Multiple Regression(with Polynomial Regression)

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Abstract—Estimating the relationship among different variable which have reason and result relation holds great importance, to estimate that Regression analysis is a statistical technique that is adapted. Main focus of this uni-variate regression is to analyse the relationship between a non linear and a linear variable and to formulate a linear equation between the two. a regression model which contain one linear and multiple non-linear independent variables is most often called multi linear regression. This paper is concentrated on the polynomial regression model, which is useful when there is reason to believe that relationship between two variables is curvilinear. The polynomial regression model has been applied using the characterisation of the connection between strains and drilling depth. Parameters of the model were estimated employing a least square method. After fitting, the model was evaluated using a number of the common indicators wont to evaluate accuracy of regression model.

I. INTRODUCTION

Regression analysis involves identifying the link between a variable quantity and one or more independent variables. It's one amongst the foremost important statistical tools which is extensively utilized in the majority sciences. It's specially used in business and economics to check the link between two or more variables that are related causally. A model of the relationship is hypothesized, and estimates of the parameter values are accustomed develop an estimated equation.

Common questions which are generally asked in this research of Multiple regression analysis generally revolve around "are there any relations between dependent and independent variable?", and "if there are some relations that exist, what is total power of the relation?"," is there any possibility to predict about orientation regarding the dependent variable?', and "if certain conditions are controlled, what influences does a special variable or a group of variables have over another variable or variables?". (Alpar, 2003).

Uni-variate analysis is the regression which uses a single independent variable while multivariate regression analysis uses more than one independent variable (Tabachinick, 1996, Buyukozturk, 2002). The relation between dependent variable and an independent variable is analysed through uni-variate regression analysis, and the equation which represents the linear relationship between the both is formulated.

In Multivariate regression analysis, an attempt is made to account for the variation between the dependent variable and the independent variable synchronically (Unver & Gamgan,

1999). Formulation of Multivariate model is represented in Figure 1.

$$y = \beta_0 + \beta_1 x_1 + \dots + \beta_n x_n + \varepsilon$$

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y - dependent variable X_i - independent variable \beta_i - parameter \varepsilon - error
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Fig. 1. Multivariate Model

The assumptions of multivariate regression analysis are normal distribution, linearity, freedom from extreme values and having no multiple ties between independent variable (Buyukozturk, 2002).

II. MULTIPLE REGRESSION WITH PYTHON

Linear Regression generally is a supervised method for machine learning rooted in statistics. From this method numeric values are forecasted using a combination of predictors which can be both numeric or binary variables. The condition for getting the variable depends on a certain relation at hand (a linear, measurable by a correlation) with the target variable.

However, in reality there are a number of factors which alter the results of the working predictive model. There are usually more than variables that work together to achieve better and reliable results from a prediction. This causes more complexity in our model and hence representing it on a two- dimensional plot is not easy. All the predictors will constitute their own unique dimension and we would have to assume that our predictors apart from being related to the response are also related among themselves and this characteristic of data is called multicollinearity.

A. Multiple Regression Formulation

The basic Multiple Regression is described in Figure 1 and in depth detail is shown in Figure 2 where dependent(response) variable Y on a set of k independent(predictor) variables X_1, X_2, X_k can be expressed as

where

- y_i = value of dependent variable, Y is for ith case.
- x_{ij} = value of jth independent variable, X_j for ith case.

$$\begin{cases} y_1 = \beta_0 + \beta_1 x_{11} + \dots + \beta_k x_{1k} + e_1 \\ y_2 = \beta_0 + \beta_1 x_{21} + \dots + \beta_k x_{2k} + e_2 \\ & \vdots \\ y_n = \beta_0 + \beta_1 x_{n1} + \dots + \beta_k x_{nk} + e_n \end{cases}$$

$$y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_k x_{ik} + e_i$$
, for $i = 1, 2, \dots, n$

Fig. 2. In depth Multiple Regression Model showing relation of independent(k) and dependent variable(Y)

- β_0 is the Y-intercept of the regression surface.
- each β_j , j=1,2,....k, is the slope of the regression surface w.r.t. variable X_j and e_i is the random error component for the *i*th case.

In the first equation we have n observations and k predictors (n > k+1) The assumptions of the multiple regression model are similar to those for the simple linear regression model. Model assumptions [1]:

B. Observations

- errors e_i are normally distributed with their mean as zero and their standard deviation σ are independent of the error terms associated with all other observations. Errors are not related to each other.
- variables X_j in the context of regression analysis are considered as fixed quantities, whereas they are random variables in the context of correlation analysis. But in both the cases X_j are totally independent of the error term. If X_j are assumed as fixed quantities, then we are assuming that we have realizations of k variables X_j and the only randomness in Y is coming from the error term.

In matrix notation, we can rewrite the regression model as described in Figure. 3.

$$Y = X \beta + e$$

Fig. 3. Matrix notation of Model

- response vector ${\bf Y}$ and error vector ${\bf e}$ are the column vectors of length n.
- vector of parameters beta is the column vector of length k+1 and its design matrix (where all elements in the first column are equal to 1, and second column's values are filled by the observed values of X₁,etc).

Here, values of β and e are unknown and assumed.

III. POLYNOMIAL REGRESSION

Polynomial Regression is a technique of Multiple Regression in which we regress a dependent variable on the powers of independent variable.

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Fig. 4. Example of a figure caption.

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REFERENCES

- Aczel, A. D., 1989. Complete Business Statistics. Irwin, p. 1056. ISBN 0-256-05710-8.
- [2] L. Massaron and A. Boschetti, Regression analysis with Python: learn the art of regression analysis with Python. Birmingham Mumbai: Packt Publishing, 2016.

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