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Auf. 6.3
a)
(define (append x y)
        (cond [ (empty? x) y]
              [(cons? x) (cons (first x) (append (rest x) y))]))
a) (append empty l) = l für alle Listen l
(append empty l)
EFUN
= (cond [ (empty? empty) l]
        [ (cons? empty) (cons (first empty) (append (rest empty) l)) ])
PRIM, ERED, EKONG
= (cond [#true l]
        [ (cons? empty) (cons (first empty) (append (rest empty) l)) ] )
COND-true, ERED
= 1
b)
(appendlempty)≡lfür alle Listen l.
• Induktionsanfang (Basisfall): l = empty
Zu zeigen: (append empty empty) \equiv empty
(append empty empty)
EFUN
= (cond [ (empty? empty) empty]
        [ (cons? empty) (cons (first empty) (append (rest empty) empty)) ] )
PRIM, ERED, EKONG
= (cond [#true empty]
        [ (cons? empty) (cons (first empty) (append (rest empty) empty)) ])
COND-true, ERED
\equiv empty
• Induktionsannahme: (append lst1 empty) \equiv lst1, lst2 \equiv (cons head lst1)
• Induktionschritt:
Zu zeigen: (append lst2 empty) \equiv lst2
(append lst2 empty)
EFUN, EKONG
= (cond [(empty? (cons head lst1)) empty]
        [(cons? (cons head lst1)) (cons (first (cons head lst1)) (append (rest (cons head lst1)) empty))
1))
PRIM, ERED, EKONG
= (cond [#false empty]
        [(cons? (cons head lst1)) (cons (first (cons head lst1)) (append (rest (cons head lst1)) empty))
1))
COND-false, ERED
= (cond [ (cons? (cons head lst1)) (cons (first (cons head lst1)) (append (rest (cons head lst1)) empty))
1))
STRUCT-predtrue, EKONG
= (cond [#true (cons (first (cons head lst1)) (append (rest (cons head lst1)) empty)) ] ))
COND-true, ERED
= (cons (first (cons head lst1)) (append (rest (cons head lst1)) empty))
PRIM, ERED, EKONG
\equiv (cons head (append lst1 empty))
Induktionsannahme, EKONG
\equiv (cons head lst1)
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Induktionsannahme, PRIM
\equiv lst2
Damit ist bewiesen: (append l empty) ≡ l für alle Listen l.
c)
(append (cons x l1) l2) \equiv (cons x (append l1 l2)) für alle x und alle Listen l1, l2.
• Induktionsanfang (Basisfall): l1 ≡ empty
Zu zeigen: (append (cons x empty) l2) = (cons x (append empty l2))
(append (cons x empty) l2)
EFUN
\equiv (cond [ (empty? (cons x empty)) | 12]
        [ (cons? (cons x empty)) (cons (first (cons x empty)) (append (rest (cons x empty)) | 1)) ] )
PRIM, ERED, EKONG
= (cond [#false l2]
        (cons? (cons x empty)) (cons (first (cons x empty)) (append (rest (cons x empty)) (1)) (1)
COND-false, ERED
\equiv (cond [ (cons? (cons x empty)) (cons (first (cons x empty)) (append (rest (cons x empty)) | 2)) ])
STRUCT-predtrue, EKONG
\equiv (cond [#true (cons (first (cons x empty)) (append (rest (cons x empty)) | 2)) ])
COND-true, ERED
\equiv (cons (first (cons x empty)) (append (rest (cons x empty)) | 12))
PRIM, ERED, EKONG
\equiv (cons x (append empty 12))
• Induktions annahme: (append (cons x l0) l2) \equiv (cons x (append l0 l2)), l1 \equiv (cons z l0)
• Induktionsschritt:
Zu zeigen: (append (cons x l1) l2) \equiv (cons x (append l1 l2))
(append (cons x l1) l2)
EFUN
\equiv (cond [ (empty? (cons x l1)) l2]
        [ (cons? (cons x l1)) (cons (first (cons x l1))(append (rest (cons x l1)) l2))])
PRIM, ERED, EKONG
= (cond [#false 12]
        [ (cons? (cons x l1)) (cons (first (cons x l1))(append (rest (cons x l1)) l2))])
COND-false, ERED
\equiv (cond [ (cons? (cons x l1)) (cons (first (cons x l1))(append (rest (cons x l1)) l2))])
STRUCT-predtrue, EKONG
\equiv (cond [#true (cons (first (cons x l1)) (append (rest (cons x l1)) l2)) ])
COND-true, ERED
\equiv (cons (first (cons x l1)) (append (rest (cons x l1)) l2))
PRIM, ERED, EKONG
\equiv(cons x (append l1 l2))
Damit ist bewiesen: (append (cons x l1) l2) \equiv (cons x (append l1 l2)) für alle x und alle Listen l1, l2.
(append l1 (append l2 l3)) ≡ (append (append l1 l2) l3) für alle Listen l1, l2, l3
• Induktionsanfang (Basisfall): l1 ≡ empty
Zu Zeigen: (append empty (append l2 l3)) ≡ (append (append empty l2) l3)
(i) (append empty (append 12 13))
EFUN
= (cond [(empty? empty) (append l2 l3)]
[ (cons? empty) (cons (first empty) (append (rest empty) (append 12 l3))) ] )
PRIM, ERED, EKONG
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\equiv (cond [#true (append 12 13)]
[ (cons? empty) (cons (first empty) (append (rest empty) (append l2 l3))) ] )
COND-true, ERED
= (append 12 13)
(ii) (append (append empty 12) 13)
Teilaufgabe (a), ERED
= (append 12 13)
ETRANS
(append empty (append 12 13)) \equiv (append (append empty 12) 13) \equiv (append 12 13)
• Induktionsannahme: (append 10 (append 12 13)) \equiv (append (append 10 12) 13), 10 \equiv (cons z 11)
• Induktionsschritt:
Zu zeigen: (append 10 (append 12 13)) = (append (append 10 12) 13)
(i) (append 10 (append 12 13))
EFUN, EKONG
\equiv (cond [ (empty? (cons z l1)) (append l2 l3)]
        [ (cons? (cons z l1)) (cons (first (cons z l1)) (append (rest (cons z l1)) (append l2 l3))) ] )
PRIM, ERED, EKONG
\equiv (cond [#false (append 12 13)]
        [ (cons? (cons z l1)) (cons (first (cons z l1)) (append (rest (cons z l1)) (append l2 l3))) ] )
COND-false, ERED
\equiv (cond [ (cons? (cons z l1)) (cons (first (cons z l1)) (append (rest (cons z l1)) (append l2 l3))) ])
STRUCT-predtrue, EKONG
\equiv (cond [#true (cons (first (cons z l1)) (append (rest (cons z l1)) (append l2 l3))) ])
COND-true, ERED
\equiv (cons (first (cons z l1)) (append (rest (cons z l1)) (append l2 l3)))
PRIM, ERED, EKONG
\equiv (cons z (append 10 (append 12 13)))
Induktionsannahme, EKONG
\equiv (cons z (append (append 10 l2) l3))
(ii) (append (append 10 l2) l3)
EFUN, EKONG
\equiv (cond [ (empty? (append (cons z l1) l2)) l3]
        [ (cons? (append (cons z l1) l2)) (cons (first (append (cons z l1) l2))
                (append (rest (append (cons z l1) l2)) l3)) ])
PRIM, ERED, EKONG
\equiv (cond [#false 13]
        [ (cons? (append (cons z l1) l2)) (cons (first (append (cons z l1) l2))
                (append (rest (append (cons z l1) l2)) l3)) ])
COND-false, ERED
\equiv (cond [ (cons? (append (cons z l1) l2)) (cons (first (append (cons z l1) l2))
                (append (rest (append (cons z l1) l2)) l3)) ])
STRUCT-predtrue, EKONG
\equiv (cond [#true (cons (first (append (cons z l1) l2))
                (append (rest (append (cons z l1) l2)) l3)) ])
COND-true, ERED
\equiv (cons (first (append (cons z l1) l2))
                 (append (rest (append (cons z l1) l2)) l3))
Teilaufgabe (c), EKONG
\equiv (cons (first (cons z (append 10 12)))
                (append (rest (cons z (append l0 l2))) l3))
PRIM, ERED, EKONG
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≡ (cons z (append (append l0 l2) l3))
ETRANS
(append l0 (append l2 l3)) ≡ (append (append l0 l2) l3) ≡ (cons z (append (append l0 l2) l3))
Damit ist bewiesen: (append l1 (append l2 l3)) ≡ (append (append l1 l2) l3) für alle Listen l1, l2, l3.
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