

VIRGINIA STANDARDS OF LEARNING

TEST ITEM SET

ALGEBRA II

2009 Mathematics Standards of Learning

Released Spring 2015

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SAMPLE A

Which expression is equivalent to $\sqrt{\frac{7x}{16}}$?

☐ **A** $\frac{7x}{4}$

☐ **B** $\frac{7x}{8}$

☐ **C** $\frac{\sqrt{7x}}{4}$

☐ **D** $\frac{\sqrt{7x}}{8}$

Directions: Type your answer in the box.

SAMPLE B

What value of x makes $\sqrt{x} - 3 = 6$ true?

Which expression is equivalent to $\sqrt{20x^{16}y^{25}}$ for positive x and y values?

- ☐ A $2x^4y^5\sqrt{5}$
- ☐ B $5x^4y^5\sqrt{2}$
- ☐ C $2x^8y^{12}\sqrt{5y}$
- ☐ D $5x^8y^{12}\sqrt{2y}$

Which expression is equivalent to $\sqrt[3]{6w^7} \cdot \sqrt[3]{4w^5}$?

- ☐ A $2w^4\sqrt[3]{3}$
- ☐ B $2w^4\sqrt[3]{6}$
- ☐ C $2w^{11}\sqrt[3]{3w^2}$
- ☐ D $2w^{11}\sqrt[3]{6w^2}$

The steps used to solve an equation are shown.

Step 1: $\frac{2}{3}r = 14i$

Step 2: $\left(\frac{3}{2}\right)\frac{2}{3}r = 14i\left(\frac{3}{2}\right)$

Step 3: $\left(\frac{3}{2} \cdot \frac{2}{3}\right)r = 14i\left(\frac{3}{2}\right)$

Step 4: $1 \cdot r = 21i$

Step 5: $r = 21i$

What property justifies the work between Step 4 and Step 5 ?

- ☐ A Identity property of multiplication
- ☐ B Inverse property of multiplication
- ☐ C Commutative property of multiplication
- ☐ D Associative property of multiplication

Which expression is equivalent to the following expression if no denominators equal zero?

$$\frac{\frac{11-w}{30w^2}}{\frac{w-11}{5w^6}}$$

☐ **A** $-\frac{w^4}{6}$

☐ **B** $-\frac{6}{w^3}$

☐ **C** $\frac{w^3}{6}$

☐ **D** $\frac{6}{w^4}$

What is the complete factorization of $(18x^4 + 12x^3 - 6x)$?

- ☐ A $6x^3(3x + 2)$
- ☐ B $6x(3x^3 + 2x^2)$
- ☐ C $6x(3x - 1)(x + 1)$
- ☐ D $6x(3x^3 + 2x^2 - 1)$

Which of these is equivalent to i^{75} ?

☐ A i

☐ B $-i$

☐ C 1

☐ D -1

For which value of b is $x^2 + bx - 60$ factorable over the set of integers?

- ☐ A 61
- ☐ B 23
- ☐ C -7
- ☐ D -16

If no denominator equals zero, which expression is equivalent to $\frac{25 - 4x^2}{6x^2 + 9x - 15} \cdot \frac{6x^2 - 2x - 4}{2x^2 - x - 10}$?

- ☐ A -2
- ☐ B 2
- ☐ C $\frac{-2(3x + 2)}{3(x + 2)}$
- ☐ D $\frac{2(3x + 2)}{3(x + 2)}$

Assuming the denominators do NOT equal zero, which expression is equivalent to $\frac{12}{x+1} + \frac{1}{x-4}$?

- ☐ A $\frac{13x - 47}{(x+1)(x-4)}$
- ☐ B $\frac{13}{(x+1)(x-4)}$
- ☐ C $\frac{13x - 47}{2x - 3}$
- ☐ D $\frac{13}{2x - 3}$

Which expression is equivalent to $\sqrt{36x^9y^{25}}$, where $x > 0$ and $y > 0$?

☐ A $6x^3y^5$

☐ B $6x^{\frac{9}{2}}y^{\frac{25}{2}}$

☐ C $18x^3y^5$

☐ D $18x^{\frac{9}{2}}y^{\frac{25}{2}}$

What nonzero value of x is a solution to the following equation?

$$\frac{x+2}{x} + \frac{x-6}{3x} = \frac{2x+9}{5x}$$

- ☐ **A** $x = \frac{27}{14}$
- ☐ **B** $x = \frac{17}{14}$
- ☐ **C** $x = \frac{13}{14}$
- ☐ **D** $x = \frac{5}{14}$

How many values of x will satisfy the equation $-2|3x - 5| = 0$?

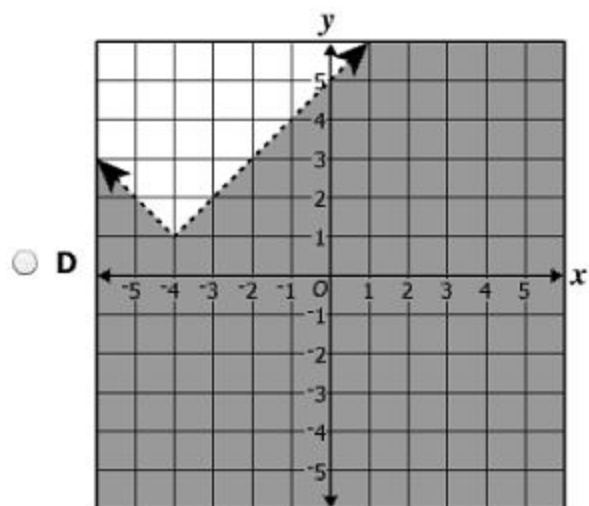
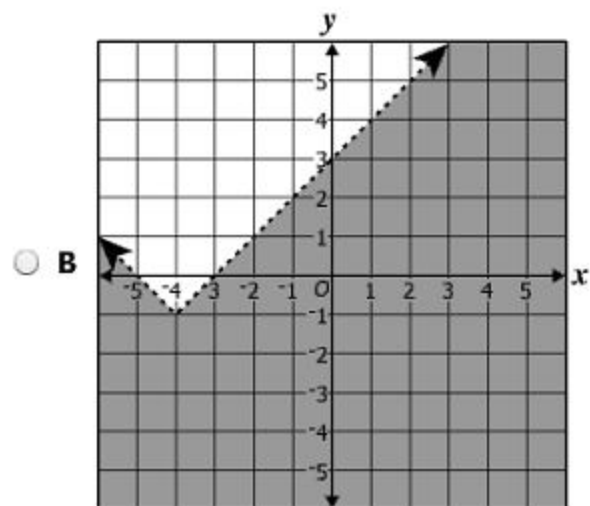
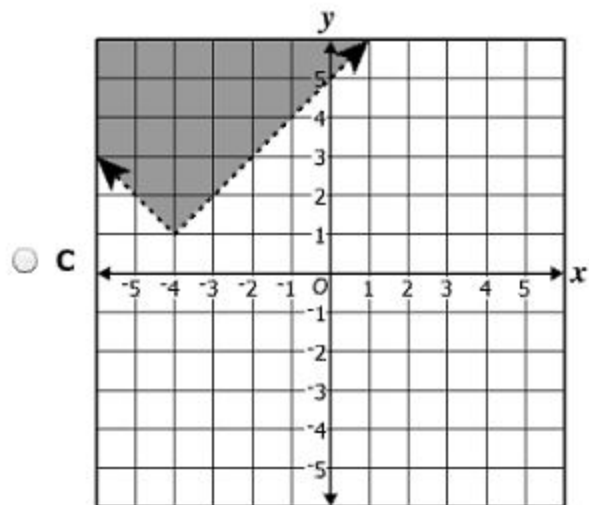
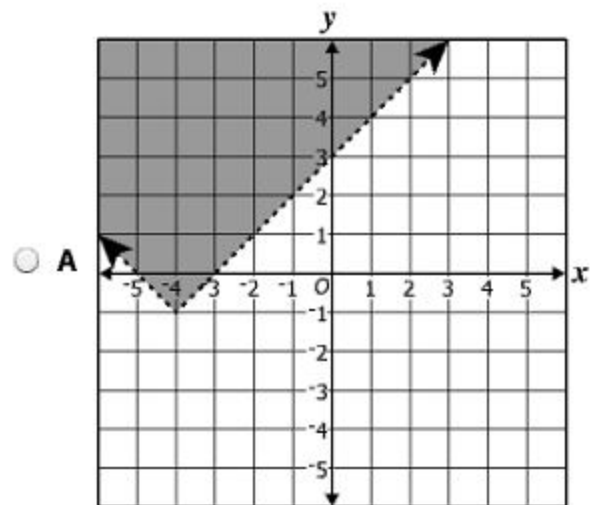
☐ A 0

☐ B 1

☐ C 2

☐ D 3

Which graph best represents the solutions for $y < |x + 4| - 1$?



What is a solution of $\sqrt{7-2x} + 5 = 8$?

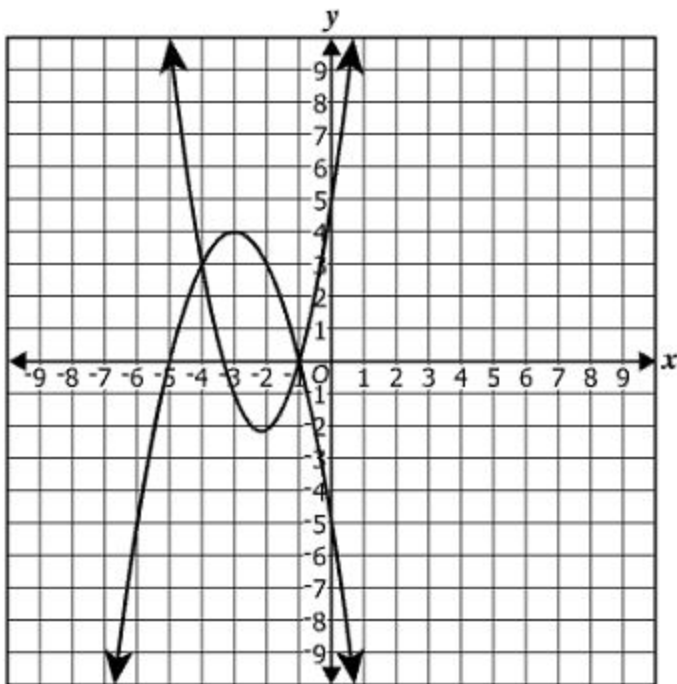
☐ **A** $x = -26$

☐ **B** $x = \frac{-19}{2}$

☐ **C** $x = \frac{-13}{2}$

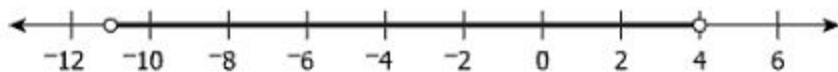
☐ **D** $x = -1$

Which is the apparent solution set of the system of equations graphed on the following grid?



- ☐ A $\{(0, -5), (0, 5)\}$
- ☐ B $\{(-3, 4), (-2, -2)\}$
- ☐ C $\{(-4, 3), (-1, 0)\}$
- ☐ D $\{(-5, 0), (-3\frac{1}{3}, 0), (-1, 0)\}$

This graph best represents the solution to which inequality?



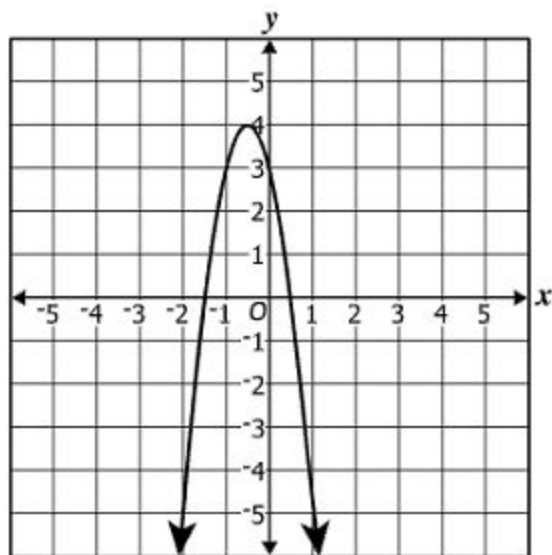
- ☐ A $|x - 11| > 4$
- ☐ B $|x - 11| < 4$
- ☐ C $|2x + 7| > 15$
- ☐ D $|2x + 7| < 15$

Directions: Type your answer in the box.

What value of x makes $\sqrt[3]{2x - 5} = 3$ true?

$x =$

What are the apparent roots of the equation graphed on the coordinate grid?



- ☐ A $\{0, 3\}$
- ☐ B $\left\{-\frac{1}{2}, 4\right\}$
- ☐ C $\left\{-\frac{3}{2}, \frac{1}{2}\right\}$
- ☐ D $\{-2, 1\}$

If no denominator is equal to zero, what is the solution set for the following equation?

$$\frac{3x - 4}{x^2} = \frac{3}{2x}$$

- ☐ A $\left\{\frac{8}{3}\right\}$
- ☐ B $\left\{\frac{8}{9}\right\}$
- ☐ C $\left\{-\frac{2}{3}, 2\right\}$
- ☐ D $\left\{-\frac{2}{3}, \frac{2}{3}\right\}$

What is the solution set for the following system of equations?

$$\begin{cases} y = 4x + 2 \\ y = x^2 + x - 8 \end{cases}$$

- ☐ A $\{(-5, -18), (2, 10)\}$
- ☐ B $\{(-1, -2), (6, 26)\}$
- ☐ C $\{(-6, -22), (1, 6)\}$
- ☐ D $\{(-2, -6), (5, 22)\}$

Directions: Click on all the correct answers.

Identify all the points where the graph of $h(x) = (x + 1)(x^2 + 8x + 16)$ intersects the x -axis.

$(-4, 0)$	$(1, 0)$
$(-2, 0)$	$(4, 0)$
$(-1, 0)$	$(16, 0)$

The function $f(x) = (1 - x)^2 - 4$ is decreasing throughout the interval —

- ☐ A $-4 < x < \infty$
- ☐ B $-\infty < x < 1$
- ☐ C $-1 < x < 3$
- ☐ D $-\infty < x < \infty$

Given: $f(x) = 4x^4 - 15$ and $g(x) = 2x + 11$

What is the value of $g(f(x))$?

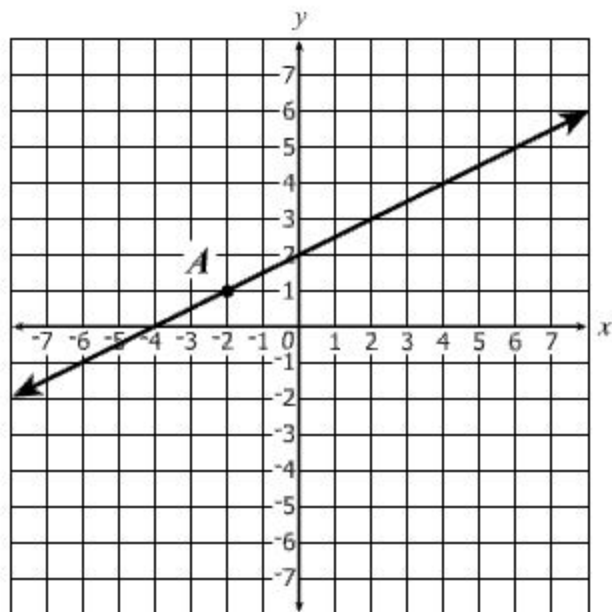
- ☐ A $8x^5 + 44x^4 - 30x - 165$
- ☐ B $8x^5 - 165$
- ☐ C $8x^4 - 4$
- ☐ D $8x^4 - 19$

A normally distributed data set has a mean of 0 and a standard deviation of 0.5 . Which is closest to the percent of values between -1 and 1 ?

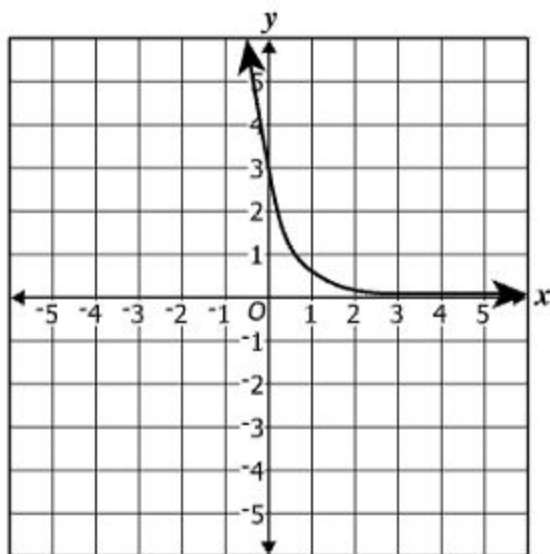
- ☐ A 34%
- ☐ B 50%
- ☐ C 68%
- ☐ D 95%

Directions: Click on the grid to plot the correct point.

Point A lies on the graph of $f(x) = \frac{1}{2}x + 2$. Locate the image of Point A that lies on the graph of $f^{-1}(x)$.



Which equation best represents this graph?



- ☐ A $f(x) = 3\left(\frac{1}{5}\right)^x$
- ☐ B $f(x) = 3\sqrt{5x}$
- ☐ C $f(x) = \frac{1}{3}\log(5x)$
- ☐ D $f(x) = \frac{1}{3}(5)^x$

If $f(x) = x^2 + 3x$ and $g(x) = 2x^2$, what is $g(f(-1))$?

☐ A -4

☐ B 0

☐ C 8

☐ D 10

The volume of a cone (V) varies jointly with its height (h) and the square of its radius (r). If k is the constant of proportionality, which of the following equations represents the correct relationship between volume, radius, and height?

☐ A $V = k(rh)^2$

☐ B $V = \frac{kr^2}{h}$

☐ C $V = \frac{k}{r^2h}$

☐ D $V = kr^2h$

What is the equation of the horizontal asymptote of the graph of the following equation?

$$f(x) = 4^{(x+1)} - 10$$

- ☐ A $y = 4$
- ☐ B $y = 0$
- ☐ C $y = -1$
- ☐ D $y = -10$

As x approaches negative infinity, which of the following describes the end behavior of $f(x) = -x^7 + bx^3 + c$?

- ☐ A $f(x)$ approaches c
- ☐ B $f(x)$ approaches 0
- ☐ C $f(x)$ approaches positive infinity
- ☐ D $f(x)$ approaches negative infinity

Jessica paid \$23,000 for her car and kept a record of its value.

Number of Years (x)	Value (in dollars) (y)
0	23,000
1	20,000
2	16,000
3	14,000
4	12,000
5	10,000

Assuming the relationship is exponential, which equation best models the curve of best fit for the data?

- ☐ A $y = 21,000(1.20)^x$
- ☐ B $y = 22,300(2.60)^x$
- ☐ C $y = 23,100(0.85)^x$
- ☐ D $y = 23,500(0.70)^x$

What is the sum of the infinite geometric series $9 - 6 + 4 - \frac{8}{3} + \dots$?

- ☐ A $\frac{29}{3}$
- ☐ B $\frac{25}{3}$
- ☐ C $\frac{27}{5}$
- ☐ D $\frac{18}{5}$

Which number is a zero of $f(x) = 7x^2 + 16x - 48$?

☐ A 12

☐ B 4

☐ C $\frac{12}{7}$

☐ D $\frac{4}{7}$

Which function is the inverse of $g(x) = x^3 + 11$?

☐ A $g^{-1}(x) = \sqrt[3]{x-11}$

☐ B $g^{-1}(x) = \sqrt[3]{x+11}$

☐ C $g^{-1}(x) = x - \sqrt[3]{11}$

☐ D $g^{-1}(x) = x + \sqrt[3]{11}$

What is the domain of $g(x) = \log(x - 1)$?

- ☐ A $\{x \mid x > 10\}$
- ☐ B $\{x \mid x > 9\}$
- ☐ C $\{x \mid x > 1\}$
- ☐ D $\{x \mid x > 0\}$

A scientist obtained a sample that contained 80 grams of radioactive Barium-122 that decays exponentially over time. The amount of Barium-122 that remained in the sample at observed times is shown in the table.

Radioactive Decay of Barium-122

Time (minutes)	Mass of Remaining Barium-122 (grams)
0	80.0
1	56.6
2	40.0
3	28.3
4	20.0

If the radioactive decay continues at the same rate, which is closest to the amount of the sample of Barium-122 remaining at 5 minutes?

- ☐ A 8.3 grams
- ☐ B 10.0 grams
- ☐ C 11.7 grams
- ☐ D 14.1 grams

What is the sum of the first 20 terms of the arithmetic sequence shown?

$$\frac{1}{3}, \frac{2}{3}, 1, \frac{4}{3}, \frac{5}{3}, \dots$$

- ☐ A 5
- ☐ B 20
- ☐ C 70
- ☐ D 140

Directions: Type your answer in the box.

What is the number of possible permutations of 8 objects taken 3 at a time?