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import numpy as np

def relu(x): return np.maximum(0, x)

def relu_deriv(x): return np.where(x > 0, 1, 0)

def calculate_error(target, prediction): return np.mean((target - prediction) ** 2)

class RNNModel:
    def __init__(self, in_size, hid_size, out_size):
        self.hid_size = hid_size
        self.W_input = np.random.randn(hid_size, in_size) * 0.05
        self.W_hidden = np.random.randn(hid_size, hid_size) * 0.05
        self.W_output = np.random.randn(out_size, hid_size) * 0.05
        self.b_hidden = np.zeros((hid_size, 1))
        self.b_output = np.zeros((out_size, 1))

        def step_forward(self, x, h_prev):
            x = x.reshape(-1, 1)
            h = relu(np.dot(self.W_input, x) + np.dot(self.W_hidden, h_prev) + self.b_hidden)
            y = np.dot(self.W_output, h) + self.b_output
            return h, y

        def full_forward(self, sequence):
            h = np.zeros((self.hid_size, 1))
            self.h_cache = [h]
            self.input_cache = sequence
            outputs = []

            for x in sequence:
                h, y = self.step_forward(x, h)
                self.h_cache.append(h)
                outputs.append(y)

            return outputs

        def compute_gradients(self, targets, outputs):
            d_W_input = np.zeros_like(self.W_input)
            d_W_hidden = np.zeros_like(self.W_hidden)
            d_W_output = np.zeros_like(self.W_output)
            d_b_hidden = np.zeros_like(self.b_hidden)
            d_b_output = np.zeros_like(self.b_output)

            dh_next = np.zeros((self.hid_size, 1))
            total_error = 0

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        for t in reversed(range(len(self.input_cache))):
            y_true = targets[t].reshape(-1, 1)
            y_pred = outputs[t]
            total_error += calculate_error(y_true, y_pred)

            dy = y_pred - y_true
            d_W_output += np.dot(dy, self.h_cache[t + 1].T)
            d_b_output += dy

            dh = np.dot(self.W_output.T, dy) + dh_next
            dh_raw = relu_deriv(self.h_cache[t + 1]) * dh

            x = self.input_cache[t].reshape(-1, 1)
            d_W_input += np.dot(dh_raw, x.T)
            d_W_hidden += np.dot(dh_raw, self.h_cache[t].T)
            d_b_hidden += dh_raw

            dh_next = np.dot(self.W_hidden.T, dh_raw)

    return d_W_input, d_W_hidden, d_W_output, d_b_hidden,
           d_b_output, total_error / len(self.input_cache)

    def update_weights(self, gradients, lr):
        d_W_input, d_W_hidden, d_W_output, d_b_hidden, d_b_output, _ =
            gradients
        self.W_input -= lr * d_W_input
        self.W_hidden -= lr * d_W_hidden
        self.W_output -= lr * d_W_output
        self.b_hidden -= lr * d_b_hidden
        self.b_output -= lr * d_b_output

def generate_sine_data(seq_length): x = np.linspace(0, 2 * np.pi, seq_length + 1)
inputs = np.sin(x[:-1]).reshape(-1, 1) targets = np.sin(x[1:]).reshape(-1, 1) return
[inputs[i] for i in range(seq_length)], [targets[i] for i in range(seq_length)]

def train_model(): seq_length = 50 inputs, targets = generate_sine_data(seq_length)

    rnn = RNNModel(in_size=1, hid_size=16, out_size=1)

                                epochs = 3000
                                lr = 0.002

    for epoch in range(epochs):

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        outputs = rnn.full_forward(inputs)
        gradients = rnn.compute_gradients(targets, outputs)
        rnn.update_weights(gradients, lr)
        loss = gradients[-1]
        if epoch % 300 == 0:
            print(f"Cycle {epoch}, Error: {loss:.4f}")

        outputs = rnn.full_forward(inputs)
        print("\nPredictions:")
        for i in range(0, seq_length, 5):
            print(f"Input: {inputs[i][0]:.3f}, Predicted: {outputs[i][0],
                0]:.4f}, Target: {targets[i][0]:.3f}")

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if name == "main": train_model()

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