

Forward Kinematics & Inverse Kinematics

2024 Computer Animation and
Special Effects

Outline

- Overview
- Objective
- Report
- Scoring
- Submission

Overview

- Forward kinematics

More amc files you can find in
<http://mocap.cs.cmu.edu/>



Demo link: <https://youtu.be/CUQRCwjztrQ>

Overview (cont.)

- Inverse kinematics



Demo Link : <https://youtu.be/CUQRCwiztrQ?si=h1e-s2eqCPDsbyYUQ&t=24>

Demo



Demo link: <https://youtu.be/CUQRCwiztrQ>

Objective

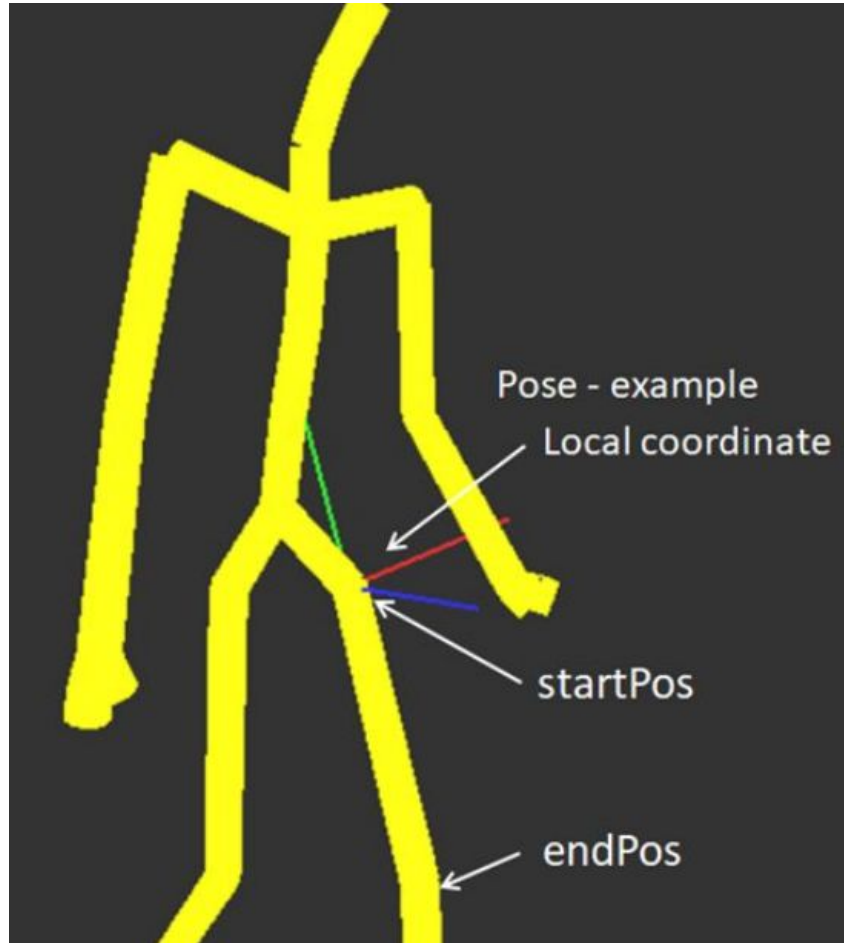
- In FK part, only one function you need to implement
 - in `kinematics.cpp`
 - `void forwardSolver(...)`

Objective (cont.)

- `void forwardSolver(...)`
 - Convert motion data from joint space to the Cartesian space
 - set each bone's global start and end position and rotation
 - Hint
 - review “[kinematics.pptx](#)” from p.1 - p.19
 - review “[acclaim_FK_IKnote.pdf](#)” from p.1 - p.4
 - read local coordinate data from posture first
 - you can probably use DFS or BFS to traverse all bones
 - you can check
 - struct [Posture](#) in [posture.h](#)
 - struct [Bone](#) in [bone.h](#)

Objective (cont.)

- Pose example
- Each bone has
 - local coordinate
 - start position
 - end position



Objective

- Because IK also use forwardSolver function, we **strongly recommend you to complete FK part first.**
- In IK part, there are two function you need to implement in this homework
 - in `kinematics.cpp`
 - `Eigen::VectorXd pseudoInverseLinearSolver(...)`
 - `bool inverseJacobianIKSolver(...)`

Objective (cont.)

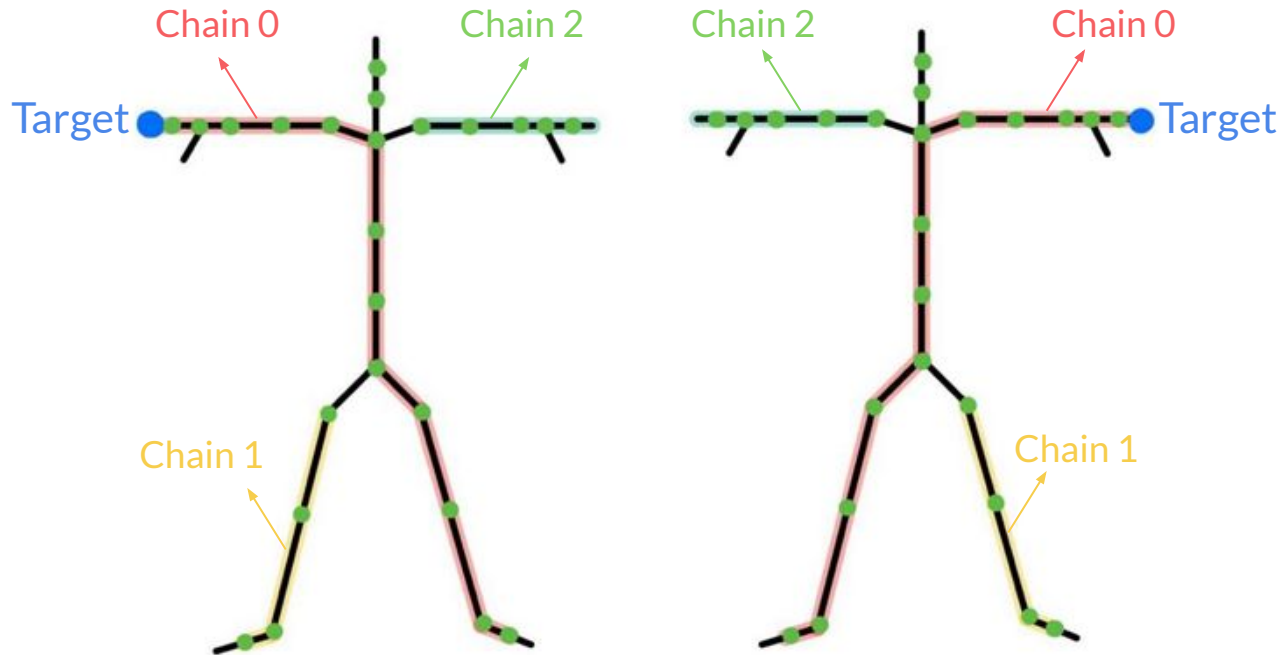
- `VectorXd pseudoInverseLinearSolver(...)`
 - Goal
 - Find solution of linear least squares system, which will be needed for inverse kinematics
 - i.e. find x which $\min(\| \text{jacobian} * x - \text{target} \|)$
 - Hint
 - You might use some pseudo-inverse methods such as `SVD`
 - There are some built-in functions in `Eigen` that you can use
 - `Eigen::Matrixs4Xf` means a matrix with 4 rows and unknown columns
 - `Eigen::Matrix4Xf m(4, 10);` // A matrix with 4 rows and 10 columns
 - `Eigen::VectorXf` means a vector with unknown size
 - `Eigen::VectorXf v(10);` // A vector with 10 elements

Objective (cont.)

- `bool inverseJacobianIKSolver(...)`
 - Goal
 - Implement inverse kinematics
 - We use inverse-Jacobain method in this homework
 - Hint
 - Review "[kinematics.pptx](#)" from p.20 - p.50
 - Review "[acclaim_FK_IKnote.pdf](#)" Inverse Kinematics part
 - Traverse each chain by `jointChains[chainIdx]`, `boneChain[chainIdx]`
 - Make `*jointChains[chainIdx][0]` touch the ball (`target_pos[chainIdx]`)
 - Joint `i` and `i+1` are the endpoints of bone `i`
 - You can check struct `Bone` in `bone.h`

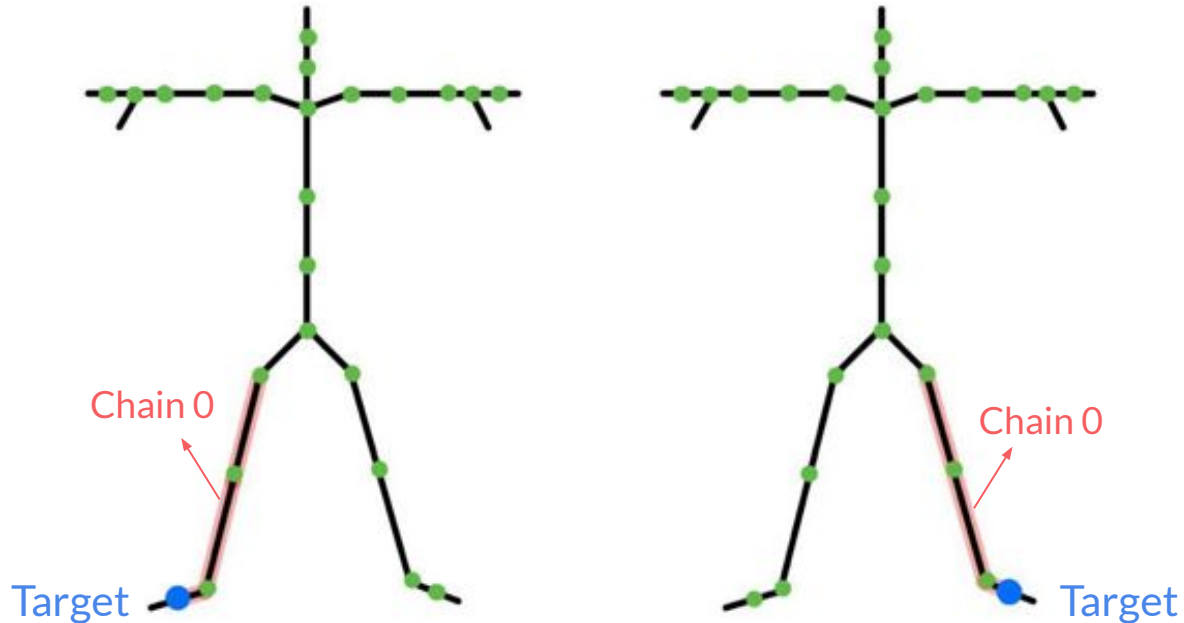
Objective (cont.)

- To achieve root movement, we employed the following methods.



Objective (cont.)

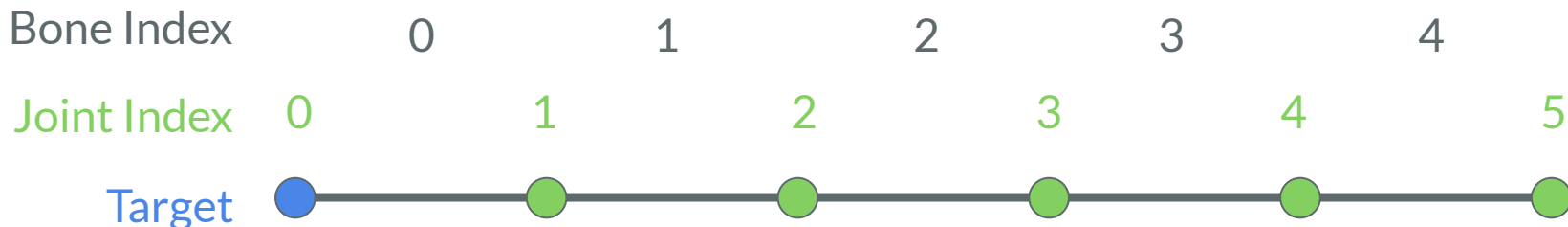
- To achieve root movement, we employed the following methods.



Objective (cont.)

- We will pass the corresponding chain as parameters into the `inverseJacobianIKSolver()` based on the currently dragged target.

```
std::vector<std::vector<Eigen::Vector4d*>> &jointChains  
std::vector<std::vector<acclaim::Bone*>> &boneChains
```



Report

- Suggested outline
 - Introduction/Motivation
 - Fundamentals
 - Describe local and global coordinates in your words
 - Implementation
 - Result and Discussion
 - IK part : How different step and epsilon affect the result
 - Bonus (Optional)
 - Conclusion
 - Demo link (Google Drive, Youtube)
 - Show your FK and IK result
 - Up to 1 min

Scoring

- Forward kinematics (40%)
- Inverse kinematics (40%)
- Report (20%)
- Bonus (up to 20%)
 - Any creativity

Submission

- Please upload **kinematics.cpp** and **report_< your student ID>.pdf** respectively
 - If you make any modifications to other codes, you will need to upload them and discuss them in the report.
- Late policies
 - Penalty of 10 points on each day after deadline
- Cheating policies
 - 0 points for any cheating on assignments
- Deadline
 - Sunday, 2024/05/05, 23:59