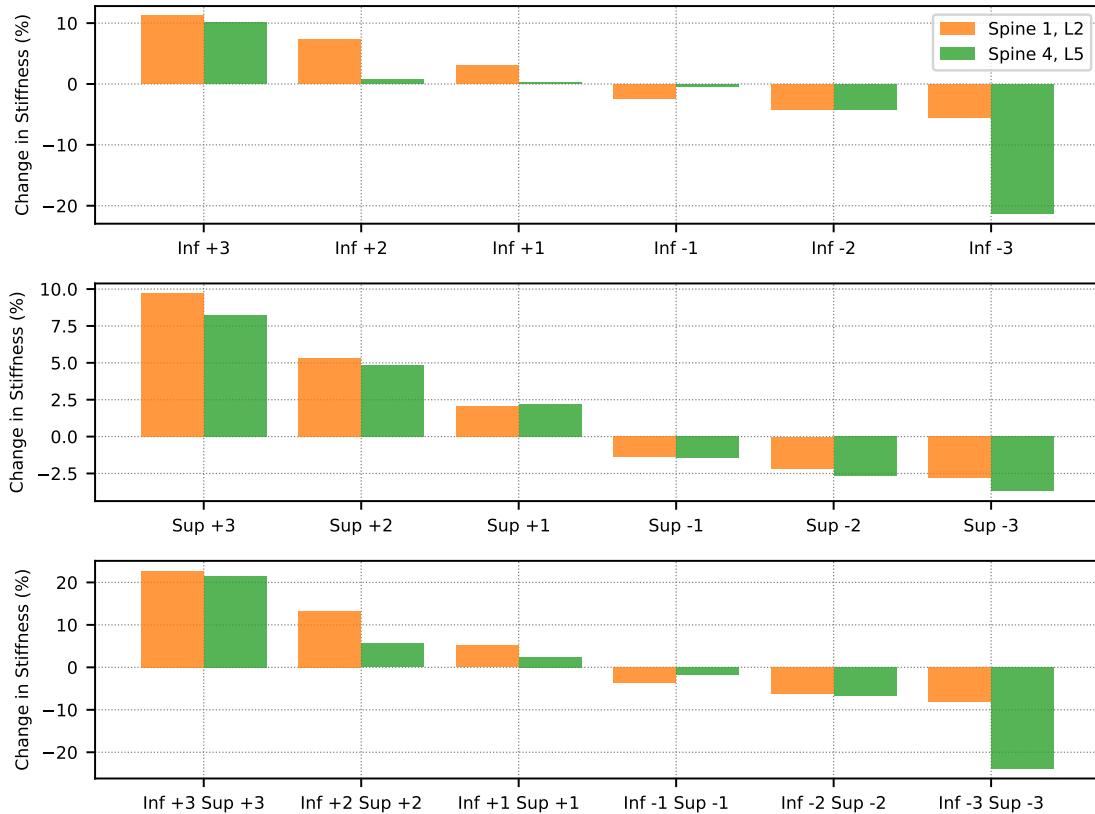


Figure 3.14: The percentage change in stiffness following a change to the endcap thickness. Inf and Sup show changes of  $\pm 1, 2$  and  $3$  mm to the inferior and superior endcap depth respectively. The endcaps have a tied contact to the vertebrae.

Further tuning of the specifics of the frictionless contact could be carried out (to see if an improved agreement could be achieved) and would be a simple addition to this sensitivity test. However, due to the greyscale conversion factor optimisation process required to test each option this would be a timely operation, which, given the relatively small effect of changing to the frictionless contact, could yield negligible results.

### 3.3.3 Material Properties

The general method for obtaining material properties for the bone elements in the FE models uses the same approach as used in section 2.3.3 where the Young's modulus of each element is equal to the greyscale value multiplied by a conversion factor. The conversion factor is optimised by comparing the computational stiffness against the experimentally acquired stiffness. For the optimisation process the vertebrae were split into two groups at random, giving a calibration and validation set, allowing a test of the validity of the greyscale conversion factor. The split of the vertebrae for these two sets can be seen in

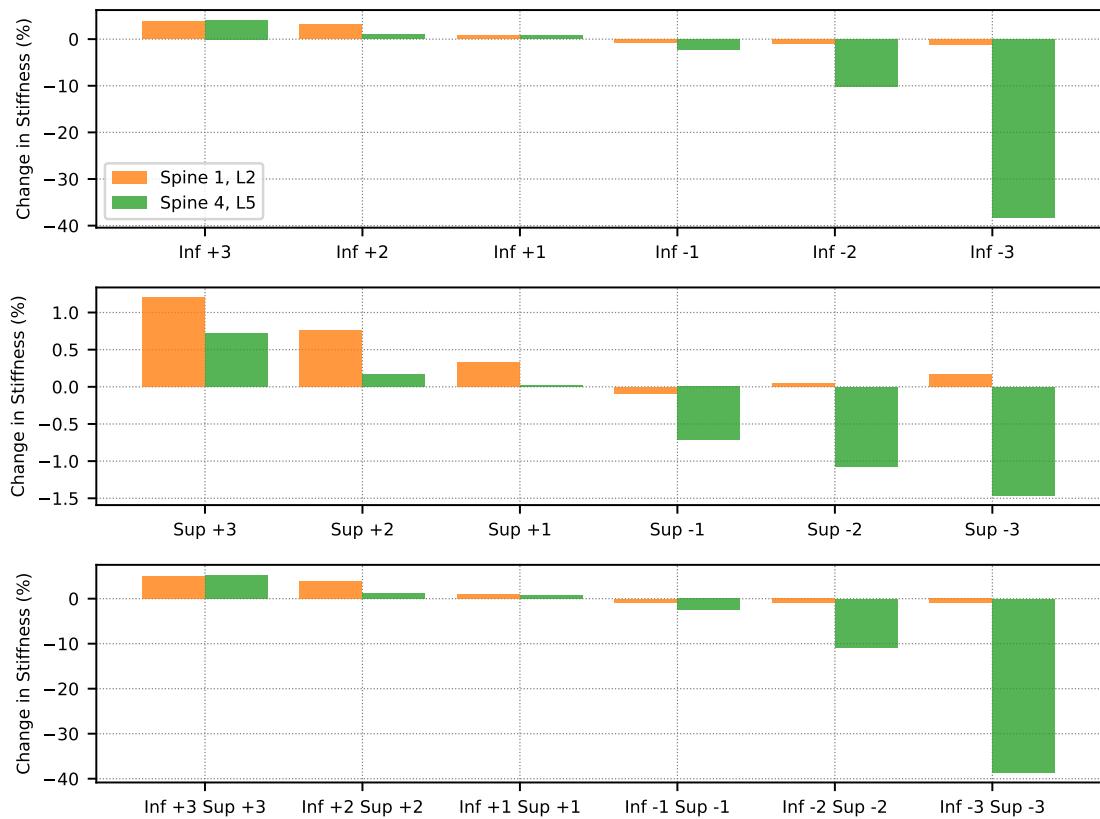


Figure 3.15: The percentage change in stiffness following a change to the endcap thickness. Inf and Sup show changes of  $\pm 1, 2$  and  $3$  mm to the inferior and superior endcap depth respectively. The endcaps have a frictionless contact to the vertebrae.

table 3.4, where the greyscale conversion factor was derived from the calibration set and applied to the validation set where the agreement was measured.

Table 3.4: The vertebrae used for the calibration set and the validation set in the optimisation process.

Calibration Set	Validation Set
Spine 1 L4	Spine 1 L1
Spine 1 L5	Spine 1 L2
Spine 2 L1	Spine 1 L3
Spine 3 L2	Spine 3 L1
Spine 4 L1	Spine 3 L3
Spine 4 L2	Spine 4 L3
Spine 4 L4	Spine 4 L5

Results from the initial optimisation process using the calibration and validation processes gave good results: the agreement of the validation set had CCC values of above 0.5. The validation set for the “normal” method had a CCC value of 0.591 and the CCC value for the validate set from the “bone volume fraction” method gave a value of 0.831.

Given the problems associated with calculating the greyscale conversion factor with various sensitivity tests described in section 3.3.1, the calibration and validation sets were only

used for the initial test, once using the “normal” method and once using the “bone volume fraction” method. This validated the use of the optimisation process while allowing more accurate greyscale conversion factors for the sensitivity tests and final values given that the input set of human vertebrae was relatively small.

### **3.3.4 Final Material Properties and Boundary Conditions for the Non-augmented Models**

Following the results of the sensitivity tests the final value from the optimisation process for the greyscale conversion factor was 0.0009625 for the BV/TV method and This was used for the bone properties for all final non-augmented models and augmented models. The optimised greyscale conversion factor for the models generated using the normal method used a value of 0.00416.

The remaining material properties used for all of the models are a Poisson’s ration of 0.3 for the bone and endcaps and a Young’s modulus of 2.45 GPa for the endcaps. Boundary conditions for the models included the frictionless contact between the vertebrae and their endcaps (for the bv/tv method, tied for the normal method), a tied contact between the analytical platen and the superior endcap where 1 mm of axial load was applied.

### **3.3.5 Modelling Augmentation**

Given the limited validation of models achieved using bovine tail vertebrae (due to the reasons discussed in Section 2.3.6), a range of different material properties and approaches to modelling the bone-cement interface were investigated. In addition to varying the material properties of the injected volumes of cement, the effect of using a combination of scans from before and after augmentation has been experimented with. To achieve this scans of pre/post augmentation were registered. This method utilised the BV/TV method described earlier, where the non-augmented full resolution binary scan is registered to the full resolution augmented scan.

#### **3.3.5.1 Registration of $\mu$ CT Scans**

Artificial brightening of regions surrounding the internal cement (specifically the concentrated volumes of barium sulphate and the artefacts associated) affect the material properties that are applied to the material, seen in the right side image in fig. 3.16. Given that the material properties are based on the greyscale background, this has the effect of

artificially stiffening or changing the properties of elements who's properties are described by these regions. To bypass this effect the two models, intact and post-augmentation models can be registered - translating them into the same spacial location. This allows the cement to be defined, masked and modelled based on the post-augmentation scan and the remaining vertebra to be defined from the non-augmented scan, using same background used for the non-augmented models. While the shape of the vertebra may have been changed over the course of its two loads, this change is less than what can be seen at 1 mm resolution and is not apparent during the registration process carried out at  $82 \mu\text{m}$  resolution.

Registration of the images was carried out in 3D Slicer, using scans of the segmented, full-resolution, non-augmented vertebrae and the full-resolution augmented vertebral scans. The method of registration was a landmark based approach using three landmarks for each vertebra, translating the scan of the augmented vertebrae to that of the non-augmented vertebra. These points were selected at the most superior point of one pedicle, the most inferior point of the other pedicle and the most inferior and anterior point of the vertebral body. The selection of these points proved to provide a repeatable registration of the vertebrae, without selecting superfluous landmarks. Once registered the resulting translated augmented vertebrae scan was cropped with respect to the non-augmented scan to provide an aligned and registered pair of scans.

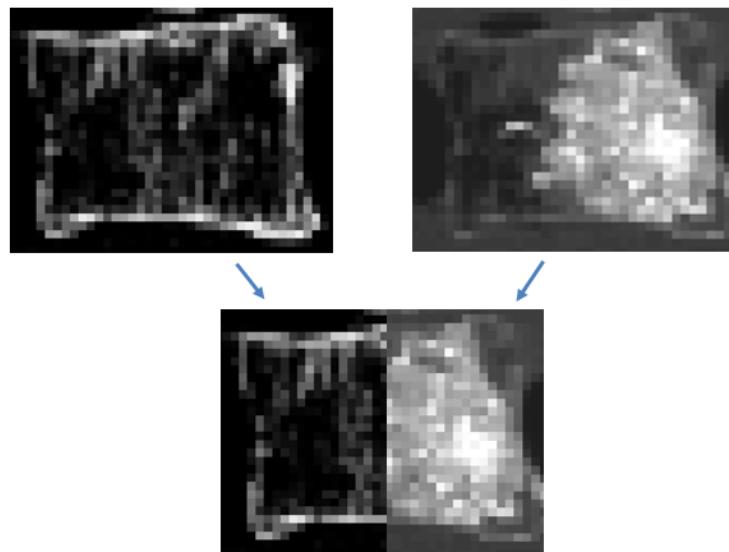


Figure 3.16: An illustration of the registration process, registering the non-augmented scan (left) with the augmented scan (right). The images are at 1 mm resolution, showing the artifacts created by the barium sulphate when viewed at this resolution, while to increase accuracy the registration carried out in Slicer 3D was at the full  $82 \mu\text{m}$  resolution.

### 3.3.5.2 Registered Scan Model Generation

The augmented models using the registered scans were created in ScanIP, following similar methods to the bone volume fraction method described in Section ???. The initial step was to import the registered augmented scans and apply an initial downsample to a resolution of  $0.5 \text{ mm}^3$ . This resolution provided enough detail to capture the detail of the injected cement volume without increasing the computational difficulty and therefore time to segment the scans.

To segment the three regions (background, bone and endcaps, and injected cement) it was found that the most reproducible and accurate method was to use the Otsu thresholding process [90], a filter that is built in to ScanIP. It was used to find four masks in the scan and works on a threshold clustering method. In this case searching for four clusters or masks separated by different thresholds and returning a mask that described the background, bone, endcaps and the cement region. From this only the cement mask was retained. The mask and background were then downsampled to 1 mm resolution and cropped to the same dimensions as the non-augmented model. From the non-augmented model, the masks describing the vertebra and endcaps were imported, along with the binarised background of the vertebra. The origin of the masks coming from the two backgrounds can be seen in fig. 3.17.

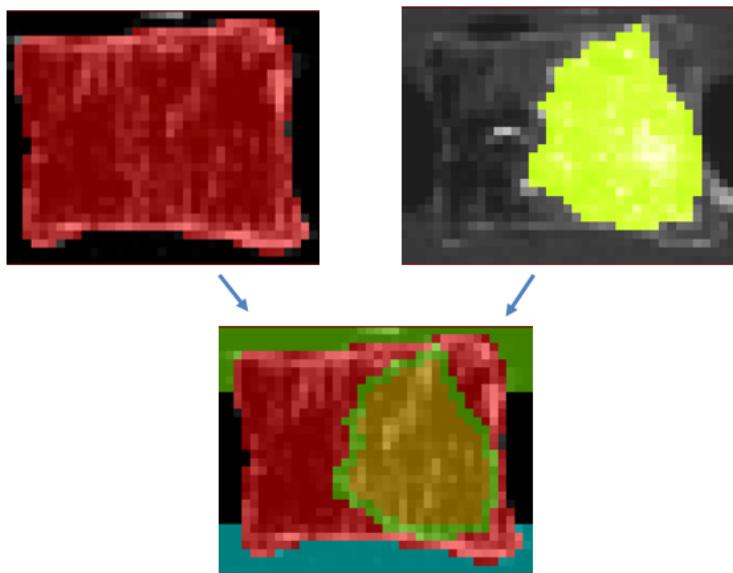


Figure 3.17: An illustration showing the origin of the masks from the non-augmented scan (left) and the augmented scan (right).

Finally, given that the non-augmented  $\mu\text{CT}$  scan is used for the material properties of the augmented models when using the method outlined above, damage caused to the vertebrae during the augmentation process is not captured in the model. Specifically the

track left behind by the vertebroplasty needle is shown clearly on the post-augmentation  $\mu$ CT scan, and while it was attempted to fill this space when cement when removing the needle in some cases this was not possible or the needle track was only partially filled. An example of the track left behind can be seen in fig. 3.18:B, with comparisons to the BV/TV background in A, and the correction, through removal of the mask in C. Removal of the vertebral mask in the regions where the needle track was clear in the post-augmentation scan was carried out using the (un)paint line tool in Simpleware ScanIP. This change to the models required further changes to the material properties of the cement and interface regions as described in section 3.3.5.3. Results of models with and without the needle track are presented in section 3.4.2.2.



Figure 3.18: Adding the needle track to registered models. A, shows the masks overlaid onto the BV/TV greyscale background, B shows the masks overlaid onto the augmented scan background and C shows the removal of the mask where the cement track is visible. The pink mask shows the cement region, yellow shows the interface and red is the vertebral mask.

### 3.3.5.3 Cement Volume Material Property Tests

Based on the results of the tests carried out on the bovine tail vertebrae in chapter 2, different material properties and approaches were attempted to further the agreement between the experimental and computational results of augmented vertebrae. These were mainly changing the material properties of the interface layer between the bone and the cement, along with the material properties of the cement volume itself.

These material properties were tested in an iterative fashion changing the properties in the material properties file read by the python setup script. Following the results of the above tests, the final material properties for the cement and interface regions are in table 3.5 for the three main methods tested.

Boundary conditions for the cement region include: tie contacts between the vertebrae and interface, and between the interface and the cement volume. The remaining material properties and boundary conditions remain the same as with the non-augmented models,

Table 3.5: The material properties for the injected cement volumes and it's surrounding interface region for the three main modelling methods used. P.P., indicates perfectly plastic

Property	Modelling Method		
	Non-registered	Registered	Registered With Needle Tracks
Cement Young's Modulus	1.7 GPa	1.2 GPa	1.5 GPa
Cement Poisson's Ratio	0.4	0.4	0.4
Interface Young's Modulus	0.005 GPa	0.008 GPa	0.01 GPa
Interface Poisson's Ratio	0.4	0.4	0.4
Interface Yield Stress	50 Pa → P.P.	5 Pa → P.P.	5 Pa → P.P.

described in section 3.3.4.

Finally, an alternate way of modelling the augmented region was attempted using the greyscale background of the non-augmented specimen to serve as a measure of the location of the cement. If the element was bright, suggesting it contained mostly bone, it suggests that the element does not contain cement. Conversely low greyscale value elements suggests limited bone and therefore more chance of containing cement. However, the initial testing using this methodology produced a poor agreement with the experimental results and investigation and optimisation of the method was stopped. The methodology and limited results are described in section A.1.

### 3.3.6 Measuring the Vertebral Body & Augmentation Volume

While the volume of the vertebral mask can be measured directly within ScanIP or Abaqus, this volume includes the remainder of the pedicles and other bone growths and spurs. The size of the pedicles that remain after their removal during dissection varies between level and spine and is especially different with the level five vertebra, where the shape and size varies dramatically. To account for this variation and to get a more accurate cement fill percentage for the augmented models elliptic cylinders were fitted to the vertebral body as shown in fig. 3.19.

This was carried out using a set of scripts written in python and rely of having stl files describing the vertebral geometry. The scripts work by finding the middle slice of a set of nodes that describe the vertebra. From the middle slice the shape of the ellipse is formed. Given that the alignment of the vertebrae is uniform, the mid point on the  $y$  axis is found by searching for the node furthest away from the weighted center,  $\pm 2$  mm of the weighted centre. The axes are defined in fig. 3.19:B. This gives the  $a$  measure of the ellipse description. The  $b$  measure is found by using a similar process - searching for the node furthest away from the centre on the  $x$  axis, within  $\pm 2$  mm. The  $a$  and  $b$  measures gave

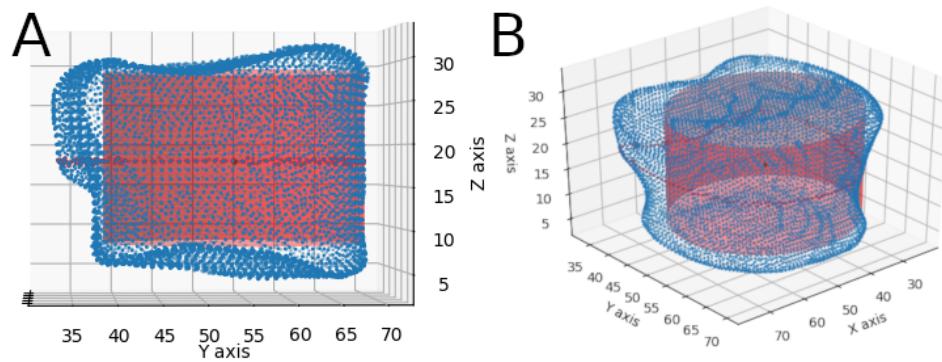


Figure 3.19: A diagram showing the fitting of the cylinders to the vertebral body, where the point cloud describing the vertebra comes from an STL file, the red ring shows the points included in the mid-slice and the central red dot indicates the center of the mid-slice.

the shape of the ellipse and the height of the elliptic cylinder was found by raising and lowering the ellipse until a node in the middle  $\pm 5$  mm of the endplate intersected the ellipse. This defined the height of the ellipse.

Vertebrae that contained a vascular channel, seen in fig. 3.20, had the channel removed by filling the space in ScanIP. This was carried out for two main reasons: the first was to allow accurate fitting of the cylinder into the vertebral (to avoid the problems shown in fig. 3.20) and to remove problems with the cement being exposed when modelling augmentation and the extra contacts / interfaces that are created. Models with the vascular channel removed were compared to the original models and it was found that there was less than 0.5 % difference for the set. This was due to the elements used to fill the channel having material properties based on the greyscale, which had values of approximately zero, given the nature of the channel. Due to the lack of any effect in removing the channel the vertebra models of augmentation did not include the vascular channel.

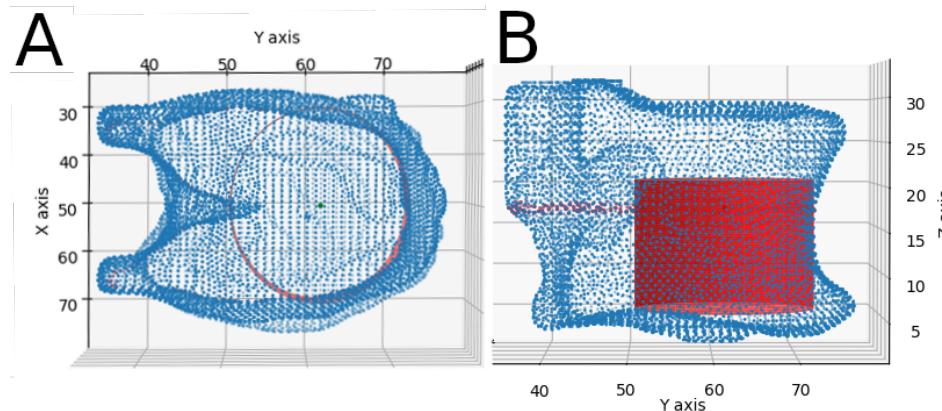


Figure 3.20: An illustration showing the problems that occur with vertebrae that have a distinctive vascular channel and the false cylinder fit that occurs.

The volume of the ellipse was found ( $V = \pi abh$ , where  $a$  and  $b$  have been described and  $h$  is the height) and compared to that of the total vertebral volume, shown in table 3.6. The

percentage reduction in vertebral body volume, from total vertebral body volume to the fitted cylinder volume, varies significantly and is due to changes to the vertebral shape outside of the main vertebral body portion. For example, Spine 2 L1 was a degenerate vertebrae with extra bone growth at the anterior limits of the vertebral body. Other large changes were due to the size of the pedicles, where larger vertebrae (Spine 4) had proportionally larger pedicles.

Table 3.6: Vertebral body volume compared to the volume of the fitted cylinder.

Specimen	Total Vertebral Body Volume (mm <sup>3</sup> )	Fitted Cylinder Volume (mm <sup>3</sup> )	Change in Volume (%)
Spine 1_L1	31229	17490	-44
Spine 1_L2	31789	20551	-35
Spine 1_L3	33519	22014	-34
Spine 1_L4	35123	22796	-35
Spine 1_L5	31189	22254	-28
Spine 2_L1	33835	17420	-48
Spine 3_L1	45866	31073	-32
Spine 3_L2	53695	34470	-36
Spine 3_L3	56003	36750	-34
Spine 4_L1	35137	22231	-37
Spine 4_L2	36791	23837	-35
Spine 4_L3	39909	26036	-35
Spine 4_L4	43357	25612	-41
Spine 4_L5	45606	26936	-41

The effect of this change on the relationship between cement fill and change in augmentation stiffness was identified and is shown in fig. 3.21. While there was a change in the relationship, a clear trend between the cement fill percentage and change in stiffness for the majority of the vertebrae is still not evident using either approach to measuring the vertebral body volume.

### 3.3.7 Visualisation of Vertebrae and Augmentation

#### 3.3.7.1 Vertebral Density Visualisation

To visualise the density distribution of the trabecular bone within the FE models, Simpleware ScanIP was used. Here, FE models were generated and the clip box was used to remove an axial half of the model from the render. Mass density material properties were then assigned to the model within the visibility options, given that material properties for the region had been set to greyscale based. This provided color maps of the density of the vertebral mid-slice. An example of this can be seen in fig. 3.31.

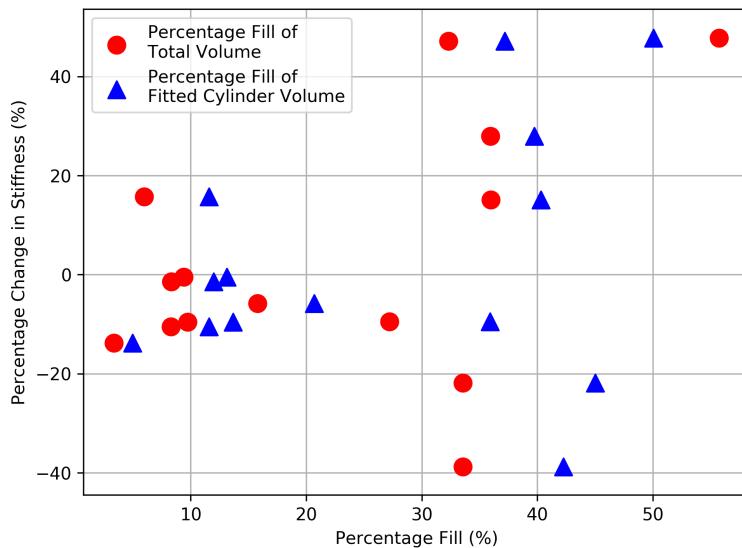


Figure 3.21: The effect of using the fitted cylinder as a measure of vertebral body volume, on the relationship between augmentation fill volume and change in stiffness following augmentation. The red points show the relationship using the total vertebral volume, with the relationship using the fitted cylinder shown in blue.

### 3.3.7.2 Cement Distribution Visualisation

Visualisation of the cement distribution in augmented vertebrae can be difficult due to the 3D nature of the cement distribution. Understanding features of the cement volume, for example determining whether cement volumes are distributed or concentrated becomes difficult. Given that 2D images of the augmented vertebrae only give an understanding of the layer in question and the 1 mm resolution of FE models makes identifying the nature of the structure from the generated model visualisation difficult. The methodology used to visualise the vertebrae and the solution to this problem was to use the 3D project feature in imageJ. This creates a 3D rendering from the stack of images and rotates the resulting object through a range of angles, in this case 360 degrees. Variables of transparency bounds, opacity bounds and the projection method can be set, in addition to the axis of rotation. These were left at their default using the brightest point projection method and the Y-axis for the rotation axis. This generated a model that could be rotated around the Y-axis, providing a view of the cement distribution through the vertebrae and not one limited to a slice by slice view. Examples of this method can be seen in figs. 3.25 to 3.28, where projections of the transverse and saggital planes can be seen.

## 3.4 Results

The results described in this section are split into two main sections: those derived and obtained through experimental means and those measured from the computational, generated models.

### 3.4.1 Experimental Results

Material properties for the vertebrae can be seen in table 3.7, with grouping evident for the bone volume fraction measurements. For example the mean BV/TV value for Spine 1 was  $0.159 \pm 0.026$ , while the mean for Spine 4 was  $0.248 \pm 0.022$  with similar results for the other two spines (although with less vertebra). Less grouping could be seen between the degree of anisotropy for the vertebrae.

The vertebral stiffness following experimental loading can be seen in table 3.8 for the non-augmented vertebrae and following vertebral augmentation. The change in stiffness can be seen in fig. 3.22 where an increase in stiffness was seen Spine 1 L2-L5 and Spine 2 L1, while the remaining vertebrae presented a reduction in stiffness following augmentation.

Table 3.7: BV/TV and degree of anisotropy (DA) values found using the ImageJ plugin BoneJ tools Volume Fraction and Annisotropy respectively using a threshold of 18.

Specimen	BV/TV	DA
Spine 1 L1	0.174	0.387
Spine 1 L2	0.17	0.364
Spine 1 L3	0.137	0.359
Spine 1 L4	0.127	0.418
Spine 1 L5	0.187	0.341
Spine 2 L1	0.391	0.199
Spine 3 L1	0.255	0.327
Spine 3 L2	0.267	0.231
Spine 3 L3	0.281	0.301
Spine 4 L1	0.257	0.239
Spine 4 L2	0.241	0.338
Spine 4 L3	0.244	0.348
Spine 4 L4	0.247	0.371
Spine 4 L5	0.249	0.186

A strong relationship was found between the percentage fill volume achieved and the bone volume fraction of the vertebra, where a reduced density of bone resulted in larger quantities of cement being injected into the vertebra before cement leakage occurred. This relationship can be seen in fig. 3.23.

There was not a clear relationship found between the cement fill of the total vertebral volume and the resulting change in stiffness following augmentation for the set of vertebrae

Table 3.8: The experimental stiffness results for pre and post augmentation.

Specimen	Non-augmented Stiffness (N/mm)	Augmented Stiffness (N/mm)	Change in stiffness (N/mm)
Spine 1 L1	2991	2339	-652
Spine 1 L2	3456	3980	523
Spine 1 L3	3244	4152	907
Spine 1 L4	3223	4744	1521
Spine 1 L5	2891	4273	1382
Spine 2 L1	6149	7119	969
Spine 3 L1	5153	4444	-709
Spine 3 L2	5357	4848	-510
Spine 3 L3	5338	4779	-559
Spine 4 L1	3277	3231	-46
Spine 4 L2	5064	5042	-22
Spine 4 L3	6098	5749	-349
Spine 4 L4	4957	4488	-468
Spine 4 L5	7185	4403	-2782

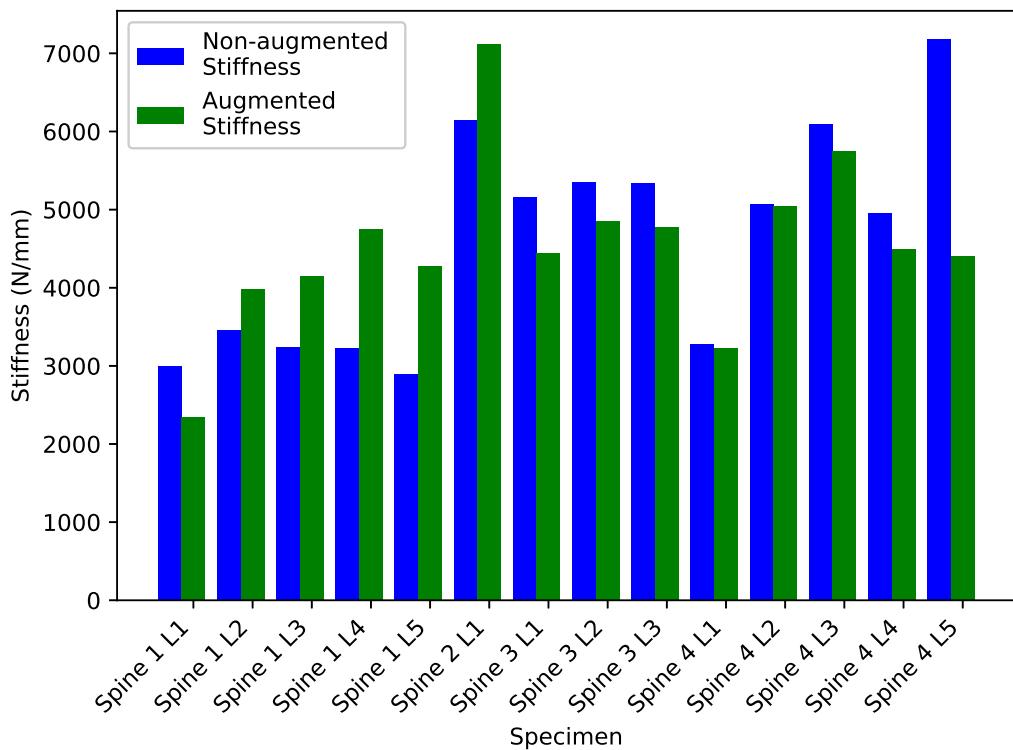


Figure 3.22: The experimental stiffness of the vertebrae pre and post augmentation. Showing that 5 of the 14 vertebrae showed an increase in stiffness following augmentation.

on the whole. However, trends could be seen when splitting vertebrae into groups with: *a*) dispersed volumes of injected cement and *b*) concentrated volumes of cement. This can be seen in fig. 3.24 where a trend ( $r = 0.83$ ) can be seen between the percentage fill of the total vertebral volume and the percentage change in stiffness for those vertebrae with concentrated volumes of cement.

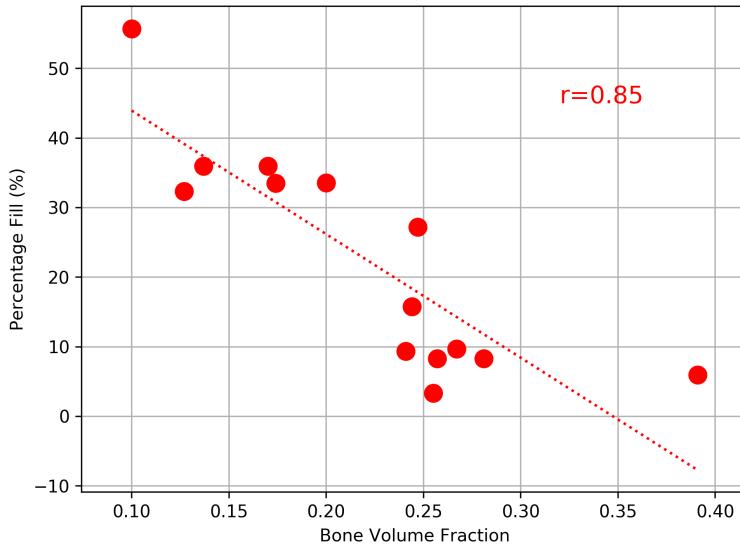


Figure 3.23: The relationship between the percentage cement fill of the total vertebral volume achieved through the augmentation procedure and the bone volume fraction value for each vertebra.

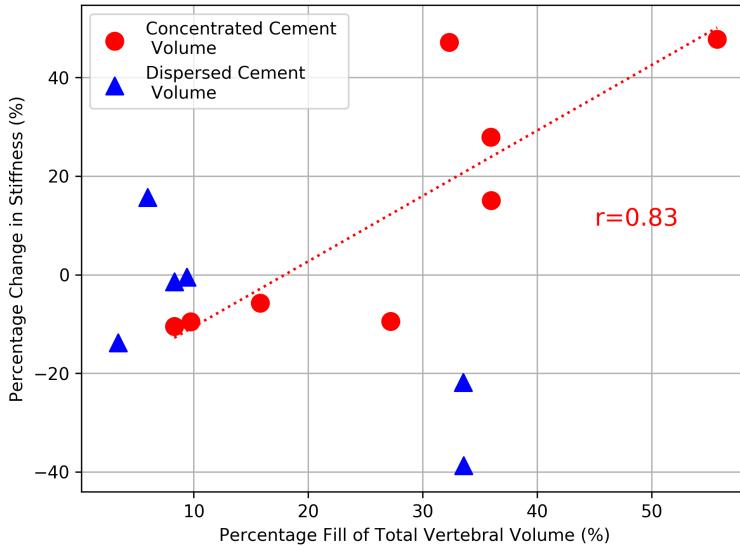


Figure 3.24: The relationship between the percentage fill of the total vertebral volume and the percentage change in the vertebral stiffness following augmentation. The line and  $r$  value are for the red points where the cement volume was characterised as concentrated. The remaining blue points indicated the vertebra where the cement volume was characterised as dispersed.

The cement distributions following augmentation can be seen in figs. 3.25 to 3.28. From the 3D projection images and slices from  $\mu$ CT stack it was determined which vertebrae contained dispersed and which vertebrae contained concentrated volumes of cement, this characterisation can be seen in table 3.9.

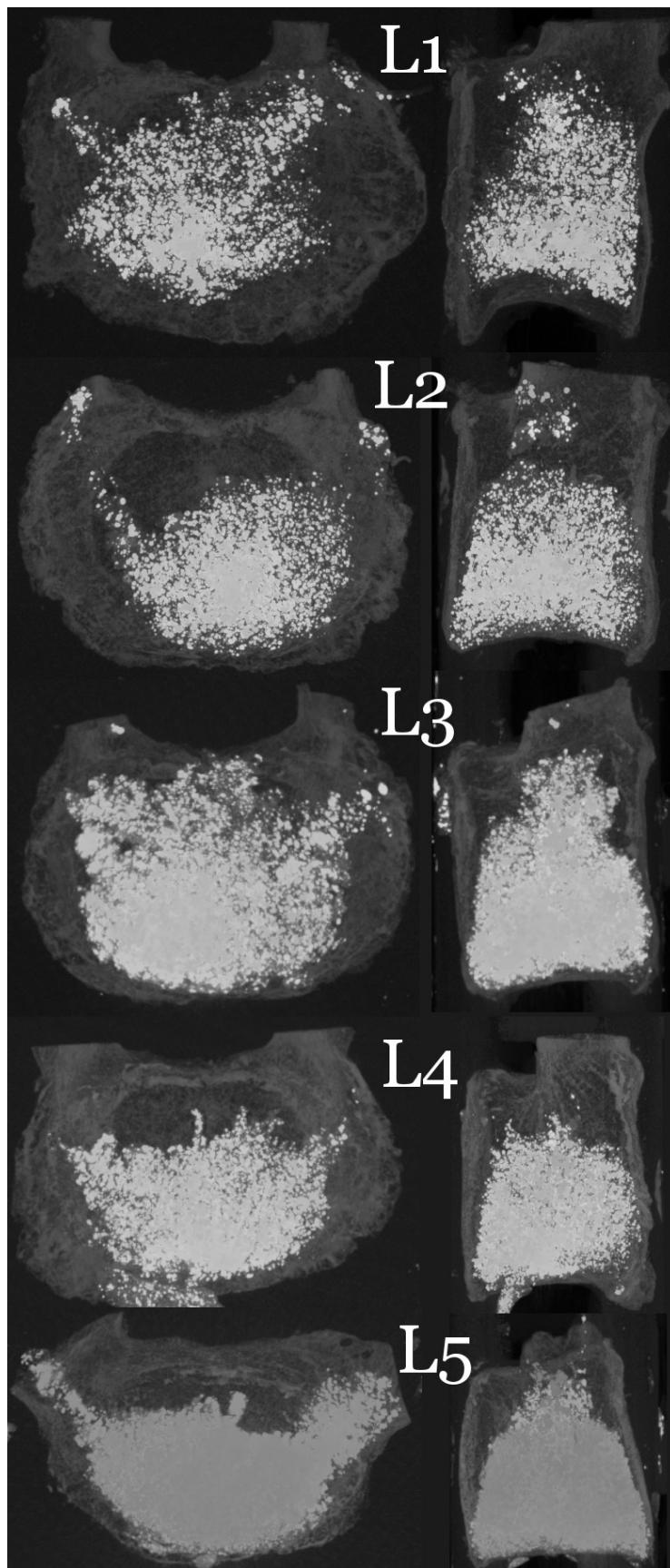


Figure 3.25: Transverse and sagittal 3D projection views of the Spine 1 spine following augmentation, with the cement region being the brighter material in the vertebral body. The L1 vertebra is defined as having a dispersed volume of cement while the remaining L2, L3, L4, L5 vertebrae have concentrated volumes of cement.

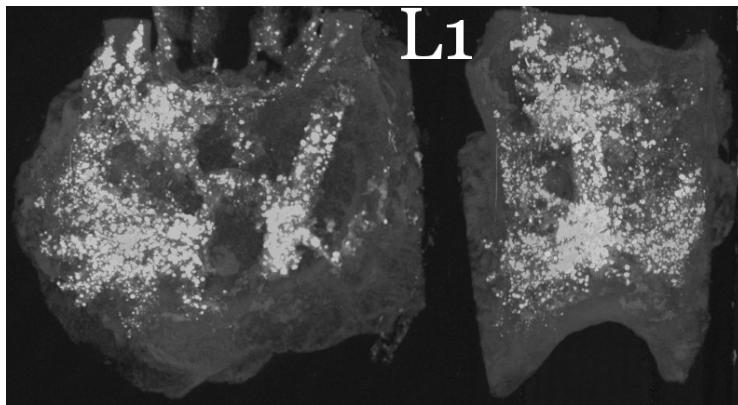


Figure 3.26: Transverse and sagittal 3D projection views of the Spine 2 spine following augmentation, with the cement region being the brighter material in the vertebral body. The vertebra is defined as having a dispersed volume of cement.

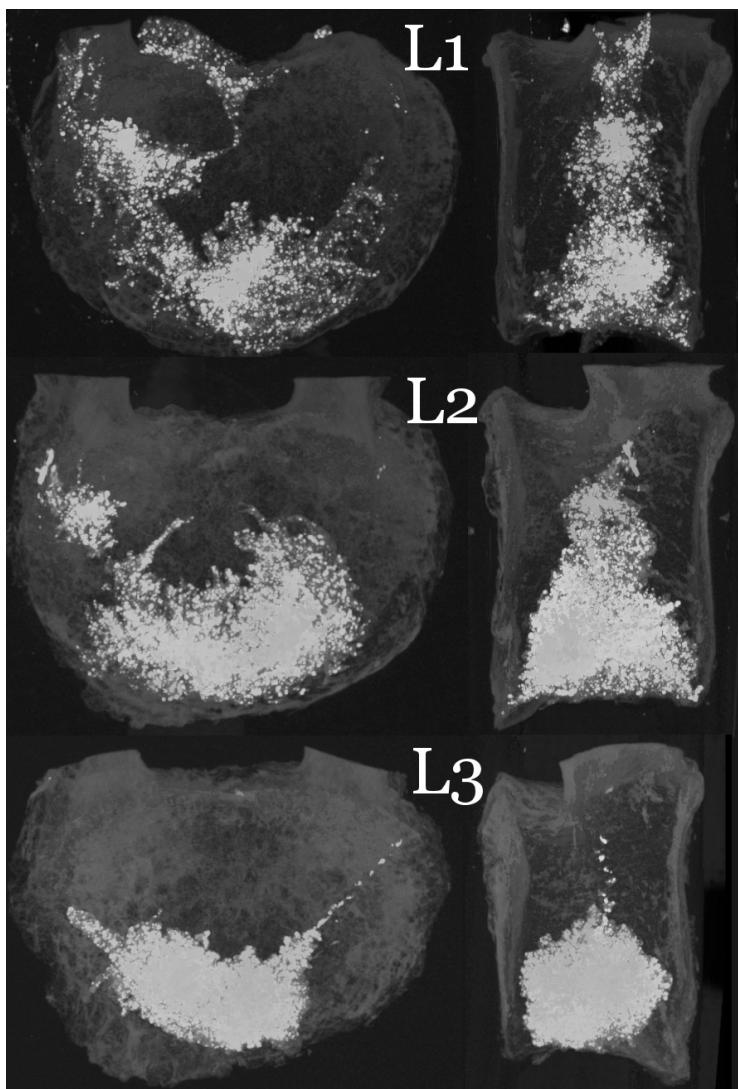


Figure 3.27: Transverse and sagittal 3D projection views of the Spine 3 spine following augmentation, with the cement region being the brighter material in the vertebral body. The L1 vertebra is defined as having a dispersed volume of cement while the remaining L2 and L3 vertebrae have concentrated volumes of cement.

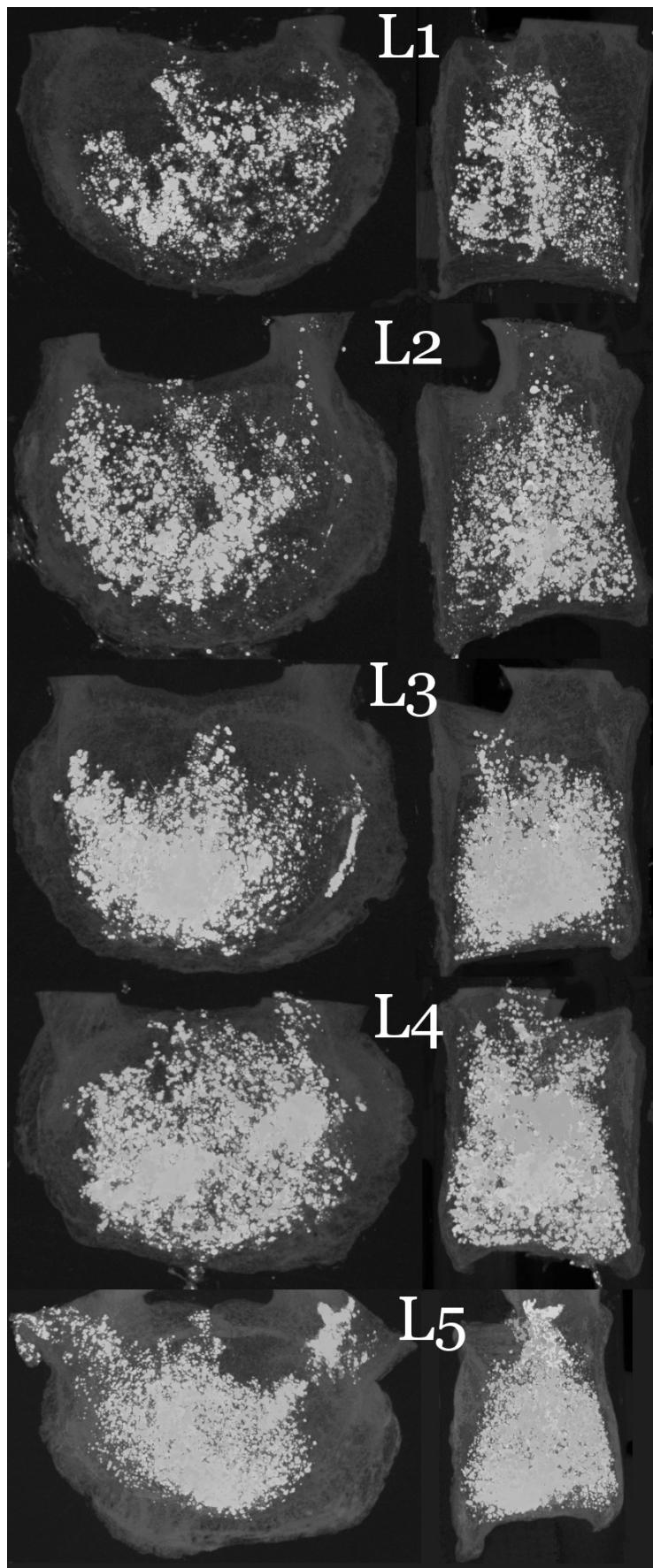


Figure 3.28: Transverse and sagittal 3D projection views of the Spine 4 spine following augmentation, with the cement region being the brighter material in the vertebral body. The L1, L2 and L5 vertebrae are defined as having a dispersed volume of cement while the remaining L3 and L4 vertebrae have concentrated volumes of cement.

Table 3.9: The characterisation of the augmented vertebrae into vertebrae with dispersed and concentrated volumes of cement.

Vertebra	Cement Distribution
Spine 1 L1	Dispersed
Spine 1 L2	Concentrated
Spine 1 L3	Concentrated
Spine 1 L4	Concentrated
Spine 1 L5	Concentrated
Spine 2 L1	Dispersed
Spine 3 L1	Dispersed
Spine 3 L2	Concentrated
Spine 3 L3	Concentrated
Spine 4 L1	Dispersed
Spine 4 L2	Dispersed
Spine 4 L3	Concentrated
Spine 4 L4	Concentrated
Spine 4 L5	Dispersed

### 3.4.2 Computational Results

#### 3.4.2.1 Non-augmented Model Results

The results of modelling the non-augmented vertebrae can be seen in fig. 3.29, comparing the initial normal method (the method used with the bovine tail vertebra in the previous chapter) with the best case using the bone volume fraction method and the results of the sensitivity test described previously. The results show a large improvement using the results of the sensitivity tests and the bone volume fraction method, with a concordance correlation coefficient improving from 0.55 to 0.86.

The effect of using the bone volume fraction method on the greyscale background and colour map of the bone density can be seen in fig. 3.30, where the much more clearly defined cortical shell and trabecular structure is evident.

The varying greyscale distribution and differences between the different spines can be seen in fig. 3.31. The general trends match the overall bone volume fraction values described earlier in table 3.7, where the vertebrae from spine 1 show much lower bone volume fractions which matches the much more blue heat maps when compared to the denser spine 2, 3 and 4.

#### 3.4.2.2 Augmented Model Results

The optimum results using the image registration and outcomes of the sensitivity tests, including the explicitly defined needle tracks can be seen in fig. 3.32 with the green

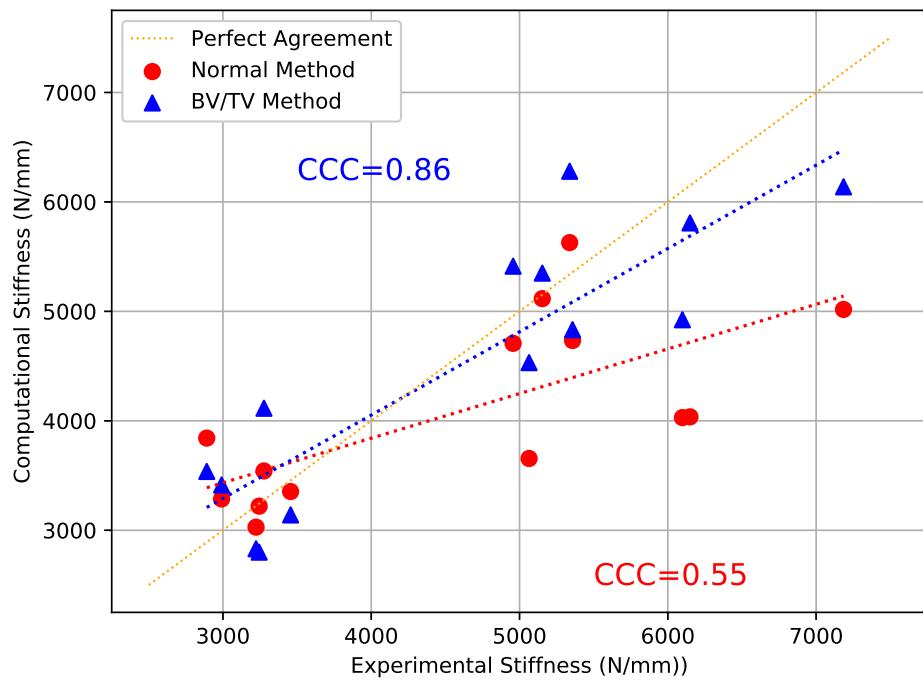


Figure 3.29: The results of using the normal method and the bone volume fraction method to model non-augmented human lumbar vertebrae. Red shows the agreement using the normal method and blue shows the agreement using the bone volume fraction method, with the orange dotted line showing perfect agreement.

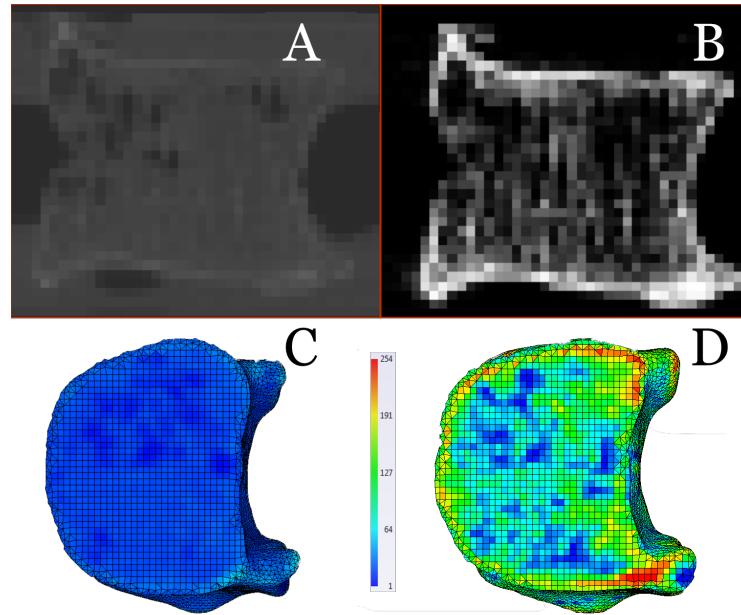


Figure 3.30: A and B: The resultant  $1 \text{ mm}^3$  greyscale background from the normal and bone volume fraction method respectively, where the brightness in A has been increased for visibility. C and D: a heat map of the greyscale values through the mid slice of models from the normal and bone volume fraction method respectively.

triangles. This registration method with the defined needle tracks achieved a  $\text{CCC} = 0.62$ , the registration method not using the needle tracks achieved a  $\text{CCC} = 0.46$ , while the initial method used (similar to the method used with the bovine tail vertebrae) achieved a

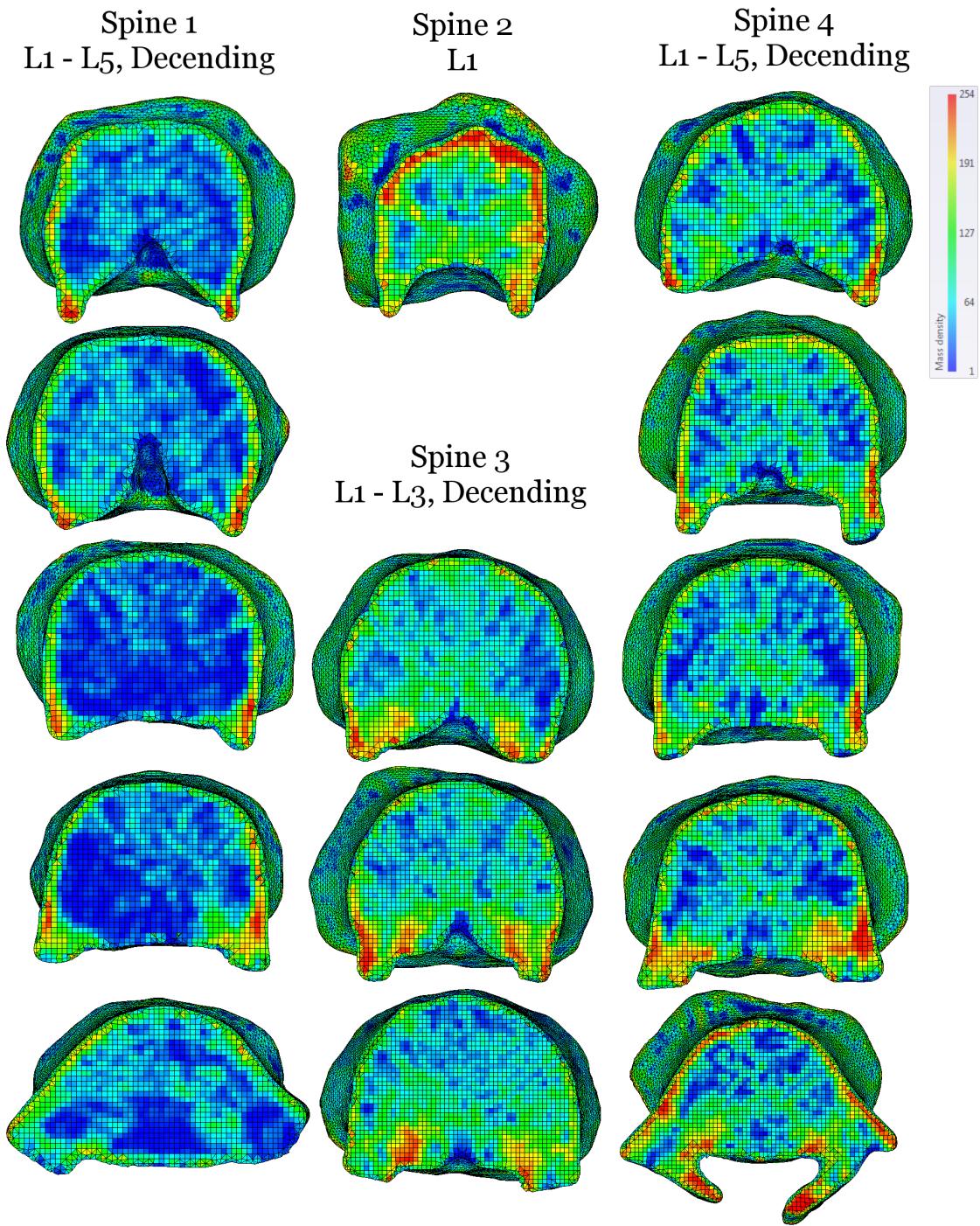


Figure 3.31: The variation in the greyscale distribution across the mid-slice of the vertebrae from spine 1, 2, 3 and 4. The general density changes as well as shifting density distributions are visible.

CCC of 0.18. Comparing the method using the registration method to the method using the registration method with defined needle tracks, computationally stiffer vertebrae were weakened and computationally weaker vertebrae were stiffened due to the higher Young's modulus for the interface and cement regions.

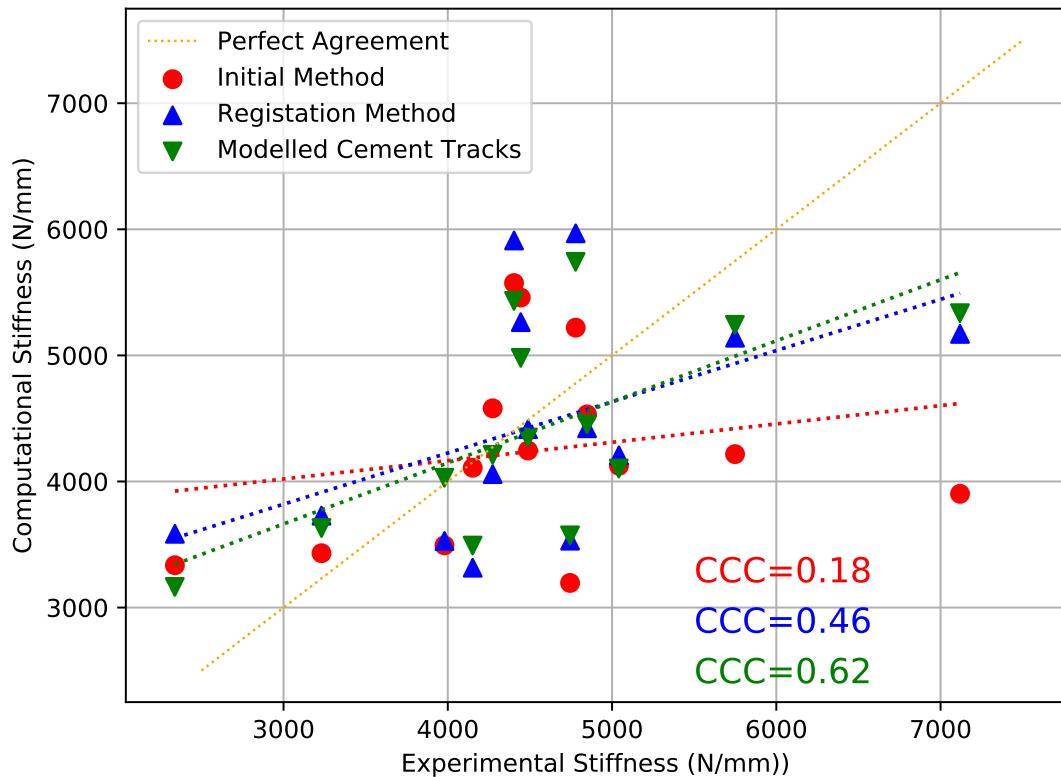


Figure 3.32: The results of using the initial method (red circles), the registration method (blue triangles) and using the defined needle tracks (green triangles), showing the agreement to the perfect  $x=y$  line in orange.

## 3.5 Discussion

The outcomes of this human vertebrae study are discussed in the following subsection. Split into three, discussing the experimental results, limitations and finally the results of the computational aspects of the study.

### 3.5.1 Experimental Results

Experimentally there was large variation seen in the results, in terms of material properties (BV/TV values), geometry and response to loading. The experimental response to loading showed a large range in the stiffness values of the vertebrae, even for vertebrae with similar volumes and for vertebrae originating from the same spine. This wide range of stiffness extends to the augmented vertebral stiffness, although the range does decrease following augmentation. The variation seen in the intact vertebrae aids the justification for the study, if such a wide range of vertebral properties exists within such a small data set then it explains why such variation is found clinically when identifying the response to vertebroplasty. For example in some of the randomised clinical trials were no statistical significance in the

output measures could be found and in studies of the epidemiology of vertebral fractures [10, 18, 91]. Some of the variation in the stiffness of the non-augmented vertebrae may be due to the different curvatures in the spines of people. These different curvatures will lead to different loads through the same vertebral level in different people and may explain why little differentiation between spinal level can be made. The different loading regime at the same level means that the density distribution within the vertebrae varies and hence to optimum location for the injected cement volumes would also vary. This idea of spinal level, varying loads and vertebral density is explored further in section 4.4.4.

Following augmentation five of the 14 vertebrae showed an increase in the stiffness, which, given the stiffness of the injected cement compared to that of trabecular bone, is an unexpectedly small number. However, this is not entirely unexpected, with a similar range of increases and reductions seen in the study by Wijayathunga et al. [38] and no statistical difference in the studies by Kinzl et al. [60, 72, 92] unless the cement distribution was distributed to both of the endplates, forming a column of cement from the superior to the inferior. Four of the vertebrae that showed an increase in stiffness were from the same spine (Spine 1), which is the spine that had a considerably smaller bone volume fraction compared to the other vertebra from other spines. Given that this spine had the smallest bone volume fraction it also received the largest quantity of cement, given the relationship between the percentage fill achieved and the bone volume fraction. This relationship is most likely due to the ease of cement injection before leakage, with more dense vertebrae failing to receive large volumes of cement before the cement found one of the vascular channels (upon which injection was stopped) and less dense vertebrae having more space to receive cement. So, the reduced BV/TV and therefore density of Spine 1 allowed both larger volumes of cement to be injected and due to its reduced density was more receptive to having its stiffness increased through augmentation. This may suggest that these type of vertebrae are the best candidates for the procedure given the risks of damage through the high intra-vertebral pressures that can be generated [86, 93]. In cases where the vertebral density is high, but high fill volumes are still pursued damage may be caused by the high pressures “pushing” trabeculae to the side. Interestingly and converse to findings presented here, the study by Aquarius et al. [86] suggested that cement volumes like those described here as concentrated were caused by high pressures “pushing” and damaging trabeculae. The more dispersed distributions gave more interdigititation due to the lower pressures and therefore resulted in reduced damage and stiffer augmented vertebrae. However, it may be the case that these dispersed and concentrated volumes described here are a different phenomenon to the ball shaped and irregular shaped cement distributions described in that

study. A potentially worrying consequence of the high pressures during the injection is the filter pressing that can occur [39], here, separation of the radio-opacifier from the cement is possible, meaning that experimentally and clinically (through fluoroscopy) the extent of the injected cement volume is potentially unknown. Additionally from a modelling perspective, a potential separation of the liquid and powder components of the PMMA may result in changing material properties of the cement region.

Cement volume positions were generally to the anterior of the vertebrae and to the middle of the inferior-superior plane, matching the desired position [24] achieved through the insertion of the needle and angling of the side opening needle tip. Given the lack of obvious variation in cement positions and shapes it was difficult to characterise the cement distributions, hence, a simplified description of the cement was used. This simplified description of the cement described whether the cement was in a concentrated volume or dispersed in a larger region or whole vertebra. Following this characterisation strong relationships were found between the change in stiffness and percentage fill, if only those vertebrae with a concentrated volume of cement were included. Suggesting that distributed volumes of cement are difficult to predict and should be avoided when carrying out the procedure using fluoroscopy, especially with more dense vertebrae where the likelihood or disperse volumes of cement increased. Many previous studies only found significant increases in the stiffness of augmented vertebrae when the cement distribution was endplate to endplate stretching from the superior to the inferior of the vertebral body [68, 86, 87]. The sagittal views of the augmented vertebral projections suggest that all vertebrae except Spine 2 L1 and Spine 3 L1 achieved such end-to-end distributions with no noticeable difference in the change in stiffness of these two vertebrae, especially given that the Spine 2 L1 vertebrae received a large increase in stiffness following vertebroplasty..

To summarise the change in stiffness following augmentation based on the material properties of the vertebrae, the following features have the greatest effect:

1. A smaller bone volume fraction results in larger quantities of cement being injected before leakage occurs.
2. If the volume of cement is contained in a concentrated volume then the greater the volume of cement then the larger the increase in stiffness following augmentation.
3. If the volume of cement is dispersed through the vertebral body then there is no relationship between the volume of cement injected and its effect of the vertebral stiffness.
4. Concentrated volumes of cement are more likely if the bone volume fraction of the

vertebra is lower (and therefore has a reduced density).

The effects of vertebral geometry and material properties on the response to augmentation will be investigated further using statistical shape modelling in chapter 4, giving a more detailed story of the suggested approaches to vertebroplasty based on the tests carried out in this study.

### 3.5.2 Limitations Regarding Specimen Numbers & Vertebral Features

One of the main limitations to the study is the numbers of vertebrae included in the set. Having four human spines with a limited number of lumbar vertebrae available from each spine, meant that only 14 out of a possible 20 vertebrae were able to be tested. This meant that there was a skew towards the top of the lumbar section with limited numbers of L4 and L5 vertebrae. Such skews to the data set have effects to any statistics applied to the data set and will be discussed more thoroughly in the chapter on Statistical Shape and Appearance modelling, section 4.4. More relevant to modelling the vertebrae is the effect this has on the determination and optimisation of the greyscale conversion factor. The large change in geometry from L4 to L5, rather than the gradual change between L1 to L4, introduces questions about the response to loading (and augmentation) for this vertebra in particular and how it differs from other levels. A resolution to this limitation would be to increase the specimen numbers and look at vertebral levels in isolation; identifying level specific differences and properties. Variation at different vertebral levels may require level specific greyscale conversion factors, such as those required when modelling different animal species [79]. However, within the current set of vertebrae greater variation was found between spine rather than level (for BV/TV, stiffness and vertebral body volume), even when including L5 vertebrae. Suggesting that segregation of vertebral levels is unnecessary for the current specimen set.

Another limitation of the study is the age range and limited information regarding vertebral health. Because of the unknown vertebral quality or health it was decided to skip the initial load to failure carried out in the bovine tail study. While no evidence of fractures could be seen in the  $\mu$ CT scans, other than slight wedge shapes, there was also no evidence of the bovine tail vertebrae having succumbed to fracture in  $\mu$ CT either, despite clear fractures on load displacement curves. Therefore the state of the vertebrae was relatively unknown in their pre-augmented state and the study therefore becomes an investigation into the effects of prophylactic vertebroplasty similar to a number of previous studies [40, 94, 95], although with the possibility that some of the vertebrae were fractured *in vivo*.

### 3.5.3 Computational Results

Many developments in the computational methods have been made through the course of this chapter, with the resulting improvements showing their importance. The significance of these developments and the results is discussed in the following subsections, split into a discussion of the improvements to modelling non-augmented vertebrae, augmented vertebrae and the results of various sensitivity studies.

#### 3.5.3.1 Non-augmented Models

The improvement in the agreement between computational stiffness and the experimental stiffness results using the bone volume fraction method and the results of the sensitivity tests is significant and provides a good foundation for modelling the more challenging augmented models. The improvement using the bone volume fraction method in isolation (without the results of the other sensitivity tests) showed a large improvement over the normal method. The normal method performed similarly on the bovine tail vertebrae as with the human lumbar vertebrae, with a CCC = 0.49 for bovine tail vertebrae and CCC = 0.55 for the human vertebrae.

The small improved agreement of modelling the human vertebrae over the bovine vertebrae when using the same “normal” method suggests that either the human vertebrae are more receptive to the modelling method used, or that the experimental procedure was more repeatable and therefore provided more accurate results. One possibility is that the less narrow human vertebrae provided an easier material to load axially, with slight off axis loads causing the vertebrae to not be seated in the endcaps correctly in the case of the bovine tail vertebrae. This sensitivity to endcap contact properties was shown earlier and given the tendency of the bovine vertebrae to be loaded non-axially (due to their narrow columnar shape) they may be more sensitive to such endcap contact properties. So, while experimentally the bovine vertebrae were able to slip in the endcaps, computationally the two materials were tied, restricting this ability and reducing the agreement with the experiment. Conversely, the wider human vertebrae had less of a tendency to slip and were less sensitive to the endcap contact. This change to the endcap contacts seems to be a common transition from similar studies where tied contacts were used [38] to more recent studies [72, 92], however the property is rarely presented in the literature.

The improvement using the bone volume fraction method is most likely due to the added definition of the trabecular bone and cortical shell, especially given how important the correct representation of load sharing is for accurate models [96]. This agreement is much

stronger than the agreement found in similar studies that used a comparable methodology to the “normal” method [38, 56, 79] and comparable to methods that used more complex although individual material properties for each model [60, 92]. An advantage the current study has over these latter studies is a uniform material property that once calibrated over a large set of vertebrae can be used on any unseen human lumbar vertebrae. Having greater definition of the cortical shell and trabecular bone alignment allows much more accurate descriptions of the load transfer through the vertebrae, rather than the more simple description with the more homogenised material properties of the normal method.

This method also removed any effect that the bone marrow, where, given the freeze/thaw cycles the marrow leaks from the vertebrae giving vertebral scans with portions of the bone marrow missing and therefore changing the greyscale background and material properties. Due to the initial segmentation and binarisation at  $82\ \mu\text{m}$  using the BV/TV method the bone marrow is not present in the segmented full resolution or downsampled scans and therefore has no impact on the material properties of the models. Conversely, using the normal method, areas lacking bone marrow would have a lower Young’s modulus and areas with bone marrow would have higher Young’s moduli, not corresponding to the actual properties of these regions and changing the load distribution.

One of the limitations of the bone volume fraction method is that it relies on having trabecular resolution scans of the vertebrae to apply the trabecular bone thresholds to. This is a similar limitation to studies that also achieved a good agreement between computational and experimental results of augmented stiffness [92], where high resolution  $\mu\text{CT}$  scans were required for the acquisition of BV/TV and fabric information for their methodology. This limits the origin of the scans to *in vitro* scans rather than *in vivo* scans where the standard clinical resolution is limited to approximately 1 mm and larger. Given the intention to generate larger populations of vertebra models for use in statistical shape modelling this limit to scan origin is an unwanted consequence. A possible solution to this problem would be to use 16 bit images rather than the currently used 8 bit images. This change gives an increase in the number of greyscale values available from the 256 of 8-bit images to over 65,000 for 16-bit images. The main benefit of the bone volume fraction method is the increased definition of bone structure and a greater contrast between the brighter, denser cortical bone, the trabecular bone and the empty, non-bone areas. Using 16-bit images along with image manipulation to change the contrast of the scans may allow the added detail and contrast to be captured with relatively low ( $\geq 1\ \text{mm}$ ) resolution scans, therefore greatly increasing the number of vertebral specimens available for use. An example of how this could be achieved is shown in fig. 3.33 where the background

from the normal method has been edited through adjusting the contrast to give a similar background to that achieved using the bone volume fraction method. The detail in the centre of the vertebral body is less clear in this example, however, it was achieved through simple contrast manipulation of the 8 bit TIFF stack, meaning that more trabecular detail could be preserved using a curves (remapping of the image tonality) and/or as already proposed, 16 bit images.

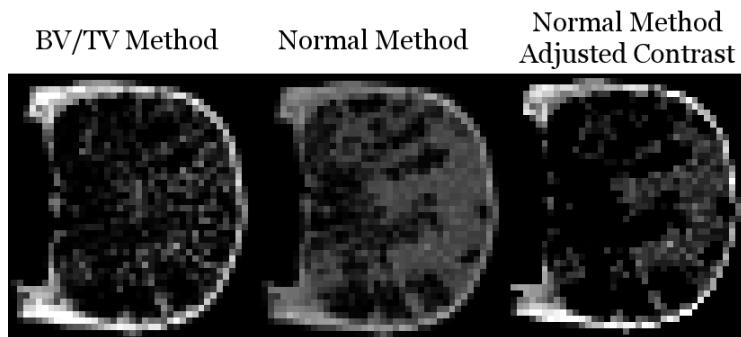


Figure 3.33: An example showing the ability to create a greyscale background similar to that achieved using the BV/TV method, but instead adjusting the contrast of the background from the normal method.

### 3.5.3.2 Augmented Models

The results of modelling augmented vertebrae showed a reduction in the agreement when compared to the non-augmented vertebral models, mirroring that found by Wijayathunga et al. [38]. Reasons for this are centred around modelling the internal cement region, given the good agreement seen between the non-augmented vertebrae and their models. More specifically the problems in modelling the cement region may be due to experimental and modelling techniques.

Issues originating from the experimental work come from the difficulty in capturing the extent of the injected cement volume, often due to clumping of the barium sulphate and separation of the barium sulphate from the other components of the PMMA cement. The clumping of barium sulphate was also found by Sikora [73], in this study agglomeration was reduced through vigorous mixing of the PMMA monomer and barium sulphate prior to mixing with the PMMA powder. However, others suggested that the separation of the barium sulphate from the cement (calcium phosphate in that study [39]) during the high pressures of the injection were the cause of the subsequent agglomeration. While this problem is minimised through segmentation of the cement region at higher resolutions before the downsampling, a problem still lies in capturing the intricate interdigitation between the cement and the trabecular bone at a resolution of 1 mm. One issue overcome

through the use of the registration method is the removal of the bright halo of the cement region (from clumps of barium sulphate) solving the problems found in the previous chapter using bovine tail vertebrae and problems encountered by others [38, 73]. This allowed more accurate modelling of the material properties of the vertebral bone and additionally better accuracy of modelling the interface, given the removal of the false, dense bone surrounding the yielding interface in the bovine tail models. The inclusion of the explicitly modelled needle tracks increased the agreement significantly, with the compromise of interrupting an otherwise automated modelling process.

An additional experimental challenge is the unknown level of damage caused to the vertebrae when the needle is inserted. Given that after clear fractures (based on load-displacement curves), damage could not be seen on  $82\text{ }\mu\text{m}$  scans of bovine tail vertebrae, it is unlikely that micro-fractures caused through needle insertion will be captured in the  $\mu\text{CT}$  scans of the human vertebrae. Further tests could investigate whether a change to the Young's modulus as a function of the density in the areas surrounding the needle tracks would improve the agreement. This could represent either damage to the bone in the form of micro-fractures or the compacted bone created by the needle.

Despite the reduced agreement of the augmented models, there was a large improvement compared to the initial method, which was the method used for modelling augmentation in the bovine tail vertebrae. As with the non-augmented models the CCC using the initial method was very similar to the CCC using the comparable method on the bovine tail vertebrae, CCC = 0.18 and 0.15 for the human and bovine models respectively. This makes the improvement using the registration significant and a beneficial step in making the models of augmented vertebrae.

Achieving improved agreement between the computation and experimental models is an obvious next step for the project and despite the range of approaches used to improve the agreement, there are some next steps. Given the difficulty capturing the detail between the cement and trabecular bone, using a higher resolution is a clear next step. However, it comes with a number of difficulties which have been shown in the study by Zhao et al. [69], where the increase in resolution presents many other unknowns that need to be modelled. For example modelling the specific interaction between the bone and the cement including the coefficient of friction between them. This would require difficult experimental investigations, given the unique environment inside the vertebrae filled with bone marrow. Along with modelling properties that are not applicable in continuum level models, there is the problem with computational cost, where the increased time to solve models would become problematic given the investigatory nature of the study and the fact that the

behaviour in simplified bone plug models is different to what is seen in whole vertebrae [74]. Perhaps the methods used by Kinzl et al. [92] would form a middle ground between the two approaches. In that study, spheres were randomly inserted into the augmentation region to represent the pores that are present, although not visible in the augmented regions of the experimentally augmented specimens. This methodology is similar to one of the approaches attempted in the current study which unfortunately performed less favourably than the currently presented approach. It involved an inverse greyscale material property for the augmented region based on the underlying non-augmented background, where empty (marrow containing) voxels were given material properties of, or close to PMMA, voxels that contained trabecular bone were given the material properties of bone and intermediate greyscale values attempted to represent the gaps that form as the cement shrinks during setting. This methodology and preliminary results can be seen in section A.1.

### 3.5.3.3 Sensitivity Test Significance and Influence on Errors

Sources of error from modelling come from discrepancies between the experimental setup and specimen geometry and material properties. Sensitivity tests carried out identified the effect of errors in accurately describing the cement cap depth and loading position accuracy, given the 1 mm accuracy limit. The maximum possible error for load position in a  $\pm 1$  mm anterior/posterior/left/right direction was less than 5%, with the worst case error for the for the encap depth tests (1 mm thicker for both endcaps) being approximately 5%. Other possible errors would include accurately capturing the model geometry, however simply eroding or dilating the vertebral mesh would not accurately describe the type of meshing errors that may occur (it is unlikely that masks would be created at  $\pm 1$  voxel around the whole model). To attempt to answer this a user variability test was carried out in section 2.3.4.5. There, the maximum user variability gave errors of 14 %, however as discussed in that chapter, users achieved consistently higher or lower stiffness' compared to their peers. Hence, a 14 % error within a single users segmentation process is both unlikely and further reduced through the use of the python script carrying out the thresholding and morphological filters to segment the model. Therefore simply adding the two main sources of error gives a worst case error of approximately 10 %, an error which when compared to the possible errors in obtaining the maximum stiffness and the errors between loading repeats, is negligible. The specific error in the experimental load is difficult to measure mainly due to the high value and limited supply of human tissue; to measure the error in repeated loads more accurately, these repeats would need to be taken in the non-augmented state given the large array of unknowns the augmentation process introduces. However,

this would have led to possible damage or unwanted fracture of the vertebrae, making the results following augmentation more difficult to interpret. As it stands the differences between repeats of the augmented vertebrae show changes of approximately -3000 N/mm to +1200 N/mm, with the large reductions originating from repeated testing in plastic regions of the load displacement curve. These large errors between repeated measures are the worst case however and it is unlikely that such errors would occur between non-augmented specimens in a loading range that avoids the potential of causing damage. Suggesting that the results presented here, being the consequence of 2 loads total (one non-augmented, one augmented), have much less error than that seen in the repeated loads.

In addition to error in measuring the stiffness, errors in the measurement of the maximum stiffness also exist due to the cut off at 1600 N in the experimental loading. This meant that for some of the vertebrae the maximum stiffness was not reached and therefore not captured in the load displacement curve. A prediction of the failure stress and an estimation of the failure load through simulation of a vertebra prior to experimental loading could help to remove this problem. However, this would have required yet another set of human vertebrae.

Changing the endcap depth presents an interesting study into the effects of over constraining the models. For the models with the tied constraints changing the endcap depth had a different effect for the two vertebrae (although the same overall trend, where thicker endcaps led to more constraint and therefore higher stiffness values). The spine 1 L2 vertebrae was equally sensitive to changing the superior and inferior depth, although gave a smaller effect when the depth was reduced (exposing more bone). The spine 4 L5 vertebrae was much more sensitive to changing the inferior endcap, especially when reducing the depth of the endcap. This large reduction in the stiffness, when removing 3 mm of endcap material from the inferior endcap, of approximately 20 % is caused by exposing a less dense area of bone, which, when no longer supported by the tied endcap resulted in the reduced stiffness. Other than this specific effect the general trend was an increased sensitivity to increasing the cement depth, with a much smaller sensitivity to exposing more bone.

Changing the endcap depths when the frictionless contact was used resulted in (for the most part) much less sensitivity to changing the endcap depth, when compared to the tied endcap models. The exception is the spine 4 L5 vertebra, where when the endcap depth is reduced a very large decrease in the stiffness is seen. This is caused by slipping that occurs between the vertebrae and the endcap, given the lack of both physical constraint and constraint in the form of a boundary condition. An illustration of this can be seen in fig. 3.34, showing that with such little constraint the anterior inferior of the vertebral

body moves further to the right (anterior). This results in the reduced stiffness recorded. However, such small endcaps were not created experimentally and therefore create no additional errors to the models. Importantly, the use of frictionless contact with the “no separation after contact” option set results in smaller sensitivity to endcap depth modelling errors and resulted in increased agreement between experiment and model for the whole set of 14 vertebrae.

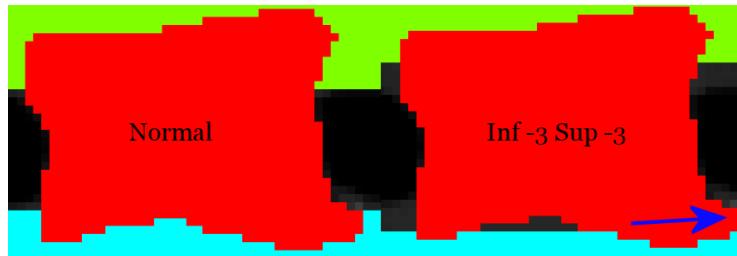


Figure 3.34: An illustration of the slipping that occurs in Spine 4 L5 when the endcap depth is reduced by 3 mm on the superior and inferior endcaps

The effect of changing the loading position aided the understanding of the mechanics of the models and their response to loading. Experimenting with different loading positions allows development of our understanding of the response to different natural loading conditions that would be experienced during daily life. This could help to answer the important question of how vertebroplasty effects adjacent level loading and how it may effect the chances of adjacent level fracture. However, these investigations have been carried out in chapter 4 where the response to loading following augmentation was investigated and, given the more systematic nature of the generated models, allowed for an easier interpretation of the results. Here, the response to loading outside of the  $\pm 1$  mm error range follows a mostly expected pattern with loads anterior, posterior, left and right at  $\geq 10$  mm away from the central loading position resulting in progressively reducing stiffness. The reduced material beneath the axial loading point explains most of these results, with the greater reduction when loaded anteriorly being due to the generally reduced density of the anterior portion. The smaller reduction in the stiffness when loaded posteriorly is due to the increased density which was in the posterior region of most of the vertebrae, which was seen in the greyscale density maps of the set. The anomalous result is the Spine 3 L2 vertebra, where posterior loading of 10 mm behind the central loading position resulted in an uncharacteristic increase in the measured stiffness. The Spine 3 L2 vertebrae had particularly degenerated superior and inferior endplates, protruding anteriorly at both ends, but with little protrusion posteriorly. This meant that when measuring the central loading position experimentally, a loading point was selected further anterior than what would have been picked without the bone growths. This explains why moving the loading

position further to the posterior resulted in an increased stiffness with respect to the central loading point, given that the central loading point was actually placed anteriorly and hence had a smaller stiffness than expected. This presents another reason for why carrying out load position tests on the generated models in chapter 4 is preferred, there, central loading can be ensured and the requirement to match the experimental loading position is removed.

### 3.6 Conclusion

Overall the models produced here can estimate the stiffness of non-augmented human lumbar vertebrae to a very high degree. The prediction abilities of models of vertebroplasty is reduced, although a large improvement over studies that used similar approaches and had similar constraints in mind (clinical resolutions for scans etc.). Importantly, the models can represent the large range of outcomes from the augmentation process, suggesting that the representation of augmentation is robust enough to model and experiment with different augmentation scenarios. Therefore providing a good starting point to use statistical shape and appearance modelling to understand the intricacies of vertebroplasty.

# Chapter 4

## Statistical Shape & Appearance Modelling

### 4.1 Introduction

Statistical shape and appearance models give the opportunity to investigate the consequences of variation in a dataset that otherwise would be difficult to isolate or obtain enough experimental specimens to find trends in the data. The effect of the anterior height of the vertebral body on the response to loading is a simple example of this. In this example, to understand the effect of anterior vertebral height experimentally, or computationally using specimen specific models, a large range of vertebrae with varying anterior heights would be required which would hopefully represent (without gaps) the range of anterior heights in the population. Even if this could be achieved, confounding factors and other variation would make the presentation of specific relationships difficult. Using statistical shape and appearance models with principal component analysis (PCA), the modes of variation can be characterised and isolated, allowing an understanding of how specific modes of variation affect the chosen measure. A caveat here (similar to specimen specific models, but potentially less obvious) is that the modes of variation are specific to the input set, the models used to make the statistical shape models. Hence, any estimations of the types of variation and the effects these modes of variations have is specific to that set of models and not necessarily applicable to the population on the whole.

#### 4.1.1 Aims of Statistical Shape & Appearance Models

The general aims of any statistical shape and appearance model are to describe the geometric and material property variation across a sample population. This is usually carried out by comparing the mean on the sample group to the main modes of variation found within it [76]. Such approaches have been used to characterise shape variation in the cervical spine [97], pelvis [98] and femur [99, 100]. Like this study, others have used statistical shape and appearance models to identify the variation in the lumbar spine for both spinal curvature variation [101, 102, 103] and to identify the variation in single vertebrae [76, 104]. Regardless of the bone in question in these studies, the aim is most often to determine the mean, which dependant on the population sample can be described as the population norm and then to understand how variations effect the outcomes of different treatments.

This chapter focusses on using the 14 human lumbar vertebra FE model from the previous chapter as the input set to create a statistical shape and appearance model based upon them. Specifically, this chapter describes the methods used to create the statistical models and aims to find the main modes of variation found within the input set. These modes of variation are then validated, ensuring the variation found in generated models based on the statistical shape model are within the realms of possibility, given the input set they are created from. Finally the generated models are artificially augmented, using the results of the previous chapter, in order to start to understand how material and geometric properties of vertebrae effect the outcomes of vertebroplasty.

#### 4.1.2 General Methodology

Generally statistical shape and appearance models start with the segmentation and creation of models that form the input set of the statistical model. Following this is a rigid registration step, where rotations and translations are applied to all meshes or models that form the input data set so that they share a common coordinate system. Methods of performing the rigid registration often use an automated approach where certain degrees of freedom are restricted to ensure registration is achieved. For example with very cylindrical vertebrae, if rotation is allowed around the coronal axis with vertebrae who's volume varies significantly, registration may never be achieved as one vertebrae would fit inside the other and rotate without end. Manual techniques can be used similar to that used in the previous chapter with pre and post augmentation scans, with automated rigid registration techniques also using landmark registration.

A mean model is usually generated by first selecting a surface mesh from the input set and registering it to the other models (surface meshes) of the input set using deformable registration, a mean model is calculated from these transformations. Each of the other vertebrae are then selected and registered to the other models from the input set until the change between generated mean vertebrae is no longer significant (described in great detail by Clogenson et al. [76]. Once the mean model has been created the transformations required to deform each input model into that mean are recorded as the variation from the mean shape.

Given the range of variation captured in those transformations from the mean to each input specimen a method of dimensional reduction is usually employed, commonly either PCA [76] or Single Value Decomposition [105]. This allows the reduction of the number of random variables being identified, allowing a focus on those that contain or describe the largest variations.

## 4.2 Methods

A plugin for Simpleware ScanIP was developed through a collaboration between the University of Leeds and Simpleware (Synopsis). The tool utilises the Insight Tool Kit (ITK) to generate a SSAM model based on an input set of finite element models created in Simpleware ScanIP. These models are the non-augmented models described in the previous chapter using the bone volume fraction methodology. The process of using the plugin with the 14 human lumbar vertebrae as the input set is described in this section.

### 4.2.1 Statistical Shape and Appearance Model Creation

The creation of the SSAM through the use of the plugin is carried out in five main steps. The first of these steps is a pre-processing step, converting the masks and backgrounds into necessary formats (.mha & .mhd) for use with the ITK toolkit.

The following step carries out rigid registration of the models, aligning the masks and backgrounds to a shared coordinate system. This is carried out using the ITK library with the registration being measured according to a mean squared image-to-image metric using a gradient descent optimiser. A limit to the number of attempts or steps allowed can be set; the default value of 100 steps for each input model was used.

The geometry of each input specimen was described in a deformable registration step, measuring the transform required to morph the mean of the input vertebrae onto each of

the input vertebrae. This step utilises the ITK FEM registration filter.

Penultimately, the transforms between the mean and each of the input vertebrae which describe the vertebral geometries are used as inputs for PCA. Here the outputs of the step include the principal components, their eigenvalue, percentage of variation captured in that component and the cumulative percentage variation captured.

Finally, the SSAM produced can be used with the ITK Image Warp filter to generate new mask and background combinations from within the envelope of geometric and material property variation created by the input set, according to the principal components. The plugin allows for the first five principal components (PC1, PC2, PC3, PC4 & PC5) to be used for as variables for model generation, altering the value of the principal components by up to three standard deviations away from the mean in both positive and negative directions.

## 4.2.2 Generating Vertebrae Models

### 4.2.2.1 Range of Shapes Generated

To attempt to understand what each of the principal components represented in terms of the variation captured by it, models were created at  $\pm 1$ ,  $\pm 2$  and  $\pm 3$  standard deviations away from the mean for the first three principal components independently. In addition to these, the mean model was generated, allowing comparisons of the other generated models against it.

Finally, in order to know whether the range of geometries, material properties and resultant stiffnesses found in the input set was represented in the SSAM within the first three principal components, models were generated which incorporated the variation found in PC1, PC2 & PC3. These models would represent the corners of a cube who's axis would be PC1, 2 & 3 and who's origin would be the mean vertebra. If the majority of input models (68 %, representing the quantity of the population expected to fit within  $\pm 1$  SD of the mean for a normally distributed input set) fit within the limits created by a cube with side length from +1 to -1 SD along each axis for geometric measurements, greyscale background and resultant stiffness, then the variation of the input set will have been captured and represented by the SSAM.

#### 4.2.2.2 FE Model Setup

Once the vertebrae were generated using the plugin the rest of the FE model was set up. This included forming endcaps to mimic the experimental setup and how the input set was loaded. Endcaps were created programmatically within the ScanIP python scripting environment with a diameter of 90 mm, approximately equal to the diameter of the experimental endcaps, with a depth of 6 mm ensuring the superior and inferior tips of the vertebrae were captured with a minimum of 1 mm between the vertebra and end of the cement. The remaining properties for the FE model are identical to those used for the models of the human vertebra which became the inputs to the PCA plugin. This includes a tied interaction between the vertebrae and endcaps and material properties for the endcaps being: Young's modulus 2.45 GPa and Poissons's ratio of 0.3. Material properties for the vertebra used the same greyscale approach as in previous chapters with the Young's modulus for each element being:

$$E = GS \times \alpha$$

Where,  $GS$  is the greyscale value for the current element (between 0 and 255) and  $\alpha$  is the conversion factor. The conversion factor used has the same value used previously for the non-augmented set of vertebrae:  $\alpha = 0.0008184$ . Applying load to the models is carried out as in the previous chapter, with 1 mm of displacement applied to a loading point, with the reaction force being measured to obtain the stiffness. The loading point is found by finding the centre of the vertebral body in the middle slice axially and translating the point axially to the maximum height of the model, including endcaps. The load is then applied through a plate which is tied to the superior endcap.

#### 4.2.2.3 Augmentation in Generated Models

Augmented models, testing the effect of augmentation on different modes of vertebral variation, were created through the creation off masks within the vertebral body. These consisted of two masks, one for the cement region itself and one for the interface region. Two methods of creating and describing these masks were attempted, the first using the mean cement volume from the experimentally augmented vertebrae in the previous chapter and the second using a mask based on an eroded vertebral body mask.

The first method utilised the same PCA plugin for ScanIP, however the models used here were those of the augmented region in the post-augmentation models. Using the masks

of the augmented regions of the vertebrae as the input for the SSAM generation gave the mean augmented region volume achieved through experimental augmentation. This mean model was then converted into a surface mesh (an STL) where it could be scaled to represent different percentage fill volumes. Fill volume was measured using the approach described in section 3.3.6, to measure the volume of the generated vertebrae. Using the volume of the mean cement volume, the “current” percentage fill was calculated (dividing the cement region’s volume by that of the vertebrae in question). The desired augmentation volume was then selected. This was either 20, 35 or 50 percent fill, given the range of fill volumes achieved experimentally. The cement volume was then scaled by  $\sqrt[3]{\frac{\text{desired \% fill}}{\text{current \% fill}}}$  on each of its axis. This gave three fill volumes for each generated model which was positioned in the centre/anterior of the vertebral body, then converted to a mask. The mask was then duplicated and eroded by one pixel to give the yielding interface layer upon which the correct material properties were applied. While a uniform cement volume shape gives the most uniform of tests, it is unreasonable to expect such a wide variety of vertebrae to have the same shape of augmented region when augmented experimentally or clinically. An additional problem is that for vertebrae that were more elongated and narrow axially, for example PC1 +3, the mean cement volume when scaled to 35 and 50 % fill would not fit inside the vertebrae.

The solution to this problem was the second approach, where the mask of the vertebral body was used as the basis for the cement volume. Here, a copy of the vertebral mask for each generated models was made, a recursive Gaussian filter 5 pixels deep was applied and then it was converted to a surface. The same method used in the previous approach was used to scale the surface to the correct and desired fill volume (taking the current volume after the recursive Gaussian filter). Once the volume had been positioned, the same process of creating the interface layer was used and models of 20, 35 and 50 percentage fill augmented models were generated.

This isn’t the perfect solution as again it is unreasonable to expect that every vertebrae receives a volume of cement that matches its own shape, it does however remove problems with the cement region extending outside of the vertebrae. Perhaps an improved method for fitting the cement volumes would be to use the mean cement volume but transform it using the same transforms that were applied to each generated vertebrae turning it from the mean vertebrae. The current version of the plugin does not allow access to these transforms however. Despite this, changing shapes and volumes of the augmented region would be the subject of any further parametric analysis, given that an optimum fill percentage and shaped would need to be found.

### 4.2.3 Measuring Vertebral Geometry

Vertebral volume or the vertebral body volume may be the easiest and most obvious measure of geometric change within a set of vertebra. It has been shown in chapter 3 that there is a strong correlation between vertebral size and stiffness and so this may be enough for a range of comparisons between spines and individual vertebrae. However, the input set of vertebrae contain a wide range of variation which can be seen visually, which may play an important role in the effect of cement augmentation and is another method of validating the outputs from the PCA generated set of models.

Measuring vertebral geometries in previous studies have either taken the measurements from x-ray scans [106, 107] or  $\mu$ CT scans [84, 108], where the measurements have been made through the moving a cursor to the locations of specific points and reporting the distance between them. While this method may produce accurate results, there is inherent human error associated, the number of measurements is limited to the number of planes available and applying this to large sets of data is time consuming which may lead to further error.

The approach used here involves using the 1 mm voxel resolution models generated in ScanIP (v. 2016) which are used for FE modelling. The mask describing the vertebral body of these vertebrae is exported as a stereolithography file (STL), allowing the surface of the vertebra to be measured. Measuring the vertebra was carried out in Matlab where the STL file was imported forming a point cloud describing the surface from the surface nodes. Once imported the point cloud was split into thirds in each of the three anatomical planes, with the points describing the vertebra within these thirds being stored in nine array variables. Cuboids were then fitted to the 3D arrays, maintaining the correct alignment and therefore prohibiting rotation of the cuboid. The cuboid fits can be seen in figs. 4.1 to 4.3.

Measuring the two longer sides of the fitted cuboids gives a total of 18 measurements describing most aspects of the vertebral geometry, these can be seen with their abbreviations in Table 4.1. This includes identifying wedge shaped vertebrae, recorded as reduced anterior height compared to the posterior height, left to right wedge shapes, recorded as sagittal left height being smaller or larger when compared to the sagittal right height.

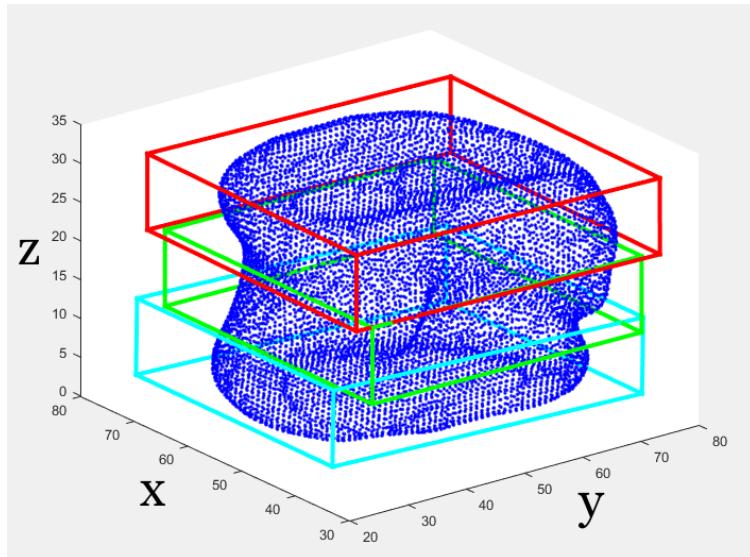


Figure 4.1: The three cuboids fitted to the vertebra point cloud in the axial plane.

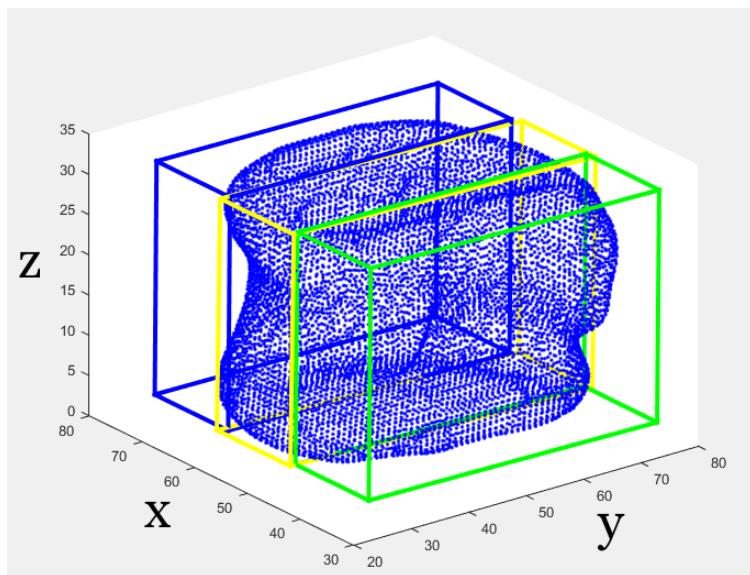


Figure 4.2: The three cuboids fitted to the vertebra point cloud in the coronal plane.

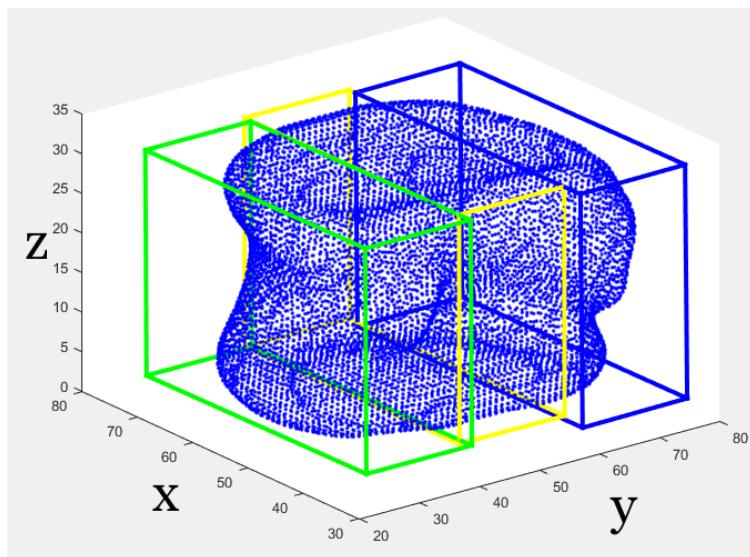


Figure 4.3: The three cuboids fitted to the vertebra point cloud in the sagittal plane.

Table 4.1: The measurements and abbreviations taken from the vertebrae.

Measurement	Abbreviation
Sagittal Left Height	SLH
Sagittal Left Depth	SLD
Sagittal Mid Height	SMH
Sagittal Mid Depth	SMD
Sagittal Right Height	SRH
Sagittal Right Depth	SRD
Coronal Anterior Height	CAH
Coronal Anterior Width	CAW
Coronal Mid Height	CMH
Coronal Mid Width	CMW
Coronal Posterior Height	CPH
Coronal Posterior Width	CPW
Axial Inferior Depth	AID
Axial Inferior Width	AIW
Axial Mid Depth	AMD
Axial Mid Width	AMW
Axial Superior Depth	ASD
Axial Superior Width	ASW

## 4.3 Results

### 4.3.1 Validating Generated Vertebrae

Validation of the generated vertebrae from the PCA plugin for scanIP is vital for ensuring any results are sensible, for example when artificially augmenting the vertebrae, and to ensure that the modes of variation previously described are genuine descriptions of the variation found within the input set. To achieve this validation, aspects important to the generated models need to be compared to the variables found in the input set. The variables compared will be the geometry and volume of the vertebrae, the greyscale background and therefore the material properties of the models and finally the resulting stiffness when loads are simulated on the generated FE model. While identifying the modes of variation in isolation are important to characterise how such variation affects the outcomes of augmentation or understanding the content and main modes of variation, combinations of the principal components generate different models that may describe different ranges of variation. Therefore, the variation found within one standard deviation of the mean for the first three principal components, including all of the combinations of standard deviations within  $\pm 1$  SD, including the mean. For example, PC 1 +1, PC 2 +1, PC 3 -1, would be one model with a combination of the first three principal components.

#### 4.3.1.1 Geometry Validation

Identifying the variation in geometry for combinations of the first three principal components, with all possible combinations within  $\pm 1$  SD of the mean is presented here. The 18 geometric measures found within the  $\pm 1$  SD models are presented in fig. 4.4. The results presented here show a strong agreement between the input and the generated models, with the means of the two sets agreeing closely, along with the range of the measurements. Outliers in the input set originate from the bone spurs and other features of the degenerated vertebrae. Differences in the range of generated vertebrae compared to the range of measurements seen in the input set are due to the input set describing only one standard deviation of variation.

Volume differences between the input set and generated vertebrae were also small, with the difference between the mean of the input set volume and the mean generated model volume being 10 %, the means being  $39500\text{ mm}^3$  and  $38245\text{ mm}^3$  respectively. The range of vertebral volumes is also comparable: the input set range is  $31189$  to  $56003\text{ mm}^3$  while the generated vertebrae for  $\pm 1$  SD with all possible combinations of PC 1, 2 and 3, have a

range of 28152 to 50462 mm<sup>3</sup>.

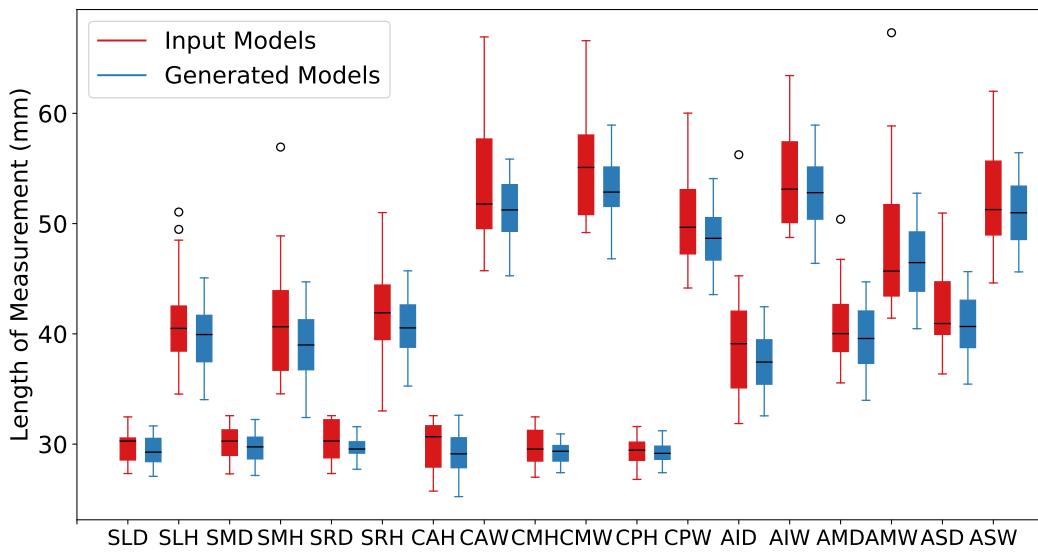


Figure 4.4: The variation in the 18 geometric measures of the input set models compared to the variation in the generated models for the first three principal components including all combinations of the +1, mean and -1 standard deviations.

#### 4.3.1.2 Material Property (Greyscale) Validation

The variation seen in the histograms representing the greyscale differences between generated models and the input can be seen in figs. 4.5 to 4.7, with the range of histograms from the input set shown as the grey range and the coloured lines showing the histogram for each of the generated models. This normalised data shows a general agreement with the shape of the curves and relative quantities being very similar. Deviations from the similarity are, for the most part, at the high and low greyscale values, where in general there are less voxels in this range for the generated models. Comparing these results to an example background in fig. 4.8, comparing an input background slice with the mean generated model mid-slice, shows that the lack of voxel counts in the high and low greyscale regions correlates with having less contrast between the densest bone in the cortical shell and the empty parts. Additionally, fig. 4.8 shows that the important feature for load transfer, the cortical shell, is preserved and accurately described in the background of the mean generated model. While the cortical shell's presence is clear, its definition and contrast between it and the trabecular bone or empty spaces is not as well preserved. Other features such as the posterior vascular channel is also preserved, albeit not as clearly as the features on the input set.

Differences in the mean greyscale between the input set and the generated models of all

combinations of  $\pm 1$  SD are 108 and 97 respectively. The ranges are 78 to 164 for the input set and 72 to 122 for the generated models for all combinations of  $\pm 1$  SD.

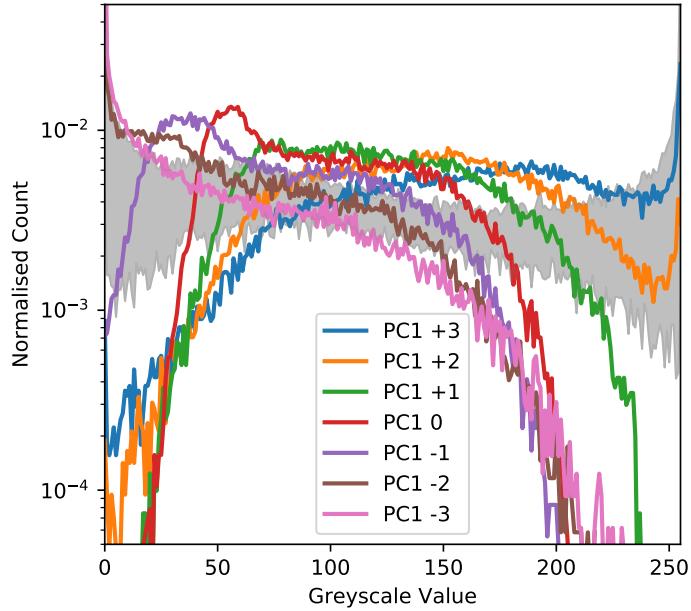


Figure 4.5: Histogram of the models generated from principal component 1, with  $\pm 3, 2 \& 1$  standard deviations away from the mean. The values are normalised with respect to the total volume of the vertebrae, allowing comparisons with different sized model. The grey background represents the range of histograms seen in the input set.

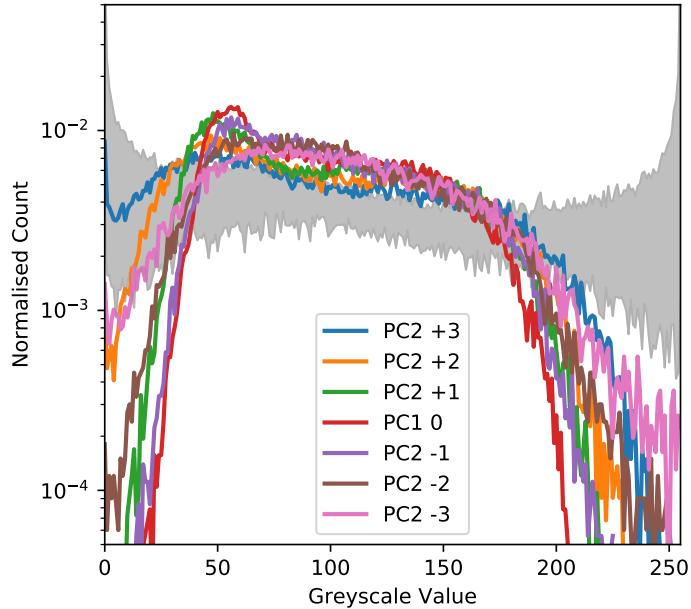


Figure 4.6: Histogram of the models generated from principal component 2, with  $\pm 3, 2 \& 1$  standard deviations away from the mean. The values are normalised with respect to the total volume of the vertebrae, allowing comparisons with different sized model. The grey background represents the range of histograms seen in the input set.

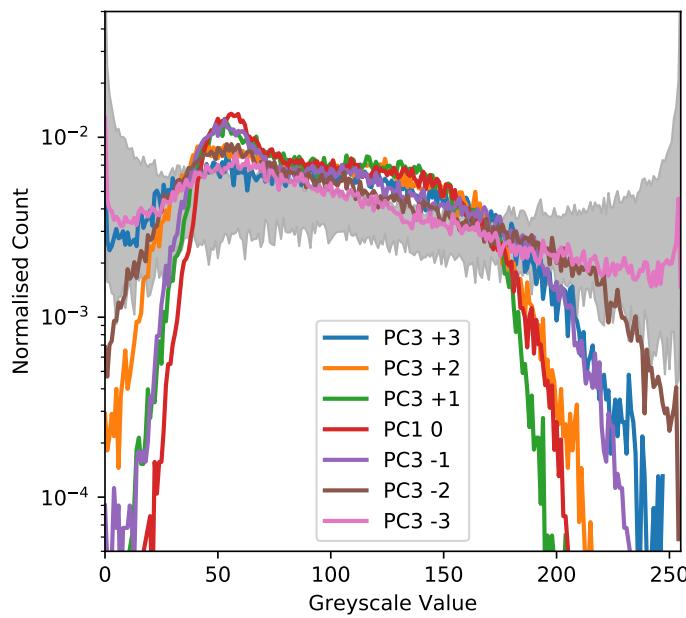


Figure 4.7: Histogram of the models generated from principal component 3, with  $\pm 3$ ,  $2$  &  $1$  standard deviations away from the mean. The values are normalised with respect to the total volume of the vertebrae, allowing comparisons with different sized model. The grey background represents the range of histograms seen in the input set.

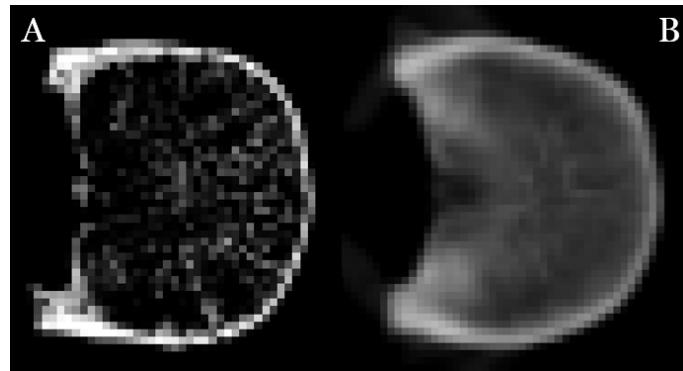


Figure 4.8: Greyscale backgrounds for the axial mid-slice from, A, the Spine 1 L1 input vertebra and B, the mean generated model.

#### 4.3.1.3 Resulting Stiffness Validation

The range of stiffness values from the generated models from all possible combinations of the first three principal components within 1 standard deviation matched closely with the range of stiffness' from the input set. These were 2791 - 6039 N/mm and 2887 - 6172 N/mm for the input and generated models respectively. Additionally the means of the sets also agreed well with the mean computational stiffness of the input set being 4508 N/mm and 4134 N/mm for the mean generated model.

Table 4.2: The stiffness of the generated models from PC1, 2 and 3, showing the fractional change to the mean model in each case.

Model	Stiffness (N/mm)	Fractional Change from the Mean
PC1 +3	6543.38	1.582
PC1 +2	5887.75	1.424
PC1 +1	5059.89	1.224
Mean	4134.88	1.000
PC1 -1	2962.82	0.717
PC1 -2	1696.47	0.410
PC1 -3	1131.86	0.274
PC2 +3	4159.29	0.980
PC2 +2	4291.53	0.831
PC2 +1	4355.98	0.770
Mean	4134.88	1.000
PC2 -1	4051.57	1.006
PC2 -2	3434.91	1.038
PC2 -3	3182.81	1.053
PC3 +3	2930.69	0.709
PC3 +2	3420.55	0.827
PC3 +1	3846.57	0.930
Mean	4134.88	1.000
PC3 -1	4409.05	1.066
PC3 -2	4240.58	1.026
PC3 -3	4141.31	1.002

### 4.3.2 Measuring & Interrogating Vertebral Variation

#### 4.3.2.1 Geometry Variation

The geometric variation found in the first three principal components has been identified using the images of the surface point clouds of the mean and +3 and -3 standard deviations away from the mean, along with the measurements of the 18 variables described previously. The images of the point clouds can be seen in ??????, showing the view of the vertebral models from the three anatomical planes with a three-dimensional view in fig. 4.9. More simplified figures can be seen in figs. 4.10 to 4.12, showing the mid-slice through each of the anatomical planes, while information is lost here, it allows a clear visualisation of the modes of variation found in the main parts of the vertebral body. Here, only the +3, mean and -3 standard deviations of the principal components are shown, this simplifies and allows clear visualisations of the main mode of variation present in each principal component. A quantification of the change in volume can be seen in table 4.3 for the mean and  $\pm 1, 2 \& 3$  standard deviations away from the mean.

Principal component one contains the least geometric variation of the first three principal components. The mid slice axially shows an almost identical shape and size between the +3,

mean and -3 standard deviations, while the coronal and sagittal planes show minor changes in the overall size and volume of the vertebrae. The changes in total vertebral volume is limited to 17 % larger and 15 % smaller than the mean model, shown in table 4.3.

Principal component two shows the most interesting geometric variation with many of the different shapes and some of the degeneration of the input set clearly visible. The large changes to the axial mid slice (fig. 4.10) of the second principal component appear to represent the different levels of the lumbar spine that made up the input set. Positive standard deviations away from the mean, especially the +3 SD slice has the much wider posterior portion aligning with that of the L5 lumbar vertebrae. Conversely the much narrower -3 SD model appears similar to the L1 lumbar vertebrae. This change in width between the +3 and -3 SD is especially evident in the coronal views in fig. 4.12. This change from vertebra reminiscent of L5 vertebrae at +3 SD to L1 vertebra at -3 SD (and therefore L3 vertebrae in the mean model) is also reflected in the sagittal views (fig. 4.11) where anterior and posterior wedge shapes can be seen in the +3 and -3 SD models respectively.

Finally, principal component three also contains a considerable quantity of the geometric variation, although much more simple. Here, the mode of geometric variation is the size of the vertebrae with the -3 SD model being considerably larger than the mean vertebral model (54 % larger) and vice versa with the +3 SD model, where its volume is much smaller than the mean vertebra (40 % smaller).

Quantification of all of the measurements taken on the generated models can be seen in table 4.3 with the acronyms for the measurements given in table 4.1. The colouration in the table allows easy identification of the changes to the vertebral geometry compared to the mean generated model, for example, while the changes to the measurements are near uniform in PC 1 & 3, the non-uniform nature of PC 2 shows the different shapes that are present and described above. Additionally it allows quantification of the shapes seen in the models, for example the anterior and posterior wedge shapes in PC 2, described with the Coronal Anterior Height and the Coronal Posterior Height having an antagonistic relationship. However, the main benefit of the table and its measurements is for the validation of the PC models against the input set, ensuring that the shapes measured in the input set are represented in the models. This is described in section 4.3.1.

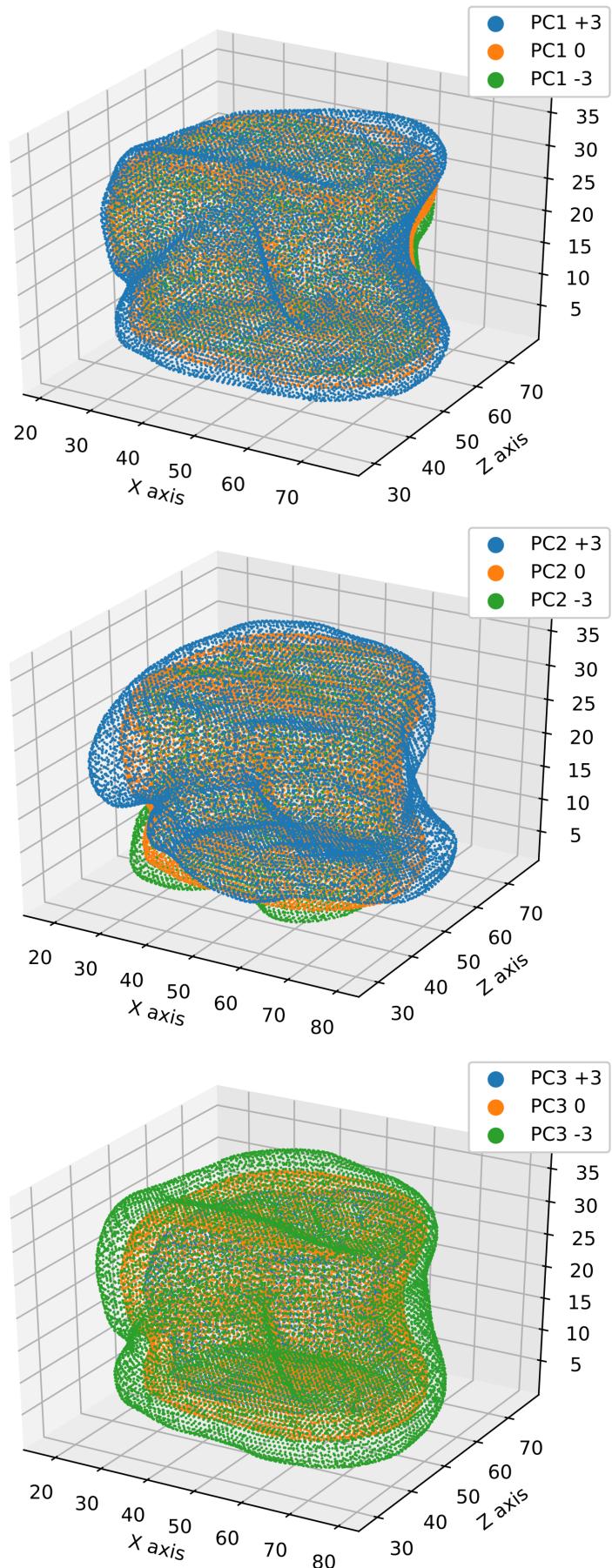


Figure 4.9: Three dimensional views of the surface point clouds of the vertebral models from the first three principal components, showing the mean, +3 and -3 standard deviations away from the mean. Showing how the geometry is captured in the first three principal components.

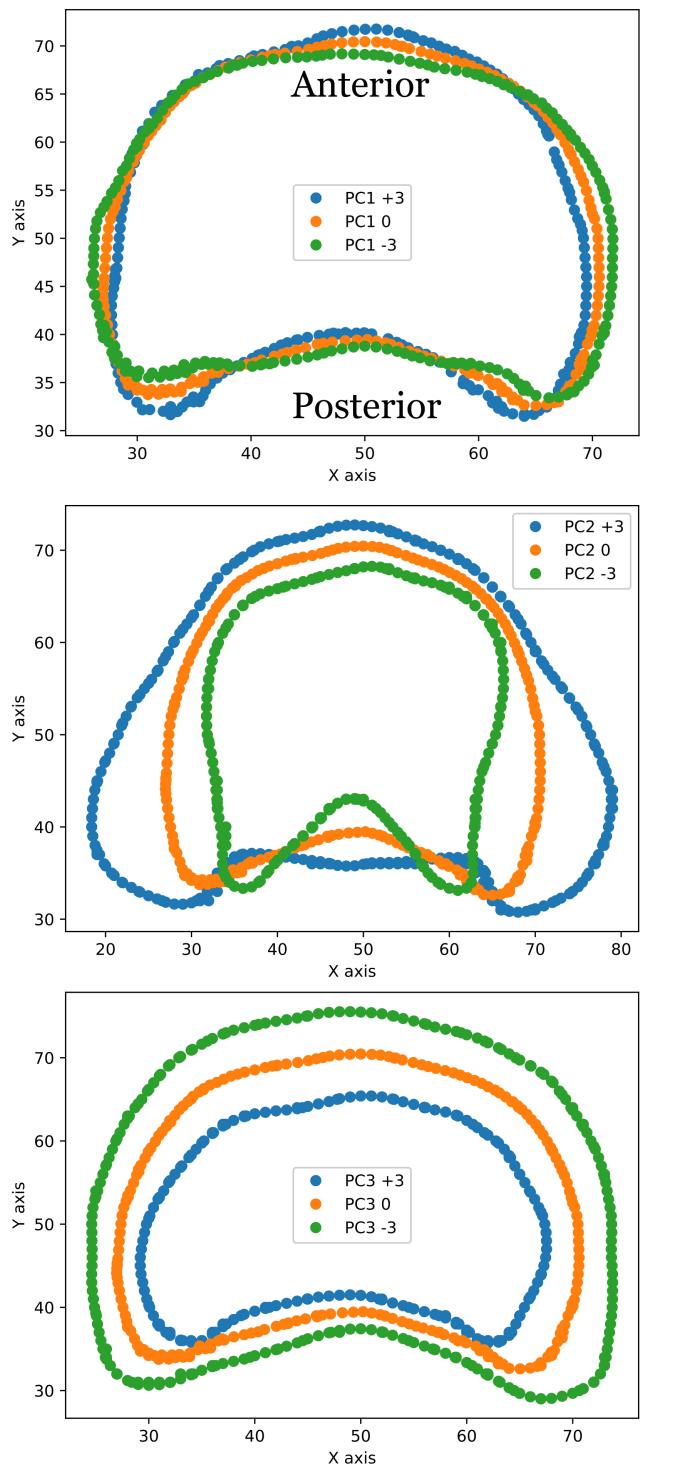


Figure 4.10: Axial views of the mid slice of the vertebral models from the first three principal components, showing the mean, +3 and -3 standard deviations away from the mean. Showing how the geometry is captured in the first three principal components.

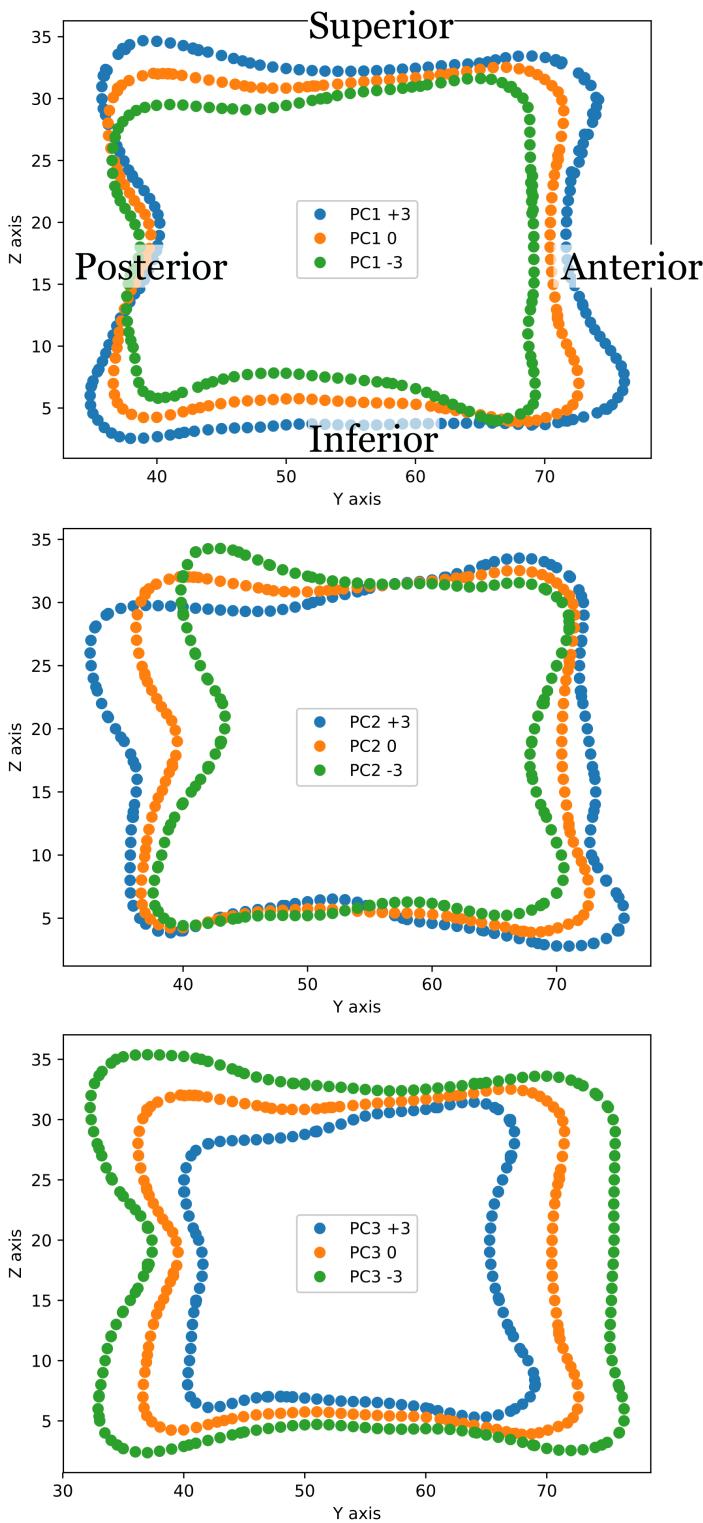


Figure 4.11: Sagittal views of the mid slice of the vertebral models from the first three principal components, showing the mean, +3 and -3 standard deviations away from the mean. Showing how the geometry is captured in the first three principal components.

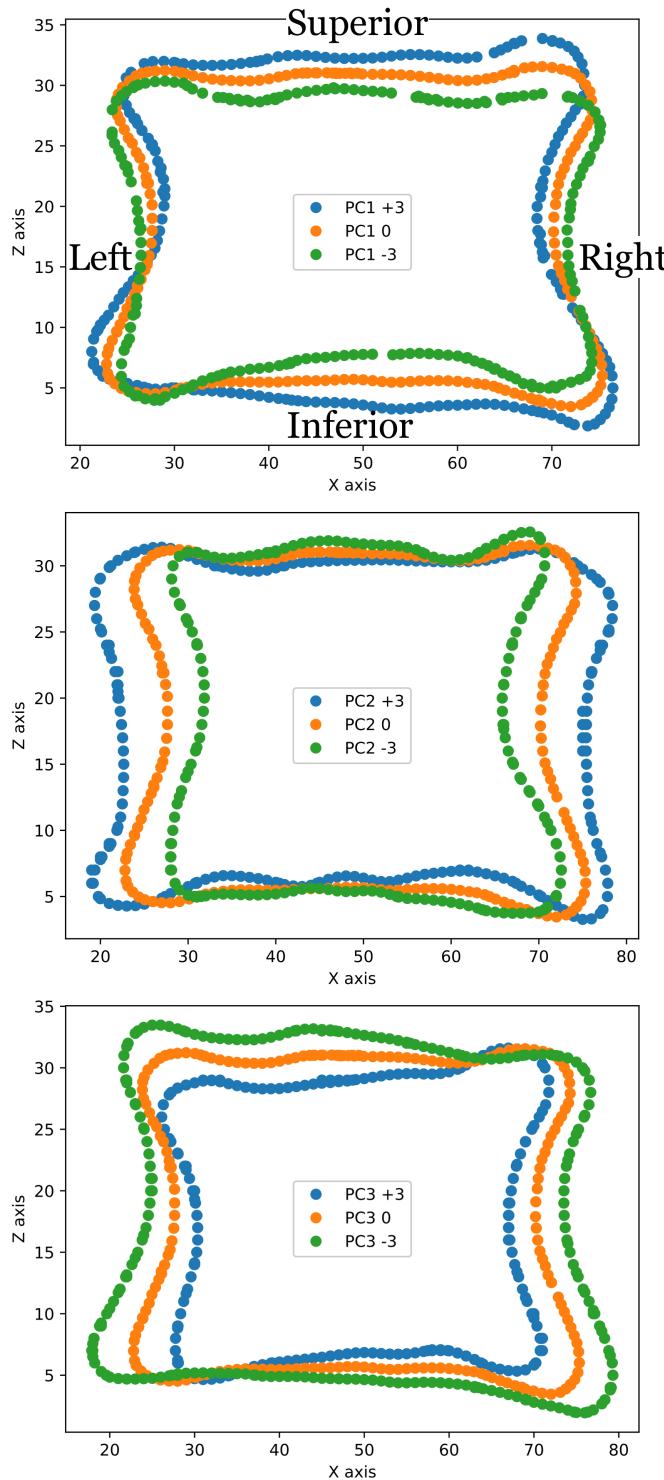


Figure 4.12: Coronal views of the mid slice of the vertebral models from the first three principal components, showing the mean, +3 and -3 standard deviations away from the mean. Showing how the geometry is captured in the first three principal components.

Table 4.3: The measurements of the 18 variables (abbreviations in table 4.1), shown as a fraction of the mean models measurements. Colouration shows the reduced measurements in red and larger measurements in green showing the geometric variation quantitatively.

	SLD	SLH	SMD	SMH	SRD	SRH	CAH	CAW	CMH	CMW	CPh	CPW	AID	AIW	AMD	AMW	ASD	ASW
PC1+3	1.119	1.121	1.130	1.157	1.138	1.119	1.143	1.038	1.122	1.057	1.068	1.038	1.147	1.057	1.110	1.004	1.129	0.976
PC1+2	1.070	1.083	1.078	1.107	1.088	1.074	1.090	1.020	1.082	1.036	1.047	1.024	1.101	1.036	1.068	1.004	1.083	0.985
PC1+1	1.030	1.040	1.042	1.052	1.051	1.038	1.053	1.000	1.038	1.022	1.022	1.011	1.048	1.022	1.031	0.992	1.040	0.996
Mean	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
PC1-1	1.002	0.956	0.987	0.952	0.966	0.960	0.949	1.007	0.967	0.984	0.988	0.984	0.956	0.984	0.973	1.013	0.962	1.011
PC1-2	0.997	0.927	0.977	0.914	0.944	0.922	0.899	1.016	0.956	0.986	0.979	0.988	0.906	0.966	0.944	1.039	0.938	1.021
PC1-3	1.001	0.906	0.976	0.901	0.918	0.885	0.863	1.031	0.956	0.996	0.983	0.979	0.858	0.948	0.923	1.054	0.918	1.031
PC2+3	1.089	1.174	1.078	1.208	1.028	1.139	0.953	1.233	1.046	1.173	1.075	1.193	1.101	1.147	1.137	1.352	1.102	1.204
PC2+2	1.049	1.114	1.042	1.133	1.021	1.095	0.970	1.136	1.017	1.107	1.044	1.137	1.058	1.100	1.091	1.239	1.067	1.124
PC2+1	1.022	1.063	1.012	1.066	0.992	1.051	0.985	1.066	0.995	1.054	1.011	1.071	1.030	1.054	1.043	1.122	1.034	1.067
Mean	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
PC2-1	1.014	0.960	1.007	0.967	1.006	0.976	1.024	0.988	0.992	0.967	0.985	0.940	1.018	0.967	0.971	0.939	0.985	0.957
PC2-2	1.052	0.930	1.049	0.967	1.034	0.956	1.059	0.966	1.005	0.932	0.968	0.872	1.026	0.932	0.960	0.901	0.972	0.902
PC2-3	1.082	0.914	1.079	0.984	1.065	0.957	1.085	0.935	1.034	0.896	0.958	0.824	1.038	0.901	0.959	0.879	0.969	0.849
PC3+3	0.912	0.830	0.944	0.828	0.952	0.857	0.853	0.868	0.984	0.868	0.965	0.876	0.794	0.835	0.811	0.905	0.842	0.898
PC3+2	0.935	0.889	0.949	0.886	0.941	0.906	0.894	0.914	0.963	0.903	0.951	0.861	0.887	0.879	0.930	0.895	0.932	
PC3+1	0.967	0.944	0.967	0.944	0.965	0.952	0.940	0.960	0.985	0.944	0.968	0.949	0.933	0.944	0.932	0.947	0.947	0.966
Mean	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
PC3-1	1.065	1.055	1.058	1.063	1.053	1.044	1.070	1.055	1.029	1.060	1.035	1.033	1.075	1.060	1.064	1.051	1.056	1.037
PC3-2	1.123	1.108	1.118	1.126	1.097	1.094	1.126	1.133	1.067	1.119	1.073	1.083	1.147	1.119	1.135	1.104	1.113	1.074
PC3-3	1.151	1.169	1.146	1.190	1.140	1.143	1.163	1.210	1.129	1.180	1.114	1.118	1.219	1.180	1.200	1.161	1.170	1.111

General changes to the volume of the generated vertebral models can be seen in fig. 4.13. This shows a small and similar change to the volume of the vertebrae in both PC1 and PC2, corresponding to general size changes and shape changes respectively. The majority of the volume changes are isolated to PC3, which again captures size variation, with little change to the shape as seen above.

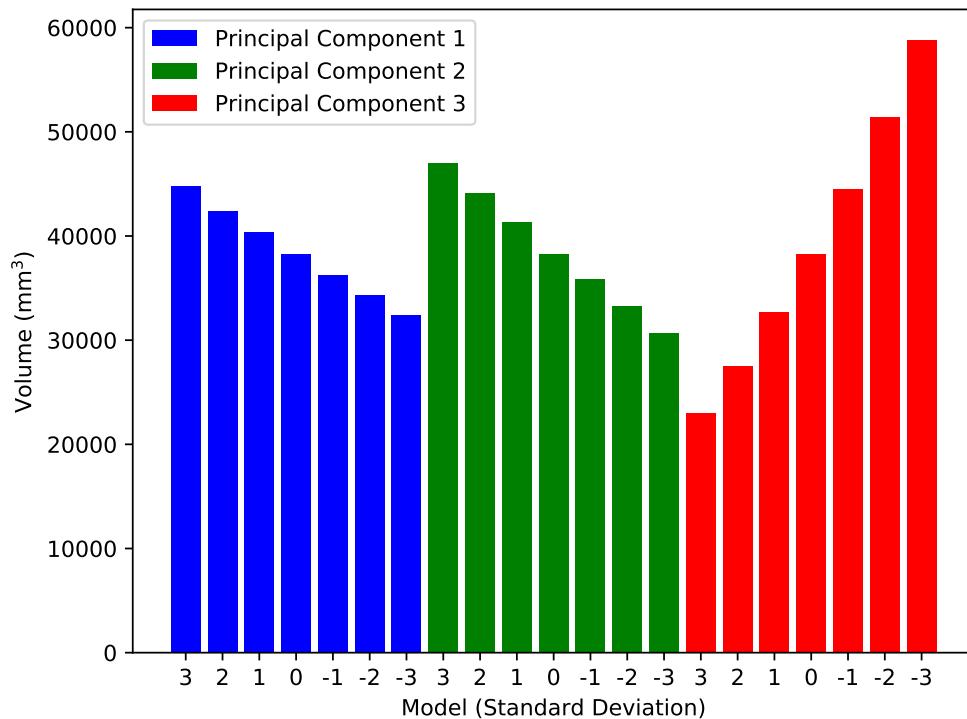


Figure 4.13: The vertebral body volume variation for the first three principal components, including the variation at  $\pm 1$ ,  $2$  &  $3$  standard deviations away from the mean and including the mean.

#### 4.3.2.2 Greyscale & Material Property Variation

Variation in the greyscale background or material properties of the vertebrae was the primary mode of variation, hence most greyscale variation being captured in principal component 1. Unlike the other modes of variation where changes exist in the other two principal components, greyscale variation is almost completely isolated to PC1, which can be seen in both the comparison of the mean greyscale value for each model in fig. 4.14 and the plots of histograms in figs. 4.5 to 4.7. The range of the mean greyscale values for PC1 are from the least dense at  $-3$  SD away from the mean with a mean greyscale value of 42, to a maximum of 162 at  $+3$  SD away from the mean.

However, despite the similarity in the mean of the greyscale variation for PC2 and PC3, the distribution varies significantly, seen in fig. 4.15. In PC2 and PC3 (although more

clearly noticeable in PC3) the density distribution shifts from the posterior to the anterior of the vertebral body. In PC2 this shift of densest material is from anterior to posterior in the models from -3 SD to +3 SD, as the vertebrae change in shape from L1-like to L5-like. In PC3 the shift of the densest part is from posterior to anterior with reducing vertebral body volume (from -3 to +3 SD). Meaning that the larger vertebrae have a much denser posterior portion and less dense anterior, while the smaller vertebrae have a much denser anterior portion with a less dense posterior/pedicle region. The density distribution in PC1's models is more uniform, with more general changes to the density as described earlier, with the -3 SD vertebrae having the least dense properties and +3 SD having the most dense. At the more dense end of PC1 (+3) the thickness of the cortical shell increases significantly compared to that of the least dense (-3). However, the contrast between the shell and the cancellous regions remain similar, while the mean model's cortical shell is less clearly defined.

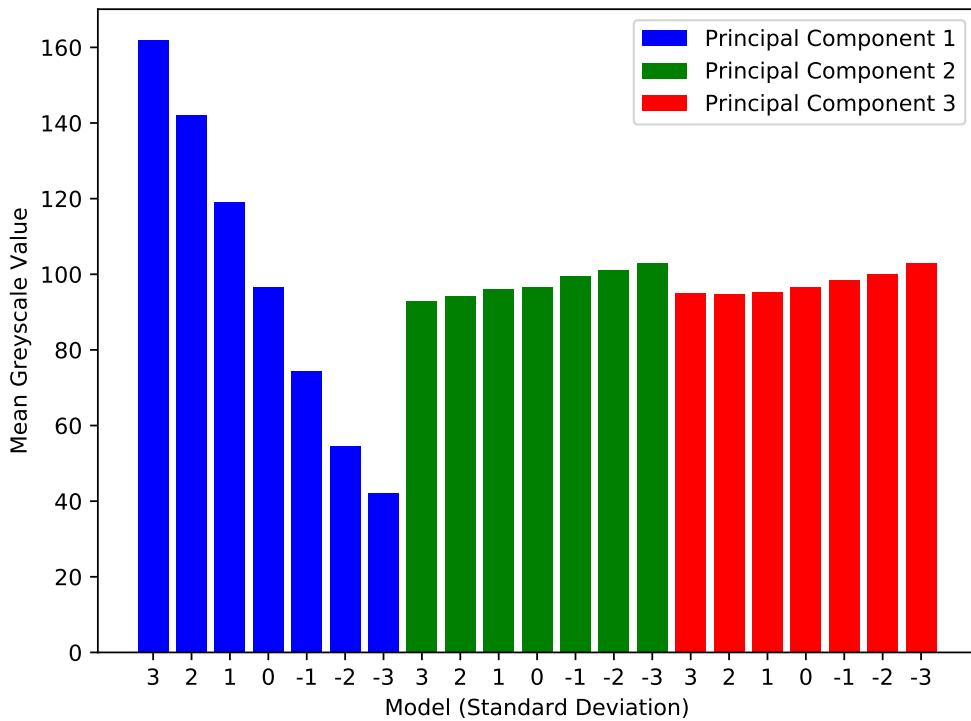


Figure 4.14: The mean greyscale variation for the first three principal components, including the variation at  $\pm 1$ , 2 & 3 standard deviations away from the mean and including the mean.

#### 4.3.2.3 Resulting Stiffness Variation

The variation in the resulting stiffness of the generated model for principal component 1 can be seen in fig. 4.16 and table 4.4. The trends within the different principal components match closely with the variation seen in the mean greyscale which can be seen in fig. 4.14.

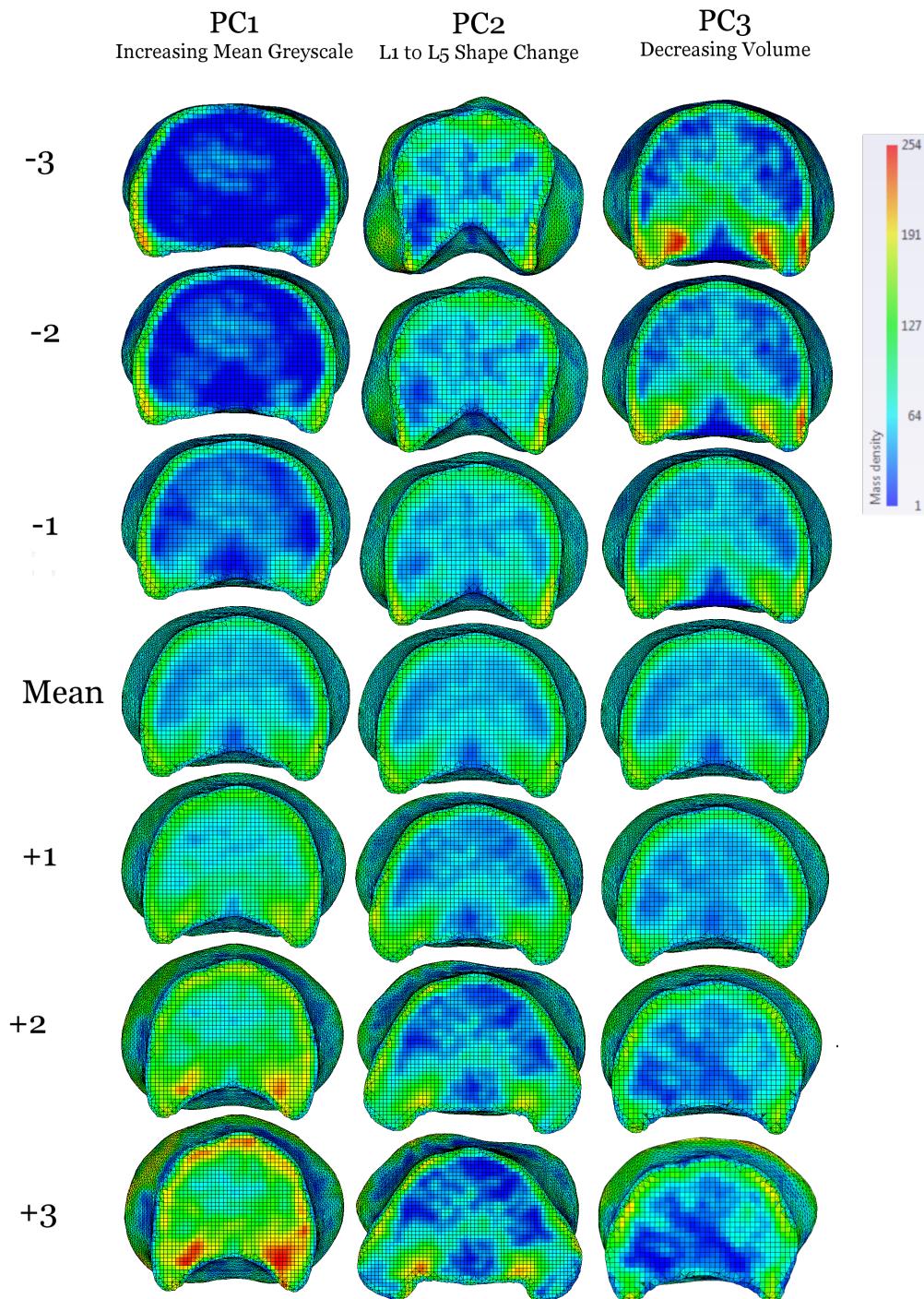


Figure 4.15: The variation in the greyscale distribution across the mid-slice of the vertebrae generated from PC1, PC2 and PC3, for each of the  $\pm 1$ , 2 and 3 standard deviations from the mean. Showing how the changing distribution of the greyscale, even for PC2 and PC3 where the mean greyscale variation is minimal. Red colours indicate denser bone and blue colours indicate the least dense bone.

This suggests a stronger relationship between the greyscale background and the resulting stiffness of the models than any of the other variations in the generated models when loaded centrally and without augmentation.

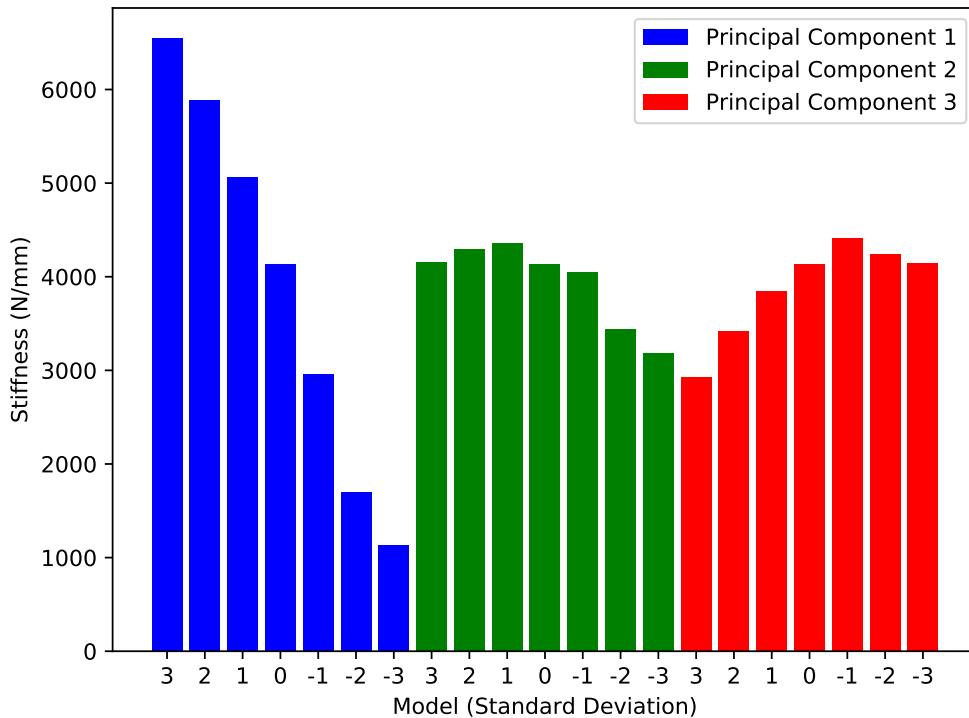


Figure 4.16: The stiffness variation for the first three principal components, including the variation at  $\pm 1$ ,  $2$  &  $3$  standard deviations away from the mean and including the mean.

#### 4.3.3 Augmentation in Generated Models

The general effect of augmentation in the generated vertebrae can be seen in figs. 4.17 to 4.19, with the effect on stiffness variation isolated to the variation seen in each principal component. The vertebrae described by PC1 show an increase in stiffness with increasing cement fill volume, except for the negative standard deviations away from the mean, where a reduction in stiffness is seen for all cement fill volumes. A bimodal relationship is also seen in the vertebrae generated from PC2 when augmentation is simulated. Here, positive standard deviations from the mean show a more pronounced increase in the stiffness at the larger fill volumes when compared to the negative standard deviations. The bimodal distribution continues in PC3 where the increasingly negative standard deviations have a more noticeable increase in the stiffness at higher cement fill volumes, correlating with the vertebrae with larger vertebral body volumes.

Table 4.4: The stiffness of the generated models from PC1, 2 and 3, showing the fractional change to the mean model in each case.

Model	Stiffness (N/mm)	Fractional Change from the Mean
PC1 +3	6543.38	1.582
PC1 +2	5887.75	1.424
PC1 +1	5059.89	1.224
Mean	4134.88	1.000
PC1 -1	2962.82	0.717
PC1 -2	1696.47	0.410
PC1 -3	1131.86	0.274
PC2 +3	4159.29	0.980
PC2 +2	4291.53	0.831
PC2 +1	4355.98	0.770
Mean	4134.88	1.000
PC2 -1	4051.57	1.006
PC2 -2	3434.91	1.038
PC2 -3	3182.81	1.053
PC3 +3	2930.69	0.709
PC3 +2	3420.55	0.827
PC3 +1	3846.57	0.930
Mean	4134.88	1.000
PC3 -1	4409.05	1.066
PC3 -2	4240.58	1.026
PC3 -3	4141.31	1.002

#### 4.3.3.1 Loading Position Effect on Augmentation

The effect of loading position on the generated vertebral stiffness for non-augmented vertebrae is similar to the effect seen with human vertebral models seen in chapter 3 and is shown in fig. 4.20, looking at posterior to anterior loads. Broadly, the stiffness is greatest when the vertebral models are loaded centrally, reducing as loads are applied at greater distances from the centre.

Posterior to anterior loads in PC1 show large reductions furthest from centre loading points, with the effect greatest for the densest vertebrae (+3 S.D.) and least for the least dense vertebrae (-3 S.D.). This reduction in stiffness at 20 mm away from the centre, posteriorly or anteriorly is proportional to the stiffness when loaded centrally, with reductions of approximately 70 % for all standard deviations from the mean.

Principle component two shows a very similar response to loading for all of the standard deviations away from the mean.

Finally, principal component three is mostly uniform, except at the posterior loading points, where the negative standard deviation models (larger vertebral body size) have a reduced effect of posterior loading.

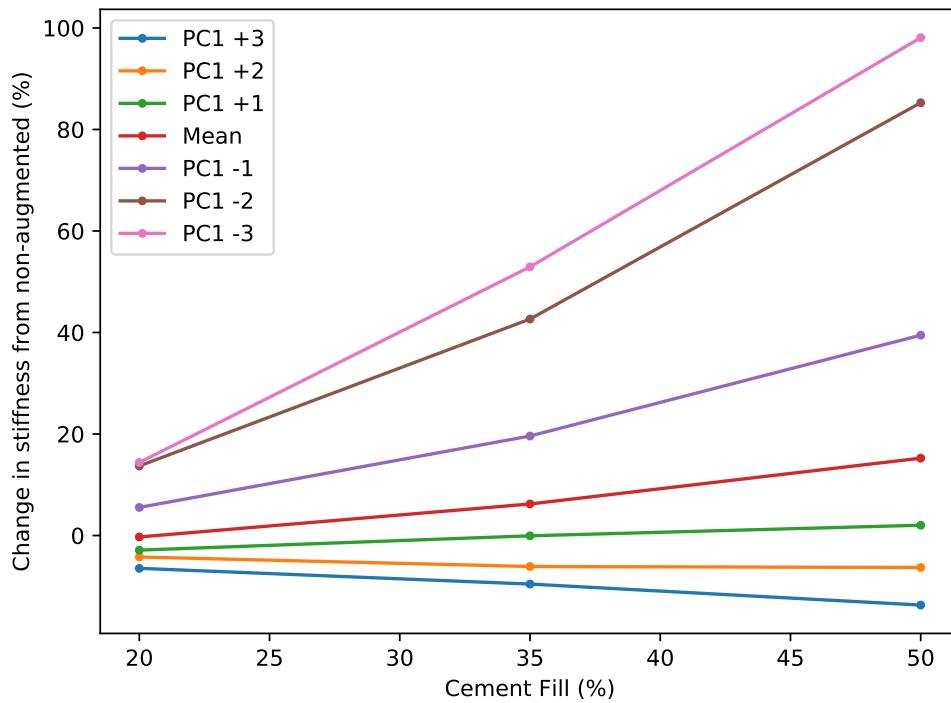


Figure 4.17: The effect of augmentation on vertebral stiffness in the vertebrae generated vertebrae from principal component 1, for 20, 35 and 50 percent fill volume. Shows the change from the non-augmented stiffness increasing with fill volume, with a more pronounced effect seen in the less dense vertebrae (-1, -2 & -3 S.D. from the mean).

The effect of loading position on the augmented vertebrae can be seen in fig. 4.21, identifying the effect of posterior and anterior loads, comparing the percentage change in stiffness from the non-augmented models. At 20 percent fill volume, loading position has little effect on the response to augmentation, with the percentage change less than 5 % for all but PC1, where only the -3 S.D. model shows a change compared to the central loading position, with an increase in stiffness when loading posteriorly.

At 35 % fill trends become apparent which continue and become more noticeable at 50 % fill. PC1 has a simple relationship where augmentation has a smaller effect when loaded at the most posterior or anterior loading positions compared to the centre for the negative standard deviations. However, in the positive standard deviations (the more dense vertebrae), the change in stiffness is greater when loaded anteriorly compared to posteriorly and similar compared to centrally loaded.

PC2 has a near uniform reduction in stiffness when loading posteriorly compared to the central loading position when filled with 35 and 50 % fill. When loaded anteriorly, augmentation has little effect on the negative standard deviation models, where the response to augmentation is similar for each loading point. For the positive standard deviation models however, there is a large increase in the anterior stiffness following augmentation,

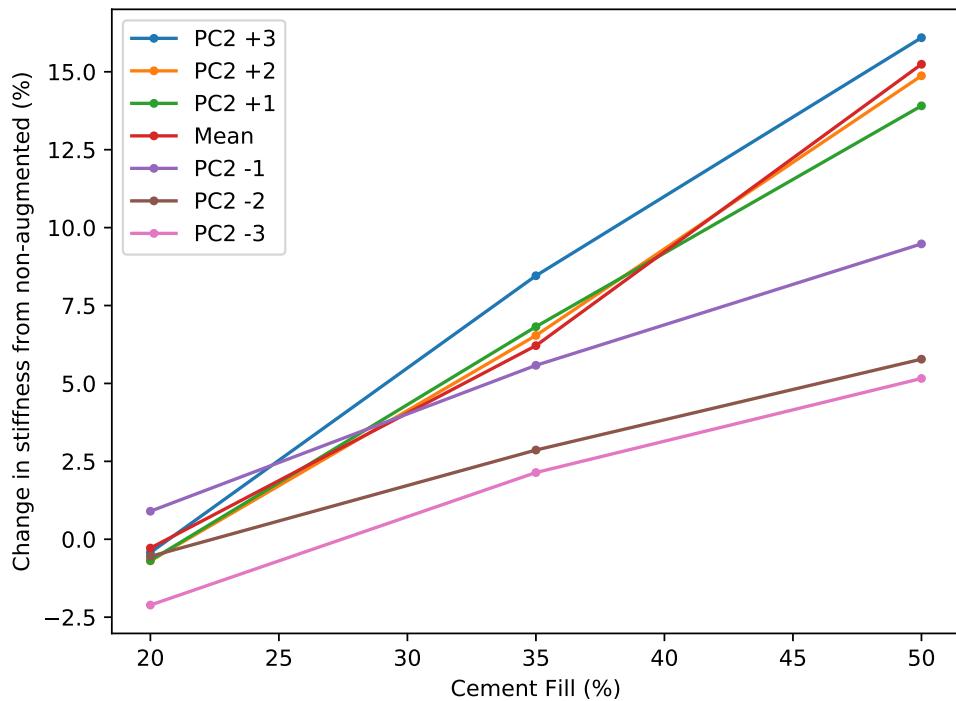


Figure 4.18: The effect of augmentation on vertebral stiffness in the vertebrae generated vertebrae from principal component 2, for 20, 35 and 50 percent fill volume. Shows the change from the non-augmented stiffness increasing with fill volume, with a more pronounced effect seen in the positive standard deviations away from the mean.

with a doubling of the change in stiffness seen in the +3 S.D. model when loaded anteriorly compared to centrally.

PC3 has a similar response to augmentation at different loading points to PC2, where posterior loads have little effect, or a reduced response compared to central loading, except for the +3 S.D. model, where augmentation has the greatest effect on stiffness when loaded posteriorly. Augmentation increased the stiffness most when loaded anteriorly for the negative standard deviations, representing the largest vertebral body volumes.

#### 4.3.3.2 Effect of Injected Cement Volume, Shape & Position

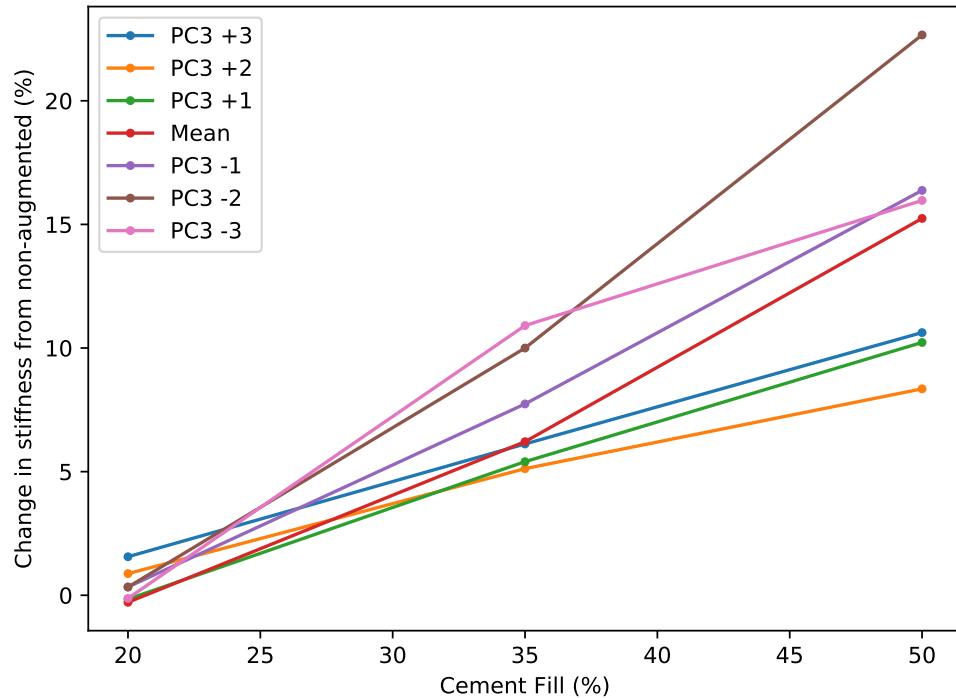


Figure 4.19: The effect of augmentation on vertebral stiffness in the vertebrae generated vertebrae from principal component 3, for 20, 35 and 50 percent fill volume. Shows the change from the non-augmented stiffness increasing with fill volume, with a more pronounced effect seen in the negative standard deviations away from the mean (larger volume).

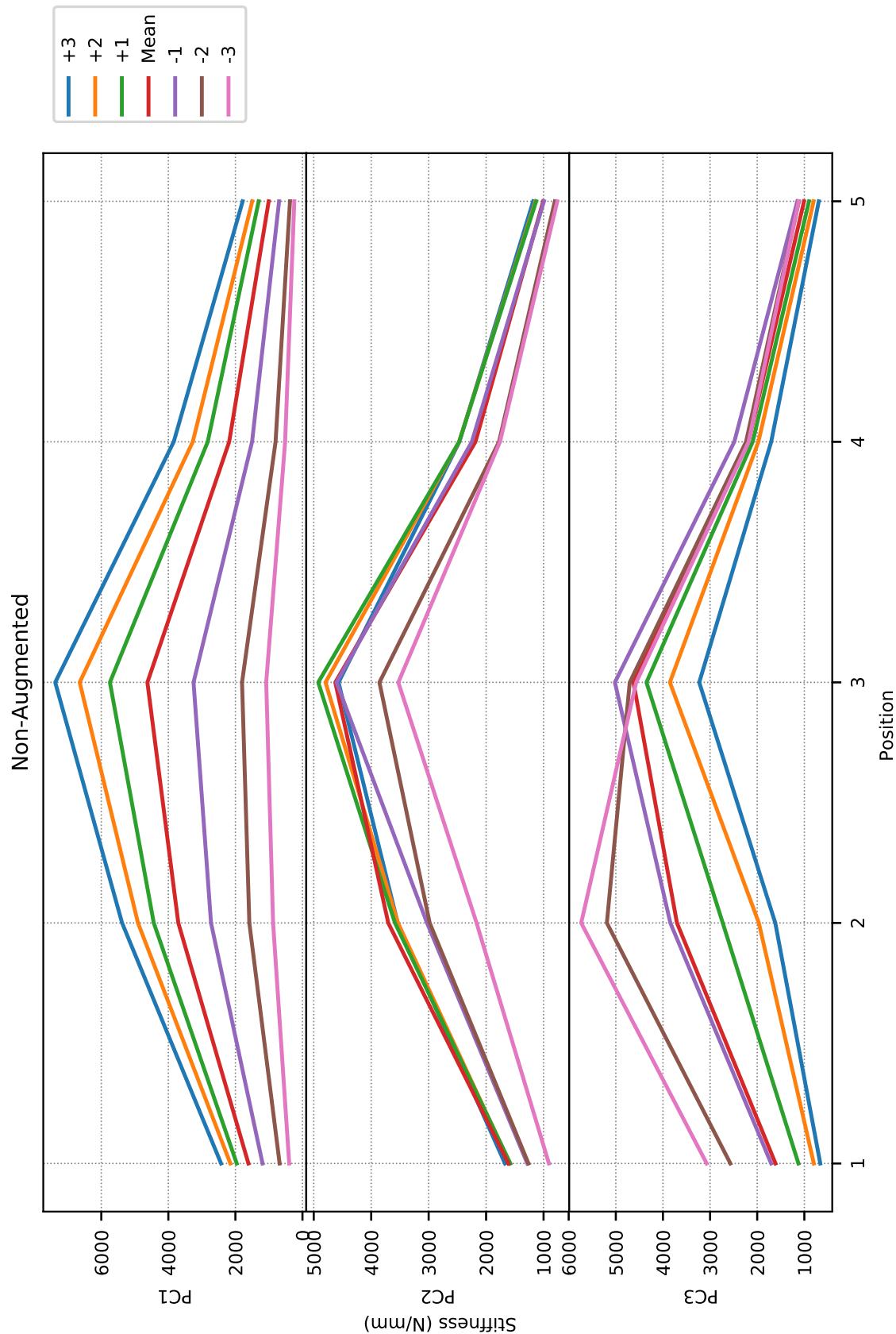


Figure 4.20: Effect of loading position on the vertebral stiffness for PC1, PC2 and PC3 from posterior to anterior loading points. Loading point 1 and 2 are 20 mm and 10 mm posterior of the central loading point respectively, loading point 3 is the central position and load points 4 and 5 are 10 mm and 20 mm anterior, respectively.

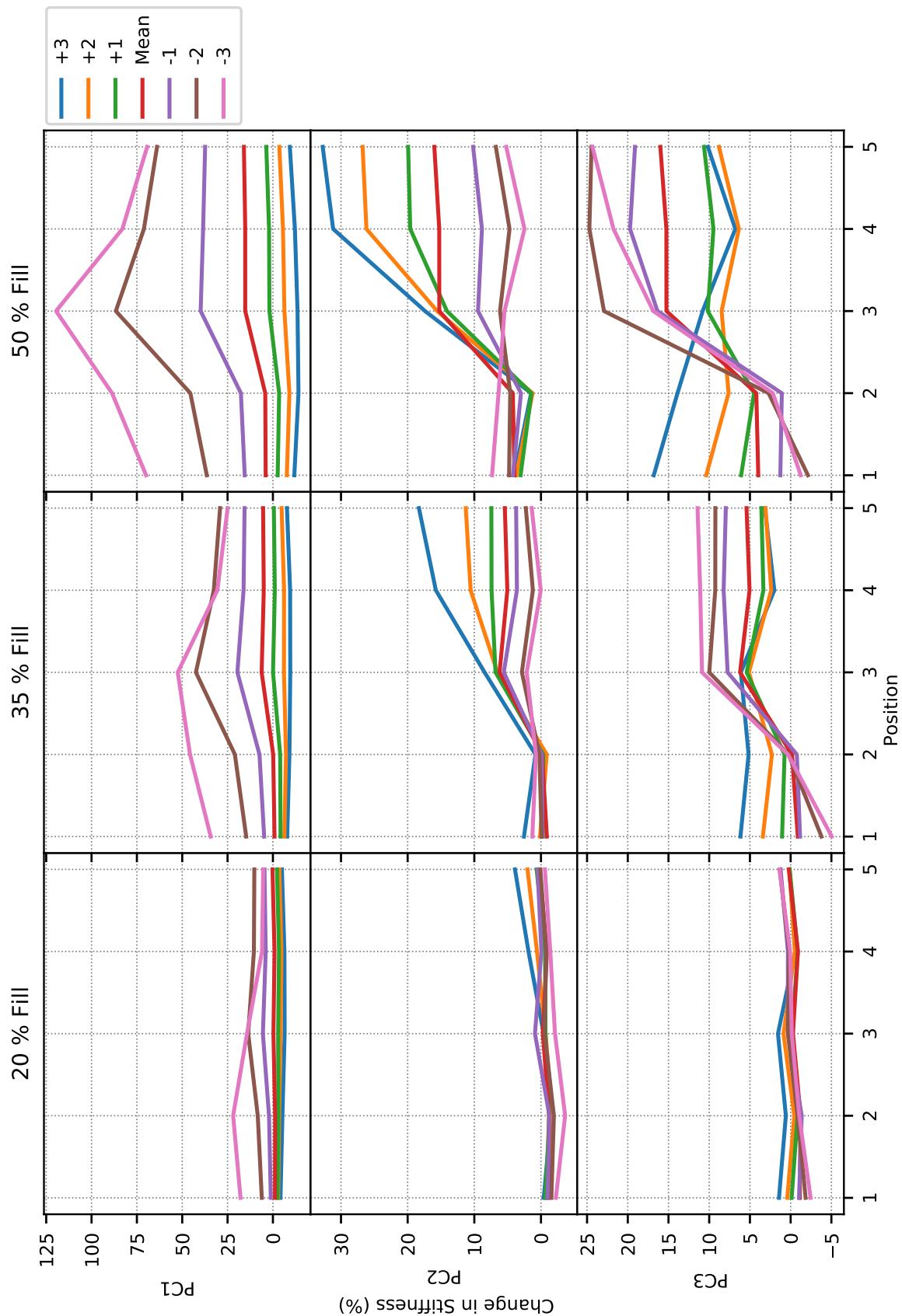


Figure 4.21: Effect of loading position on the augmented vertebral stiffness for PC1, PC2 and PC3, and 20, 35 and 50 % fill from posterior to anterior loading points. Loading point 1 and 2 are 20 mm and 10 mm posterior of the central loading point respectively, loading point 3 is the central position and load points 4 and 5 are 10 mm and 20 mm anterior, respectively.

## 4.4 Discussion

### 4.4.1 Validation

The models generated using the statistical shape modelling approach represent the input set well with the range of measurements taken matching closely to the range of measurements taken from the input set. The 18 measures of the geometry describe the geometry well, with the most important measurements being ones describing wedge shapes (with wedge fractures being the subject of many vertebroplasty procedures) and the general shape changes between L1-like and L5-like vertebrae. The range of variation within 1 standard deviation (all possible combinations of the PC1, 2 and 3) captures most of the variation seen in the input set, with an expectation that the remaining variation not captured in 1 SD would be captured in the other two standard deviations. In a few cases models produced variation that was not seen in the experimental input set; a possibility here is that the combinations of principal components used to make that model were unnatural, with another possibility being that with a larger and therefore more varied input set such variation would be seen. However, the models used in the remaining investigations were from principal components in isolation, which all fell within the range of the input set. Finally, in addition to the range being well represented, the measurements of the mean generated model align closely with the mean of the input set measurements, suggesting that the models are not skewed to one end of the variation spectrum

in between ones

### 4.4.2 Variation

### 4.4.3 Response to Augmentation

The response to small quantities of cement injected into the vertebrae is small. This is shown when comparing 20 % fill volumes to 35 and 50 % fill, where an increase in the stiffness is barely seen and only in the least dense vertebrae. Attempts to understand the effect that the position of small volumes of cement (12 % fill) has on the stiffness of the vertebrae shows sensible effects although a small percentage change to the stiffness of the vertebra compared to central positions of the cement volume.

Moving the cement volume in a lateral, left to right direction showed a reduction in stiffness when at the extremes of the vertebra, where the yielding interface of the cement volume encroached on the denser cortical shell defined by the greyscale background of the model.

The effect of the intermediate cement positions had a near symmetrical appearance - to be expected from the near symmetrical mean vertebra from the input set.

Inferior to superior movements of the cement showed a small change to the stiffness with a 2 % increase to the superior of the vertebra, though a reduction when at the topmost point of the vertebra. This can be explained by understanding the greyscale distribution of the model background or the material properties of the elements. The element found in the centre of the vertebra are less dense and have a lower Young's modulus; when the cement was positioned in the centre and near superior, less of the low Young's modulus elements were exposed, resulting in an increased stiffness.

Moving the cement volume in a posterior to anterior direction showed a reduction in stiffness when at the extremes of the vertebra similarly to the lateral movements. Away from the extremes, the stiffness rose to the anterior of the vertebra, where the bone is less dense in both natural specimens and these PCA generated models. While this would suggest that vertebroplasty injections should always aim to the anterior of the vertebra (for purely stiffness increasing reasons, not just safety), the percentage change in stiffness from the least stiff - most posterior to the stiffer position is a mere 3 %. Given that the most stiff position still had a reduction of 13 % compared to the non-augmented vertebrae, it suggests other factors may be more important and that the cement position, at least for small quantities of cement have little effect.

Compounding these results with the effect of cement position when varying the loading position...

The effect of increasing the volume of the internal cement volume of the first three principal components affected the different models differently depending on what type of variation was found within that principal component. As described previously small volumes of cement had little effect on the stiffness behaviour of the vertebral models, this extended to the 20 % models where little to no increase in the stiffness was seen. At 35 % fill effects of the augmentation were seen, somewhat mirroring what was seen experimentally, where increases in the stiffness were only seen beyond approximately 35 % fill. The effect of increasing the cement from 20 through to 50 % for the mean generated vertebra had the effect of increasing the stiffness near linearly Larger increases in the stiffness were seen for the negative standard deviations away from the mean for PC1, where the main characteristic or mode of variation was the mean greyscale values and the negative standard deviations represented the least dense vertebra. As expected these least dense vertebrae had a large increase in stiffness, increasing further with the increased volumes of cement.

Conversely, with the positive standard deviations away from the mean of PC1 which contained the densest vertebrae in the set, the increasing volume of cement reduced the stiffness of the vertebrae. Again, this mirrored what was seen experimentally, where those specimens that had the highest bone volume fraction to augmentation, with most showing a reduction in stiffness. Computationally this reduction in stiffness is due to the replacement of dense material with high Young's moduli, to material with yielding properties and low Young's moduli (the interface region), despite the Young's modulus of the cement region itself being much higher than that of bone. Experimentally, this reduction in stiffness could be due to the greater level of damage caused when inserting needles into the denser bone and other reasons described in chapter 3.

Despite some studies suggesting that small quantities of cement (less than 20 %) are enough to increase or restore the stiffness or properties of fractured vertebrae to that of the intact or natural vertebrae, the results presented here suggest otherwise. Additionally, these studies lack any validation of experimental

#### **4.4.4 Load Position Effect**

The effect of load position was investigated for the human tissue, where the possible error in choosing the loading point of the model was  $\pm 1$  mm given the resolution. The effect of moving the loading position within the 2 mm range gave changes to the stiffness of approximately 5 % (a small contribution to the total possible error). Here, the changes to the loading points are  $\pm 10$  mm and  $\pm 20$  mm, giving loading points at approximately the posterior boundary, the midpoint between the posterior boundary and the central loading position and similar points on the anterior side. This gave a reasonable understanding of the effect of anterior and posterior loading for the generated models, both with and without augmentation and more importantly a more detailed understanding of the effect of augmentation on different types of vertebra.

The response to loading for the different non-augmented vertebrae in PC1 followed the expectations given the incremental change in the density distribution. In PC2 near identical response from nearly all generated models is explained by their similar volumes and similar mean greyscale values. The -1, -2 and -3 SD models that do not fit the same trends show a reduced posterior density and hence show a reduced stiffness when loaded posteriorly. A similar effect is seen in the PC3 vertebrae where the increased posterior stiffness compared to the other models and the central loading position of -2 and -3 SD models is explained through a large increase in the posterior density. The increased anterior density for the +3

and +2 models in PC3 seem to have little effect on anterior loading.

The response to loading position when the vertebrae have certain fill volumes of cement show interesting results which are not obvious without loading at different positions. At 20 % fill volume the response to different loading position is small, changes and patterns that are present are merely amplified through the addition of larger volumes of cement. At 35 % fill the effect of the loading position is clear, and mimics (to a smaller degree) what is seen in the 50 % fill volume models. The change in stiffness for PC1 at 50% fill with anterior and posterior loads shows a reduced increase in stiffness compared to the central loading position in the negative (less dense) SD models. However, there was still a larger response to augmentation in the -2, -1, mean and +1 SD models when loaded anteriorly compared to posteriorly, suggesting that models with less dense anterior portions have increased responses to augmentation when loaded anteriorly. The most dense vertebral models in PC1 (+3, +2 SD) show little response to augmentation in general, with no clear effect of changing the loading position.

The increase in change in stiffness for the positive standard deviation models in PC2 when loaded anteriorly may be a combination of the shape of the models (the L1 to L5 shape shift from -3 to +3 SD) and the shifting density distribution from anterior to posterior with -3 to +3 SD. Given that the anterior portion of the +1, +2 and +3 SD models within PC2 have a lower anterior density, the support given to this region through augmentation may explain the increased change in stiffness. Additionally, the positive standard deviations exhibit greater anterior height. The combination of the additional height and density may explain why the increase in stiffness reaches a maximum of +33 %, greater than the +25 % maximum seen in anterior loading of the PC3 vertebrae that also show the shifting density distribution. Posterior loads have little effect to the vertebrae in PC2, with all generated models showing a very similar response, potentially adding weight to the idea that the anterior loading response is shape driven. The negative standard deviation models in PC2 show a near uniform response to the different loading position, this may be due to the smaller size along with a smaller anterior height. The reduced height suggests an increase in density (given the near uniform mean greyscale values for PC2), which, as with PC1 causes a reduced response to augmentation.

When loading is varied in PC3 there is a reverse relationship between the +2 and +3 vertebrae compared to the other models (+2 and +3 show a greater response to posterior loads, others show greater response to anterior loads and a reduced response to posterior loads). The main variable in PC3 is the size variation, however given that the cement fill volume is a constant 50 % the cause of the varied response is likely the change in

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material properties. Like PC2, this change in material properties is the shift in the density distribution where smaller +2 and +3 vertebrae have a less dense posterior region. This results in an increase in posterior stiffness following augmentation for these models due to the low stiffness/density of the posterior region. The remaining vertebrae have very dense posterior regions, explaining the reduction in posterior stiffness following augmentation - the same effect seen in the densest vertebrae of PC1. Conversely, the reduced anterior density explains the increase in stiffness following augmentation when loaded anteriorly.

Further isolation of the variation in the principal components would aid the understanding of the true cause of the different responses to augmentation, for example the combination of shape and volume changes in PC2 and PC3 with the density distribution changes. Potential risks of this however are that such variation types do not exist in isolation, at least in this dataset, for example a L1 to L5 shape variation may always exhibit the density shift. This may be due to the load sharing variation caused by the bending of the lumbar region, where the central lumbar vertebra (L3) may experience more central loading, with the L1 and L5 vertebrae experiencing anterior or posterior loads depending on the degree of lordosis in the lumbar spine. Another relationship, that may be specific to this data set is the shift in the density distribution with vertebral body volume. This relationship extends from PC2 to PC3 where the larger vertebra (likely L5 vertebrae) show an increased posterior density, suggesting that that posterior experienced larger loads in the body. Again, like PC2, the smaller vertebrae in PC3 (likely L1 vertebrae) showed greater anterior density and likely higher anterior loads in the body.



# **Chapter 5**

## **Discussion**

### **5.1 Chapter Comparisons**

#### **5.1.1 Bovine and Human Vertebra Study Comparisons**

#### **5.1.2 Human and PCA Generated Model Comparisons**

Perhaps easiest to compare are the specimen specific human vertebral models and the statistical shape models based on these.



## Appendix A

# Alternate Methodologies

### A.1 Inverse Greyscale Material Properties for Augmented Region

A different approach to modelling the cement region was also attempted. This used an inverse greyscale material property for the cement region, rather than a homogeneous material property for the region, based on the greyscale background of the non-augmented vertebral scans with the mask from the augmented models overlaid. This meant that darker regions of greyscale (within the cement volume) would be given a Young's modulus of PMMA cement (2.4 GPa) which would decrease linearly to the Young's modulus of the bone when entering into the brighter regions of the greyscale background. Representing the cement regions using this method meant that the underlying bone present inside the cement volumes is not ignored, instead the interdigitation between bone and cement is represented. While this representation is potentially inaccurate, it provides more detail than using a homogeneous material property and more detail than can be seen on the augmented vertebral scans. The relationship for the cement volume using this method was therefore:

$$E(\rho) = \alpha\rho + c_{cement} \quad (\text{A.1})$$

$$E(\rho) = -0.00842\rho + 2.4 \quad (\text{A.2})$$

Where  $\rho$  is the greyscale value of each voxel and  $E$  is the Young's modulus of each element within the cement region. This ensured that the Young's modulus of the regions containing no bone (greyscale = 0) was equal to that of the cement (approximately 2.4

GPa) and regions containing bone (greyscale = 255) had a Young's modulus equal to 250 MPa, an approximate value for trabecular bone, with a linear relationship between. Brief optimisation of the constant using values of between 0.5 and 5 with 0.5 increments was also carried out.

The results of using this approach were poor, when using the material properties as described above on their own and when incorporating these material properties into the yielding interface modelling methods. With the new material properties along, a negative CCC was achieved with  $R^2$  values of  $\leq 0.1$ . Using these material properties in combination with the yielding interface the best CCC achieved was 0.33.

The reasons for the poor agreement are difficult to determine and potentially require further testing and optimisation. The introduction of an intermediate layer between elements classed as bone and elements classed as cement, would potentially describe the shrinkage that occurs when the cement sets and other voids that form inside the augmented region. This would create properties similar to the approach used by Kinzl et al. [92], where random spheres were inserted into the augmented region to represent the voids that form. Equations for this approach would be in the form:

$$E(\rho) = \begin{cases} \alpha\rho + c_{cement}, & \text{for } \rho \leq 50 \text{ and } \rho \geq 100 \\ \beta, & \text{otherwise} \end{cases} \quad (\text{A.3})$$

Where  $\beta$  is the Young's modulus on the intermediate region between the bone and the cement, forming through the cement shrinking.

# Bibliography

- [1] H. Gray. *Anatomy of the human body*. 20th ed., 1918.
- [2] M. A. Adams and P. Dolan. “Spine biomechanics”. In: *Journal of Biomechanics* 38.10 (Oct. 2005), pp. 1972–1983.
- [3] T. Stewart and R. Hall. “(iv) Basic biomechanics of human joints: Hips, knees and the spine”. In: *Curr. Orthop.* 20.1 (Feb. 2006), pp. 23–31.
- [4] M. M. Panjabi et al. “Thoracic Human Vertebrae Quantitative Three-Dimensional Anatomy”. In: *Spine (Phila. Pa. 1976)*. 16.8 (1991), pp. 888–901.
- [5] P. M. Manohar et al. *Human lumbar vertebrae: quantitative three-dimensional anatomy*. 1992.
- [6] F. Denis. “The three column spine and its significance in the classification of acute thoracolumbar spinal injuries”. In: *Spine (Phila Pa 1976)* 8.8 (1983), pp. 817–831.
- [7] F. Magerl et al. “A comprehensive classification of thoracic and lumbar injuries”. In: *European Spine Journal* 3.4 (Aug. 1994), pp. 184–201.
- [8] J. M. Mathis et al. “Percutaneous vertebroplasty: a developing standard of care for vertebral compression fractures.” en. In: *AJNR. Am. J. Neuroradiol.* 22.February (Feb. 2001), pp. 373–381.
- [9] C. Studies, F. The, and M. Clinic. “Vertebral Compression Fractures in Elderly Osteoporosis Patients Receiving Glucocorticoid Intra-articular Injections”. In: *American Family Physician* 6.3 (2006), pp. 206–211.
- [10] L. J. Melton III and D. F. Kallmes. “Epidemiology of vertebral fractures: implications for vertebral augmentation.” In: *Academic Radiology* 13.5 (May 2006), pp. 538–45.
- [11] C. Cooper et al. “Incidence of clinically diagnosed vertebral fractures: a population-based study in Rochester, Minnesota, 1985-1989.” In: *Journal of Bone and Mineral Research* 7.2 (Feb. 1992), pp. 221–227.
- [12] F. Burstein et al. “The Use of Hydroxyapatite Cement in Secondary Craniofacial Reconstruction”. In: *Craniofacial Reconstr.* 104.5 (Jan. 1987), pp. 1270–1275.

- [13] C. Cooper, T. O'Neill, and A. Silman. "The epidemiology of vertebral fractures". In: *Bone* 14 (Jan. 1993), pp. 89–97.
- [14] T. H. Diamond et al. "Clinical outcomes after acute osteoporotic vertebral fractures: a 2-year non-randomised trial comparing percutaneous vertebroplasty with conservative therapy." In: *Medical Journal of Australia* 184.3 (2006), pp. 113–7.
- [15] M. Moro et al. "Failure load of thoracic vertebrae correlates with lumbar bone mineral density measured by DXA". In: *Calcified Tissue International* 56.3 (Mar. 1995), pp. 206–209.
- [16] A. A. BOOKMAN. *Musculoskeletal Imaging*. Vol. 38. 4. Elsevier Health Sciences, 2011, pp. 787–787.
- [17] R. Buchbinder et al. "A randomized trial of vertebroplasty for painful osteoporotic vertebral fractures." In: *New England Journal of Medicine* 361.6 (2009), pp. 557–568.
- [18] D. F. Kallmes et al. "A randomized trial of vertebroplasty for osteoporotic spinal fractures." In: *New England Journal of Medicine* 361.6 (2009), pp. 569–79.
- [19] S. M. Belkoff, J. M. Mathis, and L. E. Jasper. "The Biomechanics of Vertebroplasty". In: *Spine (Phila. Pa. 1976)*. 26.14 (2001), pp. 1537–1541.
- [20] S. M. Belkoff, J. M. Mathis, and L. E. Jasper. "Ex vivo biomechanical comparison of hydroxyapatite and polymethylmethacrylate cements for use with vertebroplasty." In: *AJNR. Am. J. Neuroradiol.* 23.10 (2002), pp. 1647–51.
- [21] P. A. Hulme et al. "Vertebroplasty and kyphoplasty: a systematic review of 69 clinical studies." In: *Spine (Phila. Pa. 1976)*. 31.17 (Aug. 2006), pp. 1983–2001.
- [22] S. Muijs. "Treatment of painful osteoporotic vertebral compression fractures: A Brief Review of the Evidence for Percutaneous Vertebroplasty". In: *J. Bone Jt. . .* (2011).
- [23] B. Jay and S. Ahn. "Vertebroplasty". In: *Semin. Intervent. Radiol.* (2013).
- [24] *Percutaneous vertebroplasty and percutaneous balloon kyphoplasty for treating osteoporotic vertebral compression fractures*. Standard. National Institute for Health and Clinical Excellence, Mar. 2013.
- [25] P. J. Atkinson. "Variation in trabecular structure of vertebrae with age." In: *Calcified Tissue Research* 1.1 (1967), pp. 24–32.
- [26] a. M. Parfitt. "Age-related structural changes in trabecular and cortical bone: cellular mechanisms and biomechanical consequences." In: *Calcified Tissue International* 36 Suppl 1.1 (1984), S123–S128.

- [27] J. Aaron et al. “Trabecular architecture in woman and men of similar bone mass with and without vertebral fracture: II. Three-dimensional histology”. In: *Bone* 27.2 (2000), pp. 277–282.
- [28] P. a. Hulme, S. K. Boyd, and S. J. Ferguson. “Regional variation in vertebral bone morphology and its contribution to vertebral fracture strength”. In: *Bone* 41.6 (2007), pp. 946–957.
- [29] L. Mosekilde, L. Mosekilde, and C. C. Danielsen. “Biomechanical competence of vertebral trabecular bone in relation to ash density and age in normal individuals.” In: *Bone* 8.2 (1987), pp. 79–85.
- [30] T. S. Keller. “Predicting the Compressive Mechanical Behavior of Bone”. In: *Journal of Biomechanics* 27.9 (1994), pp. 1159–1168.
- [31] T. Hildebrand and P. Rüeggsegger. “Quantification of Bone Microarchitecture with the Structure Model Index”. In: *Computer Methods in Biomechanics and Biomedical Engineering* 1.1 (1997), pp. 15–23.
- [32] J. S. Thomsen, E. N. Ebbesen, and L. I. Mosekilde. “Zone-dependent changes in human vertebral trabecular bone: clinical implications.” In: *Bone* 30.5 (2002), pp. 664–9.
- [33] E. N. Ebbesen et al. “Age-and Gender-Related Differences in Vertebral Bone Mass, Density, and Strength”. In: *Journal of Bone and Mineral Research* 14.8 (1999), pp. 1394–1403.
- [34] H.-J. Wilke, A. Kettler, and L. E. Claes. “Are sheep spines a valid biomechanical model for human spines?” In: *Spine (Phila. Pa. 1976)*. 22.20 (1997), pp. 2365–2374.
- [35] F. Kandziora et al. “Comparison Between Sheep and Human Cervical Spines An Anatomic, Radiographic, Bone Mineral Density, and Biomechanical Study”. In: *Spine (Phila. Pa. 1976)*. 26.9 (2001), pp. 1028–1037.
- [36] H.-J. Wilke, A. Kettler, and K. H. Wenger. “Anatomy of the Sheep Spine and Its Comparison to the Human Spine”. In: *Anatomical Record* 247.4 (1997), pp. 542–555.
- [37] Aerssens et al. “Interspecies Differences in Bone Composition, Density, and Quality: Potential Implications for in Vivo Bone Research”. In: *Endocrinology* 139.2 (1998), pp. 663–670.
- [38] V. N. Wijayathunga et al. “Development of specimen-specific finite element models of human vertebrae for the analysis of vertebroplasty.” In: *Proceedings of the Institution of Mechanical Engineers, Part H: Journal of Engineering in Medicine* 222.2 (Feb. 2008), pp. 221–228.

- [39] S. M. Tarsuslugil et al. “Development of calcium phosphate cement for the augmentation of traumatically fractured porcine specimens using vertebroplasty.” In: *Journal of Biomechanics* 46.4 (2013), pp. 711–5.
- [40] N. Furtado et al. “A biomechanical investigation of vertebroplasty in osteoporotic compression fractures and in prophylactic vertebral reinforcement.” In: *Spine (Phila. Pa. 1976)*. 32.17 (2007), E480–E487.
- [41] R. K. Wilcox et al. “A dynamic investigation of the burst fracture process using a combined experimental and finite element approach.” In: *European Spine Journal* 13.6 (2004), pp. 481–8.
- [42] G. Gurwitz, J. Dawson, and M. McNamara. “Biomechanical analysis of three surgical approaches for lumbar burst fractures using short-segment instrumentation.” In: *Spine (Phila. Pa. 1976)*. (1993).
- [43] D. Ananthakrishnan et al. “The effect on anterior column loading due to different vertebral augmentation techniques.” In: *Clin. Biomech. (Bristol, Avon)* 20.1 (2005), pp. 25–31.
- [44] U. Berlemann et al. “Adjacent vertebral failure after vertebroplasty. A biomechanical investigation.” In: *Journal of Bone and Joint Surgery. British Volume* 84.5 (2002), pp. 748–752.
- [45] S. G. Pneumaticos et al. “Effect of vertebroplasty on the compressive strength of vertebral bodies”. In: *Spine Journal* 13.12 (2013), pp. 1921–1927.
- [46] J. D. Barr et al. “Percutaneous Vertebroplasty for Pain Relief and Spinal Stabilization”. In: *Spine (Phila. Pa. 1976)*. 25.8 (Apr. 2000), pp. 923–928.
- [47] A. G. Tohmeh et al. “Biomechanical efficacy of uni- vs. bi-pedicular vertebroplasty for the treatment of osteoporotic compression fractures.” In: *Trans. Orthop. Res. Soc.* 24.17 (1999), p. 177.
- [48] S. M. Belkoff, J. M. Mathis, and E. M. Erbe. “Biomechanical Evaluation of a New Bone Cement for Use in Vertebroplasty”. In: *Spine (Phila. Pa. 1976)*. 25.9 (2000), pp. 1061–1064.
- [49] K. B. Higgins et al. “Biomechanical alterations in intact osteoporotic spine due to synthetic augmentation: finite element investigation.” In: *Journal of Biomechanical Engineering* 129.4 (2007), pp. 575–85.
- [50] J. Graham, M. Ries, and L. Pruitt. “Effect of bone porosity on the mechanical integrity of the bone-cement interface.” In: *Journal of Bone and Joint Surgery. American Volume* 85-A.10 (2003), pp. 1901–1908.

- [51] S. Belkoff et al. “Vertebroplasty: the biomechanical effect of cement volume”. In: *Trans Orthop Res Soc* 46 (2000), p. 356.
- [52] S. J. Lee et al. “Prediction and assessment of optimal volume for PMMA injection in percutaneous vertebroplasty using image and biomechanical analyses”. In: *Trans. Annu. Meet. Res. Soc.* 2002, p. 786.
- [53] A. C. Jones and R. K. Wilcox. “Finite element analysis of the spine: Towards a framework of verification, validation and sensitivity analysis”. In: *Medical Engineering & Physics* 30.10 (Dec. 2008), pp. 1287–1304.
- [54] M. Viceconti et al. “Extracting clinically relevant data from finite element simulations”. In: *Clinical Biomechanics* 20.5 (June 2005), pp. 451–454.
- [55] M. Mengoni et al. “In-Silico Models of Trabecular Bone: A Sensitivity Analysis Perspective”. en. In: (2014), pp. 393–423.
- [56] K. Robson Brown et al. “Comparative finite-element analysis: a single computational modelling method can estimate the mechanical properties of porcine and human vertebrae.” In: *Journal of the Royal Society, Interface* 11.95 (June 2014), p. 20140186.
- [57] J. M. Buckley. “Sensitivity of Vertebral Compressive Strength to Endplate Loading Distribution”. In: *Journal of Biomechanical Engineering* 128.5 (2006), p. 641.
- [58] Y. Chevalier, D. Pahr, and P. K. Zysset. “The Role of Cortical Shell and Trabecular Fabric in Finite Element Analysis of the Human Vertebral Body”. In: *Journal of Biomechanical Engineering* 131.11 (Nov. 2009), p. 111003.
- [59] S. K. Eswaran, A. Gupta, and T. M. Keaveny. “Locations of bone tissue at high risk of initial failure during compressive loading of the human vertebral body”. In: *Bone* 41.4 (Oct. 2007), pp. 733–739.
- [60] M. Kinzl et al. “The effect of standard and low-modulus cement augmentation on the stiffness, strength, and endplate pressure distribution in vertebroplasty”. In: *European Spine Journal* 21.5 (May 2012), pp. 920–929.
- [61] G. M. Treece, R. W. Prager, and A. H. Gee. “Regularised marching tetrahedra : improved iso-surface extraction”. In: *Comput. Graph.* 23 (1999), pp. 583–598.
- [62] S. K. Eswaran et al. “Cortical and Trabecular Load Sharing in the Human Vertebral Body”. In: *Journal of Bone and Mineral Research* 21.2 (Nov. 2005), pp. 307–314.
- [63] H. Ritzel et al. “The thickness of human vertebral cortical bone and its changes in aging and osteoporosis: a histomorphometric analysis of the complete spinal column from thirty-seven autopsy specimens.” In: *Journal of Bone and Mineral Research* 12.1 (1997), pp. 89–95.

- [64] D. H. Pahr and P. K. Zysset. "A comparison of enhanced continuum FE with micro FE models of human vertebral bodies". In: *Journal of Biomechanics* 42.4 (Mar. 2009), pp. 455–462.
- [65] M. a. Liebschner, W. S. Rosenberg, and T. M. Keaveny. "Effects of bone cement volume and distribution on vertebral stiffness after vertebroplasty." In: *Spine (Phila. Pa. 1976)*. 26.14 (2001), pp. 1547–1554.
- [66] G. Baroud et al. "Load shift of the intervertebral disc after a vertebroplasty: A finite-element study". In: *European Spine Journal* 12.4 (Aug. 2003), pp. 421–426.
- [67] A. Polikeit, L. P. Nolte, and S. J. Ferguson. "The effect of cement augmentation on the load transfer in an osteoporotic functional spinal unit: finite-element analysis." In: *Spine (Phila. Pa. 1976)*. 28.10 (2003), pp. 991–996.
- [68] Y. Chevalier et al. "Cement Distribution, Volume, and Compliance in Vertebroplasty". In: *Spine (Phila. Pa. 1976)*. 33.16 (2008), pp. 1722–1730.
- [69] Y. Zhao et al. "Trabecular level analysis of bone cement augmentation: a comparative experimental and finite element study." In: *Annals of Biomedical Engineering* 40.10 (Oct. 2012), pp. 2168–76.
- [70] G. Tozzi, Q.-H. Zhang, and J. Tong. "3D real-time micromechanical compressive behaviour of bone - cement interface: Experimental and finite element studies". In: *Journal of Biomechanics* 45.2 (Jan. 2012), pp. 356–363.
- [71] D. Janssen, K. a. Mann, and N. Verdonschot. "Micro-mechanical modeling of the cement-bone interface: The effect of friction, morphology and material properties on the micromechanical response". In: *Journal of Biomechanics* 41.15 (Nov. 2008), pp. 3158–3163.
- [72] M. Kinzl et al. "The mechanical behavior of PMMA/bone specimens extracted from augmented vertebrae: A numerical study of interface properties, PMMA shrinkage and trabecular bone damage". In: *Journal of Biomechanics* 45.8 (May 2012), pp. 1478–1484.
- [73] S. Sikora. "Experimental and computational study of the behaviour of trabecular bone-cement interfaces." PhD thesis. University of Leeds, 2013.
- [74] M. S. Sikora. "Experimental and Computational Study of the Behaviour of Trabecular Bone-Cement Interfaces". In: (2013), pp. 196–244.
- [75] L. Grassi et al. "Comprehensive evaluation of PCA-based finite element modelling of the human femur." In: *Medical Engineering & Physics* 36.10 (Oct. 2014), pp. 1246–52.

- [76] M. Clogenson et al. “A statistical shape model of the human second cervical vertebra”. In: *International journal of computer assisted radiology and surgery* 10.7 (2015), pp. 1097–1107.
- [77] S. P. Väänänen et al. “Generation of 3D shape, density, cortical thickness and finite element mesh of proximal femur from a DXA image.” In: *Medical Image Analysis* 24.1 (Aug. 2015), pp. 125–134.
- [78] C. Fitzpatrick, M. Baldwin, and P. Laz. “Development of a statistical shape model of the patellofemoral joint for investigating relationships between shape and function”. In: *J. . . .* (2011).
- [79] F. Y. Zapata-Cornelio et al. “Methodology to Produce Specimen-Specific Models of Vertebrae: Application to Different Species”. In: *Annals of Biomedical Engineering* 45.10 (2017), pp. 2451–2460.
- [80] S. M. Belkoff, J. C. Sanders, and L. E. Jasper. “The effect of the monomer-to-powder ratio on the material properties of acrylic bone cement”. In: *Journal of Biomedical Materials Research* 63.4 (2002), pp. 396–399.
- [81] L. E. Jasper et al. “The effect of monomer-to-powder ratio on the material properties of cranioplastic”. In: *Bone* 25.SUPPL. 1 (1999), pp. 27–29.
- [82] A. C. Jones and R. K. Wilcox. “Assessment of factors influencing finite element vertebral model predictions”. In: *Journal of Biomechanical Engineering* 129.6 (2007), pp. 898–903.
- [83] M. Mengoni. *opti4Abq (v 2.0), a generic python code to run Abaqus in an optimisation loop.* 2017.
- [84] S. H. Zhou et al. “Geometrical dimensions of the lower lumbar vertebrae - analysis of data from digitised CT images”. In: *European Spine Journal* 9.3 (2000), pp. 242–248.
- [85] A. Race, K. A. Mann, and A. A. Edidin. “Mechanics of bone/PMMA composite structures: An in vitro study of human vertebrae”. In: *Journal of Biomechanics* 40.5 (2007), pp. 1002–1010.
- [86] R. Aquarius et al. “Prophylactic vertebroplasty can decrease the fracture risk of adjacent vertebrae: an in vitro cadaveric study”. In: *Medical engineering & physics* 36.7 (2014), pp. 944–948.
- [87] J. Steens et al. “The influence of endplate-to-endplate cement augmentation on vertebral strength and stiffness in vertebroplasty”. In: *Spine* 32.15 (2007), E419–E422.

- [88] L. I.-K. Lin. “A concordance correlation coefficient to evaluate reproducibility”. In: *Biometrics* 45 (1989), pp. 255–268.
- [89] M. Doube et al. “BoneJ: Free and extensible bone image analysis in ImageJ”. In: *Bone* 47.6 (2010), pp. 1076–1079.
- [90] M. Sezgin and B. Sankur. “Survey over image thresholding techniques and quantitative performance evaluation”. In: *Journal of Electronic imaging* 13.1 (2004), pp. 146–166.
- [91] R. Buchbinder et al. “A randomized trial of vertebroplasty for painful osteoporotic vertebral fractures.” In: *New England Journal of Medicine* 361.6 (2009), pp. 557–568.
- [92] M. Kinzl et al. “An experimentally validated finite element method for augmented vertebral bodies”. In: *Clinical biomechanics* 28.1 (2013), pp. 15–22.
- [93] S. Gravius et al. “Intravertebral pressure during vertebroplasty-an in-vitro study”. In: *Zeitschrift fur Orthopadie und Unfallchirurgie* 147.1 (2009), pp. 43–47.
- [94] K. B. Higgins et al. “Biomechanical effects of unipedicular vertebroplasty on intact vertebrae”. In: *Spine* 28.14 (2003), pp. 1540–1547.
- [95] R. J. Oakland et al. “Preliminary biomechanical evaluation of prophylactic vertebral reinforcement adjacent to vertebroplasty under cyclic loading”. In: *The Spine Journal* 9.2 (2009), pp. 174–181.
- [96] S. K. Eswaran et al. “Cortical and trabecular load sharing in the human vertebral body”. In: *Journal of Bone and Mineral Research* 21.2 (2006), pp. 307–314.
- [97] T. L. Bredbenner et al. “Development and validation of a statistical shape modeling-based finite element model of the cervical spine under low-level multiple direction loading conditions”. In: *Frontiers in bioengineering and biotechnology* 2 (2014), p. 58.
- [98] S. Meller and W. A. Kalender. “Building a statistical shape model of the pelvis”. In: *International Congress Series*. Vol. 1268. Elsevier. 2004, pp. 561–566.
- [99] D. P. Nicolella and T. L. Bredbenner. “Development of a parametric finite element model of the proximal femur using statistical shape and density modelling”. In: *Computer methods in biomechanics and biomedical engineering* 15.2 (2012), pp. 101–110.
- [100] R. Bryan et al. “Statistical modelling of the whole human femur incorporating geometric and material properties”. In: *Medical engineering & physics* 32.1 (2010), pp. 57–65.

- 
- [101] A. H. Ali et al. “The accuracy of active shape modelling and end-plate measurements for characterising the shape of the lumbar spine in the sagittal plane”. In: *Computer methods in biomechanics and biomedical engineering* 15.2 (2012), pp. 167–172.
  - [102] J. R. Meakin et al. “The intrinsic shape of the human lumbar spine in the supine, standing and sitting postures: characterization using an active shape model”. In: *Journal of anatomy* 215.2 (2009), pp. 206–211.
  - [103] J. Boisvert et al. “Geometric variability of the scoliotic spine using statistics on articulated shape models”. In: *IEEE Transactions on Medical Imaging* 27.4 (2008), pp. 557–568.
  - [104] J. F. Hollenbeck et al. “Statistical shape modeling characterizes three-dimensional shape and alignment variability in the lumbar spine”. In: *Journal of biomechanics* 69 (2018), pp. 146–155.
  - [105] E. F. Chan et al. “3-dimensional metrics of proximal femoral shape deformities in Legg–Calvé–Perthes disease and slipped capital femoral epiphysis”. In: *Journal of Orthopaedic Research(R)* 36.5 (2018), pp. 1526–1535.
  - [106] I. Gilad and M. Nissan. *A study of vertebra and disc geometric relations of the human cervical and lumbar spine*. 1986.
  - [107] I. Gilad and M. Nissan. “Sagittal evaluation of elemental geometrical dimensions of human vertebrae.” In: *Journal of Anatomy* 143 (1985), pp. 115–20.
  - [108] K. M. Cheung et al. “Computed tomographic osteometry of asian lumbar pedicles”. In: *Spine (Phila. Pa. 1976)*. 19.13 (1994), pp. 1495–1498.