

# **VIRGINIA STANDARDS OF LEARNING ASSESSMENTS**

**Spring 2003 Released Test**

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## **END OF COURSE ALGEBRA II**

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## Algebra II

### DIRECTIONS

Read and solve each question. For this test you may assume that the value of the denominator of a rational expression is not zero.

#### SAMPLE

$$\frac{6(a+2)}{a} \cdot \frac{a^3}{a+2} =$$

A  $\frac{6}{a^2}$

B  $\frac{6(a+2)}{a}$

C  $6a^2$

D  $\frac{6a^2 + 24a + 24}{a^4}$

- 1 What property is illustrated by the equation

$$3x(x+2) = 3x^2 + 6x?$$

- A Associative Property of Addition
- B Reflexive Property of Equality
- C Associative Property of Multiplication
- D Distributive Property

- 2 Which of the following statements is an example of the transitive property of inequalities?

- F If  $k \geq 0$ , then  $|k| = k$ .
- G If  $k < 6$  and  $6 < m$ , then  $k < m$ .
- H If  $k < 6$ , then  $k + 2 < 8$ .
- J If  $k < 6$  and  $j > 0$ , then  $kj < 6j$ .

- 3 Which expression is equal to  $\frac{(4y^5 - 3y^2)}{5y^2}$ ?

A  $4y^5 - 2y^2$

B  $\frac{4}{5}y^3 + \frac{3}{5}$

C  $\frac{5}{4}y^{-3} - \frac{5}{3}$

D  $\frac{4}{5}y^3 - \frac{3}{5}$

- 4 Which is equivalent to

$$\frac{7a}{15b} - \frac{2b}{5}?$$

F  $\frac{a}{5}$

G  $\frac{a}{2}$

H  $\frac{7a - 6b^2}{15b}$

J  $\frac{7a - 4b}{5}$

- 5 Which is equivalent to  $(\sqrt{2})^3$ ?

A 2

B  $\sqrt{2}$

C  $2\sqrt{2}$

D  $\sqrt{6}$

6 Which is equivalent to  $\sqrt[6]{a^2b^3}$ ?

F  $\frac{1}{6}a^2b^3$

G  $a^3b^2$

H  $a^3b^{\frac{1}{2}}$

J  $a^{\frac{1}{3}}b^{\frac{1}{2}}$

7 Which is a factored form of  $9x^2 - 25$ ?

A  $(3x - 5)(3x + 5)$

B  $(3x - 5)^2$

C  $(3x + 5)^2$

D  $(9x - 25)^2$

8 Which is a factor of

$$x^2 - 2x - 15?$$

F  $(x - 3)$

G  $(x - 15)$

H  $(x + 3)$

J  $(x + 5)$

9 Which is equivalent to

$$(3 + 2i)(2 + 5i)?$$

A  $-4 + 19i$

B  $16 + 19i$

C  $6 + 29i$

D  $6 - 10i$

10 Which is equivalent to  $\sqrt{3} \cdot \sqrt{-3}$ ?

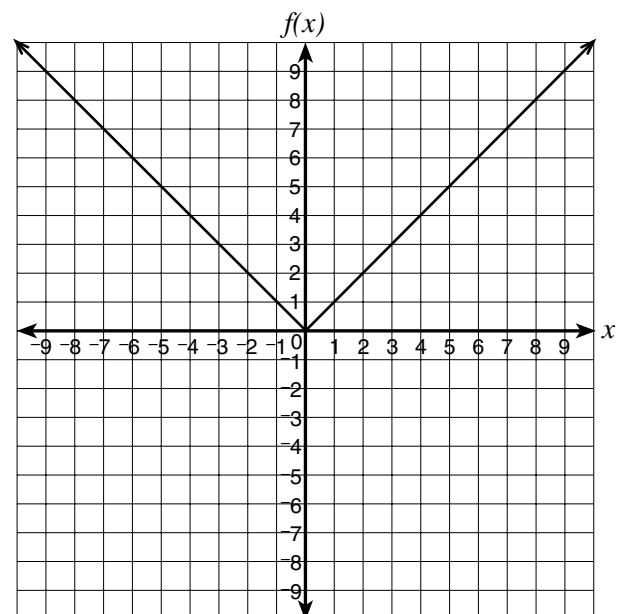
F  $3i$

G  $-3i$

H  $9$

J  $9i$

11 Which type of function is shown?



A Absolute value

B Exponential

C Linear

D Quadratic

12 Which function includes the values in the table?

$x$	-2	-1	0	1	2
$y$	3	0	-1	0	3

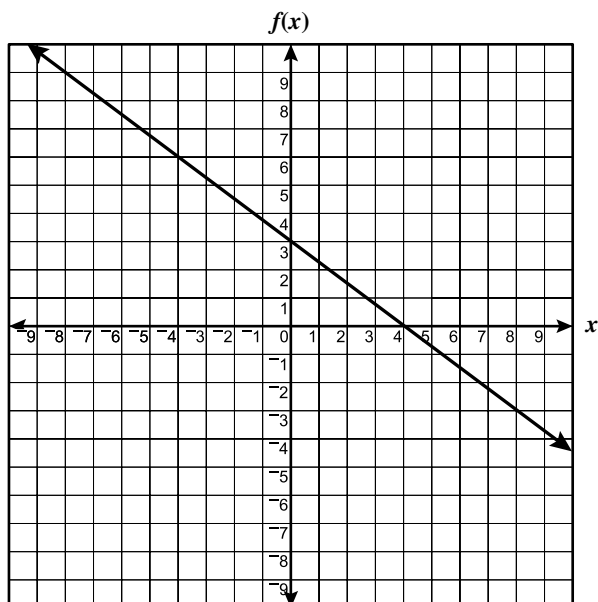
F  $y = x - 1$

G  $y = x + 1$

H  $y = x^2 - 1$

J  $y = (x - 1)^2$

13



Which function is most closely represented by the graph?

- A  $f(x) = \frac{4}{3}x$
- B  $f(x) = 3 - \frac{4}{3}x$
- C  $f(x) = 3 + \frac{3}{4}x$
- D  $f(x) = 3 - \frac{3}{4}x$

14 What is the zero of the function

$$f(x) = 12x + 27?$$

F 27

G  $\frac{9}{4}$ 

H 0

J  $-\frac{9}{4}$ 15 If the domain of  $f(x) = 3x + 5$  is  $\{-1, 0, 1, 2, 3\}$ , what is the range?

- A  $\{0, 2, 9, 11, 14\}$
- B  $\{-8, -5, -2, 1, 4\}$
- C  $\{-4, -2, -1, 5, 8\}$
- D  $\{2, 5, 8, 11, 14\}$

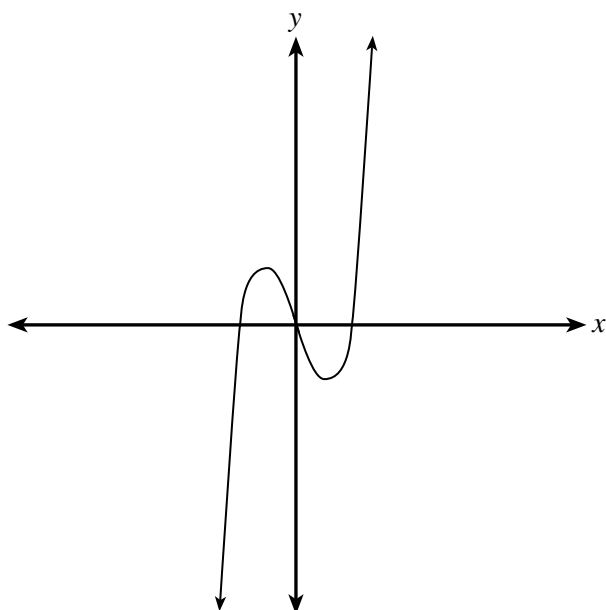
16 The polynomial function

$$y = x^3 - 3x^2 + x + 1$$

has a zero between —

- F -4 and -3
- G -2 and -1
- H -1 and 0
- J 3 and 4

17



If  $a$ ,  $b$ ,  $c$ ,  $d$ , and  $g$  are real numbers and  $a > 0$ , which equation could be represented by this curve?

- A  $y = ax + b$
- B  $y = ax^2 + bx + c$
- C  $y = ax^3 + bx^2 + cx + d$
- D  $y = ax^4 + bx^3 + cy^2 + dx + g$

18 What is the value of  $\sum_{n=1}^6 2^n$ ?

- F 62
- G 126
- H 128
- J 252

19 If  $a_n = 1 + \frac{1}{n}$ , then what is  $a_9$ ?

- A  $\frac{11}{10}$
- B  $\frac{10}{9}$
- C  $\frac{9}{8}$
- D  $\frac{3}{2}$

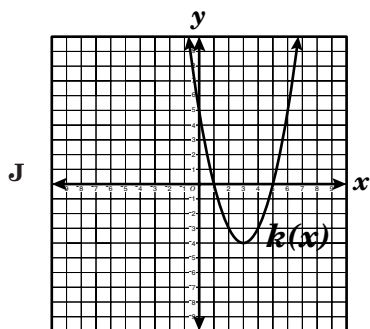
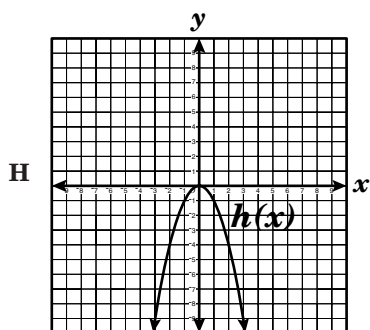
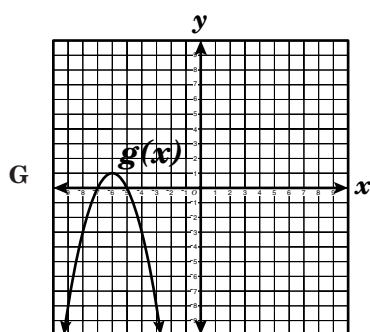
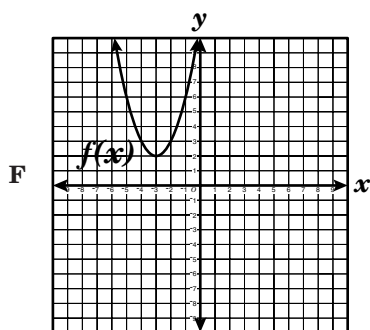
20 In which of the following is  $z$  directly proportional to  $x$  and inversely proportional to the square of  $y$ ?

- F  $z = k \frac{x^2}{y}$
- G  $z = kxy^2$
- H  $z = k \frac{x}{y^2}$
- J  $z = k \frac{y}{x}$

21 The time required to complete a job varies inversely as the number of people working. It took 4 hours for 7 electricians to wire a building. How long would it have taken 3 electricians to have done the job?

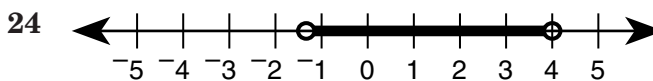
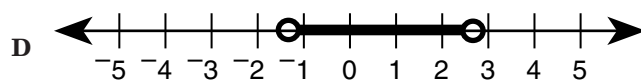
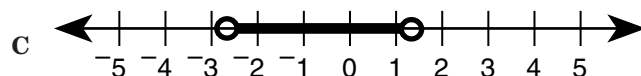
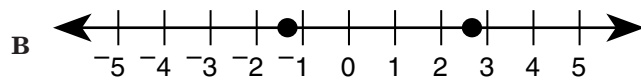
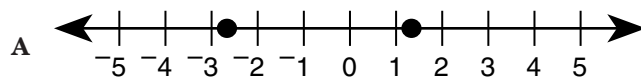
- A 1 hr 43 min
- B 5 hr 15 min
- C 7 hr 30 min
- D 9 hr 20 min

- 22 Which apparently is a graph of a quadratic function that has no real zeros?



- 23 Which graph shows the solution set for

$$|3x - 2| = 6?$$



Which inequality describes the solution set graphed above?

F  $|3x - 4| \geq 8$

G  $|3x - 4| < 8$

H  $|2x - 3| > 5$

J  $|2x - 3| \leq 5$

- 25 What are the solutions to  $x^2 - 12x + 16 = 0$ ?

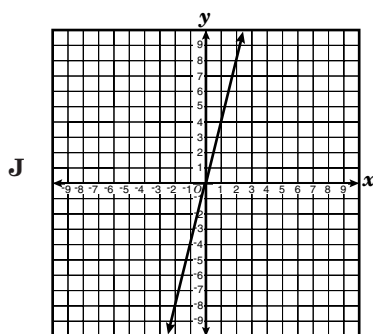
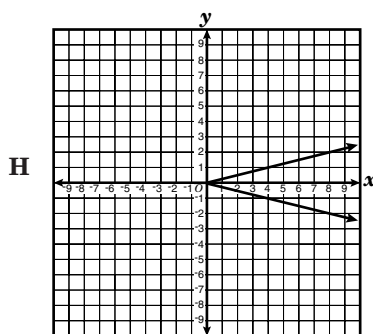
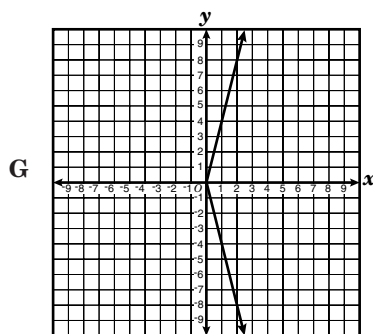
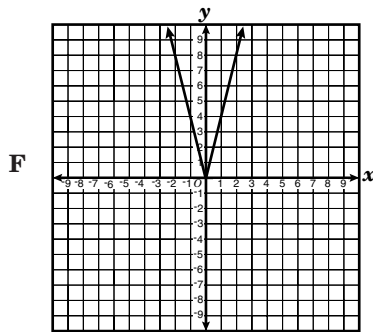
A  $-12 \pm 4\sqrt{5}$

B  $-6 \pm 2\sqrt{5}$

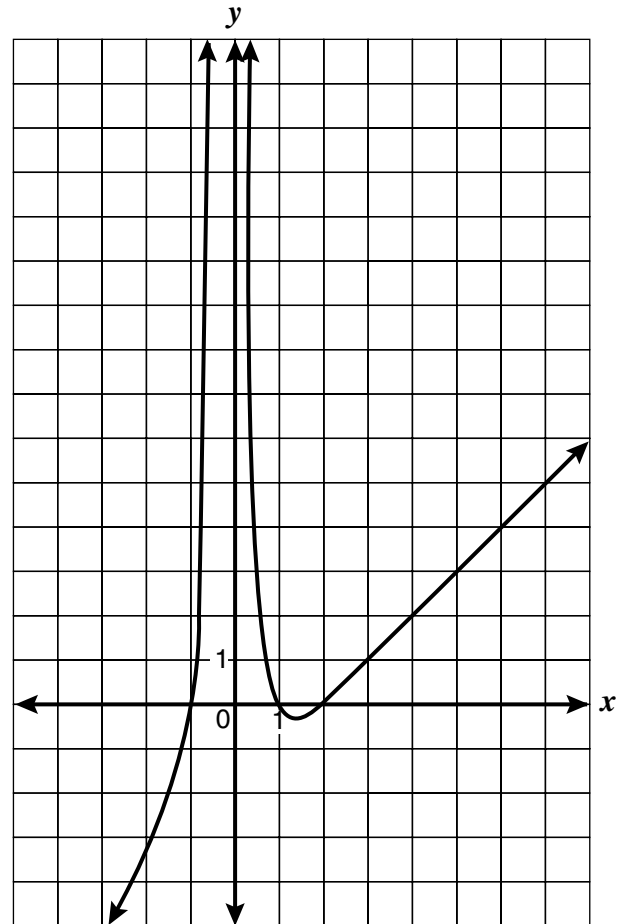
C  $6 \pm 2\sqrt{5}$

D  $12 \pm 4\sqrt{5}$

- 26 Which is apparently the graph of  $y = |4x|$ ?



- 27 This is a graph of a rational function,  $f$ .



Which is *not* a solution of the equation  $f(x) = 0$ ?

- A -2
- B -1
- C 1
- D 2

28 Which is the solution set for

$$3x^2 - 4x - 15 = 0?$$

F  $\left\{-3, \frac{5}{3}\right\}$

G  $\left\{\frac{2 \pm i\sqrt{41}}{3}\right\}$

H  $\left\{-\frac{5}{3}, 3\right\}$

J  $\left\{-\frac{2 \pm i\sqrt{41}}{3}\right\}$

29 What is the solution set for

$$\frac{1}{4}\sqrt{9+x} = 1?$$

A  $\{-7, 7\}$

B  $\{-5, 5\}$

C  $\{7\}$

D  $\{5\}$

30 For which value of  $x$  does

$$\frac{x-2}{18} = \frac{x-3}{15}?$$

F  $-8$

G  $-\frac{13}{3}$

H  $\frac{13}{3}$

J  $8$

31 The length,  $s$ , (in feet) of the skid mark left by an automobile traveling at  $r$  miles per hour can be approximated by the relation  $r = 2\sqrt{5s}$ . At the scene of an accident, police measured a skid mark of 361 feet. About how many miles per hour was the car traveling when the brakes were applied?

A 42 mph

B 54 mph

C 76 mph

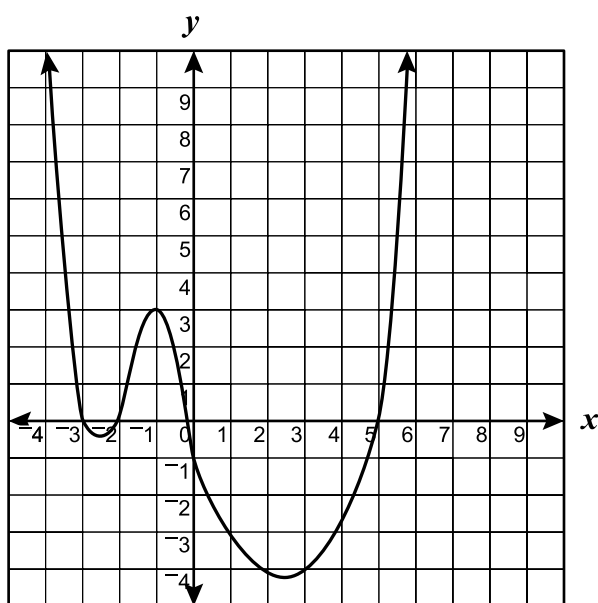
D 85 mph



- 32 Which function of  $x$  would have  $x$ -intercepts  $-\frac{1}{2}$  and 3?

F  $y = 2x^2 - 5x - 3$   
 G  $y = x^2 - x - 6$   
 H  $y = 2x^2 + 5x - 3$   
 J  $y = 2x^2 + 7x + 3$

33



Which set contains 3 apparent zeros of the polynomial function shown?

A  $\{-2.5, -1, 3\}$   
 B  $\{-3, -2, 5\}$   
 C  $\{-3, 1, 2.5\}$   
 D  $\{-3, -1, 3\}$

- 34 If  $f(x)$  is a polynomial with only factors  $x$ ,  $(x + 2)$ , and  $(x - 4)$ , what is the solution set of  $f(x) = 0$ ?

F  $\{0, 2, 4\}$   
 G  $\{-4, 0, 2\}$   
 H  $\{-2, 0, 4\}$   
 J  $\{-4, -2, 0\}$

- 35 When graphed, which of the following equations would produce a circle?

A  $x^2 - y^2 = 9$   
 B  $x + y = 9$   
 C  $y = x^2 - 9$   
 D  $x^2 + y^2 = 9$

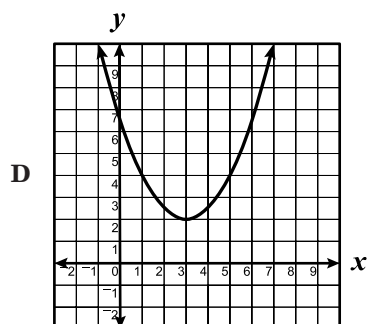
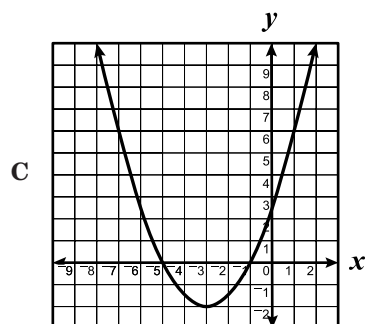
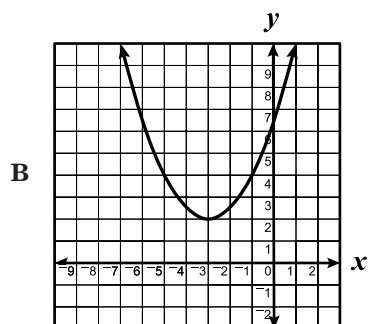
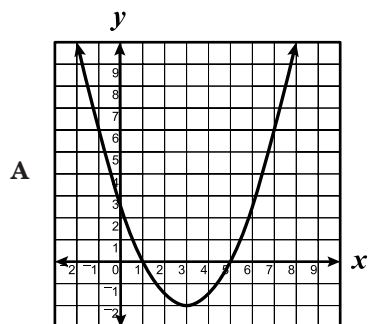
- 36 Which describes the graph of

$$\frac{x^2}{5} + \frac{y^2}{4} = 1?$$

F An ellipse  
 G A hyperbola  
 H A parabola  
 J A circle

37 Which could be the graph of

$$y - 2 = \frac{1}{2}(x + 3)^2?$$



38 Buy-Rite Electronics has 3 locations each selling 3 different models of Convair radios. Matrix  $A$  shows the inventory of each model at each location.

Store	Model			
	X	Y	Z	
South	38	12	64	$= A$
Central	42	18	42	
North	65	36	71	

Matrix  $B$  shows the cost of each model.

Model	Cost	$= B$
X	\$28.95	
Y	\$82.39	
Z	\$38.41	

For each location, which shows the total value of the inventory of all 3 models?

	South	\$110.10
F	Central	\$3,460.38
	North	\$2,496.65

	South	\$3,300.30
G	Central	\$8,403.78
	North	\$6,606.52

	South	\$4,547.02
H	Central	\$4,312.14
	North	\$7,574.90

	South	\$4,197.75
J	Central	\$5,437.74
	North	\$6,798.57

39  $Q = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$ ,  $R = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ ,  $T = [1 \quad 2]$

Which product is *not* possible?

- A  $Q \times R$
- B  $Q \times T$
- C  $R \times Q$
- D  $R \times R$

40 
$$\begin{cases} ax + by = q \\ cx + dy = r \end{cases}$$

Which matrix equation is equivalent to the system of equations above?

F  $\begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} q \\ r \end{bmatrix}$

G  $\begin{bmatrix} ax & by \\ cx & dy \end{bmatrix} = \begin{bmatrix} q \\ r \end{bmatrix}$

H  $\begin{bmatrix} a & b \\ c & d \end{bmatrix} [x \quad y] = \begin{bmatrix} q \\ r \end{bmatrix}$

J  $\begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} q \\ r \end{bmatrix}$

41 What is the multiplicative inverse of the matrix  $\begin{bmatrix} 4 & -1 \\ -7 & 8 \end{bmatrix}$ ?

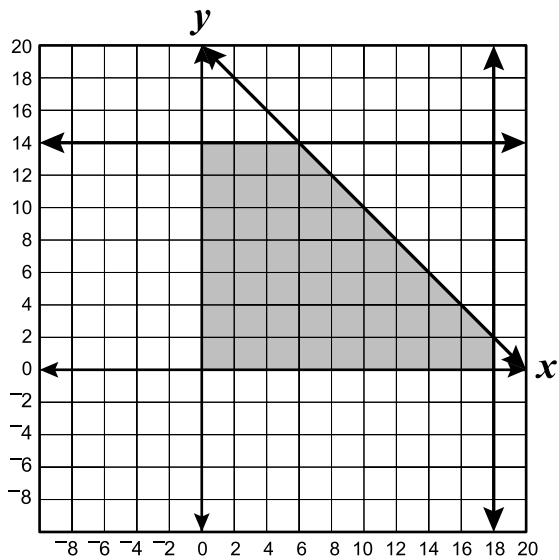
A  $\begin{bmatrix} \frac{1}{4} & -1 \\ \frac{-1}{7} & \frac{1}{8} \end{bmatrix}$

B  $\begin{bmatrix} \frac{8}{25} & \frac{1}{25} \\ \frac{7}{25} & \frac{4}{25} \end{bmatrix}$

C  $\begin{bmatrix} \frac{8}{25} & \frac{7}{25} \\ \frac{1}{25} & \frac{4}{25} \end{bmatrix}$

D  $\begin{bmatrix} -4 & 1 \\ 7 & -8 \end{bmatrix}$

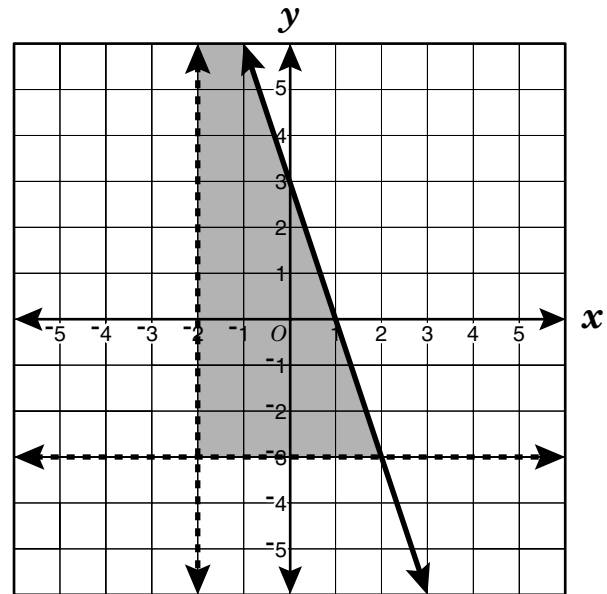
- 42 Tim makes posters on his computer. He gets \$5 for each regular size and \$8 for each large poster. To use linear programming to maximize income, Tim developed this feasible region from the set of constraints on his resources, where  $x$  = number of regular size posters and  $y$  = number of large posters.



How many of each size poster should Tim make in order to bring in the greatest amount of money?

- F 6 regular, 14 large
- G 8 regular, 12 large
- H 12 regular, 8 large
- J 18 regular, 2 large

43



Which system of inequalities best represents the graph shown?

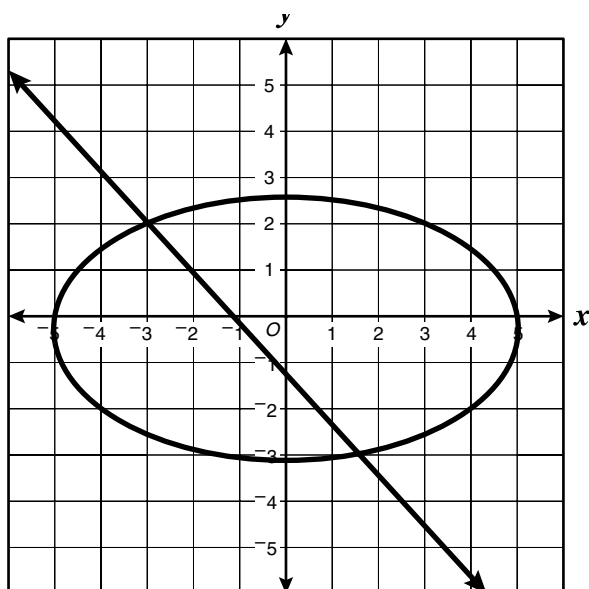
A 
$$\begin{cases} -3x + y < 3 \\ y < -3 \\ x > -2 \end{cases}$$

B 
$$\begin{cases} -3x + y \leq 3 \\ y > -3 \\ x > -2 \end{cases}$$

C 
$$\begin{cases} 3x + y \leq 3 \\ y > -3 \\ x > -2 \end{cases}$$

D 
$$\begin{cases} y \leq 3x - 3 \\ y > -3 \\ x > -2 \end{cases}$$

44



This is a portion of the graph of a system of equations. Which is most likely the solution set for the system?

- F  $\{(1.5, 2.5), (3, 2)\}$
- G  $\{(-2.5, 1.5), (2, -3)\}$
- H  $\{(-2, -3), (2.5, -1.5)\}$
- J  $\{(-3, 2), (1.5, -3)\}$

45

$$\begin{cases} 2y = x^2 - 6x - 9 \\ 2y = -x^2 + 2x + 1 \end{cases}$$

What is the solution set for this system of equations?

- A  $\{(5, -7), (-1, -1)\}$
- B  $\{(1, 1), (-5, 23)\}$
- C  $\{(1, -7), (-5, 23)\}$
- D  $\left\{\left(2, \frac{1}{2}\right)\right\}$

46 The chart gives the average number of students per computer in public schools in America.

Year	Students per computer
1990-91	20.0
1991-92	18.0
1992-93	16.0
1993-94	14.0
1994-95	10.5
1995-96	10.0
1996-97	7.8
1997-98	6.1

Assuming a linear relationship, which is the best estimate for the number of students per computer during 1989–1990?

- F 5.4
- G 10.8
- H 20.2
- J 21.9

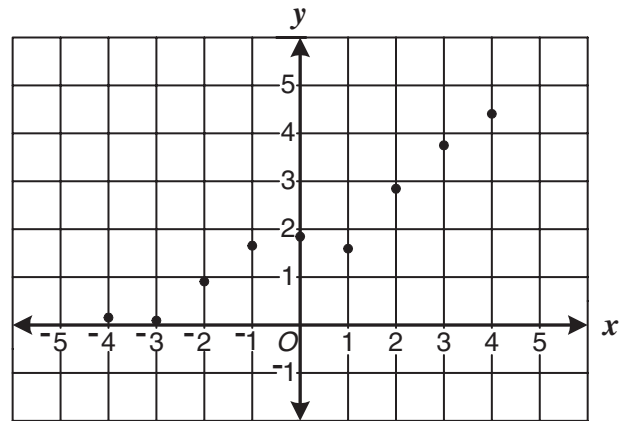
- 47 The chart shows city real estate taxes paid by four families and the assessed value of their homes.

Family	Hardy	Jacobs	Rosinni	Martinez
Value	\$50,000	\$80,000	\$100,000	\$150,000
Taxes	\$1,100	\$2,000	\$2,600	\$4,100

The tax on the Miller home was \$1,700. What was the assessed value?

- A \$60,000
- B \$65,000
- C \$68,000
- D \$70,000

48



Which is most likely the equation for the curve of best fit for the scatterplot above?

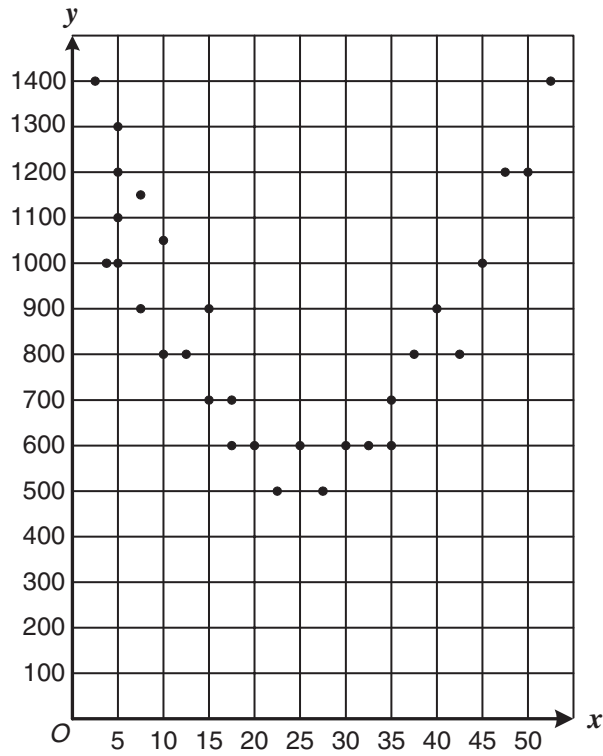
F  $y = \frac{1}{2}x + 2$

G  $y = \frac{1}{8}x + 4$

H  $y = x + 2$

J  $y = x - 3$

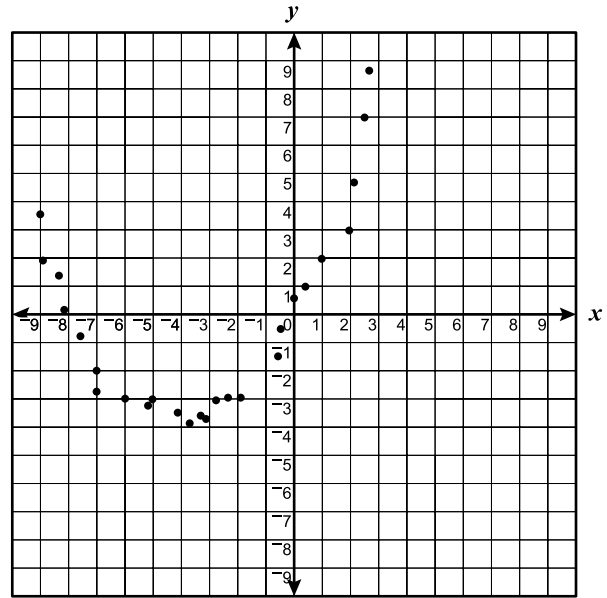
49



Which type of function would best fit the data in this scatterplot?

- A Linear
- B Exponential
- C Logarithmic
- D Quadratic

50



Which equation most closely fits the data in this scatterplot?

F  $y = \frac{2}{x} + 2$

G  $4y^2 = x^2 + 4$

H  $4y = x^2 + 8x$

J  $y = 2x - x^2$