Table 1: Chromatogram Feature Definitions

\mathcal{M}_i	The neutral mass of the i th chromatogram
\mathcal{I}_i	The total intensity array assigned to the i th chromatogram
$\mathcal{I}_{i,j}$	The sum of all peak intensities for peaks observed in the j th scan for the i th chromatogram
$\mathcal{I}_{i,j,k}$	The intensity assigned to the k th peak at the j th scan for the i th chromatogram
\mathbf{c}_i	The set of charge states observed for the i th chromatogram
$\mathcal{I}_{i,c=j}$	The total intensity assigned to the i th chromatogram with charge state j
$\mathbf{t}_{i,j}$	The time of the j th scan of the i th chromatogram
$\mathbf{env}_{i,j,k}$	The normalized experimental isotopic envelope composing the k th peak of the j th scan of the i th chromatogram, whose members sum to 1
\mathbf{a}_i	The set of adduction states observed for the i th chromatogram
$\mathcal{I}_{i,a=j}$	The total intensity assigned to the i th chromatogram with adduct j
\hat{g}_i	The glycan composition assigned to the i th chromatogram, or \emptyset if there was no matched glycan composition

1 Chromatographic Feature Evaluation

For each candidate feature, we computed several statistics to estimate how distinguishable the observed signal was from random noise. We use the following quantities from each LC-MS feature:

1.1 Chromatographic Peak Shape

An LC-MS elution profile should be composed of one or more peak-like components, each following a bi-Gaussian peak shape model (Yu and Peng (2010)) or in less ideal chromatographic circumstances, a skewed Gaussian peak shape model. We fit these models using non-linear least squares (NLS). As measures of goodness of fit are not generally available for NLS, we use the following criterion:

$$\hat{y}_{i} = NLS(\mathcal{I}_{i}, \mathbf{t}_{i})$$

$$e_{i,NLS} = \mathcal{I}_{i} - \hat{y}_{i}$$

$$\bar{y}_{i} = \mathbf{t}_{i} \left(\left(\mathbf{t}_{i}^{t} \mathbf{t}_{i} \right)^{-1} \mathbf{t}_{i} \mathcal{I}_{i} \right)$$

$$e_{i,null} = \mathcal{I}_{i} - \bar{y}_{i}$$

$$\mathcal{L}_{i} = 1 - \frac{\sum e_{i,NLS}^{2}}{\sum e_{i,null}^{2}}$$
(1)

where line score describes how much the peak shape fit improves on a ordinary least squares regression linear model.

We apply two competitive peak fitting strategies to address distorted, overlapping, or multimodal elution profiles. The first works iteratively by finding a best-matching peak shape using non-linear least squares, subtracting the fitted signal and checks if there is another peak with at least half as tall as the removed peak, if so repeating the process until no peak can be found, saving each peak model so constructed. The second approach starts by locating local minima between putative peaks, and partitioning the chromatogram into sub-groups which would are fit independently. This method generates a candidate list of minima, and selects the case which has the greatest difference between the minimum and its pair of maxima to split the feature at. The strategy which produces the maximum \mathcal{L}_i is chosen.

1.2 Composition Dependent Charge State Distribution

As the number of monosaccharides composing a glycan increases, the number of possible sites for charge localization increases. Under normal conditions, we would expect to observe the same molecule in multiple charge states (Maxwell et al. (2012)).

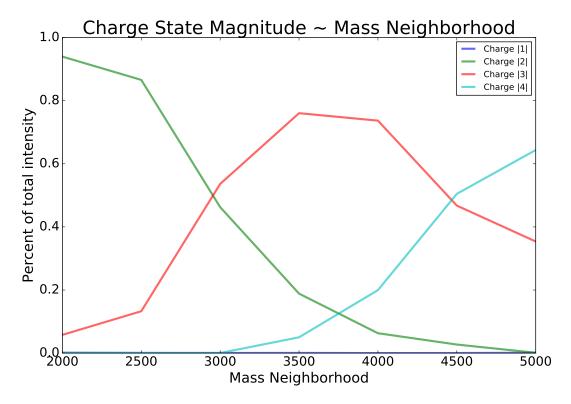


Figure 1: The trend of charge state relative abundance for acidic glycans

Which charge states are expected would depend upon the size of the molecule and it's constituent units' electronegativity. In it's native state, **NeuAc**'s acidic group causes glycans with one or more **NeuAc** to have a propensity for higher negative charge states (Varki and Schauer (2009)). To capture this relationship, we modeled the probability of observing a glycan composition for sialylated and unsialylated compositions separately. For permethylated glycans, charge is carried by protons or metallic cation adducts like sodium, the relationship between acidic monosaccharides and charge state propensities is weaker.

$$m_{i} = (\lfloor (\mathcal{M}_{i}/w)/10 \rfloor + 1) * 10$$

$$\mathcal{H}_{i,j} = \frac{\mathcal{I}_{i,c=j}}{\mathcal{I}_{i}}$$

$$P(c,m) = |m| \sum_{m_{i} \in m} \mathcal{H}_{i,j}$$

$$\mathscr{C}_{i} = \sum_{c_{i,j} \in \mathbf{c}_{i}} P(c_{i,j}, m_{i})$$
(2)

where w is the width of the mass bin divided by 10 and P(c, m) is defined as part of the model estimation procedure.

1.3 Adduction Rate

For the samples AGP-permethylated-2ul-inj-55-SLens and Perm-BS-070111-04-Human-Serum we also include an Adduction Frequency model score \mathcal{A}_i , following the same pattern as the charge state distribution, with the same extension of justification from Maxwell et~al.~(2012). We use one mass scaling model for all glycan compositions as ammmonium adduction is not expected to be composition dependent.

$$\mathcal{H}_{i,j} = \frac{\mathcal{I}_{i,a=j}}{\mathcal{I}_i}$$

$$P(a,m) = |m| \sum_{m_i \in m} \mathcal{H}_{i,j}$$

$$\mathscr{A}_i = \sum_{a_{i,j} \in \mathbf{a}_i} P(a_{i,j}, m_i)$$
(3)

We fit the adduction rate model on AGP-permethylated-2ul-inj-55-SLens in order to make our comparison to third-party data less biased given limited sample data.

1.4 Isotopic Pattern Consistency

Our ahead-of-time deconvolution procedure uses an averagine isotopic model and does not capture the consistency of the isotopic pattern that was fit with the isotopic pattern of the glycan composition that matched that peak. The criterion

$$\mathscr{I}_{i} = 1 - 2\mathcal{I}_{i}^{-t}\mathbf{I}_{i} \sum_{j}^{J} \sum_{k}^{K} \mathcal{I}_{i,j,k} \mathbf{env}_{i,j,k}^{t} \left(\ln \mathbf{env}_{i,j,k} - \ln \mathbf{tid}_{i} \right)$$

$$\tag{4}$$

where **tid** is the theoretical isotopic pattern derived from either \hat{g}_i or an averagine interpolated for \mathcal{M}_i if $\hat{g}_i = \emptyset$. This computes a per-peak intensity weighted mean G-test comparing the goodness of fit between the experimental envelope and the theoretical isotopic pattern.

1.5 Observation Spacing Score

The less time between observations of a glycan composition the less likely the chromatogram is to contain peaks missing or caused by isotopic pattern interference or missing information.

$$\mathscr{T}_i = 1 - 2\mathcal{I}_i^{-t} \mathbf{I}_i \sum_{j=1}^J \mathcal{I}_{i,j} (\mathbf{t}_{i,j} - \mathbf{t}_{i,j-1})$$
(5)

As this feature depends heavily on the speed of the mass spectrometer, a scaling coefficient must be estimated from the data to reduce the penalty on slower instruments.

1.6 Summarization Score

Each scoring feature $\in [\mathcal{L}_i, \mathcal{C}_i, \mathcal{I}_i, \mathcal{I}_i]$ is penalized by $\epsilon = 1e-6$ bounded in the range [0,1), with values below 0 set to ϵ .

$$s_i = \sum_{f_{i,j} \in \text{features}_i} \ln \frac{f_{i,j}}{1 - f_{i,j}} \tag{6}$$

producing a value between $(-\infty, \infty)$. $s_i < 8$ reflects multiple poor feature scores and is unexpected to be real, while $s_i > 15$ is consistent with model expectations.

2 A more complete derivation of $\hat{\phi}$

To obtain the optimal ϕ , we take the partial derivative of ℓ w.r.t ϕ_m

$$0 = \frac{\partial \ell}{\partial \phi_m} \left((\mathbf{s} - \phi_0)^t (\mathbf{s} - \phi_0) + \lambda \left[\phi_o - \tau_o, \quad \phi_m - \tau_m \right] \begin{bmatrix} \mathbf{L_{oo}} & \mathbf{L_{om}} \\ \mathbf{L_{mo}} & \mathbf{L_{mm}} \end{bmatrix} \begin{bmatrix} \phi_o - \tau_o \\ \phi_m - \tau_m \end{bmatrix} \right)$$
(7)
$$= \lambda (\phi_o - \tau_o)^t \mathbf{L_{om}} + \lambda \mathbf{L_{mo}} (\phi_o - \tau_o) + \lambda (\phi_m - \tau_m)^t (\mathbf{L_{mm}}^t + \mathbf{L_{mm}})$$

$$= 2\lambda \mathbf{L_{mo}} (\phi_o - \tau_o) + 2\lambda \mathbf{L_{mm}} (\phi_m - \tau_m)$$

$$-\mathbf{L_{mm}} (\phi_m - \tau_m) = \mathbf{L_{mo}} (\phi_o - \tau_o)$$

$$(\phi_m - \tau_m) = -\mathbf{L_{mm}}^{-1} \mathbf{L_{mo}} (\phi_o - \tau_o)$$

$$\hat{\phi}_m = -\mathbf{L_{mm}}^{-1} \mathbf{L_{mo}} (\phi_o - \tau_o) + \tau_m$$

(8)

and w.r.t. ϕ_o

$$0 = \frac{\partial \ell}{\partial \phi_o} \left((\mathbf{s} - \phi_o)^t (\mathbf{s} - \phi_o) + \lambda \left[\phi_o - \tau_o, \quad \phi_m - \tau_m \right] \left[\mathbf{L}_{\mathbf{mo}} \quad \mathbf{L}_{\mathbf{nm}} \right] \left[\phi_o - \tau_o \right] \right)$$

$$= -2\mathbf{s} + 2\phi_o + \lambda \left(\mathbf{L}_{\mathbf{oo}} + \mathbf{L}_{\mathbf{oo}}^t \right) (\phi_o - \tau_o) + \lambda \mathbf{L}_{\mathbf{om}} (\phi_m - \tau_m) + \lambda \mathbf{L}_{\mathbf{mo}}^t (\phi_m - \tau_m)$$

$$= -2\mathbf{s} + 2\phi_o + 2\lambda \mathbf{L}_{\mathbf{oo}} (\phi_o - \tau_o) + 2\lambda \mathbf{L}_{\mathbf{om}} (\phi_m - \tau_m)$$

$$\mathbf{s} = \phi_o + \lambda \left(\mathbf{L}_{\mathbf{oo}} (\phi_o - \tau_o) + \mathbf{L}_{\mathbf{om}} (\phi_m - \tau_m) \right)$$

$$= \phi_o + \lambda \left(\mathbf{L}_{\mathbf{oo}} (\phi_o - \tau_o) + \mathbf{L}_{\mathbf{om}} (-\mathbf{L}_{\mathbf{mm}}^{-1} \mathbf{L}_{\mathbf{mo}} (\phi_o - \tau_o) + \tau_m - \tau_m) \right)$$

$$= \phi_o + \lambda \left(\mathbf{L}_{\mathbf{oo}} (\phi_o - \tau_o) - \mathbf{L}_{\mathbf{om}} \mathbf{L}_{\mathbf{mm}}^{-1} \mathbf{L}_{\mathbf{mo}} (\phi_o - \tau_o) \right)$$

$$\mathbf{s} - \tau_o = \phi_o - \tau_o + \lambda \left(\mathbf{L}_{\mathbf{oo}} (\phi_o - \tau_o) - \mathbf{L}_{\mathbf{om}} \mathbf{L}_{\mathbf{mm}}^{-1} \mathbf{L}_{\mathbf{mo}} (\phi_o - \tau_o) \right)$$

$$= \mathbf{I} (\phi_o - \tau_o) + \lambda \left(\mathbf{L}_{\mathbf{oo}} (\phi_o - \tau_o) - \mathbf{L}_{\mathbf{om}} \mathbf{L}_{\mathbf{mm}}^{-1} \mathbf{L}_{\mathbf{mo}} (\phi_o - \tau_o) \right)$$

$$= \left[\mathbf{I} + \lambda \left(\mathbf{L}_{\mathbf{oo}} - \mathbf{L}_{\mathbf{om}} \mathbf{L}_{\mathbf{mm}}^{-1} \mathbf{L}_{\mathbf{mo}} \right) \right] (\phi_o - \tau_o)$$

$$(\phi_o - \tau_o) = \left[\mathbf{I} + \lambda \left(\mathbf{L}_{\mathbf{oo}} - \mathbf{L}_{\mathbf{om}} \mathbf{L}_{\mathbf{mm}}^{-1} \mathbf{L}_{\mathbf{mo}} \right) \right]^{-1} (\mathbf{s} - \tau_o)$$

$$\hat{\phi}_o = \left[\mathbf{I} + \lambda \left(\mathbf{L}_{\mathbf{oo}} - \mathbf{L}_{\mathbf{om}} \mathbf{L}_{\mathbf{mm}}^{-1} \mathbf{L}_{\mathbf{mo}} \right) \right]^{-1} (\mathbf{s} - \tau_o) + \tau_o$$

$$(10)$$

3 Estimation of Laplacian Regularization Parameters

We model the relationship between \mathbf{s} , $\phi_{\mathbf{o}}$, and τ as a set of gaussian distribution.

$$(\mathbf{s}|\phi_{\mathbf{o}}, \tau) \sim \mathcal{N}(\phi_{\mathbf{o}}, \Sigma)$$
 (11)

$$\Sigma = \rho \mathbf{I} \tag{12}$$

$$\left(\begin{bmatrix} \phi_{\mathbf{o}} \\ \phi_{\mathbf{m}} \end{bmatrix} \middle| \tau \right) \sim \mathcal{N}(\mathbf{A}\tau, \lambda^{-1}\mathbf{L}^{-}) \tag{13}$$

$$(\phi_{\mathbf{o}}|\tau) \sim \mathcal{N}\left(\mathbf{A}_{\mathbf{o}}\tau, \Sigma_{\phi_o}\right) \tag{14}$$

$$\Sigma_{\phi_o} = \lambda^{-1} \left(\mathbf{L_{oo}} - \mathbf{L_{om}} \mathbf{L_{mm}^{-1}} \mathbf{L_{mo}} \right)^{-1}$$
(15)

$$\tau \sim \mathcal{N}\left(0, \sigma^2 \mathbf{I}\right) \tag{16}$$

Fully expanded, this becomes

$$\begin{bmatrix} \mathbf{s} \\ \phi_{\mathbf{o}} \\ \tau \end{bmatrix} \sim \mathcal{N} \begin{pmatrix} \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \Sigma + \Sigma_{\phi_o} + \sigma^2 \mathbf{A_o} \mathbf{A_o}^t & \Sigma_{\phi_o} + \sigma^2 \mathbf{A_o} \mathbf{A_o}^t & \sigma^2 \mathbf{A_o} \\ \Sigma_{\phi_o} + \sigma^2 \mathbf{A_o} \mathbf{A_o}^t & \Sigma_{\phi_o} + \sigma^2 \mathbf{A_o} \mathbf{A_o}^t & \sigma^2 \mathbf{A_o} \\ \sigma^2 \mathbf{A_o}^t & \sigma^2 \mathbf{A_o}^t & \sigma^2 \mathbf{I} \end{bmatrix}$$

$$(17)$$

We can form the conditional distribution $\tau|\mathbf{s}$ which has a mean

$$\mu_{\tau|\mathbf{s}} = 0 + (\sigma^2 \mathbf{A_o}^t) \left(\Sigma + \Sigma_{\phi_o} + \sigma^2 \mathbf{A_o} \mathbf{A_o^t} \right)^{-1} \mathbf{s}$$
(18)

$$= \mathbf{A_o}^t \left(\tilde{\rho} \mathbf{I} + \frac{1}{\tilde{\lambda}} \mathbf{L_{oo}}^- + \mathbf{A_o} \mathbf{A_o^t} \right)^{-1} \mathbf{s}$$
 (19)

We assume that $\sigma^2 \gg 1$, and treat λ and ρ as relative to σ^2 , as $\tilde{\rho}$ and $\tilde{\lambda}$. This model gives us an estimate for τ given a value for ρ and λ . As ρ has no direct role in the central tendency of ϕ or \mathbf{s} , we choose to fix the value of $\tilde{\rho} = 0.1$, which leaves only $\tilde{\lambda}$. We estimate the optimal $\tilde{\lambda}$ by grid search, minimizing the predicted residual error sum of squares (PRESS) statistic.

$$\underset{\tilde{\lambda}}{\operatorname{arg\,min}} \frac{\mathbf{s} - \hat{\phi}_{\mathbf{o}}}{\left(1 - \left(\mathbf{I} + \tilde{\lambda}\mathbf{L}\right)^{-1}\right)^{2}} \tag{20}$$

This formulation depends upon the value of \mathbf{s} and is sensitive to low scoring matches, which can lead to incorrect estimates of τ and PRESS. We therefore perform a grid search over both $\tilde{\lambda}$ and a minimum threshold for \mathbf{s} , γ .

As we increase γ we remodel the graph \mathcal{G} , removing nodes whose score is below γ . For each pair of neighbors of removed node g_m , (g_u, g_v) , if $L_1(g_u, g_v) > L_1(g_u, g_m) + L_1(g_m, g_v)$, we add an edge from g_u to g_v with weight $\frac{1}{L_1(g_u, g_m) + L_1(g_m, g_v)}$, up to a limit of $L_1(g_k, g_m) < 5$. We give the result of this grid search the name \mathbf{r} . At each point, on the grid, we save the value of τ in $r_{\lambda_i, \gamma_j, \tau}$ and the PRESS in $r_{\lambda_i, \gamma_j, PRESS}$. To select the optimal parameters, we traverse the grid along γ , computing τ_{γ} :

$$\bar{\lambda}_j = \operatorname*{arg\,min}_{\lambda_i} r_{\lambda_i, \gamma_j, PRESS} \tag{21}$$

$$\tau_{\gamma_j} = |r_{\bar{\lambda}_j, \gamma_j, \tau}| * \left(\frac{\gamma_j}{b} + (1 - \frac{1}{b})\right)$$
(22)

where b is a bias factor defining how much weight to give to higher values of γ which correspond to networks made up of higher confidence assignments. We chose b=4. We define $\bar{\tau}_{\gamma}=\max \tau_{\gamma}$ and define the vector $\bar{\gamma}=\left[\gamma_{j}\leftarrow\tau_{\gamma_{j}}\geq\bar{\tau}_{\gamma}*0.95\right]$. This favors values of γ where large values of τ are selected, meaning that the neighborhoods are well populated, while also giving an estimate for $\tilde{\lambda}$ that is non-zero. We term the values of γ in $\bar{\gamma}$ the target thresholds of s.

To estimate $\tilde{\lambda}$ and τ from these results, we select the columns of the grid \mathbf{r} at each $\gamma_j \in \bar{\gamma}$ and applied the following procedure:

$$\bar{\tau}_{\gamma} = \max \tau_{\gamma} \tag{23}$$

$$\bar{\gamma} = \left\{ \gamma_j \leftarrow \tau_{\gamma_j} \ge \bar{\tau}_{\gamma} * 0.9 \right\} \tag{24}$$

$$\bar{\lambda} = \left\{ \bar{\lambda}_j \leftarrow \gamma_j \in \bar{\gamma} \right\} \tag{25}$$

$$\mathbf{s}_{\gamma_{\mathbf{j}}} = \{ s_i \leftarrow s_i > \gamma_j \} \tag{26}$$

$$\bar{\tau}_{\mathbf{j}} = \mu_{\tau | \mathbf{s}_{\gamma_j}, \bar{\lambda}_j} \tag{27}$$

$$\hat{\lambda} = \frac{1}{|\bar{\lambda}|} \sum_{j} \bar{\lambda}_{j} \tag{28}$$

$$\hat{\tau} = \frac{1}{|\bar{\tau}|} \sum_{j}^{J} \bar{\tau}_{\mathbf{j}} \tag{29}$$

$$\hat{\gamma} = \frac{1}{|\bar{\gamma}|} \sum_{j} \bar{\gamma}_{j} \tag{30}$$

where \mathbf{s}_{γ_j} is the set of observed scores which are greater than γ_j , but where the estimation of is carried out with the complete Laplacian \mathbf{L} , not the reduced network used to compute \mathbf{r} . This set of averaged estimates of $\hat{\lambda}$ and $\hat{\tau}$ are then used to estimate $\hat{\phi}_o$ by 10, labeled 7 in the main text.

4 MS^n Signature Ion Criterion

This feature was not used in the main article in order to make the comparison between our results and previously published work more straight forward.

When MS^n scans are present, it may be useful to consider only those MS^1 features which are associated with MS^n scans that contain glycan-like signature ions. We include an algorithm for classifying an MS^n scan as being "glycan-like":

$$I = max(intensity(p)) \tag{31}$$

$$t = I * 0.01 \tag{32}$$

$$p_{oxonium} = \{ p_i \leftarrow |ppmerror(mass(p_j), mass(f_g))| < e, f_g \in oxonium(g), f_g \neq Fucose, intensity(p_i) > t \}$$
 (33)

$$p_{edges} = \{(p_i, p_j) \leftarrow |ppmerror(mass(p_j) - mass(p_i), mass(f_g))| < e,$$

$$(34)$$

$$oxonium(f_g) \in g, intensity(p_i) > t, intensity(p_j) > t\}$$

$$s_{oxonium} = \frac{1}{|p_{oxonium}|} \sum_{p_i}^{p_{oxonium}} \left(\frac{intensity(p_i)}{I} \right) * min(log_4|p_{oxonium}|, 1)$$
(35)

$$s_{edges} = \frac{1}{|p_{edges}|} \sum_{p_i, p_j}^{p_{edges}} \left(\frac{intensity(p_i) + intensity(p_j)}{I} \right) * min(log_4|p_{edges}|, 1)$$
(36)

$$s_q = max(s_{oxonium}, s_{edges}) \tag{37}$$

(38)

Where p is the set of peaks in the scan, g is the glycan composition, e the required parts-per-million mass accuracy. oxonium() is a function that given a glycan composition g, produces fragments f_g of g composed of between one and three monosaccharides, commonly observed as oxonium ions alone, or as the mass difference between two peaks formed from consecutive fragmentation of a glycosidic bond. This method is not intended to identify a glycan structure, just detect patterns in the signal peaks of the MS^n scan that could indicate the fragmentation of a glycan.

$ au_i$	20150930-06-AGP	AGP-DR-Perm-glycans-1	AGP-permethylated-2 ul -inj-55- $SLens$
high-mannose	0.000	0.000	0.000
hybrid	11.520	7.240	21.092
bi-antennary	15.691	12.859	20.627
asialo-bi-antennary	0.000	0.000	13.253
tri-antennary	21.752	21.693	21.550
asialo-tri-antennary	0.000	0.000	6.792
tetra-antennary	15.993	15.276	17.452
asialo-tetra-antennary	0.000	0.000	0.000
penta-antennary	11.446	10.127	7.282
asialo-penta-antennary	0.000	0.000	0.000
hexa-antennary	2.211	0.000	0.000
asialo-hexa-antennary	0.000	0.000	0.000
hepta-antennary	0.000	0.000	0.000
asialo-hepta-antennary	0.000	0.000	0.000
$\hat{\lambda}$	0.99	0.99	0.99
$\hat{\gamma}$	15.74	16.22	17.64

Table 2: Estimated values of smoothing parameters τ , λ , and γ for each AGP-based dataset and using a combinatorial database

$ au_i$	20141031-07-Phil-82	20141128-11-Phil-82
high-mannose	17.070	19.395
hybrid	14.039	17.147
bi-antennary	0.000	0.000
asialo-bi-antennary	16.287	17.689
tri-antennary	0.000	0.000
asialo-tri-antennary	15.220	18.865
tetra-antennary	0.000	0.000
asialo-tetra-antennary	7.103	7.660
penta-antennary	0.000	0.000
asialo-penta-antennary	0.000	3.365
hexa-antennary	0.000	0.000
asialo-hexa-antennary	0.000	0.000
hepta-antennary	0.000	0.000
asialo-hepta-antennary	0.000	0.000
λ	0.99	0.99
$\hat{\gamma}$	16.51	15.50

Table 3: Estimated values of smoothing parameters τ , λ , and γ for each Phil-82-based dataset and using a combinatorial database

5 Algorithmic Performance on All Datasets

For more details on each sample, please see Table 2 in the main text.

5.1 Results for AGP

We analyzed three different sample workups of N-glycans released from Alpha 1 Acid Glycoprotein. See Table 2 for a comparison of estimated τ values for each sample. For AGP-DR-Perm-glycans-1 and AGP-perm-thylated-2ul-inj-55-SLens, we used an MS^n Signature Ion Criterion threshold of 0.17 to filter out large contaminants that may be introduced by permethylation reagents.

The estimate of γ for 20150930-06-AGP was larger than the score for the larger penta-antennary

5.2 Results for Phil-82

We analyzed native and deutero-reduced and permethylated N-glycans released from virions of Influenza-A Virus strain Phillipines 1982. See Table 3 for a comparison of estimated τ values for each sample.

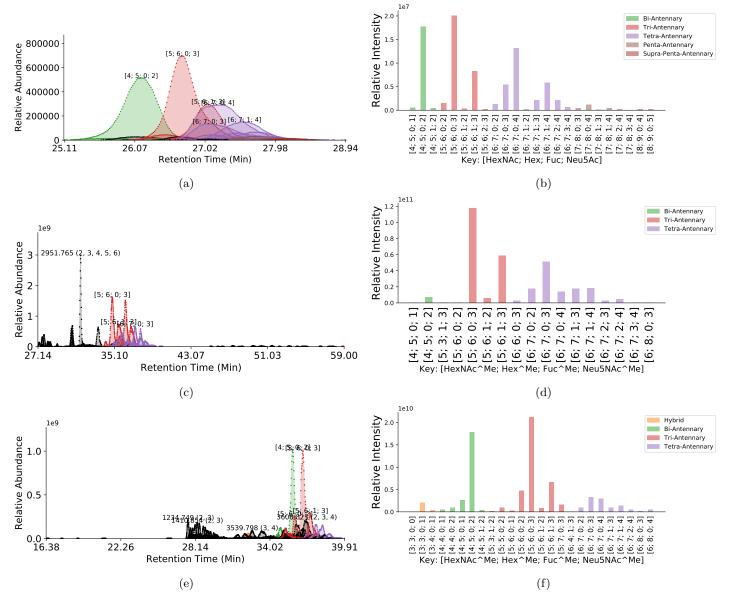


Figure 2: Chromatogram Assignments for 20150930-06-AGP (a, b), AGP-DR-Perm-glycans-1 (c, d) and AGP-permethylated-2ul-inj-55-SLens (e, f)

5.3 Results for IGG

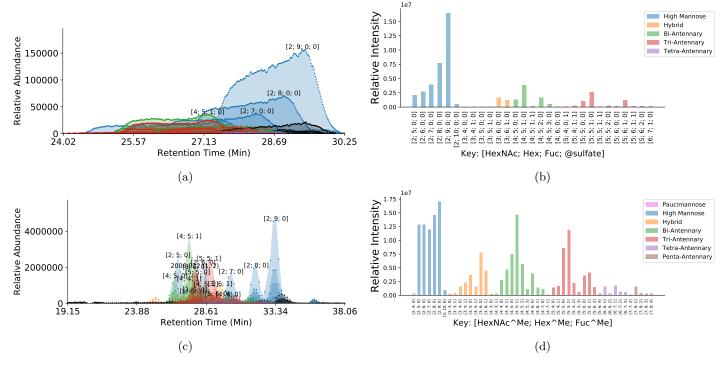


Figure 3: Chromatogram Assignments for 20141031-07-Phil-82 (a, b) and 20141128-11-Phil-82 (c, d)

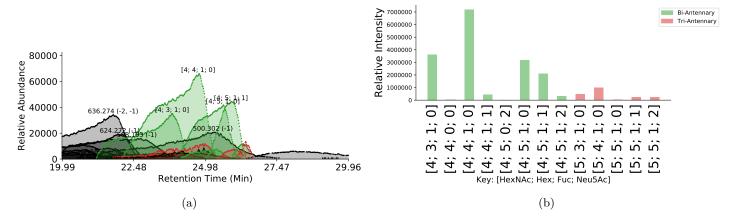


Figure 4: Chromatogram Assignments for 20151002-02-IGG

$ au_i$	20151002-02-IGG
high-mannose	0.000
hybrid	15.737
bi-antennary	12.594
asialo-bi-antennary	13.614
tri-antennary	7.657
asialo-tri-antennary	15.724
tetra-antennary	4.252
asialo-tetra-antennary	0.000
penta-antennary	0.000
asialo-penta-antennary	0.000
hexa-antennary	0.000
asialo-hexa-antennary	0.000
hepta-antennary	0.000
asialo-hepta-antennary	0.000
$\hat{\lambda}$	0.99
$\hat{\gamma}$	14.12

Table 4: Estimated values of smoothing parameters τ , λ , and γ for IGG using a combinatorial database

6 Differences in Assigned Glycans for Perm-BS-070111-04-Serum

Of the compositions assigned by our algorithm that were not mentioned in Yu et al. (2013) but were annotated in the original publication of this dataset in Hu and Mechref (2012) include HexNAc3 Hex4, HexNAc3 Hex4 NeuAc1, and HexNAc5 Hex3. Because our database was constructed based on combinatorial rules that did not take into account all biosynthetic constraints, we include infeasible compositions in our search space, such as HexNAc2 Hex10 Fuc1 and HexNAc5 Hex3 Fuc1 NeuAc2. Future work could be done to restrict the database to only biosynthetically feasible glycan compositions. This would also have benefits for the construction of the composition network where only those compositions which have an enzymatic reaction to from one to the other would have an edge connecting them, such that HexNAc5 Hex6 NeuAc2 would not have an edge to HexNAc5 Hex7 NeuAc2 as in our current model.

7 glySpace Integration and Upload

We converted our N-glycan compositions into partially determined topologies assuming that the chitobios core was present to ensure that they were classified as N-glycans.

From Perm-BS-070111-04-Serum

```
{Fuc:1; Hex:5; HexNAc:3; Neu5Ac:1}

{Fuc:2; Hex:5; HexNAc:4; Neu5Ac:2}

{Fuc:2; Hex:6; HexNAc:5; Neu5Ac:3}

{Fuc:2; Hex:7; HexNAc:6; Neu5Ac:3}

{Fuc:2; Hex:7; HexNAc:6; Neu5Ac:4}

{Hex:7; HexNAc:6; Neu5Ac:2}

{Hex:7; HexNAc:6; Neu5Ac:3}

{Hex:8; HexNAc:7; Neu5Ac:3}

{Hex:8; HexNAc:7; Neu5Ac:4}

{Hex:9; HexNAc:8; Neu5Ac:2}
```

From 20141103-02-Phil-BS

```
{@sulfate:1; Fuc:1; Hex:4; HexNAc:5}
{@sulfate:1; Fuc:1; Hex:5; HexNAc:4}
{@sulfate:1; Fuc:1; Hex:5; HexNAc:5}
{@sulfate:1; Fuc:2; Hex:4; HexNAc:5}
{@sulfate:1; Fuc:2; Hex:6; HexNAc:5}
{@sulfate:1; Fuc:2; Hex:9; HexNAc:8}
{@sulfate:1; Fuc:3; Hex:4; HexNAc:5}
{@sulfate:1; Fuc:3; Hex:6; HexNAc:5}
{@sulfate:1; Fuc:3; Hex:9; HexNAc:8}
{@sulfate:1; Fuc:4; Hex:6; HexNAc:5}
{@sulfate:1; Fuc:4; Hex:8; HexNAc:7}
{@sulfate:1; Fuc:4; Hex:9; HexNAc:8}
{@sulfate:1; Hex:10; HexNAc:9}
{@sulfate:1; Hex:4; HexNAc:5}
{Osulfate:1; Hex:5; HexNAc:4}
{Fuc:2; Hex:8; HexNAc:7}
{Fuc:3; Hex:7; HexNAc:6}
{Fuc:3; Hex:8; HexNAc:7}
{Fuc:4; Hex:8; HexNAc:7}
{Hex:10; HexNAc:9}
```

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