#### VIRGINIA STANDARDS OF LEARNING

**Spring 2007 Released Test** 

# END OF COURSE GEOMETRY

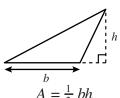
Form M0117, CORE 1

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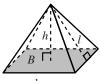
## **Geometry Formula Sheet**

#### **Geometric Formulas**

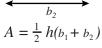


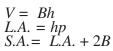






 $A = \frac{1}{2} bh$ 











$$A = lw$$
$$p = 2(l + w)$$

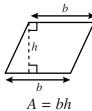


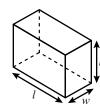
$$V = \pi r^{2}h$$

$$L.A. = 2\pi rh$$

$$S.A. = 2\pi r(h+r)$$

 $V = \frac{4}{3} \pi r^3$ <br/> $S.A. = 4\pi r^2$ 







$$a c c c$$

$$b$$

$$c^2 = a^2 + b^2$$

V = lwhS.A. = 2lw + 2lh + 2wh

 $V = \frac{1}{3} \pi r^2 h$   $L.A. = \pi r l$   $S.A. = \pi r (l + r)$ 

## **Geometric Symbols**

Example	Meaning			
$\angle A$	angle A			
m∠A	measure of angle A			
$\overline{AB}$	line segment AB			
AB	measure of line segment AB			
$\overrightarrow{AB}$	line AB			
$\triangle ABC$	triangle ABC			
$\square$ ABCD	rectangle ABCD			
∠ZABCD	parallelogram ABCD			

Example	Meaning		
$\overrightarrow{AB}$	vector AB		
	right angle		
$\overrightarrow{AB} \parallel \overrightarrow{CD}$	Line <i>AB</i> is parallel to line <i>CD</i> .		
$\overrightarrow{AB}\bot\overrightarrow{CD}$	Line $AB$ is perpendicular to line $CD$ .		
$\angle A \cong \angle B$	Angle $A$ is congruent to angle $B$ .		
$\triangle A \sim \triangle B$	Triangle $A$ is similar to triangle $B$ .		
	Similarly marked segments are congruent.		
	Similarly marked angles are congruent.		

#### **Abbreviations**

Volume	V
Lateral Area	L.A.
Total Surface Area	S.A.
Area of Base	В

Ρi

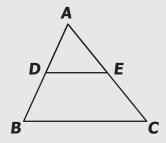
$$\pi\approx 3.14$$

$$\pi \approx \frac{22}{7}$$

#### **Directions**

Read each question carefully and choose the best answer. Then mark the space on your answer document for the answer you have chosen.

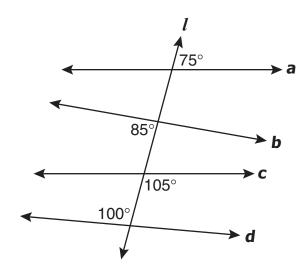
#### **SAMPLE**



If  $\triangle ABC$  is similar to  $\triangle ADE$ , then AB:AD=?:AE. Which replaces the "?" to make the statement true?

- $\mathbf{A}$  AC
- **B** AE
- C DE
- $\mathbf{D}$  BC

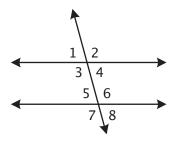
# 1 Transversal l cuts lines a, b, c, and d.



## Which two lines are parallel?

- $\mathbf{A}$  a and c
- **B** a and d
- **C** b and c
- **D** b and d

2



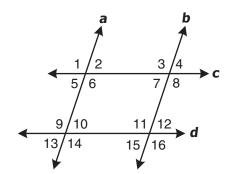
In the figure above,  $\angle 2$  and  $\angle 6$  are a pair of —

- **F** consecutive interior angles
- **G** alternate interior angles
- **H** vertical angles
- J corresponding angles

3 One exterior angle of a regular polygon measures 72°. What is the measure of one interior angle?

- **A** 18°
- **B** 108°
- **c** 360°
- **D** 540°

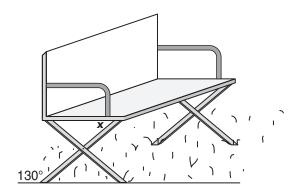
4 In this drawing,  $a \parallel b$  and  $c \parallel d$ .



### Which angle is *not* necessarily congruent to $\angle 1$ ?

- **F** ∠3
- **G** ∠9
- **H** ∠12
- **J** ∠16

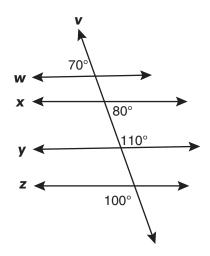
5 The support legs on a bench are attached in such a way that the angle made by one leg with the ground is 130°.



What must the measure of the angle marked x be in order for the seat of the bench to be parallel to the ground?

- **A** 50°
- **B** 65°
- **C** 90°
- **D** 130°

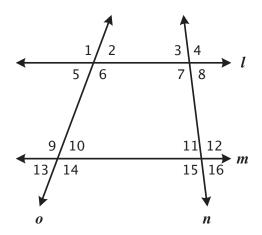
### 6 Line *v* is a transversal.



#### Which is a true statement?

- **F**  $w \parallel y \text{ and } x \parallel z$
- **G**  $w \parallel x$  and  $y \parallel z$
- **H**  $w \parallel z \text{ and } x \parallel y$
- **J**  $w \parallel x \text{ and } x \parallel y$

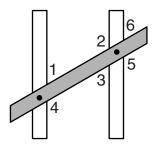
7



In the drawing above,  $\angle 4$  and  $\angle 12$  are —

- A alternate interior angles
- **B** consecutive interior angles
- **C** corresponding angles
- **D** a linear pair

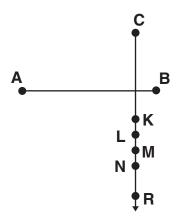
8 A carpenter nailed a board across two beams, forming the angles shown.



Which equal measures would ensure the beams are parallel?

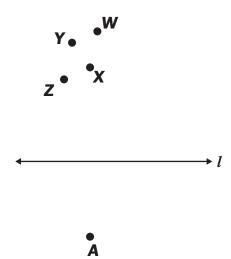
- **F**  $m \angle 1 = m \angle 2$
- **G**  $m \angle 1 = m \angle 3$
- **H**  $m \angle 2 = m \angle 5$
- **J**  $m \angle 3 = m \angle 4$

9



# Which segment is congruent to $\overline{AB}$ ?

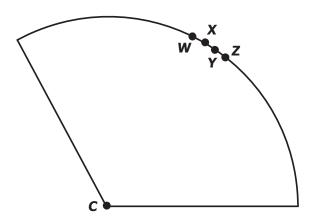
- $\mathbf{A}$   $\overline{CK}$
- B CL
- **C** *CM*
- **D**  $\overline{CN}$



Which point apparently lies on the perpendicular to l from A?

- $\mathbf{F}$  X
- $\mathbf{G}$  Y
- **H** Z
- J W

11 One piece of pie is left for two boys to share.



Where should the pie be cut to ensure each gets an equal piece?

- $\mathbf{A}$   $\overline{CZ}$
- $\mathbf{B} \quad \overline{CY}$
- **C** CX
- **D** CW

- 12 If  $p \rightarrow q$ , and  $q \rightarrow r$ , then
  - **F**  $r \rightarrow p$
  - **G**  $p \rightarrow r$
  - **H**  $\sim r \rightarrow p$
  - **J**  $r \rightarrow \sim p$

13 If the conditional statement

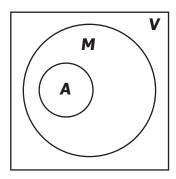
"If you have a laptop, then you have a computer"  $\;$ 

is represented by  $p \rightarrow q$ , what is the symbolic representation of

"If you have a computer, then you do not have a laptop"?

- **A**  $q \rightarrow \sim p$
- **B**  $\sim q \rightarrow p$
- **C**  $p \rightarrow \sim q$
- **D**  $\sim q \rightarrow \sim p$

14 In the Venn diagram below, *V* represents the set of all vehicles, *M* represents the set of all motorized vehicles, and *A* represents the set of all automobiles.

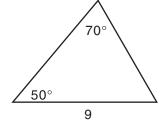


### Based on the diagram, which is a valid conclusion?

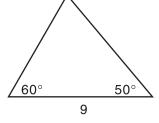
- **F** All automobiles are motorized vehicles.
- **G** All motorized vehicles are automobiles.
- **H** Some automobiles are not motorized vehicles.
- **J** No automobiles are motorized vehicles.

# 15 Which triangle below is *not* congruent to the other three triangles?

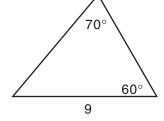




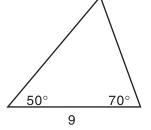
В



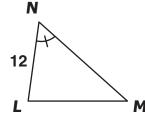
C

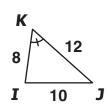


D



**16** 

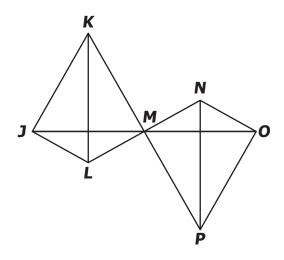




Which additional piece of information would prove that  $\triangle IJK \sim \triangle LMN$ ?

- **F** NM = 18
- **G** LM = 18
- **H** NM = 15
- $J \qquad \textit{LM} = 10$

17 Given: *M* is the midpoint of  $\overline{LN}$  and  $\overline{KP}$ .



The given information is sufficient to prove  $\triangle KML \cong \triangle PMN$  by which postulate/theorem?

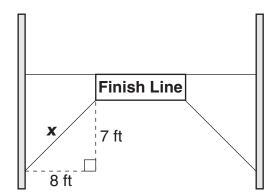
- **A** Angle-Side-Angle
- **B** Side-Side-Side
- **C** Side-Angle-Side
- **D** Angle-Angle-Side

- 18 Which of the following could *not* be the lengths of the sides of a triangle?
  - **F** 6 ft, 3 ft, 9 ft
  - **G** 3 cm, 4 cm, 5 cm
  - **H** 4 in., 6 in., 8 in.
  - **J** 5 km, 2 km, 4 km

- 19 In  $\triangle DEF$ , m $\overline{DE}$  = 8 inches, m $\overline{EF}$  = 6 inches, and m $\overline{DF}$  = 10 inches. Which lists the angles in order from *smallest* to *largest*?
  - **A**  $\angle D, \angle E, \angle F$
  - **B**  $\angle F, \angle D, \angle E$
  - **C**  $\angle E, \angle F, \angle D$
  - **D**  $\angle D, \angle F, \angle E$

- 20 In  $\triangle ABC$ , if m $\angle C < m \angle B < m \angle A$ , then
  - **F** AB < AC < BC
  - **G** AC < AB < BC
  - **H** AB < BC < CA
  - $\mathbf{J} \qquad BC < AB < CA$

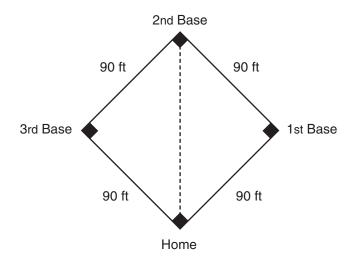
21 To mark the end of a race, a finish-line banner is stretched across the road as shown in the drawing.



Which is closest to the length of the support rope designated by  $\boldsymbol{x}$  in the drawing?

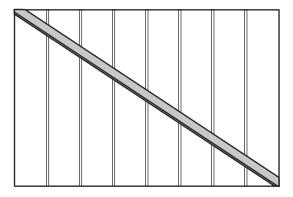
- **A** 9.5 ft
- **B** 10.6 ft
- **C** 12.0 ft
- **D** 15.0 ft

22 A baseball diamond is in the shape of a square, 90 feet on a side.



What is the direct distance from home plate to second base?

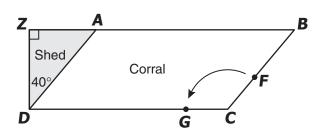
- **F** 90 ft
- **G**  $90\sqrt{2}$  ft
- **H**  $90\sqrt{3}$  fl
- **J** 180 ft



What is the length of a diagonal brace that could be used for a wall 9 feet high and 12 feet long?

- **A** 12 ft
- **B** 13 ft
- **C** 14 ft
- **D** 15 ft

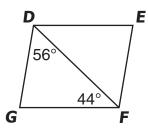
24 Gene's horse corral, labeled *ABCD* in the drawing, is shaped as a parallelogram and is adjacent to the shed, labeled *ZAD*.



If a gate, labeled *CF*, opens all the way to the corral fence, position labeled *CG*, through how many degrees does the gate swing?

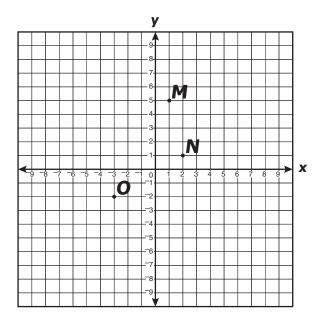
- **F** 40°
- **G** 50°
- **H** 130°
- **J** 140°

25 A diagonal of parallelogram *DEFG* forms angles with measures as shown.



What is the measure of  $\angle DEF$ ?

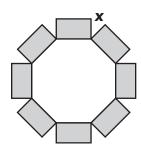
- **A** 44°
- **B** 56°
- **C** 80°
- **D** 100°



Quadrilateral *MNOP* is a parallelogram. The coordinates of three of its vertices are M(1,5), N(2,1), and O(-3,-2). If (x,2) are the coordinates of P, what is the value of x?

- **F** -5
- **G** -4
- **H** -3
- **J** 0

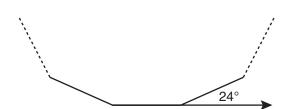
27 Rectangular flowerbeds are built on each side of a fishpond in the shape of a regular octagon.



What is the measure of the angle, x, between two consecutive flowerbeds?

- **A** 30°
- **B** 45°
- **C** 60°
- **D** 90°

28

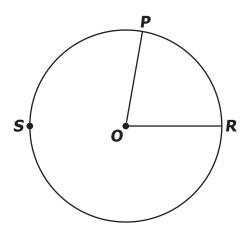


A portion of a regular polygon is shown. The polygon has —

- **F** 15 sides
- **G** 16 sides
- **H** 18 sides
- **J** 20 sides

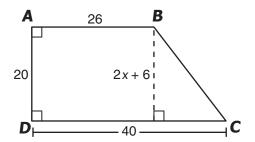
- 29 Each interior angle of a regular polygon has a measure of 162°. The polygon has a total of
  - **A** 17 sides
  - **B** 18 sides
  - **C** 19 sides
  - **D** 20 sides

30 In circle  $O_r$ , the degree measure of  $\widehat{PSR}$  is 280°.



What is the degree measure of  $\angle POR$ ?

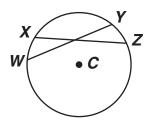
- **F** 160°
- **G** 85°
- **H** 80°
- **J** 40°



# What is the value of x in trapezoid ABCD?

- **A** 17
- **B** 13
- **C** 10
- **D** 7

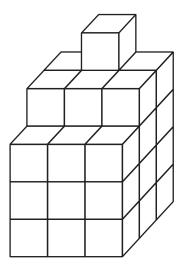
32 In circle C, m  $\widehat{WX} = 25^{\circ}$ , m $\widehat{XY} = 40^{\circ}$ , m  $\widehat{YZ} = 25^{\circ}$ , and  $\widehat{WY} = 24$  centimeters.



## What is the length of $\overline{XZ}$ ?

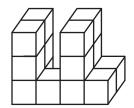
- **F** 12 cm
- **G** 24 cm
- **H** 25 cm
- **J** 65 cm

- A pizza has a diameter of 16 inches. Which is closest to the area of one slice if the pizza is divided into 6 equal pieces?
  - **A** 134.1 sq in.
  - **B** 117.1 sq in.
  - **C** 67.2 sq in.
  - **D** 33.5 sq in.



Assuming the solid is constructed from cubes measuring 1 unit on each edge and that the figure is completely solid, what is the volume of the cubic solid shown above?

- **F** 12 cubic units
- **G** 34 cubic units
- **H** 59 cubic units
- **J** 68 cubic units



Which could not be a two-dimensional view of the block of cubes shown above?

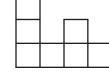
Α



В



C





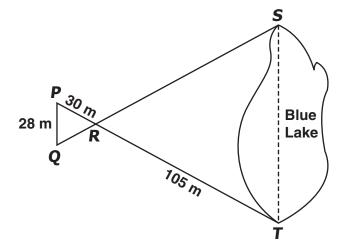
#### 36 Which is closest to the volume of a sphere with a radius equal to 8 centimeters?

- 267.9 cm<sup>3</sup> F
- 803.8 cm<sup>3</sup> G
- **H** 1,607.7 cm<sup>3</sup>
- 2,143.6 cm<sup>3</sup> J

# 37 What is the total surface area of a rectangular prism box that measures 5 feet by 1 foot by 1 foot?

- **A** 5 sq ft
- **B** 20 sq ft
- **C** 22 sq ft
- **D** 30 sq ft

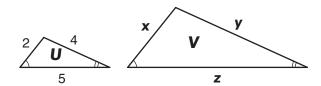
38



# If $\overrightarrow{PQ}$ is parallel to $\overrightarrow{ST}$ , what is ST, the width of the lake?

- **F** 62 meters
- **G** 70 meters
- **H** 84 meters
- **J** 98 meters

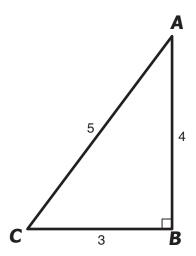
39 The ratio of the perimeter of  $\triangle U$  to the perimeter of  $\triangle V$  is 1:2.



If the triangles are similar, what is the value of x + y?

- **A** 3
- **B** 6
- **C** 12
- **D** 18

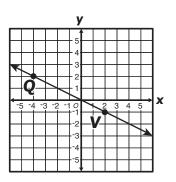
40 Right triangle *ABC* has the measures shown.



What is the maximum number of different lines of symmetry that can be drawn through  $\triangle ABC$ ?

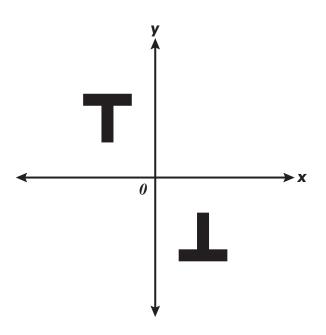
- **F** 0
- **G** 1
- **H** 2
- **J** 3

41



What is the apparent slope of  $\overrightarrow{QV}$ ?

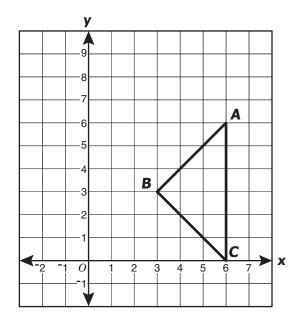
- **A** -2
- **B**  $-\frac{1}{2}$
- **c**  $\frac{1}{2}$
- **D** 2



## In relation to one figure, the other figure is apparently a —

- **F** reflection across the line y = 1
- **G** reflection across the line y = x
- **H** 90° rotation about the origin
- **J** 180° rotation about the origin

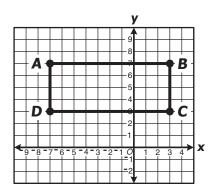
43 Triangle ABC is placed on a grid as shown.



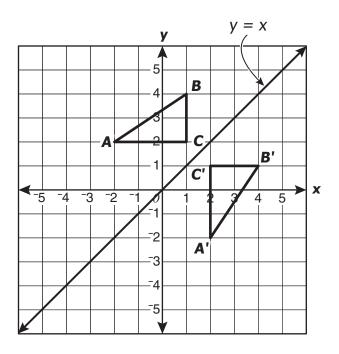
## The apparent midpoint of $\overline{\it AB}$ is —

- **A** (1.5, 1.5)
- **B** (3, 3)
- **C** (4.5, 4.5)
- **D** (4.5, 1.5)

44 Rectangle ABCD is placed in a coordinate plane as shown.



- Which equation describes a line of symmetry for rectangle ABCD?
- **F** x = 2
- **G** x = 5
- $\mathbf{H} \qquad y = 5$
- $\mathbf{J} \qquad y = x$



## $\triangle A'B'C'$ is apparently the result of —

- **A** reflecting  $\triangle ABC$  across the *y*-axis
- **B** reflecting  $\triangle ABC$  across the *x*-axis
- **C** rotating  $\triangle ABC$  about the point (1, 2)
- **D** reflecting  $\triangle ABC$  across the line y = x