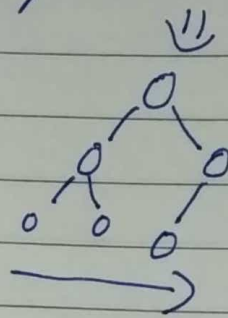


Heap

Heap is a complete binary tree that comes with a heap order property.

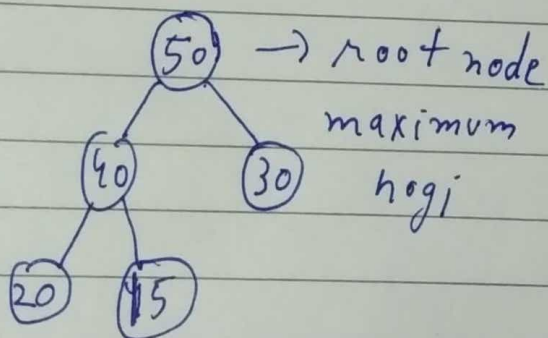
every level is completely filled except last level

nodes added from left (lean towards left)

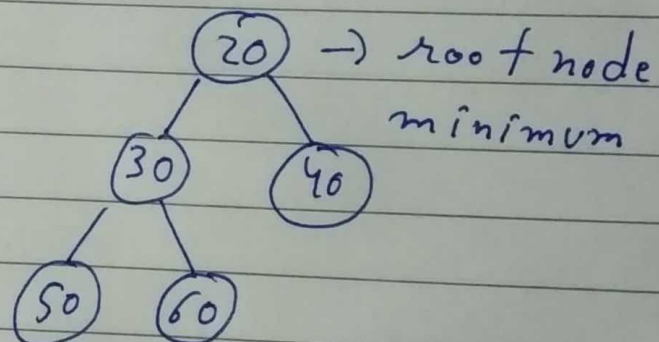


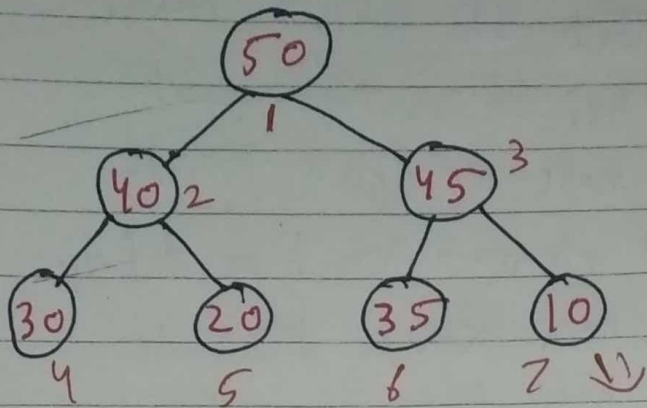
Tab bhi Koi node add Karni hai to left me dalege phle

Max heap



Min heap





Node $\rightarrow i$
 Parent $(i) \rightarrow (i/2)$
 left child $(i) \rightarrow 2 * i$
 right child $(i) \rightarrow 2 * i + 1$

Insertion:-

X	40	45	30	20	35	10	
0	1	2	3	4	5	6	

(50 insert
karna
bhl
gya)

```
void insert (A[], n, value)
{
```

```
    n = n + 1;
```

```
    A[n] = value;
```

```
    int i = n;
```

```
    while (i > 1)
    {
```

```
        int parent = i / 2;
```

```
        if (A[parent] < A[i])
```

```
        {
            swap (A, parent, i);
```

```
            i = parent;
```

```
        }
```

```
    }
```

```
    {
```

```
        return;
```

```
    }
```

```
}
```

```
}
```

\rightarrow element ko sabse phle last me dal do

parent

\rightarrow element ka ~~parent~~ find kija

\rightarrow kya parent element se chota hai

\rightarrow to swap kardo
ab agar swap kardiya
to ab phir yahi
condition check
karo

Deletion:-

```
void delete (A[], n)
{
```

```
    A[1] = A[n]; → last element ko 1 pe dal diya
    n = n-1;
    i = 1;
    while (i < n)
    {
```

Jab bhi delete karna hai to matlab root node ko delete karege

ab check karege kya se max heap hai ya nahi

left or right me se jo larger hai wo a gya

```
        int left = A[2*i];
        int right = A[2*i+1];
        int larger = left > right ? 2*i : 2*i+1;
        if (A[i] < A[larger]) → agar larger bda hai
        {
            swap(A, i, larger);
            i = larger;
        }
        else
        {
            return;
        }
    }
}
```

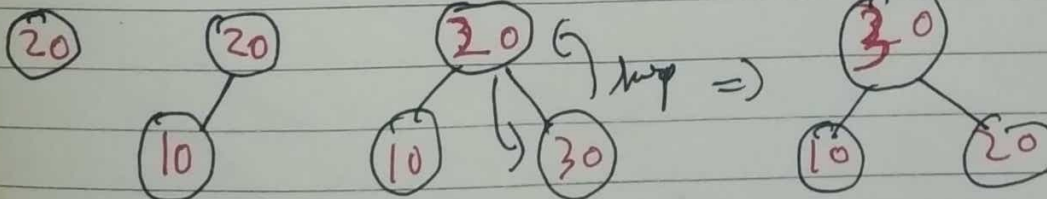
parent se to swap kardo phir heap wali property ko check karte raho

→ Heapify method to build a Max heap

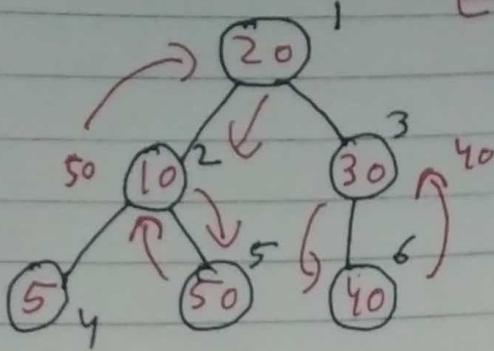
20 10 30 5 50 40

→ apko input me ek array milega jise heap me convert karo

Time complexity → $O(n \log n)$



1	2	3	4	5	6
20	10	30	5	50	40
0	1	2	3	4	5



Time complexity $\rightarrow O(n)$

$$\frac{6}{2} = 3$$

```

buildHeap (int a[], int n) {
    for (int i = n/2; i > 0; i--)
    {
        heapify(a, n, i);
    }
}

```

$\frac{n}{2}$ se n tak ki jo nodes hai unhe process karne ki jarurat nahi kyunki wo leaf nodes hai ham uske phle ki nodes ko

check karege

```

Void heapify (int a[], int n, int i)
{
    int largest = i;  $\rightarrow$  node
    int l = 2 * i;  $\rightarrow$  uske childrens
    int r = 2 * i + 1;
    if (l <= n && a[l] > a[largest]) {
        largest = l;  $\rightarrow$  comparing with left child
    }

```

```

    if (r <= n && a[r] > a[largest]) {
        largest = r;  $\rightarrow$  comparing with right child
    }

```

```

    if (largest != i) {
        swap(a, i, largest);  $\rightarrow$  swap kardo
        heapify(a, n, largest);  $\rightarrow$  phirse is function ko call karo
    }
}

```