

# ICTP Ocean Modelling Summer School Lab

## *CVMix Vertical Mixing Library*

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# Community Earth System Model (CESM)

# Community Earth System Model

## About

A flexible global climate model

- Couples atmosphere, ocean, land, and sea ice components.
- CESM 1.2 was released in June 2013 ([CESM 1.2.2](#) in June 2014)
- CESM 2.0 will be available in June 2016 (I think)

NCAR's coupler + community's component models; lots of component development done at NCAR as well

## How flexible?

- Active components: CAM [atmosphere], [POP \[ocean\]](#), CLM [land], CICE [sea ice]
- Provides data models (for example - force POP with atmospheric data instead of an active model)
- Also provides "stub" models (for example, running CLM with data atmosphere does not require any ocean or sea ice forcing)

# Running CESM

Four commands to run CESM on a supported machine

**Run the following from \$CESMROOT/scripts:**

- (1) `./create_newcase -case $CASEDIR/$CASENAME -compset  
$COMPSET -res $RESOLUTION -mach $MACHINE`

**Run the following from \$CASEDIR:**

- (2) `./cesm_setup`
- (3) `./$CASENAME.build`
- (4) `./$CASENAME.submit`

What will this run?

The default setup is a 5-day simulation; output will depend on the components selected.

# More Information

## Coming up

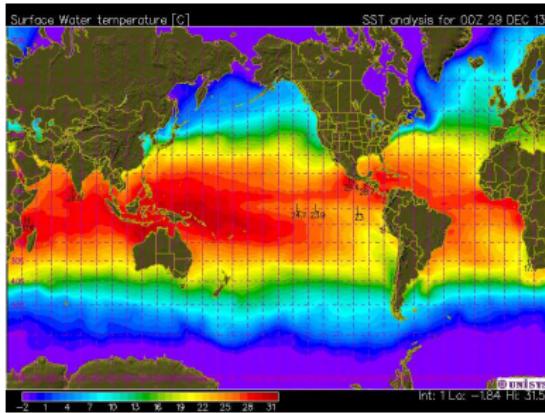
- Later in this talk, I will talk about setting up a couple of ocean-only runs on argo
  - I'll point you to \$CESMROOT
  - I'll tell you that ocean is the only active component in a "C" compset (data atmosphere and sea ice, stub land)
- For general information, see  
<http://www.cesm.ucar.edu/models/cesm1.2/>

## But first...

... Let's talk about vertical mixing and CVMix

# The Community Vertical Mixing Project

# Why is Vertical Mixing Important to Ocean Models?



<http://weather.unisys.com/archive/sst/sst-131229.gif> (Dec 29, 2013)

## Basics

- Sea surface temperature (SST) has a major role in atmosphere ↔ ocean energy exchange
- Vertical mixing is one of many processes affecting SST
  - Occurs on scales that are not resolved by current ocean models, need to use parameterization instead
- Other physical quantities (tracers, salinity, etc) also affected by mixing

# Mixing in Ocean Models

## Current state

- Numerous techniques for parameterizing the mixing process
- Model developers choose their favorite parameterization(s) and code them up as part of the ocean model

## CVMix project

- **Our goal:** produce an easy-to-use library containing a range of parameterizations
- **Secondary goal:** provide a stand-alone driver to test the library on its own
  - Note: we use the term “stand-alone driver” a bit loosely. CVMix can compute single-column diffusivities given proper input, but lacks the capability to see how diffusivities change over time.

# Why CVMix?

## Driving force

[CESM Workshop \(Breckenridge\) 2012](#): MPAS-O (ocean model from LANL) did not have a KPP module yet and MOM5 (from GFDL) was using an outdated implementation – lab wanted to improve on for MOM6.

- CVMix is now used in development of MPAS-O and MOM6, and will [eventually] replace the mixing modules in POP.

## Other benefits

- ① Reduce duplicate code – for example, static mixing occurs as a step in many parameterizations
- ② CSEG is working to include non-POP / non-data ocean models in CESM
  - Vertical mixing library allows [some] physics to stay the same even if dynamics change
  - Allow more detailed model inter-comparisons

# The CVMix Mission

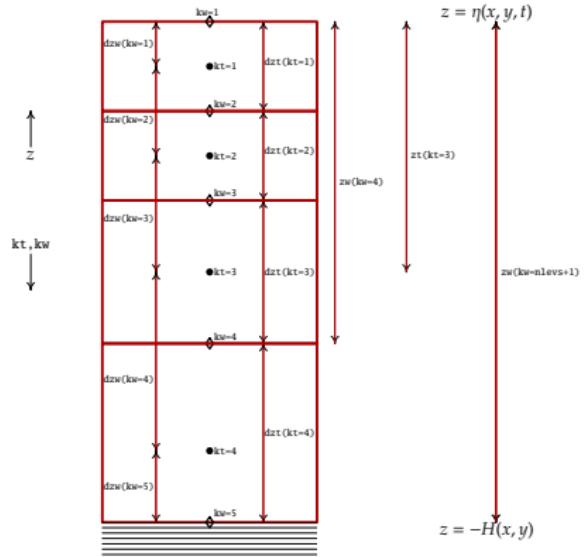
## CVMix will...

- Provide a transparent, robust, flexible, well documented, open source library for use in parameterizing ocean vertical mixing processes.
- Contain a consensus of **first-order closures** that **return a vertical diffusivity, viscosity, and possibly a non-local transport**.
- Be comprised of Fortran modules that may be used in a stand-alone manner or incorporated into ocean models.
- Be developed within a community of scientists and engineers who make use of CVMix modules for a variety of research needs.

CVMix modules will be freely distributed under GPLv2 using an open source methodology.

# Vertical Mixing Overview

- Divide column into `nlevs` levels
- Data on cell centers and interfaces
- Center index  $kt = 1 \dots nlevs$
- Interface index  $kw = 1 \dots nlevs+1$
- Depth  $z$ 
  - $\eta$  at surface
  - 0 at average sea level
  - $-H(x, y)$  at bottom (positive up!)



What does a vertical mixing parameterization look like?

- Inputs: combination of parameters and physical values in column
- Outputs: viscosity ( $\nu$ ) and tracer diffusivity ( $\kappa$ ) coefficients on cell interfaces

# [Some] Mixing Parameterizations

## ① Static background mixing

- Constant mixing (Ekman, 1905)
- Bryan-Lewis (1979)
- Henyey et al. (1986)

## ② Tidal mixing

- Simmons et al. (2004)
- Polzin (2009) / Melet et al. (2013)

## ③ Shear-induced mixing (“Richardson number mixing”)

- Pacanowski and Philander (1981)
- Large et al. (1994), henceforth LMD94
- Jackson et al. (2008)

## ④ Double diffusion mixing (Schmitt, 1994 / LMD94 / Danabasoglu et al., 2006)

## ⑤ K-profile parameterization (“KPP”; LMD94)

## ⑥ Convective adjustment (density based as well as Brunt-Väisälä)

Blue indicates method is already in package.

# More Parameterizations on the Way

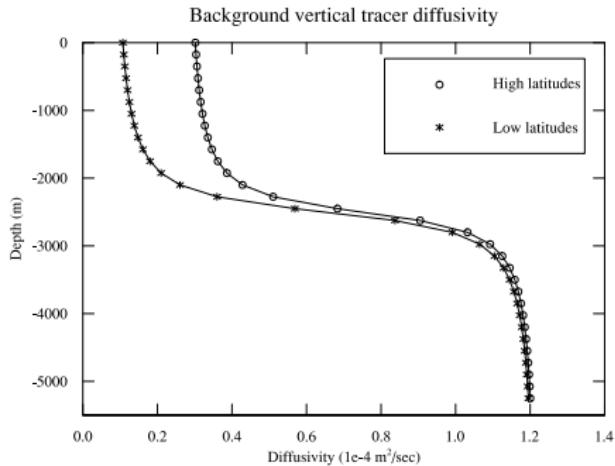
## Various stages of progress

- Langmuir (surface wave) mixing – brought in to KPP by group at Brown University, currently in testing
- KPP bottom surface layer – mentioned by Enrique in a couple of conversations, maybe on a to-do list?
- **Your favorite scheme here** – this is a community model!

# Bryan-Lewis Profile

Want diffusivity to increase towards bottom of ocean (mimic tidal mixing).

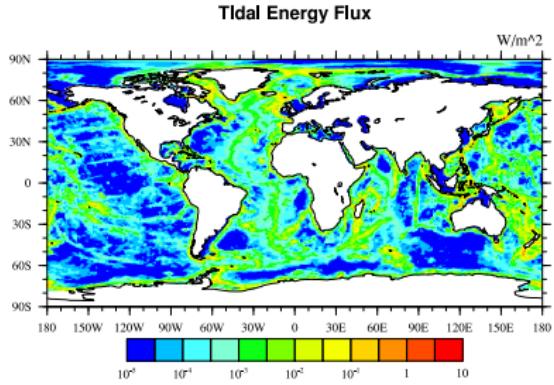
At right: diffusivity profile of two columns representing columns in different latitudes.



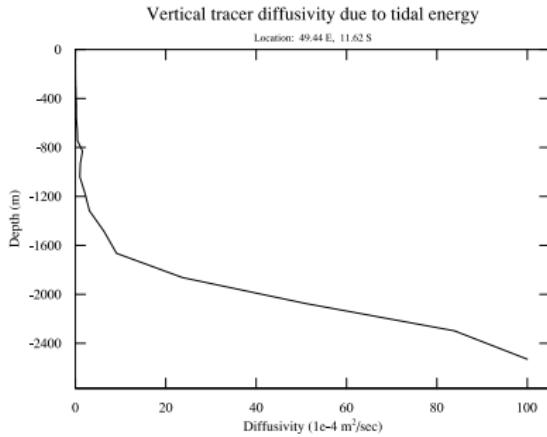
Diffusivity and viscosity depend on depth

$$\kappa = c_0 + \frac{c_1}{\pi} \tan^{-1} \left( c_2 ((-z) - c_3) \right)$$
$$\nu = \text{Pr} \kappa$$

# Tidal Mixing



Tidal Energy Flux Map



Diffusivity North of Madagascar

Diffusivity depends on tidal energy flux, depth, density, and buoyancy

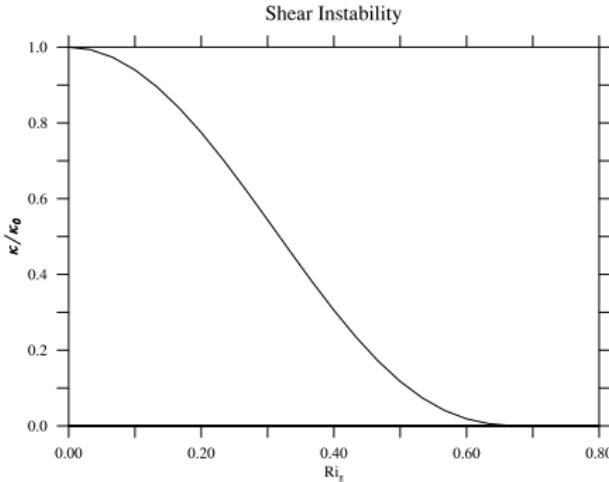
$$\kappa = \frac{q \Gamma E(x, y) F(x, y, z)}{\rho N^2}$$

$$F(x, y, z) = \frac{e^{-z/\zeta}}{\zeta(e^{H(x,y)/\zeta} - e^{-\eta(x,y)/\zeta})}$$

# Shear Mixing

Want diffusivity to decrease as Richardson number ( $Ri$ ) increases;  $\kappa = 0$  if  $Ri \geq Ri_0 = 0.7$ .

At right: The stand-alone driver produces the shear mixing diffusivity profile plot from Fig. 3 of [LMD94](#).



Diffusivity and viscosity depend on Richardson number

$$\kappa = \begin{cases} \kappa_0 & Ri \leq 0 \\ \kappa_0 [1 - (Ri/Ri_0)^{p_1}]^{p_2} & 0 < Ri < Ri_0 \\ 0 & Ri \geq Ri_0 \end{cases}$$
$$\nu = Pr\kappa$$

# Double Diffusion Mixing

## Two regimes

Determine which regime we are in via stratification parameter

$$R_\rho = \frac{\alpha}{\beta} \left( \frac{\partial \Theta / \partial z}{\partial S / \partial z} \right),$$

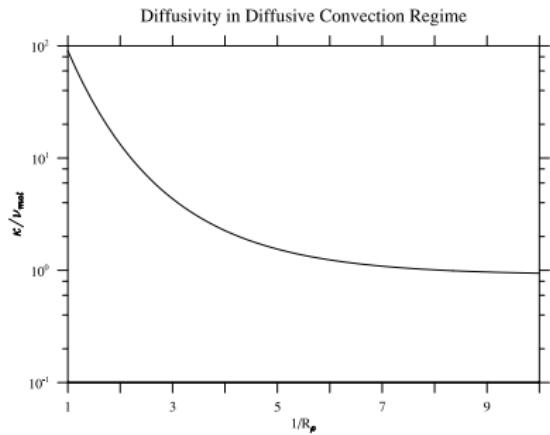
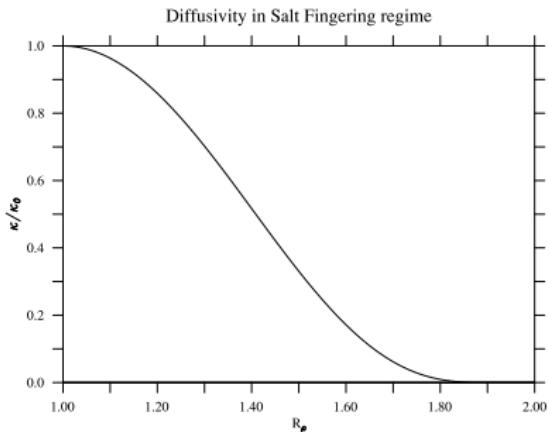
where  $\alpha$  is the thermal expansion coefficient and  $\beta$  is the haline contraction coefficient:

- ① Salt Fingering ( $\partial S / \partial z > 0$  and  $1 < R_\rho < R_\rho^0$ ); salt water above fresher water  $\Rightarrow$  salt water will sink
- ② Diffusive Convective Instability ( $\partial \Theta / \partial z < 0$  and  $0 < R_\rho < 1$ ); cold water above warm water  $\Rightarrow$  cold water will sink

## And that's not all...

Double diffusion also introduces idea of different diffusivity for temperature and salinity ( $\kappa_\Theta$  and  $\kappa_S$ , respectively).

# Double Diffusion Mixing



Diffusivity profiles for the two regimes (Fig. 4 in [LMD94](#)).

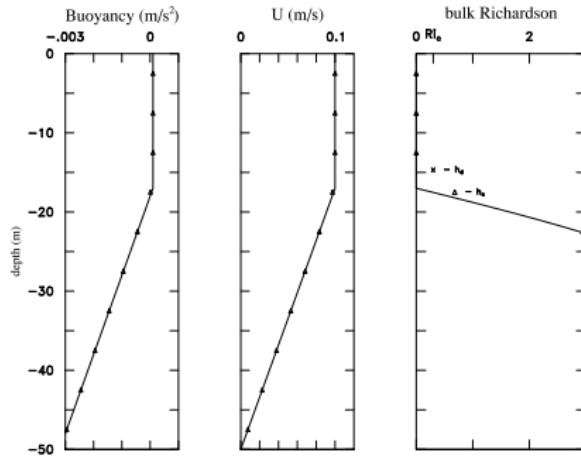
## Salt-fingering regime

$$\begin{aligned}\kappa_S &= \kappa_0 \left[ 1 - \left( \frac{R_\rho - 1}{R_\rho^0 - 1} \right)^{p_1} \right]^{p_2} \\ \kappa_\Theta &= 0.7 \kappa_S\end{aligned}$$

## Diffusive convective regime

$$\kappa_\Theta = \nu_{\text{mol}} \cdot c_1 \exp \left( c_2 \exp \left[ c_3 \frac{1 - R_\rho}{R_\rho} \right] \right)$$
$$\kappa_S = \max(0.15R_\rho, 1.85R_\rho - 0.85)\kappa_\Theta$$

# KPP Mixing



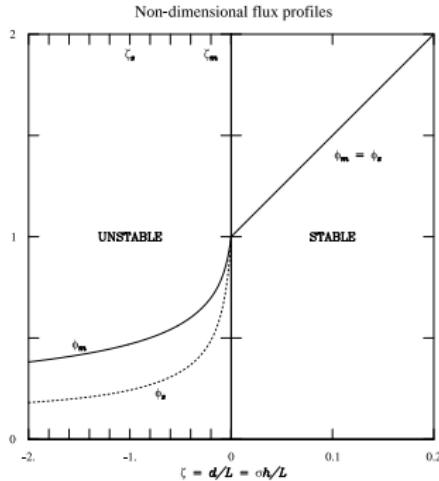
Bouyancy, velocity, and bulk Richardson values (Fig. C1 in LMD94).

The boundary layer depth ( $h$ ) computed based on bulk Richardson number

$$Ri_b(z) = \frac{-z(B_r - B(z))}{|\mathbf{V}_r - \mathbf{V}(z)|^2 + \mathbf{V}_t^2(z)}$$

$\mathbf{V}_t$  is unresolved velocity shear, see Eq. (23) in LMD94.

# KPP Mixing



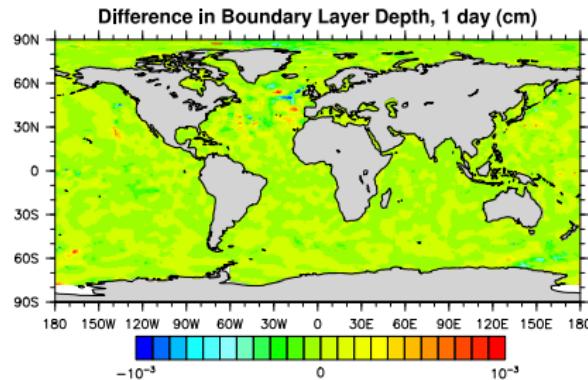
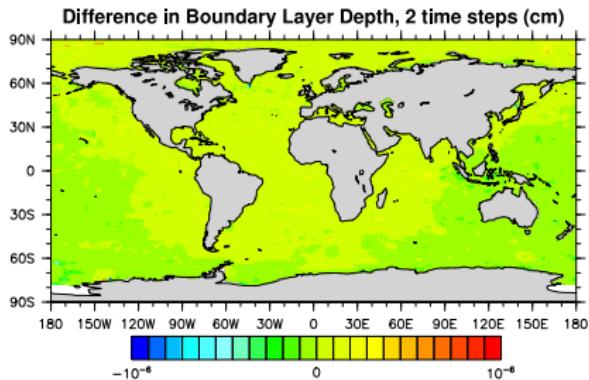
Flux profiles  $\phi$  (Fig. B1 in [LMD94](#)).

Inside the boundary layer, diffusivity is given by

$$\nu | \kappa = h w_{m|s}(-z/h) G(-z/h)$$

$w_{m|s}$ , the turbulent velocity scale for momentum or scalar quantities, is inversely proportional to  $\phi_{m|s}$ ;  $G$  is a shape function defined to ensure a smooth  $\kappa$ .

# CVMix in POP



POP vs POP+CVMix (slide out of date)

## What part of CVMix is available in POP?

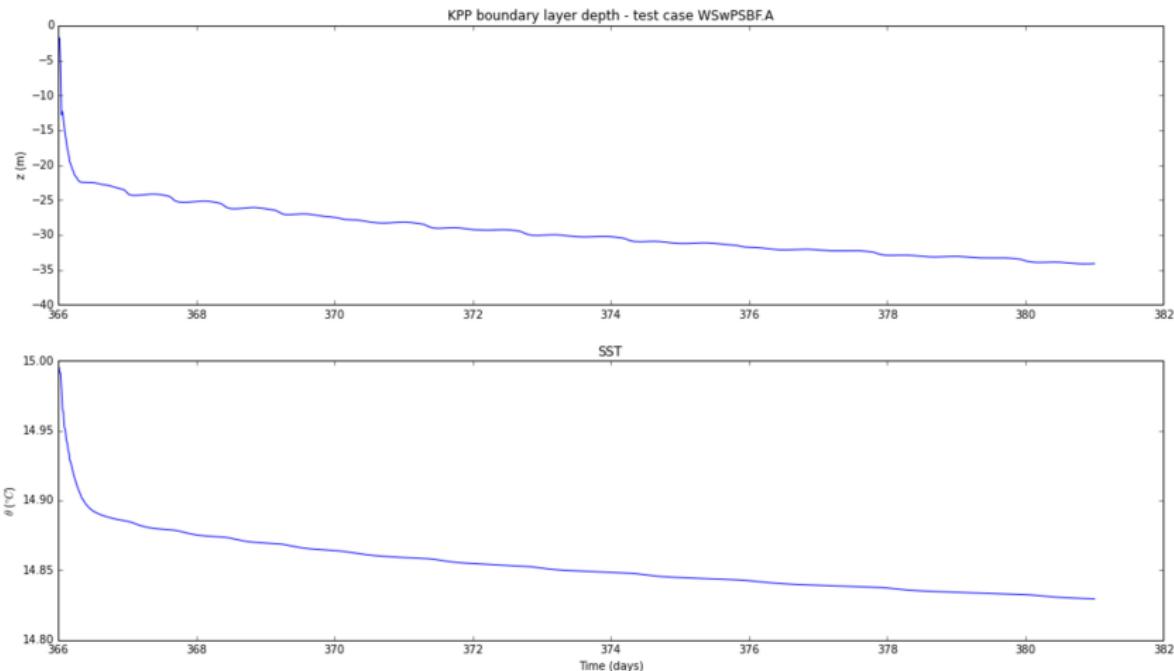
- Just used in KPP boundary layer (no internal mixing yet)
  - ① CVMix is used to compute bulk Richardson number and boundary layer depth
  - ② POP computes internal mixing coefficients
  - ③ CVMix updates mixing coefficients inside boundary layer

# An Idealized Testcase for 1D Mixing

## Testcase setup

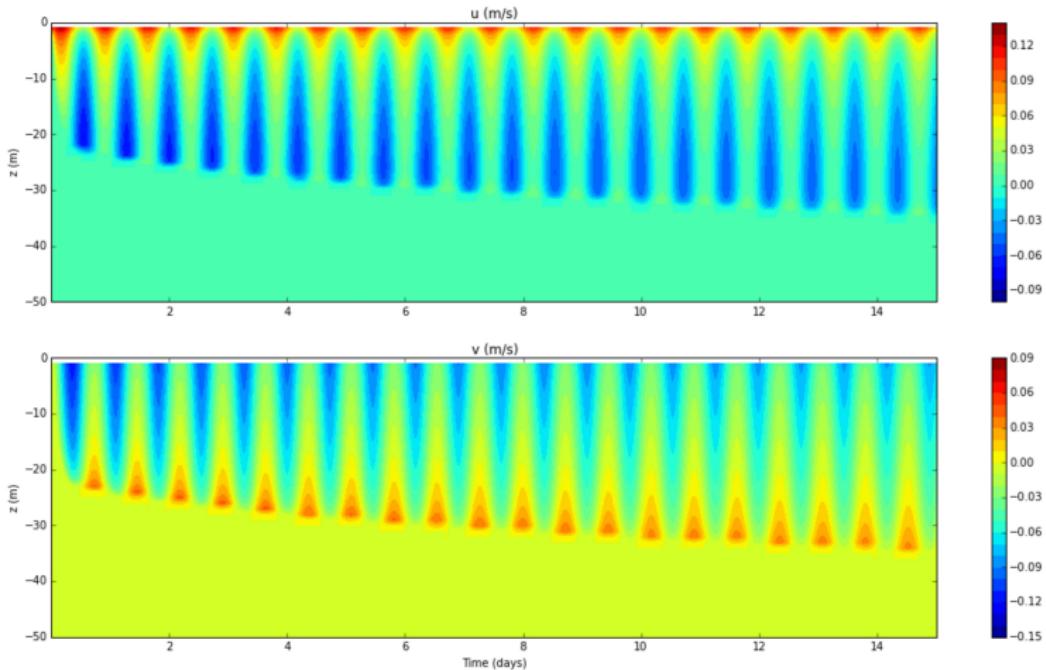
- 400 m column of water, 1m vertical resolution ( $\Rightarrow$  400 levels)
- Initial conditions
  - Temperature is  $15^\circ$  at surface and  $11^\circ$  at bottom (decreasing linearly)
  - Salinity is 35 psu throughout
  - Velocities ( $u, v$ ) are set to 0
- Surface forcing:
  - Wind stress is  $0.1 \text{ N/m}^2$  in zonal direction, 0 meridional
  - Surface heat flux is 0  $\text{W/m}^2$
- Coriolis:  $f = 10^{-4} \text{ sec}^{-1}$
- No mixing except for KPP
- Run for 15 days with 20 minute time step

# Output - Boundary Layer Depth and SST



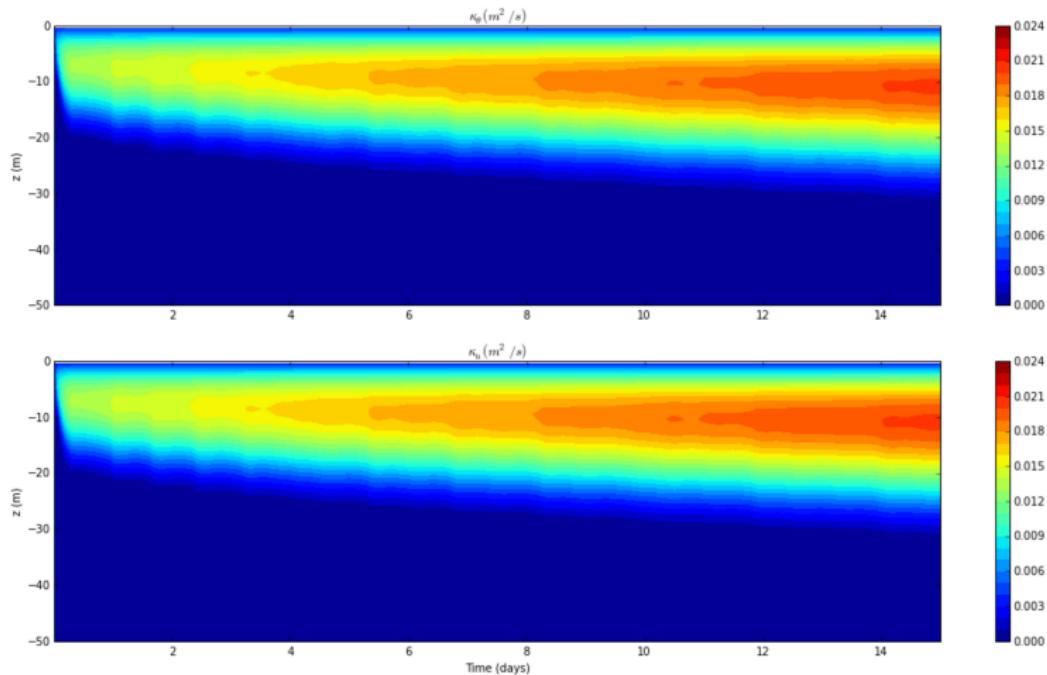
Top - boundary layer depth; Bottom - SST

# Output - Velocity



Top - zonal velocity; Bottom - meridional velocity

# Output - Diffusivity



Top - Temperature diffusivity; Bottom - momentum diffusivity

## Lab Exercises

# Filling in Specifics from an Earlier Slide

## First step for running CESM

Run the following from \$CESMROOT/scripts:

```
(1) ./create_newcase -case $CASEDIR/$CASENAME -compset  
$COMPSET -res $RESOLUTION -mach $MACHINE
```

## Variable definitions

- \$CESMROOT = /home/mlevy/codes/cesm1\_2\_2.cvmix
- \$CASEDIR is up to you, but I recommend something like ~cases/
- \$CASENAME is also up to you, but be descriptive
  - Pro tip: Useful to include compset and resolution
- \$COMPSET = C
- \$MACHINE = argo
- \$RESOLUTION varies – global experiments use T62\_g37 (nominal ocean resolution of 3°, displaced pole); 1D experiments use 1D\_1D

# A Little Diversion Regarding Resolutions

## Understanding the ‘-res’ option

- CESM assumes you are running components on two grid
  - ① Atmosphere and land models share a grid
  - ② Ocean and sea ice share a grid
- Specify resolution of the form `[atm]-[ocn]`
- You can run the atmosphere and land on different grids by specifying `[atm]-[lnd]-[ocn]` but ocean and sea ice MUST use same grid
- The ‘production’ ocean grid is `g16`, nominal  $1^\circ$  displaced pole but the  $3^\circ$  grid is much cheaper  $\Rightarrow$  better for testing / teaching
- The `1D` ocean grid is not part of the CESM release – Gokhan and I created it to make it easier to test CVMix
  - Turns off horizontal mixing / other horizontal forcings
  - Tracers and velocity are collocated (staggered in global resolution)
  - Uses linear equations of state
- `T62` is the “native” resolution of atmospheric forcing data

# Effect of 1D Resolution on Namelist

## KPP namelist in global resolution

```
&vmmix_kpp_nml
bckgrnd_vdc1 = 0.16
bckgrnd_vdc2 = 0.0
bckgrnd_vdc_ban = 1.0
bckgrnd_vdc_dpth = 1000.0e02
bckgrnd_vdc_eq = 0.01
bckgrnd_vdc_linv = 4.5e-05
bckgrnd_vdc_psim = 0.13
lcheckekmo = .false.
lcvmix = .false.
```

ldbldiff = .true.
lhoriz_varying_bckgrnd = .true.
linertial = .false.
llangmuir = .false.
lrich = .true.
lshort_wave = .true.
num_v_smooth_ri = 1
prandtl = 10.0
rich_mix = 50.0
/

# Effect of 1D Resolution on Namelist

## KPP namelist in single column resolution

```
&vmix_kpp_nml
bckgrnd_vdc1 = 0.0
bckgrnd_vdc2 = 0.0
bckgrnd_vdc_ban = 0.0
bckgrnd_vdc_dpth = 0.0
bckgrnd_vdc_eq = 0.0
bckgrnd_vdc_linv = 4.5e-05
bckgrnd_vdc_psim = 0.0
lcheckekmo = .false.
lcvmix = .false.
```

ldbl\_diff = .false.  
lhoriz\_varying\_bckgrnd = .false.  
linertial = .false.  
llangmuir = .false.  
lrich = .false.  
lshort\_wave = .true.  
num\_v\_smooth\_ri = 1  
prandtl = 10.0  
rich\_mix = 50.0  
/

# Effect of 1D Resolution on Namelist

Also added a new namelist

```
&pop1d_nml  
global_shf_coeff = 0.0  
global_taux = 0.1  
lcompute_coriolis = .false.  
single_col_coriolis = 0.0001  
single_col_lat = 0.0  
single_col_lon = 0.0  
/
```

<b>Description</b>
Surface heat flux ( $\text{W}/\text{m}^2$ )
$\tau_x$ ( $\text{N}/\text{m}^2$ )
if true, $f = 2\Omega \sin(\theta)$
otherwise, this is $f$
latitude of single column
longitude of single column
(must match domain file!)

## Apologies

I should not have used `global_*` for variable names, that's a terrible convention! The first implementation of 1D model was actually run on a  $3^\circ$  grid producing identical columns; I should have changed these to `single_col_*` for the new grid.

# Configuring and Building Your Case

## Issue commands from \$CASEDIR

- ① Run `./cesm_setup`
- ② Make build-time changes
  - CESM build settings are in `env_build.xml`
  - Can modify CESM component source code by copying module to `SourceMods/src.[comp]/` and editing in your case directory
- ③ Build the model by running `./$CASENAME.build`
- ④ Make run-time changes
  - Component namelists are changed by adding entries to `user_nl_[comp]` (after change run `preview_namelists`)
  - Read-only copies of component namelists in `CaseDocs/` (named `*_in`)
  - CESM settings are in `env_run.xml`  
*Pro tip: You don't need to edit the text file directly! Instead run `./xmlchange VARIABLE=new_value`*
- ⑤ Run the model with `./$CASENAME.submit`
  - Output will be in `~/scratch/$CASENAME/run`

# Running on argo

## Logging in

Two step process:

- ① ssh -XY [username]@ssh.ictp.it
- ② ssh -XY argo.ictp.it

## Parallel jobs

- We have access to the esp\_guest queue
  - 4 nodes ⇒ only 4 jobs running simultaneously
  - Run showfree esp\_guest to see how many nodes are available
  - Run qstat -u \$USERNAME to see the status of your jobs  
Q for "in the queue", R for "running"
  - Run qstat -r esp\_guest to see what is running in the guest queue
- Most exercises should run in 5 or 10 minutes
- Short runtime + single node job means we can also squeeze into testing queue (1 more node)

# ODTÜ Wi-Fi Password

## Connecting to the wireless

Network name: ng2k

Username: ozsoy

Password: ozzo123

# Visualization Tips

## Loading tools on argo

- ncview should be in your path by default
- Run `module load nco` to add the netCDF operators – we specifically want `ncdiff` to look at differences between two cases
- For 1D: there is a very basic NCL script in  
`/home/mlevy/1D_scripts`
  - ① Copy to your home directory and edit case name.
  - ② Before you run for the first time, run `module load ncl`
  - ③ execute with `ncl 1D\ visualization.ncl`

## Looking at output locally

- If you have ipython on your laptop, there is a notebook designed for looking at 1D output available via git by cloning  
`git@github.com:mnlevy1981/1D_POP_output_ICTP.git`

# Visualization Tips

## Variables of interest

- `HBLT` – Boundary layer depth
- `RI_BULK` – Bulk Richardson number
- `VVC`, `VDC_T`, `VDC_S` – Diffusivities (momentum, temperature, salinity)
- `TEMP`, `SALT`, `UVEL`, `VVEL` – Temperature, salinity, velocity components

## Default output (resolution-dependent)

- Look in `~/scratch/$CASENAME/run/`
- Global exercises
  - Monthly average of 3D fields
  - Output stored in `$CASENAME.pop.h.0001-01.nc`
- Single column exercise
  - Output every timestep (20 minutes)
  - Output stored in `$CASENAME.pop.h.0001-01-02-01200.nc`

# Exercise #1 – Global Control

## About the test

In this test, we run a global ocean model for one month.

- ① Create a new case using the following settings
  - ① Component Set: *C*
  - ② Resolution: *T62\_g37*
- ② The default simulation is 5 days long, change this to 1 month:  
`./xmlchange STOP_N=1,STOP_OPTION=nmonths`
- ③ Build and run the model

## Exercise #2 – Use CVMix for KPP

### About the test

In this test, we use the CVMix library's version of KPP instead of the POP-specific implementation.

- ① Create a clone of your case from exercise #1 (See next slide!)
- ② Make the necessary change to `user_nl.pop2` to enable CVMix for the boundary layer computation

*Hint: look for `lcvmix` in `CaseDocs/pop2_in`*

- ③ Build and run the model for one month. Verify cloning the case brought over the changes from `env_run.xml` by running

```
./xmlquery STOP_N,STOP_OPTION
```

- ④ How are the results different from those of exercise #1?

*Note: In the POP history files, the variable HBLT is boundary layer depth. What other variables might be interesting to look at?*

# How to Use create\_clone

- ① Instead of `./create_newcase`, run  
`./create_clone -clone $CASEDIR/$OLDCASENAME -case $CASEDIR/$NEWCASENAME`  
Copies `env_*.xml` and `user_nl_*`
- ② In `$CASEDIR/$NEWCASENAME`, run `./cesm_setup`
- ③ Time-saving hint: if you are not making changes to the source code, you can use the same executable (otherwise you need to run `$NEWCASENAME.build`). To re-use the executable:
  - ① In `$CASEDIR/$OLDCASENAME`, run `./xmlquery EXEROOT` and copy the executable directory to your clipboard
  - ② In `$CASEDIR/$NEWCASENAME`, run `./xmlchange EXEROOT=[copied directory]`
  - ③ In `$CASEDIR/$NEWCASENAME`, run `./xmlchange BUILD_COMPLETE=TRUE`

# Exercise #3 – 1D Control

## About the test

In this test, we run a single column ocean test for 15 days using the CVMix KPP routines. There is no surface heat flux and the windstress is specified by  $(\tau_x, \tau_y) = (0.1, 0)$  N/m<sup>2</sup>

- ① Create a new case using the following settings
  - ① Component Set: *C*
  - ② Resolution: *1D\_1D*
- ② The default simulation is 5 days long, change this to 16 days:  
`./xmlchange STOP_N=16`  
NOTE: this only runs POP for 15 days
- ③ The default option uses POP's KPP routines, edit `user_nl_pop2` to use CVMix's routines instead
- ④ Build and run the model

# Exercise #4 – Change $\tau_x$ and Surface Heat Flux

## About the test

In this test, we remove the wind stress but apply strong cooling at the surface (heat flux =  $-100 \text{ W/m}^2$ ).

- ① Create a clone of your case from exercise #3
- ② Make the necessary change to `user_nl_pop2` to set zonal surface wind stress to  $0 \text{ N/m}^2$  and surface heat flux to  $-100 \text{ W/m}^2$   
*Hint: look for `global_taux` and `global_shf_coeff` in `CaseDocs/pop2.in`*
- ③ Build and run the model for 16 days
- ④ How are the results different from those of exercise #3?

# Exercise #5 – Change $\tau_x$ and Surface Heat Flux (again)

## About the test

In this test, we keep the  $0.1 \text{ N/m}^2$  wind stress and also apply a strong surface heat flux ( $100 \text{ W/m}^2$ ).

- ① Create a clone of your case from exercise #3
- ② Make the necessary change to `user_nl_pop2` to set surface heat flux to  $100 \text{ W/m}^2$
- ③ Build and run the model for 16 days
- ④ How are the results different from those of exercise #3 and #4?

# Running CVMix Without an Ocean Model

## Setup (argo or your local machine)

- Clone git repository at `git@github.com:CVMix/CVMix-src.git`
- Build by running `make` (or `make netcdf`) from `src/`
- First time you build, you will be prompted for compiler name and netcdf location. On argo:
  - First run `module load intel netcdf/4.3.1/intel/2013`
  - Compiler is ifort and location of nc-config is  
`/opt/netcdf/4.3.1/intel/2013/bin`
- Successful build ⇒ run pre-set tests in `reg_tests`
- No MPI needed means no waiting in the queue

## Caveat

CVMix does not solve equations of state or do any time stepping – it just tests that “correct” diffusivities are produced for specific parameter specifications

# Homework – Bring CVMix to your Model

## If you are interested

- POP source code is in `$CESMR0OT/models/ocn/pop2/source/`
- Main mixing driver is `vertical_mix.F90`; KPP is in `vmix_kpp.F90`
- Look for “call cvmix\_” in the KPP code
  - ① `call cvmix_init_kpp` initializes KPP module
  - ② `call cvmix_kpp_compute_OBL_depth` computes depth of ocean boundary layer
  - ③ `call cvmix_coeffs_kpp` computes diffusivity coefficients
- To compute boundary layer depth, need bulk Richardson number (`cvmix_kpp_compute_bulk_Richardson` function)
- Need to massage model data into CVMix data type
  - See `cvmix_data_type` structure, defined in `cvmix/cvmix_kinds_and_types.F90`
  - POP uses `cvmix_put`, but data type can also use pointers instead of memory copy
- Probably easier to start with non-KPP module...

## References

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